

Two recent exotic results from Fermilab & New light particles

(HyperCP events & D0 anomaly)

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Outline

- The HyperCP events
 - Experiments: HyperCP (Fermilab) , KTeV (Fermilab) , Belle (KEK) data
 - Theoretical interpretations: a new light particle
 - Implications to B decay processes

- The D0 anomalous like-sign dimuon charge asymmetry
 - Experimental data from D0 (Fermilab)
 - Theory: a model-independent approach with a light spin-1 particle

The HyperCP events

Introduction

- The detection of a new particle having a sub-GeV mass would likely hint at the presence of physics beyond the SM.
- This possibility has been raised recently by the observation of three events for the rare decay mode $\Sigma^+ \rightarrow p \mu^+ \mu^-$ with dimuon invariant masses narrowly clustered around 214.3 MeV by the HyperCP Collaboration a few years ago.

Evidence for the Decay $\Sigma^+ \rightarrow p\mu^+\mu^-$

H. K. Park,⁸ R. A. Burnstein,⁵ A. Chakravorty,⁵ Y. C. Chen,¹ W. S. Choong,^{2,7} K. Clark,⁹ E. C. Dukes,¹⁰ C. Durandet,¹⁰
J. Felix,⁴ Y. Fu,⁷ G. Gidal,⁷ H. R. Gustafson,⁸ T. Holmstrom,¹⁰ M. Huang,¹⁰ C. James,³ C. M. Jenkins,⁹ T. Jones,⁷
D. M. Kaplan,⁵ L. M. Lederman,⁵ N. Leros,⁶ M. J. Longo,^{8,*} F. Lopez,⁸ L. C. Lu,¹⁰ W. Luebke,⁵ K. B. Luk,^{2,7}
K. S. Nelson,¹⁰ J.-P. Perroud,⁶ D. Rajaram,⁵ H. A. Rubin,⁵ J. Volk,³ C. G. White,⁵ S. L. White,⁵ and P. Zyla⁷

(HyperCP Collaboration)

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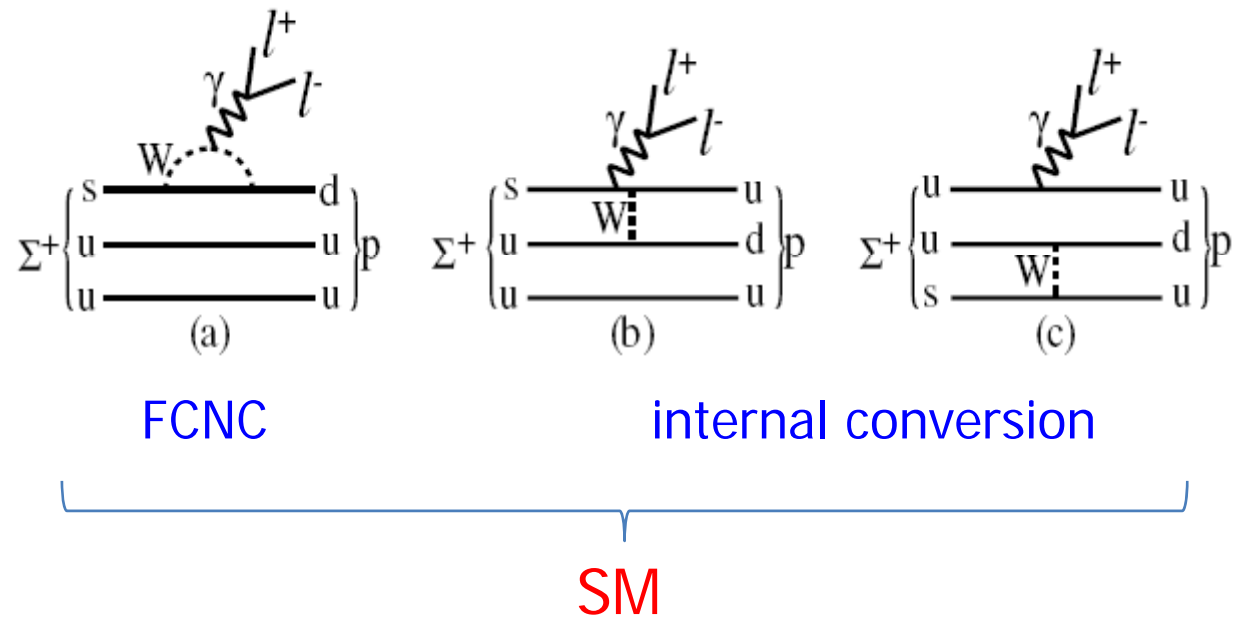
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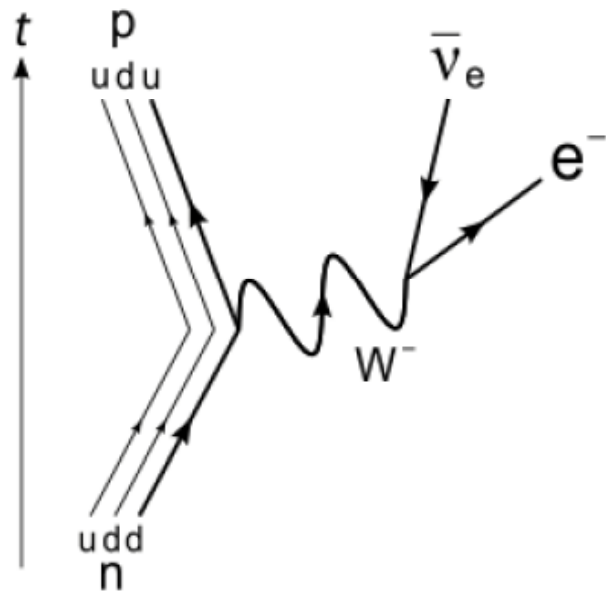
HyperCP data (Fermilab) (2/4)

$$\Sigma^+ \rightarrow p \mu^+ \mu^-$$

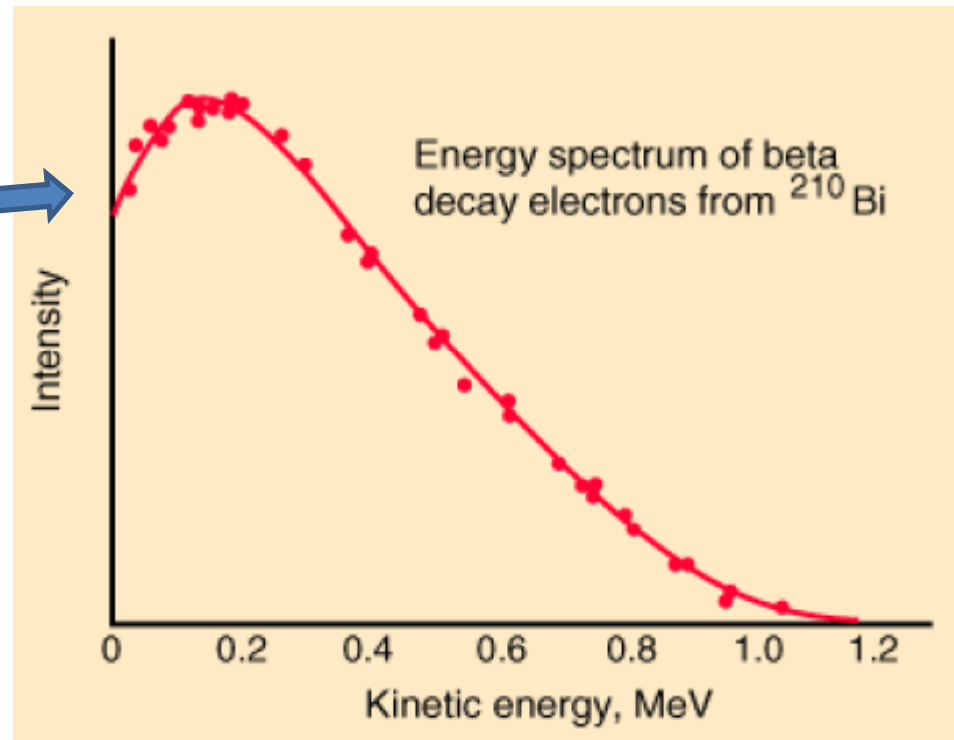
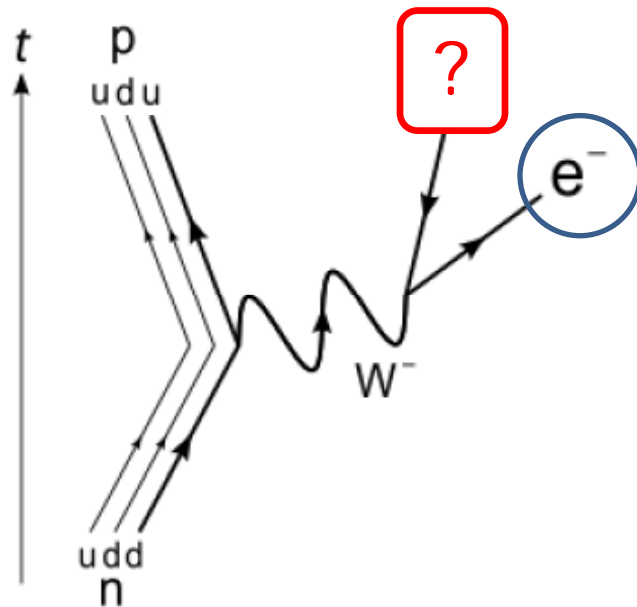
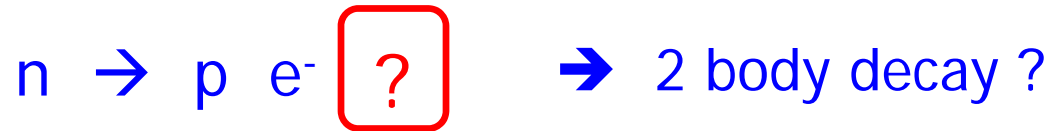


