

Search for new physics from

$$B \rightarrow K_2^*(\rightarrow K\pi)l^+l^-$$
$$B_s \rightarrow f_2'(\rightarrow KK)l^+l^-$$

decays

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Based on collaboration with R.H. Li (李润辉), and W. Wang(王伟),
arXiv: 1012.2129, PRD83, 034034 (2011)



中台世界

outline



- **Introduction**

- $B \rightarrow K_2^*(\rightarrow K\pi)l^+l^-$ in SM

- Angular distribution

- BR, FBA, fL.

$(B_s \rightarrow f_2' l^+ l^-)$



- **Two New Physics scenarios**

- Brief introduction

- Parameters obtained by fitting

- Effect on the SM results



- **Summary**

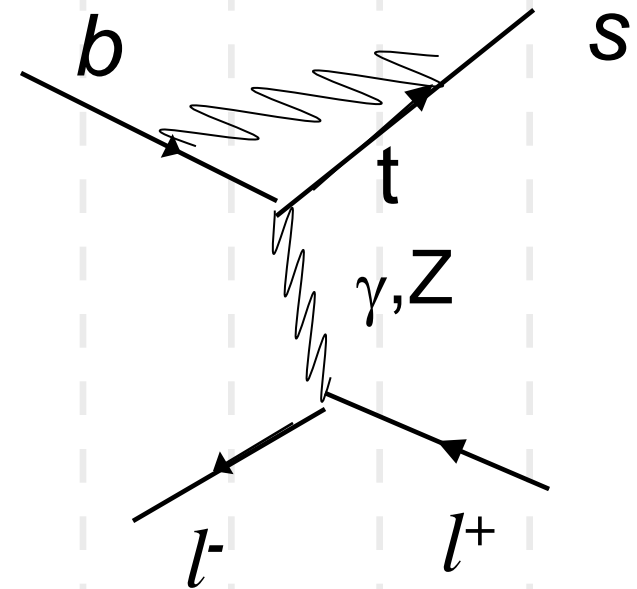


Flavor changing Electroweak penguin operators

$$O_7 = \frac{e m_b}{8\pi^2} \bar{s} \sigma^{\mu\nu} (1 + \gamma_5) b F_{\mu\nu} + \frac{e m_s}{8\pi^2} \bar{s} \sigma^{\mu\nu} (1 - \gamma_5) b F_{\mu\nu}.$$

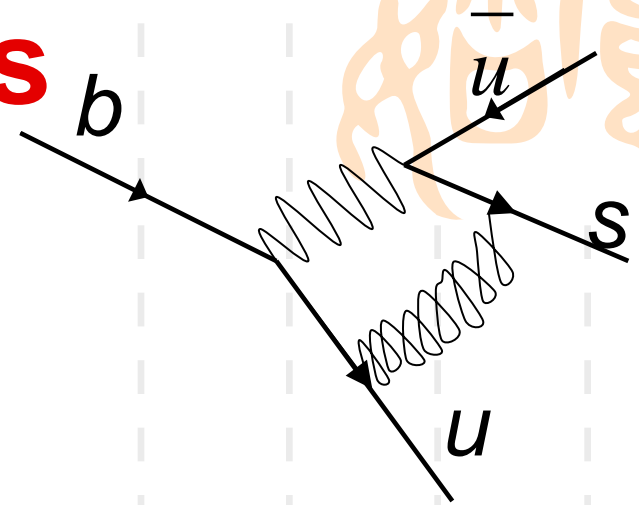
$$O_9 = \frac{\alpha_{\text{em}}}{2\pi} (\bar{l} \gamma_\mu l) (\bar{s} \gamma^\mu (1 - \gamma_5) b),$$

$$O_{10} = \frac{\alpha_{\text{em}}}{2\pi} (\bar{l} \gamma_\mu \gamma_5 l) (\bar{s} \gamma^\mu (1 - \gamma_5) b)$$



No tree level flavor changing neutral current in SM

With QCD corrections from the four quark operators



$$H_{eff} = \frac{G_F}{\sqrt{2}} V_{CKM} \sum_i C_i O_i$$

$$O_1 = \bar{u} \gamma^\mu L u \cdot \bar{s} \gamma_\mu L b$$

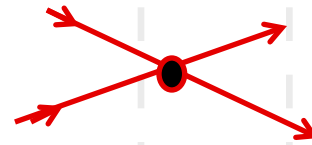
$$O_2 = \bar{s} \gamma^\mu L u \cdot \bar{u} \gamma_\mu L b$$

$$O_3 = \bar{s} \gamma^\mu L b \cdot \sum_q \bar{q} \gamma_\mu L q$$

$$O_4 = \bar{s}_\alpha \gamma^\mu L b_\beta \cdot \sum_q \bar{q}_\beta \gamma_\mu L q_\alpha$$

$$O_5 = \bar{s} \gamma^\mu L b \cdot \sum_q \bar{q} \gamma_\mu R q$$

$$O_6 = \bar{s}_\alpha \gamma^\mu L b_\beta \cdot \sum_q \bar{q}_\beta \gamma_\mu R q_\alpha$$