Digression: History of β decay (1/3)

$$n \rightarrow p e^- \bar{\nu}_e$$

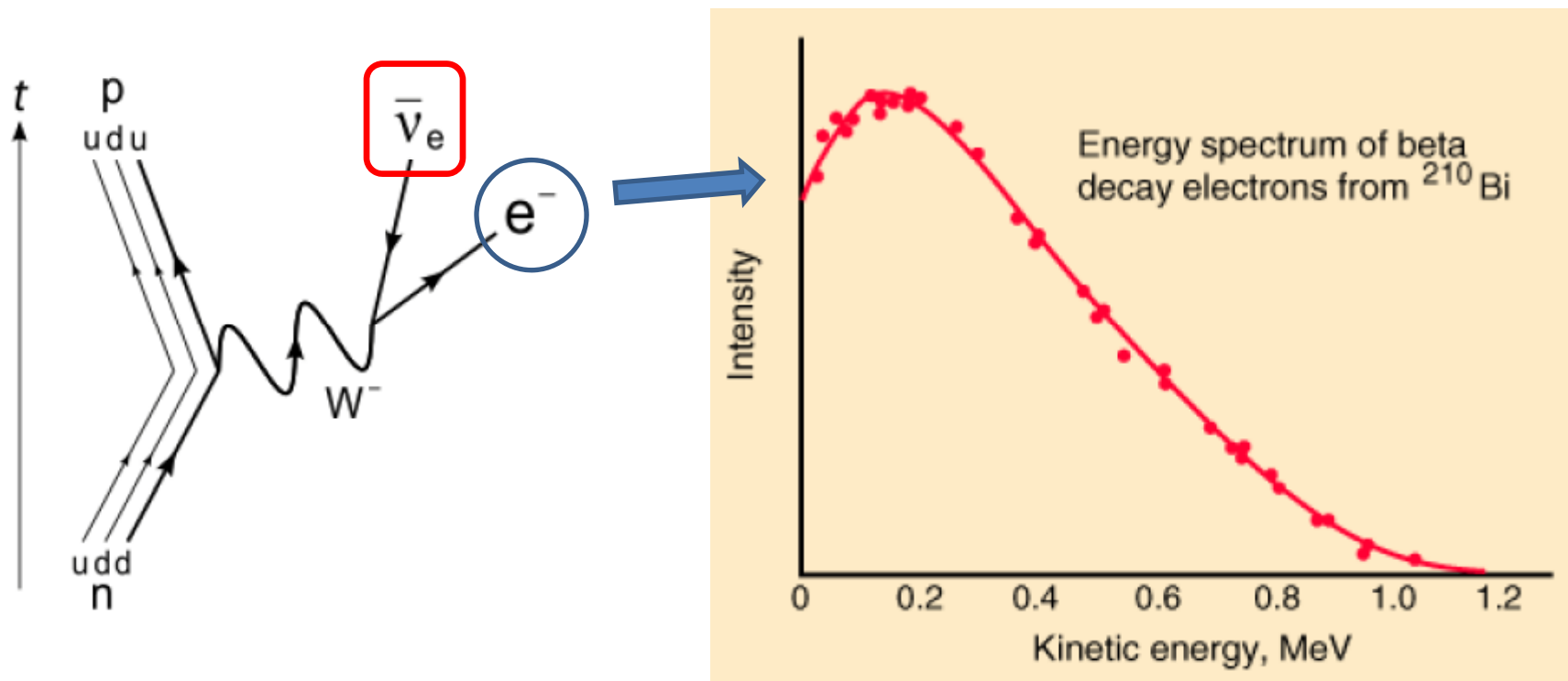


Digression: History of β decay (2/3)



Continuous energy spectrum

Digression: History of β decay (3/3)

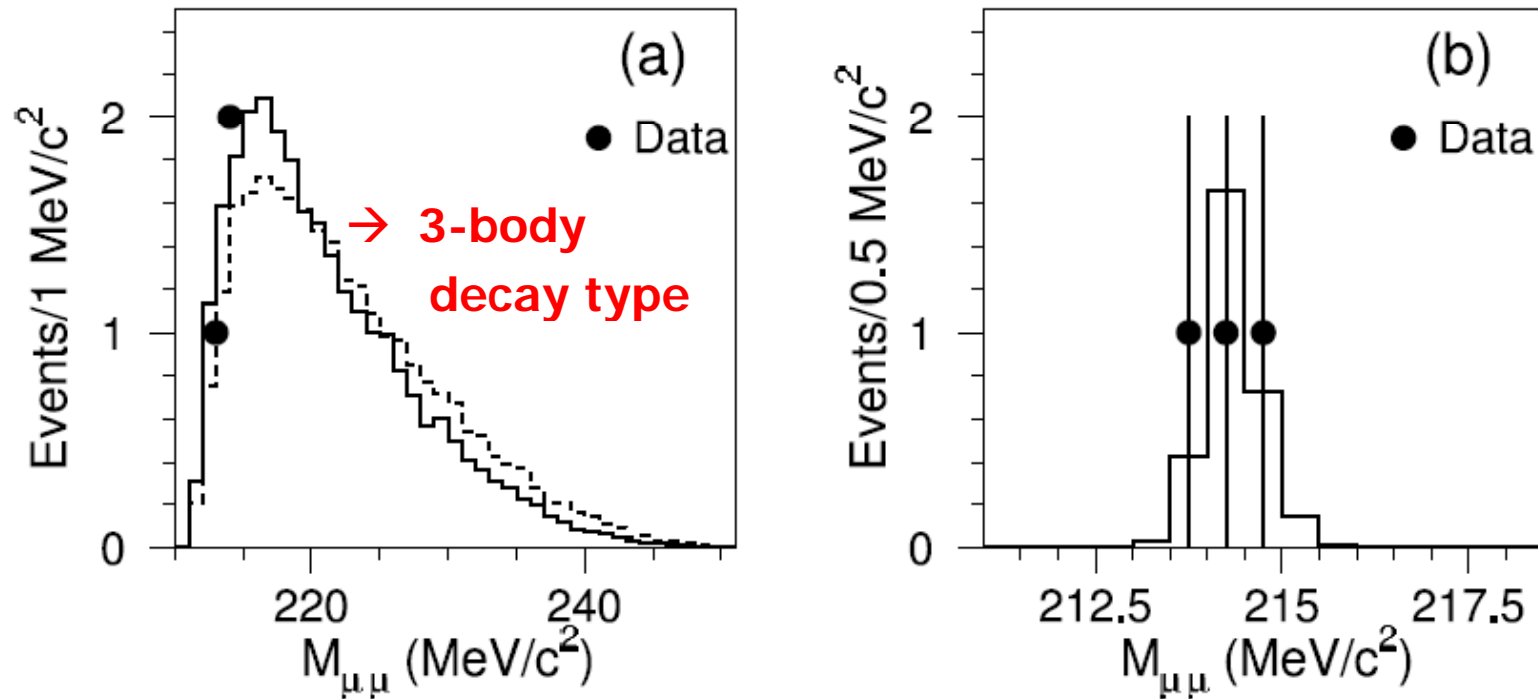
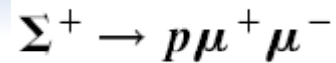


Continuous energy spectrum
→ 3 body decay

What if an **opposite** situation happens?

(i.e., 3 body decay ?? → No, 2 body decay !!)

HyperCP data (Fermilab) (3/4)



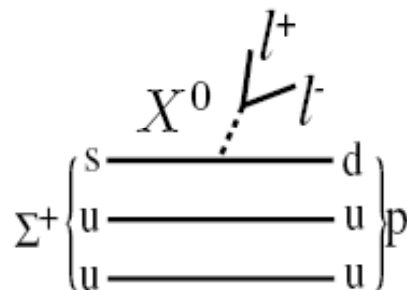
213.7, 214.3, 214.7 MeV/c^2

→ within 1 MeV/c^2 !!

FIG. 4. Real (points) and MC (histogram) dimuon mass distributions for (a) $\Sigma^+_{p\mu\mu}$ MC events (arbitrary normalization) with a form-factor decay (solid histogram) and uniform phase-space decay (dashed histogram) model, and (b) $\Sigma^+_{pP\mu\mu}$ MC events normalized to match the data.

HyperCP data (Fermilab) (4/4)

- The dimuon mass distribution for $\Sigma^+ \rightarrow p \mu^+ \mu^-$ decay is expected to be broad (\leftarrow 3-body decays).
- Assuming a “3-body decay,” the probability that the three events have the same dimuon mass (within $1 \text{ MeV}/c^2$) is less than 1% !!
- ➔ The unexpectedly narrow dimuon mass distribution may suggest a two-body decay:



$$\Sigma^+ \rightarrow pX^0, X^0 \rightarrow \mu^+\mu^-$$

with a X^0 mass of $214.3 \pm 0.5 \text{ MeV}/c^2$

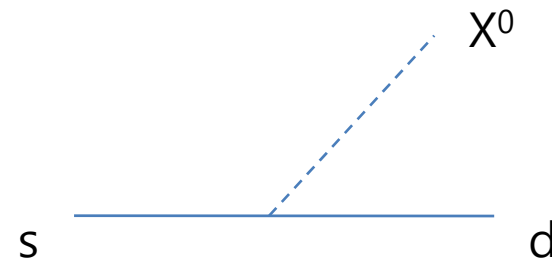
- In the spinless case, X^0 could be
 - Sgoldstino in SUSY models
D.S. Gorbunov and V.A. Rubakov (2006)
 - CP-odd Higgs boson in the next-to-minimal SUSY SM (NMSSM)
X.G. He, J. Tandean and G. Valencia (2007)
- In the spin-1 case, one possible candidate for X^0 is
 - Gauge (U) boson of an extra U(1) gauge group in some extensions of the SM
C.H. Chen, C.Q. Geng, and C.W. Kao (2008);
M. Pospelov (2008); M. Reece and L.T. Wang (2009)

Possible new particle (X^0) interpretations (2/2)

- The presence of X^0 in $\Sigma^+ \rightarrow p \mu^+ \mu^-$ implies that it also contributes to other $|\Delta S| = 1$ transitions: e.g., $K \rightarrow \pi \mu^+ \mu^-$.

$$\mathcal{L}_{qq'X} = i\bar{q}'(g_S + g_P\gamma_5)q X + \text{H.c.}$$

(Spin 0 case)



- The "scalar part" of the s-d- X coupling is already constrained by $K \rightarrow \pi \mu \mu$ data to be negligibly small.

The "pseudoscalar part" of the s-d- X coupling can be probed by $K \rightarrow \pi \pi \mu \mu$ measurements.
 → KTeV experiment

KTeV data (Fermilab)

$$\text{Br}(K_L \rightarrow \pi^0 \pi^0 X^0 \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) < 9.44 \times 10^{-11}$$

arXiv:0911.4516

$$\mathcal{B}(K_L \rightarrow \pi^0 \pi^0 X_P \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (8.3_{-6.6}^{+7.5}) \times 10^{-9}$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \pi^0 X_A \rightarrow \pi^0 \pi^0 \mu^+ \mu^-) = (1.0_{-0.8}^{+0.9}) \times 10^{-10}$$

He, Tandean, Valencia

- The scenario in which X has spin 0 and its s-d- X pseudoscalar coupling is “real” is disfavored.
 - ➔ But, the case where the s-d- X pseudoscalar coupling is almost “purely imaginary” is still allowed.
- The scenario in which X has spin 1 is not yet strongly challenged by the KTeV data.

Belle data (KEK)

$$\mathcal{B}(B^0 \rightarrow K^{*0}X^0, K^{*0} \rightarrow K^+\pi^-, X^0 \rightarrow \mu^+\mu^-) < 2.01 \times 10^{-8}$$

$$\mathcal{B}(B^0 \rightarrow \rho^0X^0, \rho^0 \rightarrow \pi^+\pi^-, X^0 \rightarrow \mu^+\mu^-) < 1.51 \times 10^{-8}$$

PRL 105, 091801 (2010)

- This results rule out some of “sgoldstino” scenario.
 - ➔ The Belle result also restricts the **spinless X^0** scenario.

Focus on B decays

- Various B meson decay processes can be used to search for the hypothetical new particle X^0 .

→ B decays become important to probe the X^0 .

- Consider the contributions of X with “spin 1.” C.H. Chen & C.Q. Geng (2007)

- Adopt a model-independent approach.

- Our assumptions are

- Assume that X has both “vector” and “axial-vector” couplings to b-d & b-s.

- X does not interact strongly and decays inside the detector

with $\mathcal{B}(X \rightarrow \mu^+ \mu^-) = 1$.

Effective Lagrangian with a Light X^0

- Assuming that X has spin 1 & does not carry electric or color charge, the Lagrangian describing the effective b - q - X couplings ($q = d, s$) is

$$\begin{aligned}\mathcal{L}_{bqX} &= -\bar{q}\gamma_\mu(g_{Vq} - g_{Aq}\gamma_5)b X^\mu + \text{H.c.} \\ &= -\bar{q}\gamma_\mu(g_{Lq}P_L + g_{Rq}P_R)b X^\mu + \text{H.c.}\end{aligned}$$

$$g_{Lq,Rq} = g_{Vq} \pm g_{Aq}, \quad P_{L,R} = \frac{1}{2}(1 \mp \gamma_5).$$

Generally, the constants $g_{Vq,Aq}$ can be complex.

B⁰ - bar B⁰ mixing (1/3)

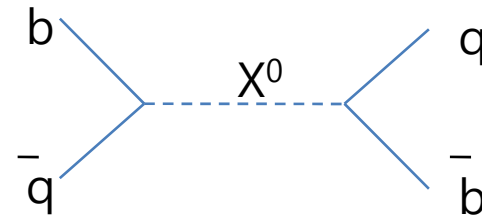
- It is characterized by the physical mass difference ΔM_q ($q = d, s$) between the heavy and light mass-eigenstates in the B_q^0 - \bar{B}_q^0 system.

$$\Delta M_q = 2 |M_{12}^q|, \quad \text{where } M_{12}^q = M_{12}^{q,\text{SM}} + M_{12}^{q,X}$$

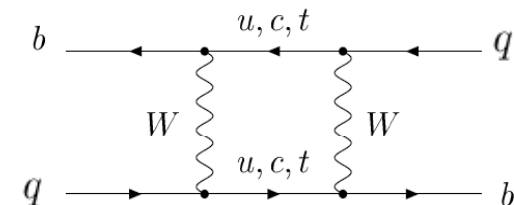
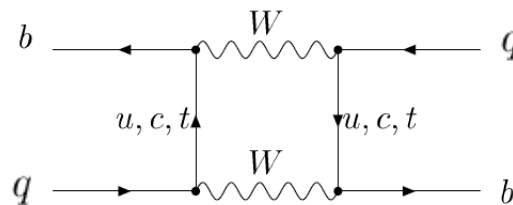
$$2m_{B_q} M_{12}^q = \langle B_q^0 | \mathcal{H}_{b\bar{q} \rightarrow \bar{b}q} | \bar{B}_q^0 \rangle$$



$$\Delta M_q^{\text{exp}} = \Delta M_q^{\text{SM}} |1 + \delta_q|, \quad \delta_q = \frac{M_{12}^{q,X}}{M_{12}^{q,\text{SM}}}$$



$$\delta_q = \frac{M_{12}^{q,X}}{M_{12}^{q,\text{SM}}} =$$



$B^0 - \bar{B}^0$ mixing (2/3)

$$\begin{aligned} \text{Re } \delta_d &= \left\{ -4.4 \left[(\text{Re } g_{Vd})^2 - (\text{Im } g_{Vd})^2 \right] - 8.2 (\text{Re } g_{Vd})(\text{Im } g_{Vd}) \right. \\ &\quad \left. + 17 \left[(\text{Re } g_{Ad})^2 - (\text{Im } g_{Ad})^2 \right] + 33 (\text{Re } g_{Ad})(\text{Im } g_{Ad}) \right\} \times 10^{12} \\ \text{Re } \delta_s &= \left\{ -2.5 \left[(\text{Re } g_{Vs})^2 - (\text{Im } g_{Vs})^2 \right] + 0.2 (\text{Re } g_{Vs})(\text{Im } g_{Vs}) \right. \\ &\quad \left. + 9.9 \left[(\text{Re } g_{As})^2 - (\text{Im } g_{As})^2 \right] - 0.7 (\text{Re } g_{As})(\text{Im } g_{As}) \right\} \times 10^{11} \end{aligned}$$