Introduction

- Unlike $b \rightarrow s \gamma$ or $B \rightarrow K^* \gamma$, which have only limited physical observables
- $b \rightarrow s l^+ l^-$, and especially $B \rightarrow K^* l^+ l^-$, with a number of observables accessible (exp. also easier), provides a wealth of information of weak interactions, ranging from the **forward-backward asymmetries, isospin asymmetries, and polarization fractions**

About $K_2^*(1430)$ and $f_2'(1525)$

$\Gamma = 100 \text{ MeV}$, 73 MeV

$\rightarrow K \pi$

$\rightarrow K K$

l	s	J	$2s+1L_J$	J^{PC}	Meson
$l = 0$	$s = 0$	$J = 0$	1S_0	0^{-+}	Pseudoscalar (P)
	$s = 1$	$J = 1$	3S_1	1^{--}	Vector (V)
$l = 1$	$s = 0$	$J = 1$	1P_1	1^{+-}	Axial-vector ($A(^1P_1)$)
	$s = 1$	$J = 0$	3P_0	0^{++}	Scalar (S)
		$J = 1$	3P_1	1^{++}	Axial-vector ($A(^3P_1)$)
		$J = 2$	3P_2	2^{++}	Tensor (T)

$$B \rightarrow K_2^* l^+ l^- \quad (B_s \rightarrow f_2' l^+ l^-)$$

- 5 polarization states: $J_z = -2, -1, 0, 1, 2$
- 3 contribute to $\bar{B}^0 \rightarrow K_2^* l^+ l^-$, $J_z = -1, 0, 1$, because of angular momentum conservation

- Similar to K^* mesons. $\bar{B}^0 \rightarrow K_2^* l^+ l^-$ formulism can be got by some substitution in $\bar{B}^0 \rightarrow K^* l^+ l^-$ formulism in pQCD approach.

Form factors needed for the exclusive decays

- Definition similar to the $B \rightarrow K^*$ case

$$\langle K_2^*(P_2, \epsilon) | \bar{s} \gamma^\mu b | \bar{B}(P_B) \rangle = -\frac{2V(q^2)}{m_B + m_{K_2^*}} \epsilon^{\mu\nu\rho\sigma} \epsilon_{T\nu}^* P_{B\rho} P_{2\sigma},$$

$$\begin{aligned} \langle K_2^*(P_2, \epsilon) | \bar{s} \gamma^\mu \gamma_5 b | \bar{B}(P_B) \rangle &= 2im_{K_2^*} A_0(q^2) \frac{\epsilon_T^* \cdot q}{q^2} q^\mu + i(m_B + m_{K_2^*}) A_1(q^2) \left[\epsilon_{T\mu}^* - \frac{\epsilon_T^* \cdot q}{q^2} q^\mu \right] \\ &\quad - iA_2(q^2) \frac{\epsilon_T^* \cdot q}{m_B + m_{K_2^*}} \left[P^\mu - \frac{m_B^2 - m_{K_2^*}^2}{q^2} q^\mu \right], \end{aligned}$$

$$\langle K_2^*(P_2, \epsilon) | \bar{s} \sigma^{\mu\nu} q_\nu b | \bar{B}(P_B) \rangle = -2iT_1(q^2) \epsilon^{\mu\nu\rho\sigma} \epsilon_{T\nu}^* P_{B\rho} P_{2\sigma},$$

$$\langle K_2^*(P_2, \epsilon) | \bar{s} \sigma^{\mu\nu} \gamma_5 q_\nu b | \bar{B}(P_B) \rangle = T_2(q^2) [(m_B^2 - m_{K_2^*}^2) \epsilon_{T\mu}^* - \epsilon_T^* \cdot q P^\mu] + T_3(q^2) \epsilon_T^* \cdot q \left[q^\mu - \frac{q^2}{m_B^2 - m_{K_2^*}^2} P^\mu \right]$$