(1) $q = d$

$$\Delta M_d^{\text{exp}} = (0.507 \pm 0.005) \text{ ps}^{-1} \quad \Delta M_d^{\text{SM}} = (0.563_{-0.076}^{+0.068}) \text{ ps}^{-1}$$

using the approximation $|1 + \delta_d| \simeq 1 + \text{Re } \delta_d$,



$$-0.22 \leq \text{Re } \delta_d \leq +0.02$$

(2) $q = s$

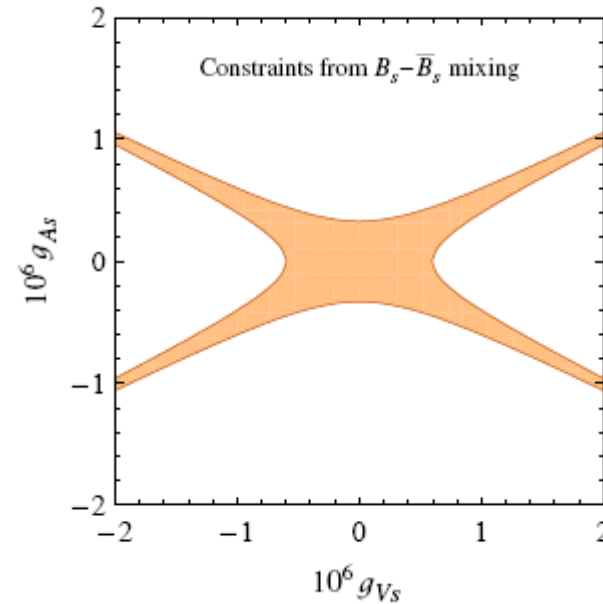
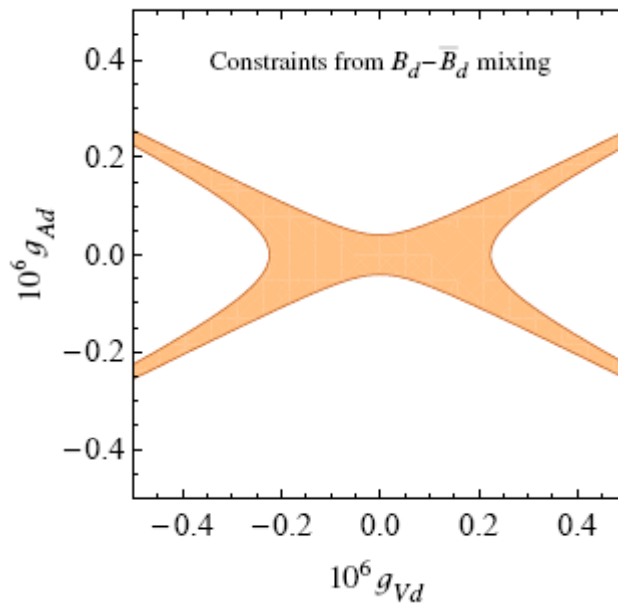
$$\Delta M_s^{\text{exp}} = (17.77 \pm 0.12) \text{ ps}^{-1} \quad \Delta M_s^{\text{SM}} = (17.6_{-1.8}^{+1.7}) \text{ ps}^{-1}$$



$$-0.09 \leq \text{Re } \delta_s \leq 0.11$$

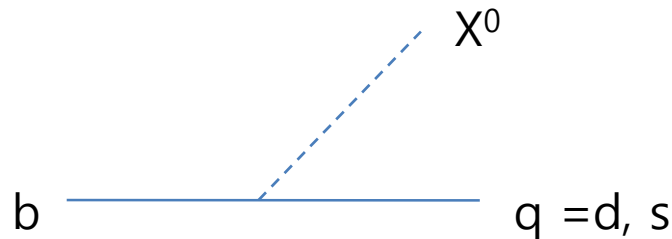
B⁰ - bar B⁰ mixing (3/3)

$$\begin{aligned}
 -0.7 \times 10^{-14} &< (\text{Re } g_{Vd})^2 - (\text{Im } g_{Vd})^2 + 1.9 (\text{Re } g_{Vd})(\text{Im } g_{Vd}) < 5.0 \times 10^{-14} \\
 -1.3 \times 10^{-14} &< (\text{Re } g_{Ad})^2 - (\text{Im } g_{Ad})^2 + 1.9 (\text{Re } g_{Ad})(\text{Im } g_{Ad}) < 0.2 \times 10^{-14} \\
 -4.4 \times 10^{-13} &< (\text{Re } g_{Vs})^2 - (\text{Im } g_{Vs})^2 - 0.1 (\text{Re } g_{Vs})(\text{Im } g_{Vs}) < 3.6 \times 10^{-13} \\
 -0.9 \times 10^{-13} &< (\text{Re } g_{As})^2 - (\text{Im } g_{As})^2 - 0.1 (\text{Re } g_{As})(\text{Im } g_{As}) < 1.1 \times 10^{-13}
 \end{aligned}$$



if $g_{Vq, Aq}$ are taken to be real.

Inclusive decay $b \rightarrow q X$



- Decay rate:

$$\Gamma(b \rightarrow qX) = \frac{|p_X|}{8\pi m_b^2 m_X^2} \left\{ |g_{Vq}|^2 \left[(m_b + m_q)^2 + 2m_X^2 \right] \left[(m_b - m_q)^2 - m_X^2 \right] \right. \\ \left. + |g_{Aq}|^2 \left[(m_b - m_q)^2 + 2m_X^2 \right] \left[(m_b + m_q)^2 - m_X^2 \right] \right\}$$

- Branching ratio:

$$\mathcal{B}(b \rightarrow sX) \simeq \frac{\Gamma(b \rightarrow sX)}{\Gamma_{B_d^0}} = 8.55 \times 10^{13} (|g_{Vs}|^2 + |g_{As}|^2) \quad \searrow$$

- BaBar data:

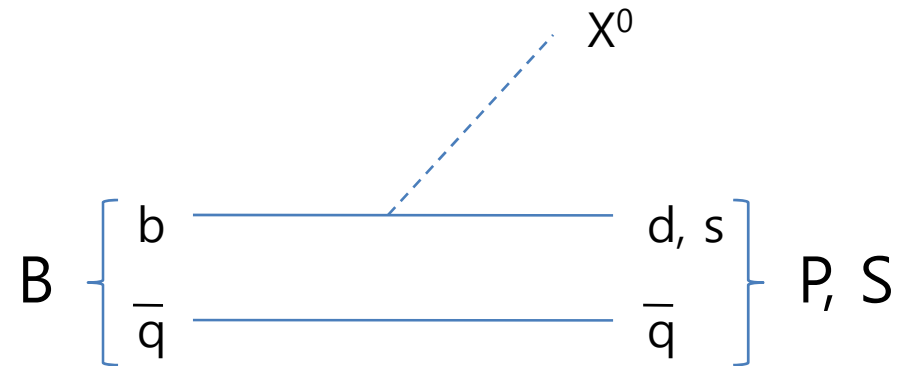
$$|g_{Vs}|^2 + |g_{As}|^2 < 8.0 \times 10^{-21}$$

$$\mathcal{B}(b \rightarrow sl^+l^-)_{m_{\ell\ell} \in [0.2 \text{ GeV}, 1.0 \text{ GeV}]} = (0.08 \pm 0.36_{-0.04}^{+0.07}) \times 10^{-6} \quad \swarrow$$

the average over $\ell = e$ and μ .

$$\mathcal{B}(b \rightarrow sX) < 6.8 \times 10^{-7} \quad 90\% \text{-C.L.}$$

B → P X decays (1/2)



- Decay amplitude & rate:

$$\mathcal{M}(\bar{B} \rightarrow PX) = \frac{2g_{Vq}}{\kappa_P} F_1^{BP} \varepsilon_X^* \cdot p_P$$

the vector coupling only!

$$\mathcal{M}(\bar{B} \rightarrow SX) = \frac{2ig_{Aq}}{\kappa_S} F_1^{BS} \varepsilon_X^* \cdot p_S$$

the axial-vector coupling only!

$$\Gamma(B \rightarrow P(S)X) = \frac{|\mathbf{p}_X|^3}{2\pi \kappa_{P(S)}^2 m_X^2} |g_{V(A)q} F_1^{BP(S)}|^2$$

B → P X decays (2/2)

$$\mathcal{B}(B^+ \rightarrow \pi^+ X) = 1.06 \times 10^{13} |g_{Vd}|^2$$

$$\mathcal{B}(B_d \rightarrow \pi^0 X) = 4.96 \times 10^{12} |g_{Vd}|^2$$

$$\mathcal{B}(B^+ \rightarrow K^+ X) \simeq \mathcal{B}(B_d \rightarrow K^0 X) = 1.85 \times 10^{13} |g_{Vs}|^2$$