Non-perturbative variables, difficult to calculate in QCD

Form factors calculated in pQCD to leading order of $1/m_b$

F	$F(0)$	a	b
$V^{BK_2^*}$	$0.21^{+0.04+0.05}_{-0.04-0.03}$	$1.73^{+0.02+0.05}_{-0.02-0.03}$	$0.66^{+0.04+0.07}_{-0.05-0.01}$
$A_0^{BK_2^*}$	$0.18^{+0.04+0.04}_{-0.03-0.03}$	$1.70^{+0.00+0.05}_{-0.02-0.07}$	$0.64^{+0.00+0.04}_{-0.06-0.10}$
$A_1^{BK_2^*}$	$0.13^{+0.03+0.03}_{-0.02-0.02}$	$0.78^{+0.01+0.05}_{-0.01-0.04}$	$-0.11^{+0.02+0.04}_{-0.03-0.02}$
$A_2^{BK_2^*}$	$0.08^{+0.02+0.02}_{-0.02-0.01}$
$T_1^{BK_2^*}$	$0.17^{+0.04+0.04}_{-0.03-0.03}$	$1.73^{+0.00+0.05}_{-0.03-0.07}$	$0.69^{+0.00+0.05}_{-0.08-0.11}$
$T_2^{BK_2^*}$	$0.17^{+0.03+0.04}_{-0.03-0.03}$	$0.79^{+0.00+0.02}_{-0.04-0.09}$	$-0.06^{+0.00+0.00}_{-0.10-0.16}$
$T_3^{BK_2^*}$	$0.14^{+0.03+0.03}_{-0.03-0.02}$	$1.61^{+0.01+0.09}_{-0.00-0.04}$	$0.52^{+0.05+0.15}_{-0.01-0.01}$
$V^{B_s f_2'}$	$0.20^{+0.04+0.05}_{-0.03-0.03}$	$1.75^{+0.02+0.05}_{-0.00-0.03}$	$0.69^{+0.05+0.08}_{-0.01-0.01}$
$A_0^{B_s f_2'}$	$0.16^{+0.03+0.03}_{-0.02-0.02}$	$1.69^{+0.00+0.04}_{-0.01-0.03}$	$0.64^{+0.00+0.01}_{-0.04-0.02}$
$A_1^{B_s f_2'}$	$0.12^{+0.02+0.03}_{-0.02-0.02}$	$0.80^{+0.02+0.07}_{-0.00-0.03}$	$-0.11^{+0.05+0.09}_{-0.00-0.00}$
$A_2^{B_s f_2'}$	$0.09^{+0.02+0.02}_{-0.01-0.01}$
$T_1^{B_s f_2'}$	$0.16^{+0.03+0.04}_{-0.03-0.02}$	$1.75^{+0.01+0.05}_{-0.00-0.05}$	$0.71^{+0.03+0.06}_{-0.01-0.08}$
$T_2^{B_s f_2'}$	$0.16^{+0.03+0.04}_{-0.03-0.02}$	$0.82^{+0.00+0.04}_{-0.04-0.06}$	$-0.08^{+0.00+0.03}_{-0.09-0.08}$
$T_3^{B_s f_2'}$	$0.13^{+0.03+0.03}_{-0.02-0.02}$	$1.64^{+0.02+0.06}_{-0.00-0.06}$	$0.57^{+0.04+0.05}_{-0.01-0.09}$

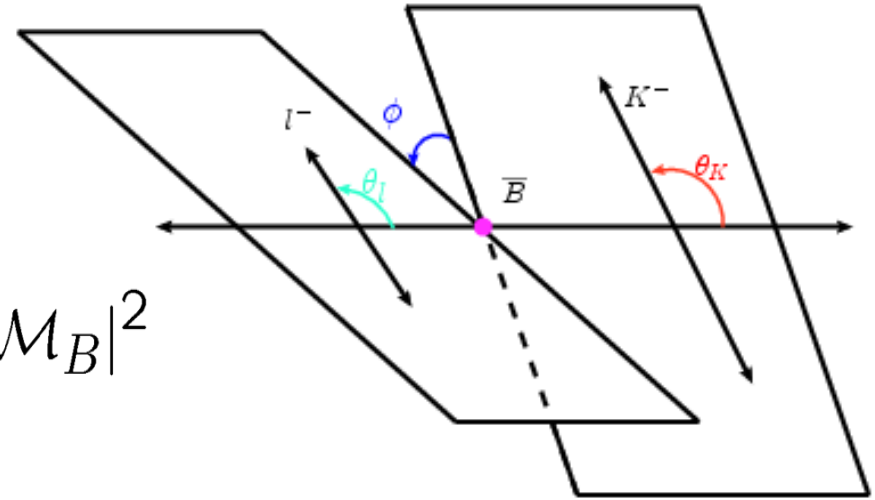
Branching ratios are proportional to form factors, have large uncertainties, but Angular distribution is not

Partial decay width

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_K d\cos\theta_l d\phi} = \frac{3}{8} |\mathcal{M}_B|^2$$

$|\mathcal{M}_B|^2$ is decomposed into 11 terms

$$\begin{aligned} |\mathcal{M}_B|^2 = & [I_1^c C^2 + 2I_1^s S^2 + (I_2^c C^2 + 2I_2^s S^2) \cos(2\theta_l) \\ & + 2I_3 S^2 \sin^2 \theta_l \cos(2\phi) + 2\sqrt{2}I_4 CS \sin(2\theta_l) \cos \phi \\ & + 2\sqrt{2}I_5 CS \sin(\theta_l) \cos \phi + 2I_6 S^2 \cos \theta_l \\ & + 2\sqrt{2}I_7 CS \sin(\theta_l) \sin \phi + 2\sqrt{2}I_8 CS \sin(2\theta_l) \sin \phi \\ & + 2I_9 S^2 \sin^2 \theta_l \sin(2\phi)] \end{aligned}$$



Angular distribution

$$I_7 = \sqrt{2}\beta_l [\text{Im}(A_{L0}A_{L||}^*) - \text{Im}(A_{R0}A_{R||}^*)]$$

$$I_8 = \frac{1}{\sqrt{2}}\beta_l^2 [\text{Im}(A_{L0}A_{L\perp}^*) + \text{Im}(A_{R0}A_{R\perp}^*)]$$

$$I_9 = \beta_l^2 [\text{Im}(A_{L||}A_{L\perp}^*) + \text{Im}(A_{R||}A_{R\perp}^*)]$$

- $A_{Ri} = A_{Li}|_{C_{10} \rightarrow -C_{10}}$
- Up to one-loop matrix element and resonances taken out, only C_9^{eff} contributes an imaginary part.