Exp. data:

$$\mathcal{B}(B^+ \rightarrow \pi^+ \mu^+ \mu^-) < 6.9 \times 10^{-8}$$

$$\mathcal{B}(B_d \rightarrow \pi^0 \mu^+ \mu^-) < 1.84 \times 10^{-7} \quad \text{at 90\% C.L.}$$

$$\mathcal{B}(B \rightarrow K \mu^+ \mu^-)_{m_{\mu\mu} \leq 2 \text{ GeV}} = (0.81_{-0.16}^{+0.18} \pm 0.05) \times 10^{-7}$$

$$\mathcal{B}(B \rightarrow K X) < 3.2 \times 10^{-8}$$

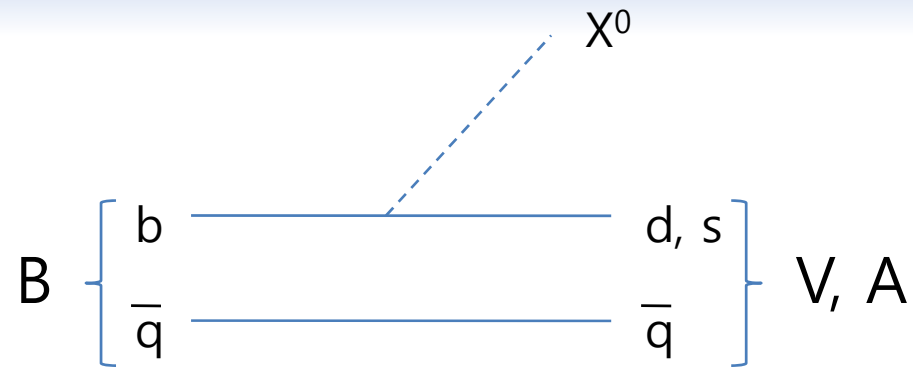


$$|g_{Vd}|^2 < 6.5 \times 10^{-21}$$

$$|g_{Vs}|^2 < 1.7 \times 10^{-21}$$

most stringent
constraints !

B → V X decays



$$\mathcal{B}(B_d^0 \rightarrow \rho^0 X) = 1.77 \times 10^{10} |g_{Vd}|^2 + \underline{6.18 \times 10^{12} |g_{Ad}|^2}$$

$$\mathcal{B}(B_d^0 \rightarrow K^{*0} X) = 5.45 \times 10^{10} |g_{Vs}|^2 + \underline{1.79 \times 10^{13} |g_{As}|^2}$$

Belle data:

$$\mathcal{B}(B_d \rightarrow \rho^0 X) < 0.81 \times 10^{-8}$$

$$\mathcal{B}(B_d \rightarrow K^{*0} X) < 2.3 \times 10^{-8} \quad \text{at 90\% C.L.}$$



$$0.00286 |g_{Vd}|^2 + |g_{Ad}|^2 < 1.3 \times 10^{-21}$$

$$0.00304 |g_{Vs}|^2 + |g_{As}|^2 < 1.3 \times 10^{-21}$$

Combining $B \rightarrow PX$ & VX decays

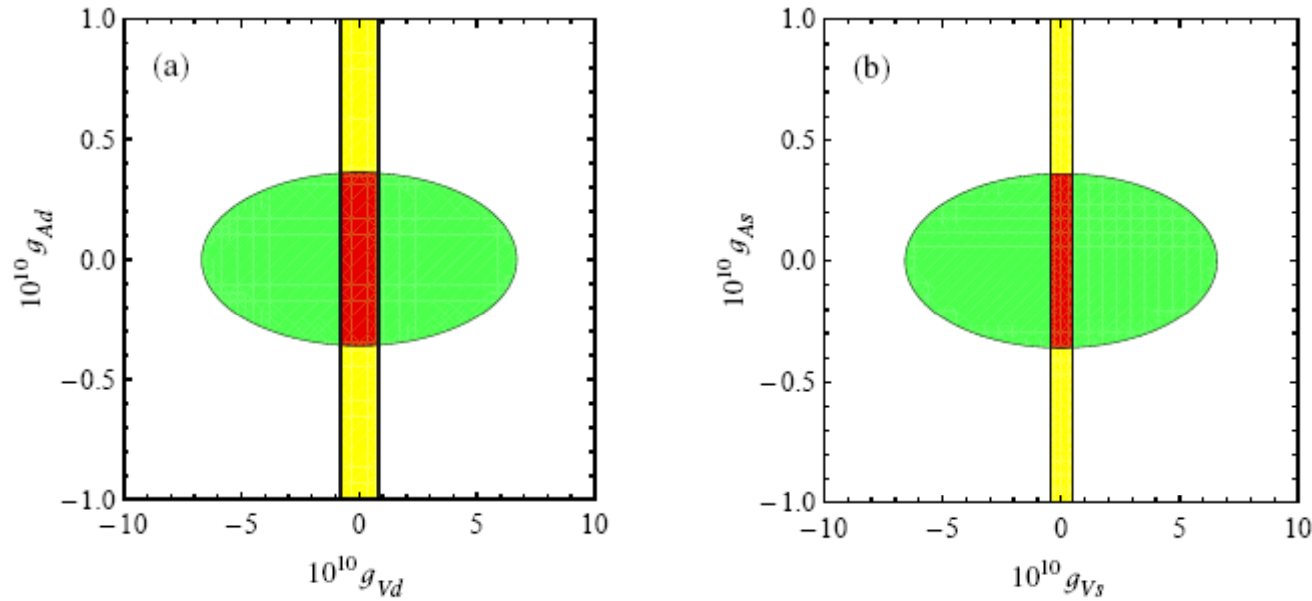


FIG. 3: Parameter space of g_{Vq} and g_{Aq} , taken to be real, subject to constraints on (a) $B \rightarrow \pi X$ (lightly shaded, yellow region), $B \rightarrow \rho X$ (medium shaded, green region), and both of them (heavily shaded, red region) and (b) $B \rightarrow KX$ (lightly shaded, yellow region), $B \rightarrow K^*X$ (medium shaded, green region), and both of them (heavily shaded, red region).

$$\begin{aligned}
 |g_{Vd}|^2 &< 6.5 \times 10^{-21}, & |g_{Ad}|^2 &< 1.3 \times 10^{-21} \\
 |g_{Vs}|^2 &< 1.7 \times 10^{-21}, & |g_{As}|^2 &< 1.3 \times 10^{-21}
 \end{aligned}$$

Our predictions: $B \rightarrow P X$ decays

- Using g_{Vd} bounds:

$$\mathcal{B}(B_d^0 \rightarrow \pi^0 X) < 3.2 \times 10^{-8}$$

$$\mathcal{B}(B_d^0 \rightarrow \eta X) < 2.4 \times 10^{-8},$$

$$\underline{\mathcal{B}(B_s^0 \rightarrow K^0 X) < 8.2 \times 10^{-8}},$$

$$\mathcal{B}(B_d^0 \rightarrow \eta' X) < 1.6 \times 10^{-8},$$

$$\mathcal{B}(B_c \rightarrow D_d^+ X) < 1.7 \times 10^{-8}$$

- Using g_{Vs} bounds:

$$\mathcal{B}(B_s^0 \rightarrow \eta X) < 1.2 \times 10^{-8},$$

$$\mathcal{B}(B_s^0 \rightarrow \eta' X) < 1.7 \times 10^{-8}$$

$$\mathcal{B}(B_c \rightarrow D_s^+ X) < 2.3 \times 10^{-9},$$

Our predictions: $B \rightarrow V X$ decays

- Using g_{Vd} & g_{Ad} bounds:

$$\begin{aligned} \mathcal{B}(B^+ \rightarrow \rho^+ X) &< 1.7 \times 10^{-8}, & \mathcal{B}(B_d^0 \rightarrow \omega X) &< 7.0 \times 10^{-9}, \\ \mathcal{B}(B_s^0 \rightarrow K^{*0} X) &< 2.2 \times 10^{-8}, & \mathcal{B}(B_c \rightarrow D_d^{*+} X) &< 5.0 \times 10^{-9} \end{aligned}$$

- Using g_{Vs} & g_{As} bounds:

$$\mathcal{B}(B_s^0 \rightarrow \phi X) < 3.9 \times 10^{-8}, \quad \mathcal{B}(B_c \rightarrow D_s^{*+} X) < 3.9 \times 10^{-9}$$

Our predictions: $B \rightarrow SX$ & AX

- $B \rightarrow SX$

In contrast to the $B \rightarrow PX$ case, g_{Aq} is the only relevant coupling !

$$\mathcal{B}(B^+ \rightarrow a_0^+(1450)X) < 1.1 \times 10^{-8}, \quad \mathcal{B}(B_d^0 \rightarrow a_0^0(1450)X) < 5.1 \times 10^{-9}$$
$$\mathcal{B}(B^+ \rightarrow K_0^{*+}(1430)X) \simeq \mathcal{B}(B_d^0 \rightarrow K_0^{*0}(1430)X) < 1.0 \times 10^{-8}.$$

- $B \rightarrow AX$

In contrast to the $B \rightarrow VX$ case, the g_{Vq} term in the longitudinal component H_0 is dominant.

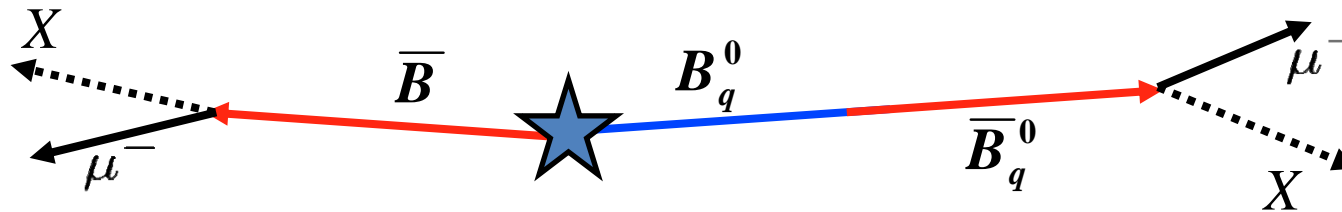
$$\mathcal{B}(B^+ \rightarrow a_1^+(1260)X) \simeq 2\mathcal{B}(B_d^0 \rightarrow a_1^0(1260)X) < 1.6 \times 10^{-8}$$
$$\mathcal{B}(B^+ \rightarrow b_1^+(1235)X) \simeq 2\mathcal{B}(B_d^0 \rightarrow b_1^0(1235)X) < 1.2 \times 10^{-7}$$
$$\mathcal{B}(B^+ \rightarrow K_1^{*+}(1270)X) \simeq \mathcal{B}(B_d^0 \rightarrow K_1^{*0}(1270)X) < 2.6 \times 10^{-8}$$
$$\mathcal{B}(B^+ \rightarrow K_1^{*+}(1400)X) \simeq \mathcal{B}(B_d^0 \rightarrow K_1^{*0}(1400)X) < 1.3 \times 10^{-8}$$

Summary

- The possibility that X has spin 1 is not well challenged by experiment yet.
- Various B meson decay processes can be used to search for the hypothetical new particle X^0 .
 - ➔ The $B \rightarrow M X$ branching ratios are predicted to reach the 10^{-7} level, which is comparable to the upper limits ($\sim 10^{-8}$) for the branching ratios of $B \rightarrow \rho^0 X, K^{*0} X$ recently measured by Belle.
- We would like to encourage our experimental colleagues to make more efforts to search for the X^0 , e.g., at Belle II and LHCb experiments.

The D0 anomaly

D0 Anomaly (1/2)



- ◆ The D0 Collaboration, with 6.1 fb^{-1} of data anomalously large CP violation in the like-sign dimuon charge asymmetry

$$A_{\text{sl}}^b \equiv \frac{N_b^{++} - N_b^{--}}{N_b^{++} + N_b^{--}}$$

where N_b^{++} and N_b^{--} represent the number of events containing two b hadrons decaying semileptonically and producing two positive or two negative muons, respectively.

The D0 result

$$A_{\text{sl}}^b = -(9.57 \pm 2.51 \pm 1.46) \times 10^{-3}$$

3.2 σ away from the standard model (SM) prediction of -0.2×10^{-3}

D0 Anomaly (2/2)

- ◆ A_{sl}^b is related to the asymmetries $a_{\text{sl}}^{d,s}$ in B_d and B_s decays by

$$A_{\text{sl}}^b = (0.506 \pm 0.043)a_{\text{sl}}^d + (0.494 \pm 0.043)a_{\text{sl}}^s$$

a_{sl}^q is the “wrong-charge” asymmetry,

$$a_{\text{sl}}^q \equiv \frac{\Gamma(\bar{B}_q \rightarrow \mu^+ X) - \Gamma(B_q \rightarrow \mu^- X)}{\Gamma(\bar{B}_q \rightarrow \mu^+ X) + \Gamma(B_q \rightarrow \mu^- X)}$$

- ◆ Using the current experimental value $a_{\text{sl}}^d = -0.0047 \pm 0.0046$ which is consistent with zero

to obtain the D0 value of A_{sl}^b

$$a_{\text{sl}}^s = -0.0146 \pm 0.0075$$

much larger than the SM prediction $(2.1 \pm 0.6) \times 10^{-5}$

Partial List of References (appeared in 2010)

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~ 70 papers so far

Theory (1/2)

- ◆ mass and width differences ΔM_s and $\Delta\Gamma_s$, respectively,
between the heavy and light mass-eigenstates in the B_s - \bar{B}_s system
off-diagonal elements M_s^{12} and Γ_s^{12} of the mass and decay matrices, respectively,
which characterize B_s - \bar{B}_s mixing.

$$(\Delta M_s)^2 - \frac{1}{4}(\Delta\Gamma_s)^2 = 4 |M_s^{12}|^2 - |\Gamma_s^{12}|^2$$

$$\Delta M_s \Delta\Gamma_s = 4 |M_s^{12}| |\Gamma_s^{12}| \cos \phi_s$$

$$\phi_s = \arg(-M_s^{12}/\Gamma_s^{12})$$

$$a_{\text{sl}}^s = \frac{4 |M_s^{12}| |\Gamma_s^{12}| \sin \phi_s}{4 |M_s^{12}|^2 + |\Gamma_s^{12}|^2}$$

Theory (2/2)

- ◆ Since $\Delta\Gamma_s \ll \Delta M_s$ and $|\Gamma_s^{12}| \ll |M_s^{12}|$,

$$\Delta M_s \simeq 2 |M_s^{12}|, \quad \Delta\Gamma_s \simeq 2 |\Gamma_s^{12}| \cos \phi_s$$

$$a_{sl}^s \simeq \frac{|\Gamma_s^{12}| \sin \phi_s}{|M_s^{12}|} \simeq \frac{2 |\Gamma_s^{12}| \sin \phi_s}{\Delta M_s}$$

- ◆ Experimental values

$$\Delta M_s^{\text{exp}} = 17.77 \pm 0.12 \text{ ps}^{-1}$$

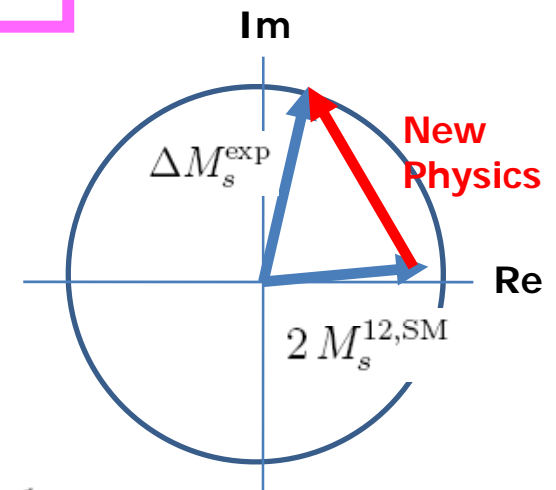
$$\Delta\Gamma_s^{\text{exp}} = 0.062_{-0.037}^{+0.034} \text{ ps}^{-1}$$

- ◆ SM predictions

$$2 M_s^{12,\text{SM}} = 20.1(1 \pm 0.40) e^{-0.035i} \text{ ps}^{-1}$$

$$2 |\Gamma_s^{12,\text{SM}}| = 0.096 \pm 0.039 \text{ ps}^{-1}$$

$$\phi_s^{\text{SM}} = (4.2 \pm 1.4) \times 10^{-3} = 0.24^\circ \pm 0.08^\circ$$



Lenz, Nieste;
Kubo, Lenz

Effective Lagrangian with a Light X^0

- ◆ Assuming that X has spin 1 & does not carry electric or color charge, the Lagrangian describing the effective b - q - X couplings ($q = d, s$) is

$$\begin{aligned}\mathcal{L}_{bqX} &= -\bar{q}\gamma_\mu(g_{Vq} - g_{Aq}\gamma_5)b X^\mu + \text{H.c.} \\ &= -\bar{q}\gamma_\mu(g_{Lq}P_L + g_{Rq}P_R)b X^\mu + \text{H.c.}\end{aligned}$$

$$g_{Lq,Rq} = g_{Vq} \pm g_{Aq}, \quad P_{L,R} = \frac{1}{2}(1 \mp \gamma_5).$$

Generally, the constants $g_{Vq,Aq}$ can be complex.