Without higher order QCD corrections

$$I_7 = 0, I_8 \text{ and } I_9 \text{ is tiny}$$

They could be chosen as the window to observe those effects that can change the behavior of the Wilson coefficients, such as NP effects.

BRs, f_L

With the recent pQCD results for $\bar{B}^0 \rightarrow K_2^*$ form factors

Branching ratios:

$$BR(B \rightarrow K_2^* \mu^+ \mu^-) = (2.5^{+1.6}_{-1.1}) \times 10^{-7},$$

$$BR(B \rightarrow K_2^* \tau^+ \tau^-) = (9.6^{+6.2}_{-4.5}) \times 10^{-10}.$$

Longitudinal Polarization
fractions:

$$f_L \equiv \frac{\Gamma_0}{\Gamma} = \frac{\int dq^2 \frac{d\Gamma_0}{dq^2}}{\int dq^2 \frac{d\Gamma}{dq^2}}$$

$$f_L(B \rightarrow K_2^* \mu^+ \mu^-) = (66.6 \pm 0.4)\%,$$

$$f_L(B \rightarrow K_2^* \tau^+ \tau^-) = (57.2 \pm 0.7)\%$$

Estimate BRs from exp.

- Experimentally, we have

$$\mathcal{B}(\bar{B}^0 \rightarrow K_2^* \gamma) = (12.4 \pm 2.4) \times 10^{-6},$$

$$\mathcal{B}(\bar{B}^0 \rightarrow K^* \gamma) = (43.3 \pm 1.5) \times 10^{-6}.$$

$$\mathcal{B}(\bar{B}^0 \rightarrow K^* l^+ l^-) = (1.09 \pm 0.12) \times 10^{-6}$$

- Assume $R = \mathcal{B}(K_2^*) / \mathcal{B}(K^*)$ is **the same for radiative and semi-leptonic** decays, we have

$$\mathcal{B}_{\text{exp}}(B^0 \rightarrow K_2^{*0} l^+ l^-) = (3.1 \pm 0.7) \times 10^{-7}$$

Compare with KC Yang, **PRD79:114008,2009**

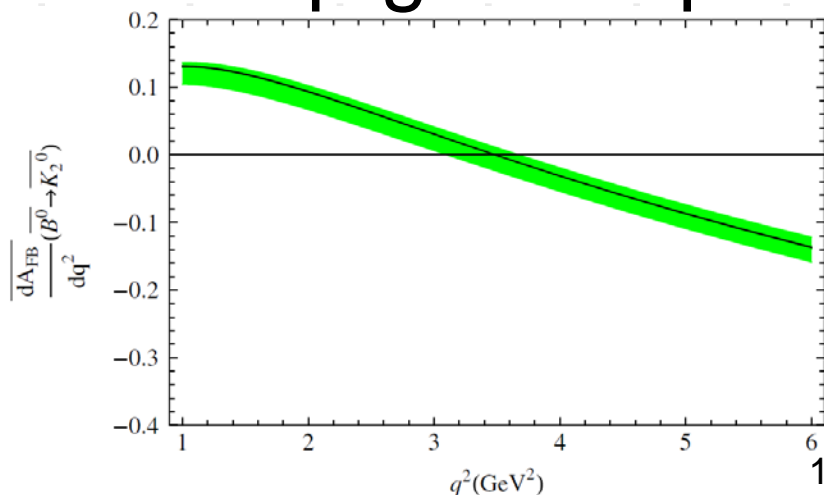
$$\mathcal{B}(B^0 \rightarrow K_2^{*0}(1430) \mu^+ \mu^-) = (3.5_{-1.0}^{+1.1+0.7}) \times 10^{-7}$$

D. Forward-backward asymmetry

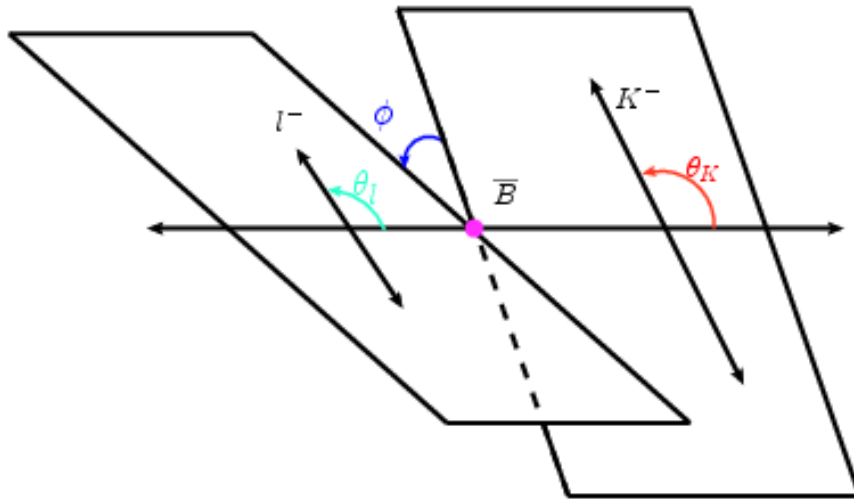
The differential forward-backward asymmetry of $\bar{B} \rightarrow \bar{K}_2^* l^+ l^-$ is defined by

$$\frac{dA_{\text{FB}}}{dq^2} = \left[\int_0^1 - \int_{-1}^0 \right] d \cos \theta_l \frac{d^2 \Gamma}{dq^2 d \cos \theta_l} = \frac{3}{4} I_6$$