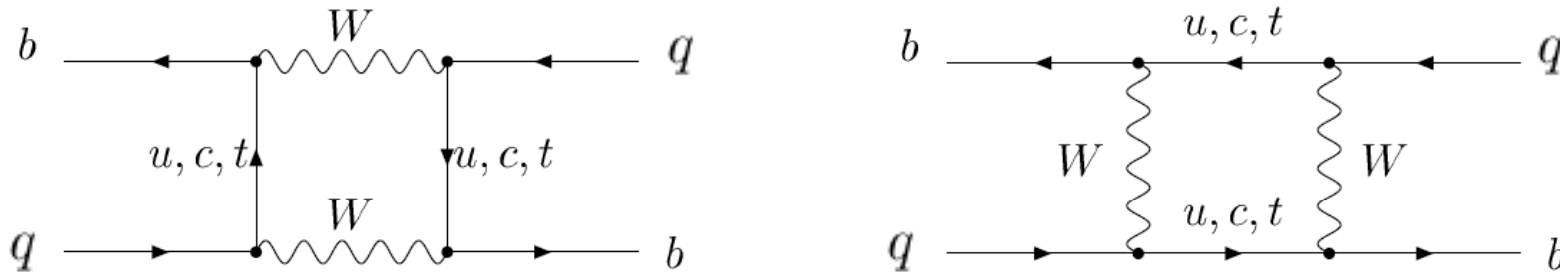
$B^0 - \bar{B}^0$ mixing: M_s^{12} (1/3)

- It is characterized by the physical mass difference ΔM_q ($q = d, s$) between the heavy and light mass-eigenstates in the $B_q^0 - \bar{B}_q^0$ system.

$$\Delta M_q = 2 |M_{12}^q|, \quad \text{where } M_{12}^q = M_{12}^{q,\text{SM}} + M_{12}^{q,X}$$

$$2m_{B_q} M_{12}^q = \langle B_q^0 | \mathcal{H}_{b\bar{q} \rightarrow \bar{b}q} | \bar{B}_q^0 \rangle$$

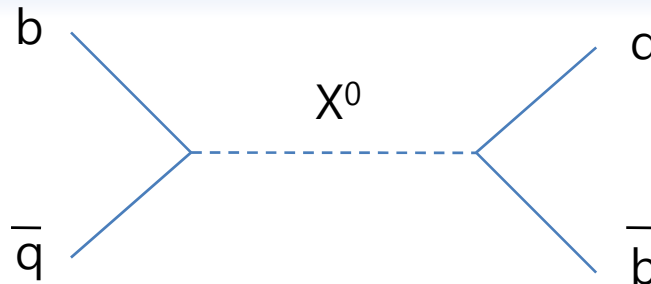
SM:



$$M_{12}^{q,\text{SM}} \simeq \frac{G_F^2 m_W^2}{12\pi^2} f_{B_q}^2 m_{B_q} \eta_B B_{B_q} (V_{tb} V_{tq}^*)^2 S_0(\bar{m}_t^2/m_W^2)$$

$B^0 - \bar{B}^0$ mixing: M_s^{12} (2/3)

X contribution:



for the tree-level transition $b\bar{q} \rightarrow X^* \rightarrow \bar{b}q$ $2m_{B_q} M_{12}^q = \langle B_q^0 | \mathcal{H}_{b\bar{q} \rightarrow \bar{b}q} | \bar{B}_q^0 \rangle$

$$\mathcal{H}_{bd \rightarrow \bar{d}\bar{b}}^X = \frac{1}{2} [\bar{b} \gamma_\mu (g_L P_L + g_R P_R) d] \frac{-i \left(g^{\mu\nu} - \frac{p^\mu p^\nu}{m_X^2} \right)}{p^2 - m_X^2} [\bar{b} \gamma_\nu (g_L P_L + g_R P_R) d]$$

dominant if $m_X \ll m_b$



$$M_{12}^{q,X} = \frac{f_{B_q}^2 m_{B_q}}{3(m_X^2 - m_{B_q}^2)} \left[(g_{Vq}^2 + g_{Aq}^2) P_1^{\text{VLL}} + \frac{g_{Vq}^2 (m_b - m_q)^2 + g_{Aq}^2 (m_b + m_q)^2}{m_X^2} P_1^{\text{SLL}} \right. \\ \left. + (g_{Vq}^2 - g_{Aq}^2) P_1^{\text{LR}} + \frac{g_{Vq}^2 (m_b - m_q)^2 - g_{Aq}^2 (m_b + m_q)^2}{m_X^2} P_2^{\text{LR}} \right]$$

$B^0 - \bar{B}^0$ mixing: M_s^{12} (3/3)

$$\Delta M_s^{\text{exp}} = 2|M_s^{12}|$$

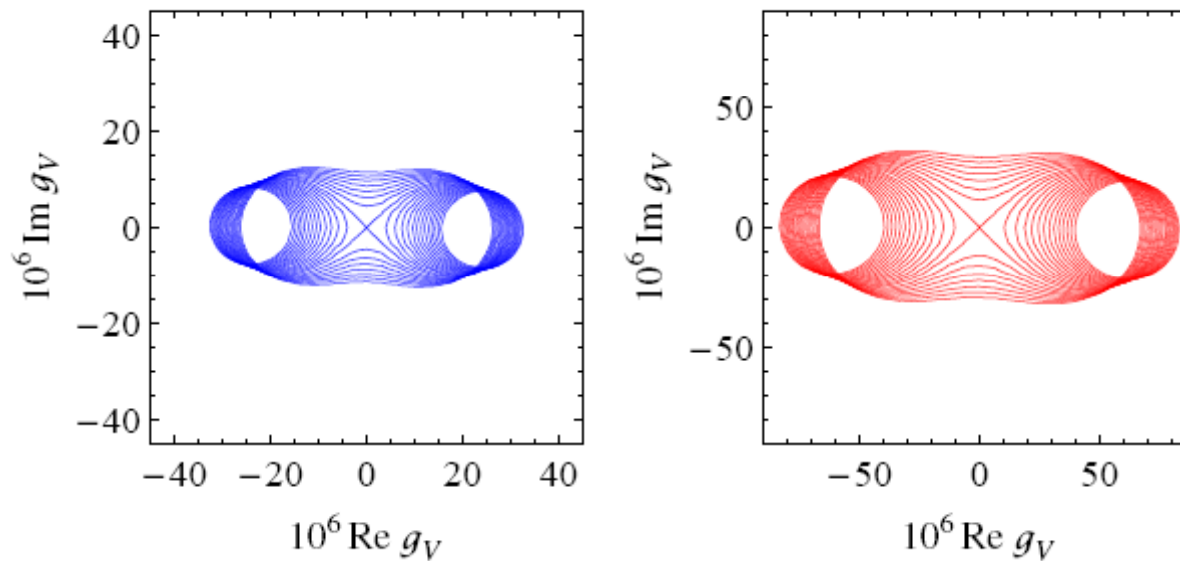


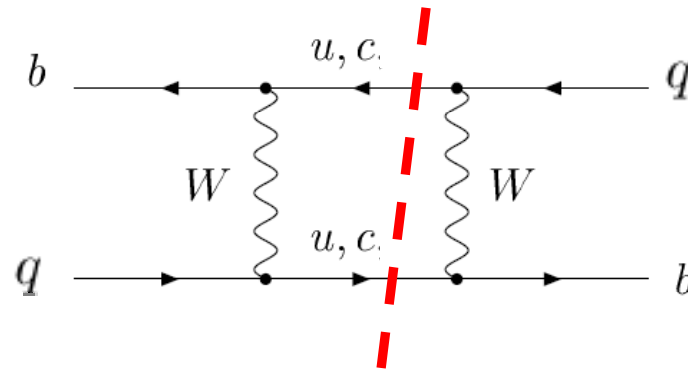
FIG. 1: Regions of $\text{Re } g_V$ and $\text{Im } g_V$ allowed by $\Delta M_s^{\text{exp}} = 2|M_s^{12}|$ constraint for $m_X = 2 \text{ GeV}$ (left plot) and $m_X = 4 \text{ GeV}$ (right plot) under the assumption $g_A = 0$.