- The forward backward asymmetry varies from positive to negative as q^2 grows up
- The 0-cross point is sensitive to new physics



Forward and Backward Asymmetry



$$\frac{dA_{FB}}{dq^2} = \left[\int_0^1 - \int_{-1}^0 \right] d \cos \theta_l \frac{d^2 \Gamma}{dq^2 d \cos \theta_l}$$

The zero-crossing point s_0 of FBAs is determined by the equation

$$C_9 A_1(s_0) V(s_0) + C_{7L} \frac{m_b(m_B + m_{K_2^*})}{s_0} A_1(s_0) T_1(s_0) + C_{7L} \frac{m_b(m_B - m_{K_2^*})}{s_0} T_2(s_0) V(s_0) = 0$$

$$s_0(B \rightarrow K_2^* \mu^+ \mu^-) = (3.49 \pm 0.04) \text{ GeV}^2$$

Smaller uncertainty

Similarly for $B_s \rightarrow f_2' l^+ l^-$

$$\mathcal{B}(B_s \rightarrow f_2' \mu^+ \mu^-) = (1.8_{-0.7}^{+1.1}) \times 10^{-7},$$

$$f_L(B_s \rightarrow f_2' \mu^+ \mu^-) = (63.2 \pm 0.7)\%,$$

$$s_0(B_s \rightarrow f_2' \mu^+ \mu^-) = (3.53 \pm 0.03) \text{ GeV}^2$$

$$\mathcal{B}(B_s \rightarrow f_2' \tau^+ \tau^-) = (5.8_{-2.1}^{+3.7}) \times 10^{-10},$$

$$f_L(B_s \rightarrow f_2' \tau^+ \tau^-) = (53.9 \pm 0.4)\%.$$

NP scenario: Vector-like quark model (VQM)

Expanding SM including a $SU(2)_L$ singlet down type quark, Yukawa sector of SM is modified to

$$\mathcal{L}_Y = \bar{Q}_L Y_D H d_R + h_D \bar{Q}_L H D_R + m_D \bar{D}_L D_R + h.c.$$

This modification brings FCNC for the mass eigenstates at tree level.

The interaction for b - s - Z in VQM is

$$\mathcal{L}_{b \rightarrow s} = \frac{g c_L^s \lambda_{sb}}{\cos \theta_W} \bar{s} \gamma^\mu P_L b Z_\mu + h.c.,$$

free parameter

$$\lambda_{sb} = |\lambda_{sb}| \exp(i\theta_s)$$

with which the effective Hamiltonian for $b \rightarrow sl^+l^-$ is given as

$$\mathcal{H}_{b \rightarrow sl^+l^-}^Z = \frac{2G_F}{\sqrt{2}} \lambda_{sb} c_L^s (\bar{s}b)_{V-A} \left[c_L^\ell (\bar{l}l)_{V-A} + c_R^\ell (\bar{l}l)_{V+A} \right]$$

NP scenario: Vector-like quark model (VQM)

The VQM effects can be absorbed into the Wilson coefficients C_9 and C_{10}

$$C_9^{\text{VLQ}} = C_9^{\text{SM}} - \frac{4\pi}{\alpha_{\text{em}}} \frac{\lambda_{sb} c_L^s (c_L^l + c_R^l)}{V_{ts}^* V_{tb}},$$

$$C_{10}^{\text{VLQ}} = C_{10}^{\text{SM}} + \frac{4\pi}{\alpha_{\text{em}}} \frac{\lambda_{sb} c_L^s (c_L^l - c_R^l)}{V_{ts}^* V_{tb}}.$$

Lepton section in VQM is the same as in SM.

NP scenario: Family non-universal Z' model

Expand SM by simply including an additional $U(1)'$ symmetry. The current is

$$J_{Z'}^\mu = g' \sum_i \bar{\psi}_i \gamma^\mu [\epsilon_i^{\psi_L} P_L + \epsilon_i^{\psi_R} P_R] \psi_i,$$

which couples to a family non-universal Z' boson.

After rotating to the mass eigen basis, **FCNC appears at tree level in both LH and RH section.**

Interaction for b - s - Z' is given as

$$\mathcal{L}_{\text{FCNC}}^{Z'} = -g' (B_{sb}^L \bar{s}_L \gamma_\mu b_L + B_{sb}^R \bar{s}_R \gamma_\mu b_R) Z'^\mu + \text{h.c.}$$

The effective Hamiltonian for $b \rightarrow sl^+l^-$ is given as

$$\mathcal{H}_{\text{eff}}^{Z'} = \frac{8G_F}{\sqrt{2}} (\rho_{sb}^L \bar{s}_L \gamma_\mu b_L + \rho_{sb}^R \bar{s}_R \gamma_\mu b_R) (\rho_{ll}^L \bar{l}_L \gamma^\mu l_L + \rho_{ll}^R \bar{l}_R \gamma^\mu l_R)$$

NP scenario: Family non-universal Z' model

Different from VQM, the couplings in both the quark and lepton section are free parameters.

Too many free parameters. So we set $\rho_{sb}^R = 0$ in our analysis to reduce freedoms.

Z' also only affects C_9 and C_{10} phenomenally:

$$C_9^{Z'} = C_9 - \frac{4\pi \rho_{sb}^L (\rho_{ll}^L + \rho_{ll}^R)}{\alpha_{em} V_{tb} V_{ts}^*}, \quad C_{10}^{Z'} = C_{10} + \frac{4\pi \rho_{sb}^L (\rho_{ll}^L - \rho_{ll}^R)}{\alpha_{em} V_{tb} V_{ts}^*}$$

Constrain the model parameters by exp.

Data used for fitting

$b \rightarrow cl\bar{\nu}$ $(10.58 \pm 0.15) \times 10^{-2}$	$b \rightarrow sl^+l^-$ $(3.66^{+0.76}_{-0.77}) \times 10^{-6}$	$\bar{B}^0 \rightarrow K^*l^+l^-$ $(1.09^{+0.12}_{-0.11}) \times 10^{-6}$	
$q^2(\text{GeV}^2)$	$\mathcal{B}(10^{-7})$	F_L	$-A_{FB}$
[0, 2]	1.46 ± 0.41	0.29 ± 0.21	0.47 ± 0.32
[2, 4.3]	0.86 ± 0.32	0.71 ± 0.25	0.11 ± 0.37
[4.3, 8.68]	1.37 ± 0.61	0.64 ± 0.25	0.45 ± 0.26
[10.09, 12.86]	2.24 ± 0.48	0.17 ± 0.17	0.43 ± 0.20
[14.18, 16]	1.05 ± 0.30	-0.15 ± 0.28	0.70 ± 0.24
> 16	2.04 ± 0.31	0.12 ± 0.15	0.66 ± 0.16
[1, 6]	1.49 ± 0.47	0.67 ± 0.24	0.26 ± 0.31

Heavy Flavor Averaging Group, arXiv:1010.1589;
Particle Data Group, J. Phys. G 37,075021.

Definition of χ^2

$$\chi_i^2 = \frac{(B_i^{\text{the}} - B_i^{\text{exp}})^2}{(B_i^{\text{err}})^2}$$

Constrain the VQM parameters

$$\left. \begin{aligned} \operatorname{Re}\lambda_{sb} &= (0.07 \pm 0.04) \times 10^{-3} \\ \operatorname{Im}\lambda_{sb} &= (0.09 \pm 0.23) \times 10^{-3} \end{aligned} \right\} \rightarrow \left\{ \begin{array}{l} |\lambda_{sb}| < 0.3 \times 10^{-3} \\ \text{Phase less constrained} \end{array} \right.$$

Constraints on the Wilson coefficients

with $\chi^2/d.o.f. = 2.4$

$$|\Delta C_9| = |C_9 - C_9^{SM}| < 0.2$$

$$|\Delta C_{10}| = |C_{10} - C_{10}^{SM}| < 2.8$$

Constrain the Z' model parameters

Assume $\Delta C_9, \Delta C_{10}$ as real

$$\Delta C_9 = 0.88 \pm 0.75, \quad \Delta C_{10} = 0.01 \pm 0.69$$

Both ΔC_9 and ΔC_{10} are complex numbers.

$$\begin{aligned} \Delta C_9 &= (-0.81 \pm 1.22) + (3.05 \pm 0.92)i && \text{with } \chi^2/d.o.f. = 2.3 \\ \Delta C_{10} &= (1.00 \pm 1.28) + (-3.16 \pm 0.94)i && \text{with } \chi^2/d.o.f. = 2.4 \end{aligned}$$

$\text{Im}[C_{10}]$ has little effect on χ^2

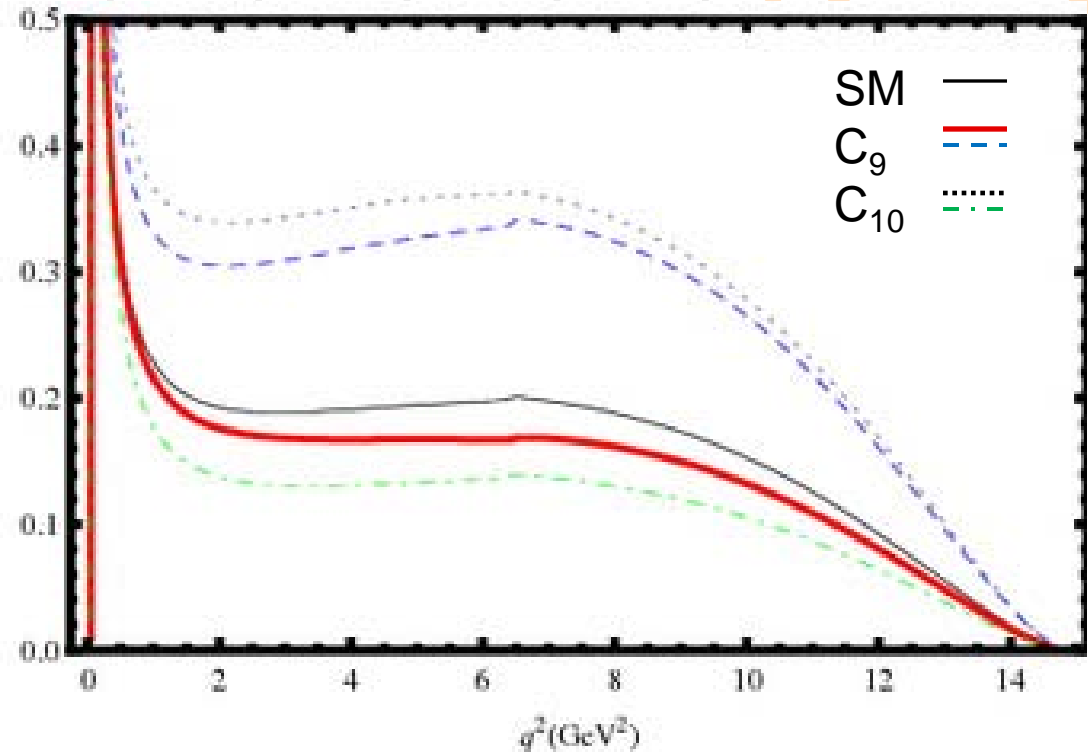
Combining the above results $|\Delta C_9| < 3, \quad |\Delta C_{10}| < 3$

New Physics effects in observables

In the NP effects, we choose $\Delta C_9 = 3e^{i\pi/4, i3\pi/4}$ and $\Delta C_{10} = 3e^{i\pi/4, i3\pi/4}$ as the reference points.

$$\frac{dBr}{dq^2}$$

Br (10^{-7}) may be enhanced, however, large uncertainties

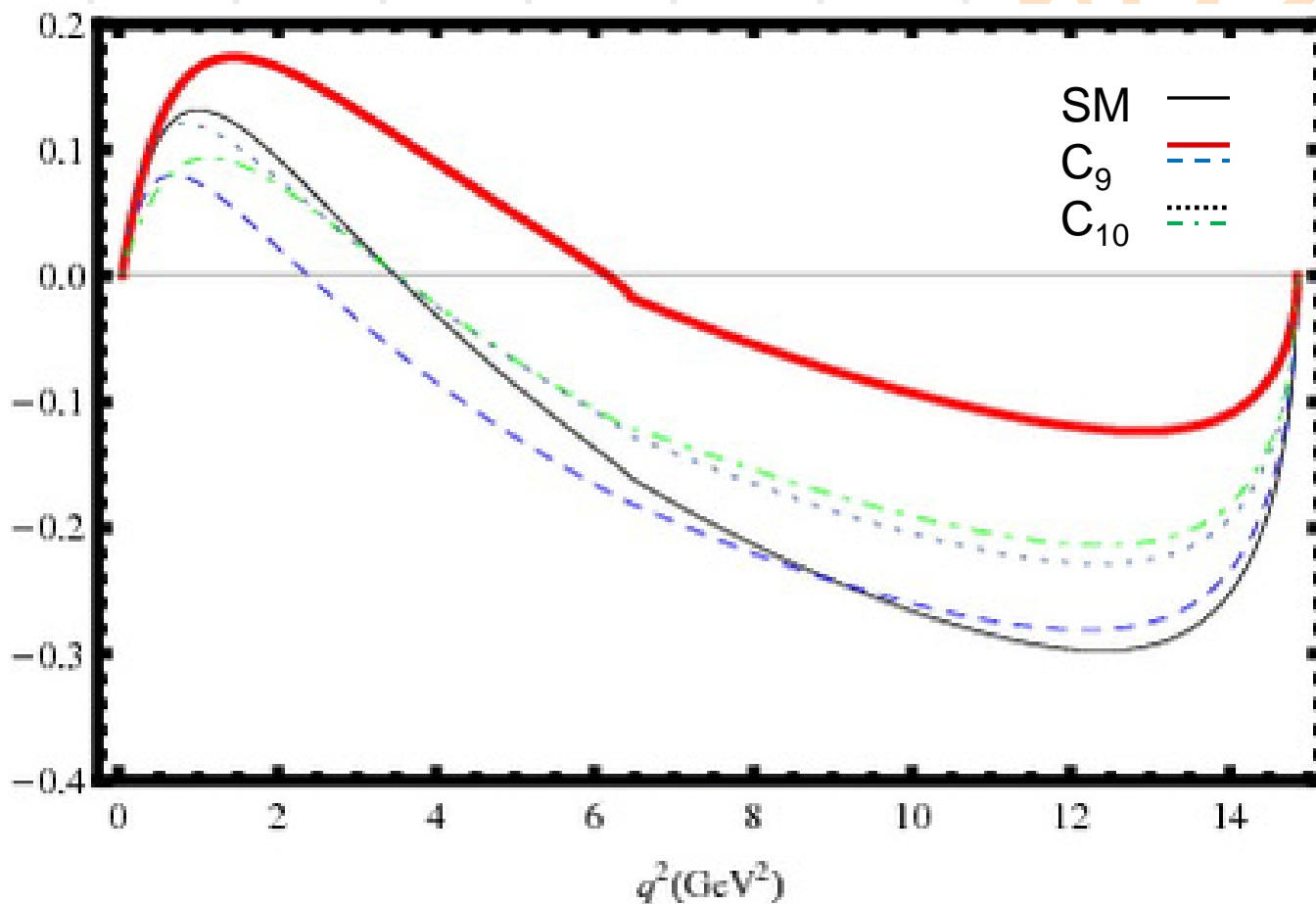


In this parameter space, $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$ is consistent with the recent measurement. $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 5.1 \times 10^{-8}$

New Physics effects in observable

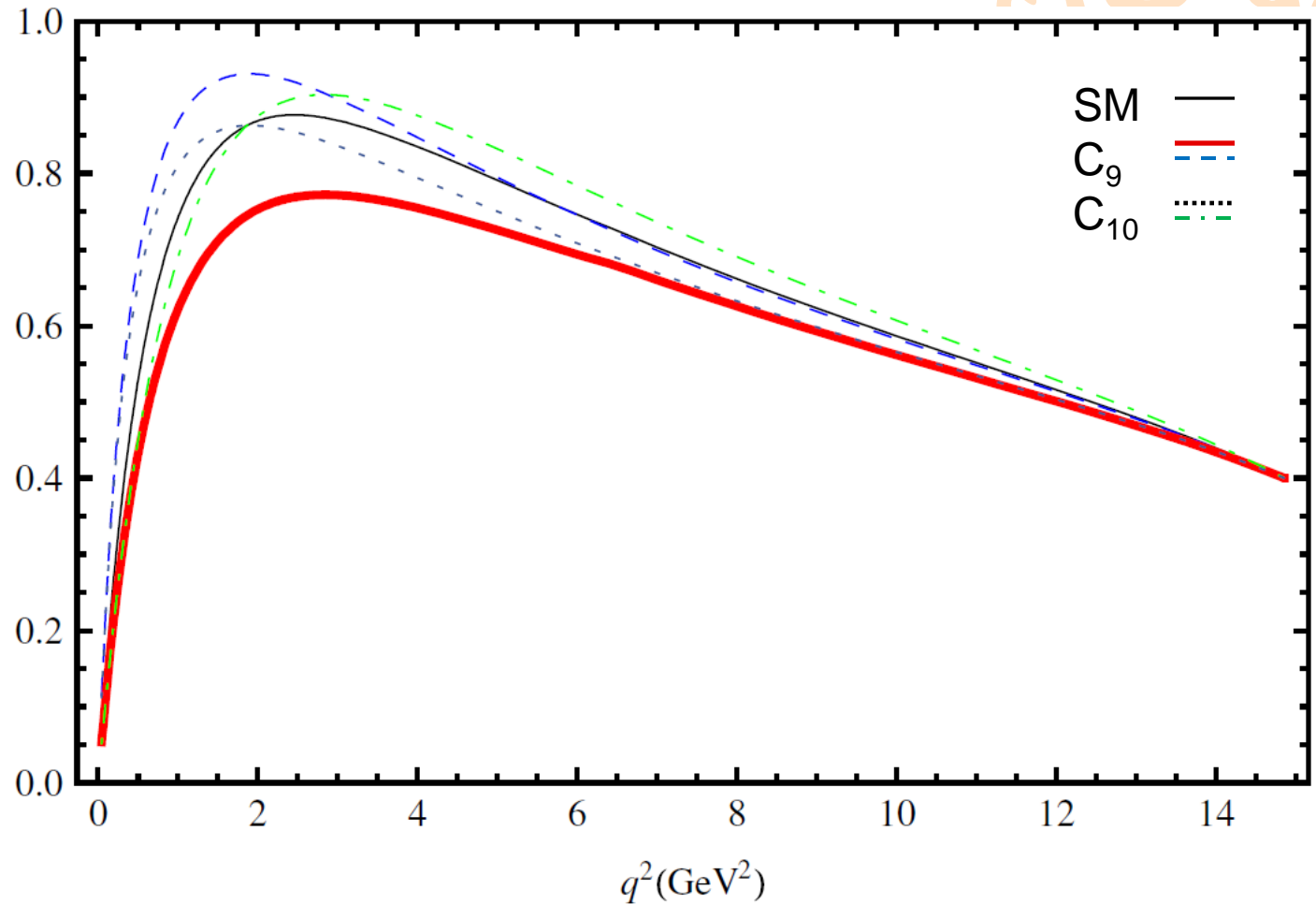
$$\overline{\frac{dA_{FB}}{dq^2}}$$

Zero-crossing point of AFB may be changed significantly in new physics model.



Polarization fraction f_L

some changes of Polarization fraction f_L in new physics model.



Summary



- $\bar{B}^0 \rightarrow K_2^*(\rightarrow K\pi)l^+l^-$ is investigated in SM.
 - ◆ $\mathcal{B}(B \rightarrow K_2^*\mu^+\mu^-) = (2.5_{-1.1}^{+1.6}) \times 10^{-7}$
 - ◆ expected to be observed in future Exp.

FBA, polarization fractions, etc, are investigated, with small uncertainties.

- Two NP scenarios (VQM, Z' model) are investigated.

Parameter space constrained with data of $\bar{B}^0 \rightarrow K^*l^+l^-$ and $b \rightarrow sl^+l^-$.

Zero-crossing point of FBA can be changed dramatically, which are sensitive to NP effects

吉祥

Thank you