$B^0 - \bar{B}^0$ mixing: Γ_s^{12} (1/3)

- ◆ As for Γ_s^{12} , it is in general affected by any physical state f into which both B_s and \bar{B}_s can decay.

$$\Gamma_s^{12} = \sum'_f (\mathcal{M}(B_s \rightarrow f))^* \mathcal{M}(\bar{B}_s \rightarrow f)$$

In the SM, this is dominated by the CKM-favored $b \rightarrow c\bar{c}s$ tree-level processes



$$\left| \frac{\Gamma_s^{12}}{M_s^{12}} \right| \sim 10^{-3}$$

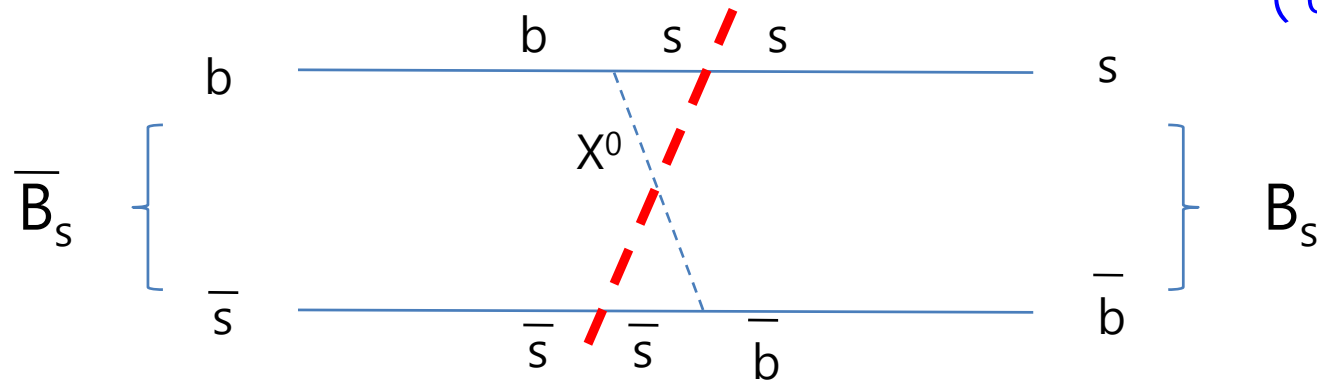
$B^0 - \bar{B}^0$ mixing: Γ_s^{12} (2/3)

- ◆ In contrast, with the X mass $m_X < m_b$, the dominant processes contributing to $\Gamma_s^{12,X}$ arise from decays induced by $b(\bar{b}) \rightarrow s(\bar{s}) X$, such as $\bar{B}_s(B_s) \rightarrow \eta X$, $\bar{B}_s(B_s) \rightarrow \eta' X$, and $\bar{B}_s(B_s) \rightarrow \phi X$.

$$\Gamma_s^{12,X} = \sum'_{f_X} (\mathcal{M}(B_s \rightarrow f_X))^* \mathcal{M}(\bar{B}_s \rightarrow f_X)$$

If $m_X < m_b$, m_X can be produced as a “physical particle” !

(cf. heavy Z')



$B^0 - \bar{B}^0$ mixing: Γ_s^{12} (3/3)

$$\Gamma(b \rightarrow sX)$$

$$\Gamma_s^{12,X} \simeq \frac{|\vec{p}_X|}{8\pi m_b^2 m_X^2} \left\{ g_V^2 \left[(m_b + m_s)^2 + 2m_X^2 \right] \left[(m_b - m_s)^2 - m_X^2 \right] + g_A^2 \left[(m_b - m_s)^2 + 2m_X^2 \right] \left[(m_b + m_s)^2 - m_X^2 \right] \right\}$$

$$\Gamma_s^{12,X} \simeq \Gamma_s^{12,X}(\eta X) + \Gamma_s^{12,X}(\eta' X) + \Gamma_s^{12,X}(\phi X)$$

$$\Gamma_s^{12,X}(PX) = \frac{g_V^2 |\vec{p}_P|^3}{2\pi m_X^2} (F_1^{B_s P})^2$$

$$\Gamma_s^{12,X}(\phi X) = \frac{|\vec{p}_\phi|}{8\pi m_{B_s}^2} (H_0^2 + H_+^2 + H_-^2)$$

Theory (1/2)

- ◆ mass and width differences ΔM_s and $\Delta\Gamma_s$, respectively,
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off-diagonal elements M_s^{12} and Γ_s^{12} of the mass and decay matrices, respectively,
which characterize B_s - \bar{B}_s mixing.

$$(\Delta M_s)^2 - \frac{1}{4}(\Delta\Gamma_s)^2 = 4 |M_s^{12}|^2 - |\Gamma_s^{12}|^2$$

$$\Delta M_s \Delta\Gamma_s = 4 |M_s^{12}| |\Gamma_s^{12}| \cos \phi_s$$

$$\phi_s = \arg(-M_s^{12}/\Gamma_s^{12})$$

$$a_{\text{sl}}^s = \frac{4 |M_s^{12}| |\Gamma_s^{12}| \sin \phi_s}{4 |M_s^{12}|^2 + |\Gamma_s^{12}|^2}$$

$a_{sl}^{s, \text{exp}}, (\Delta M_s^{\text{exp}} \Delta \Gamma_s^{\text{exp}}), \Gamma(b \rightarrow sX)$

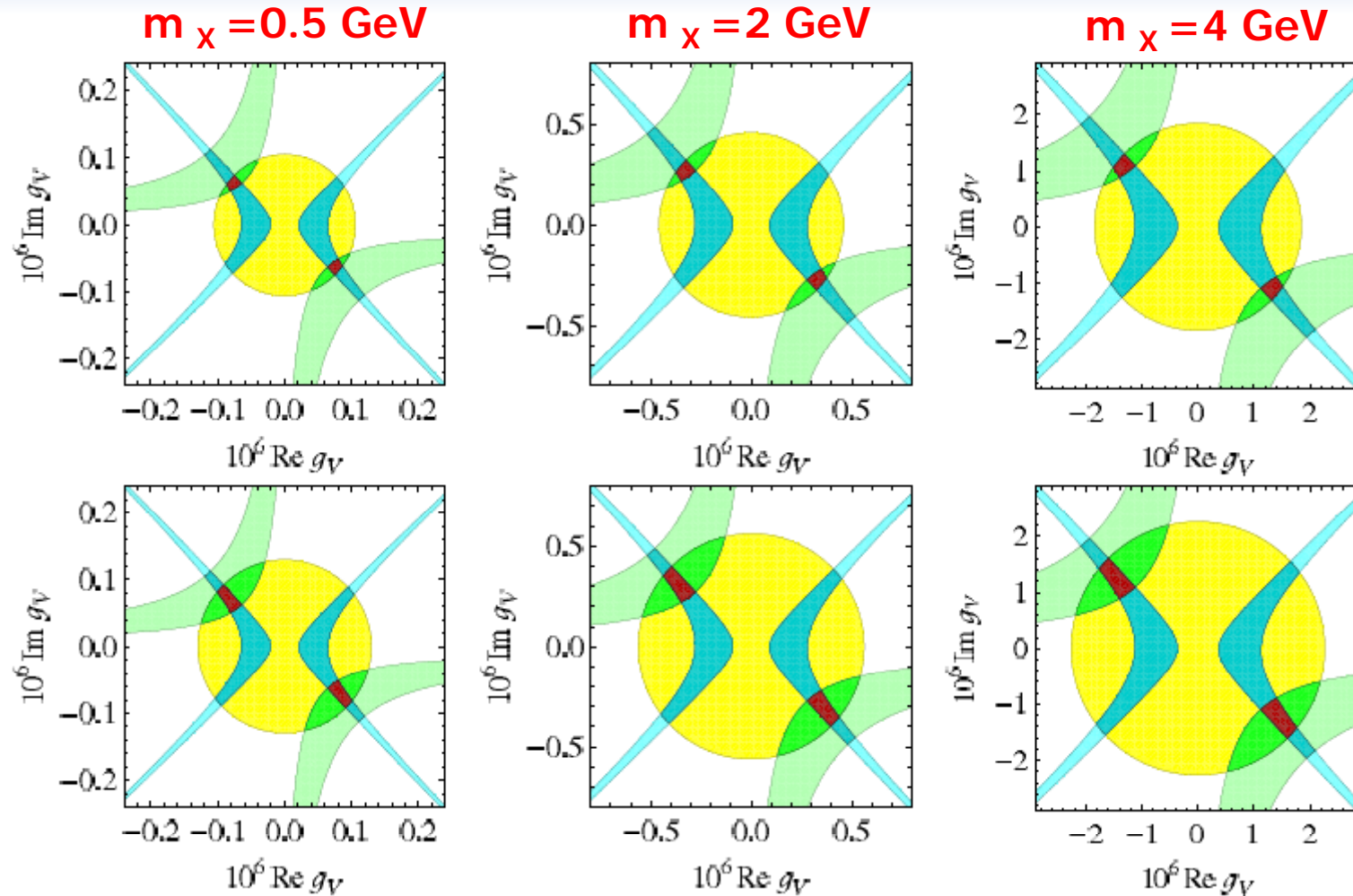


FIG. 2: Regions of $\text{Re } g_V$ and $\text{Im } g_V$ allowed by $a_{sl}^{s, \text{exp}}$ constraint (green), $\Delta M_s^{\text{exp}} \Delta \Gamma_s^{\text{exp}}$ constraint (blue), $\Gamma(b \rightarrow sX) < 0.1 \text{ ps}^{-1}$ (yellow), and all of them (dark red) for $m_X = 0.5 \text{ GeV}$ (upper left plot), 2 GeV (upper middle plot), and 4 GeV (upper right plot), under the assumption $g_A = 0$. The lower plots are the same as the upper ones, except that $\Gamma(b \rightarrow sX) < 0.15 \text{ ps}^{-1}$.

$$\left| \Gamma_s^{12} / \Gamma_s^{12,SM} \right|, \quad \sin \phi_s$$

$$m_X = 4 \text{ GeV}$$

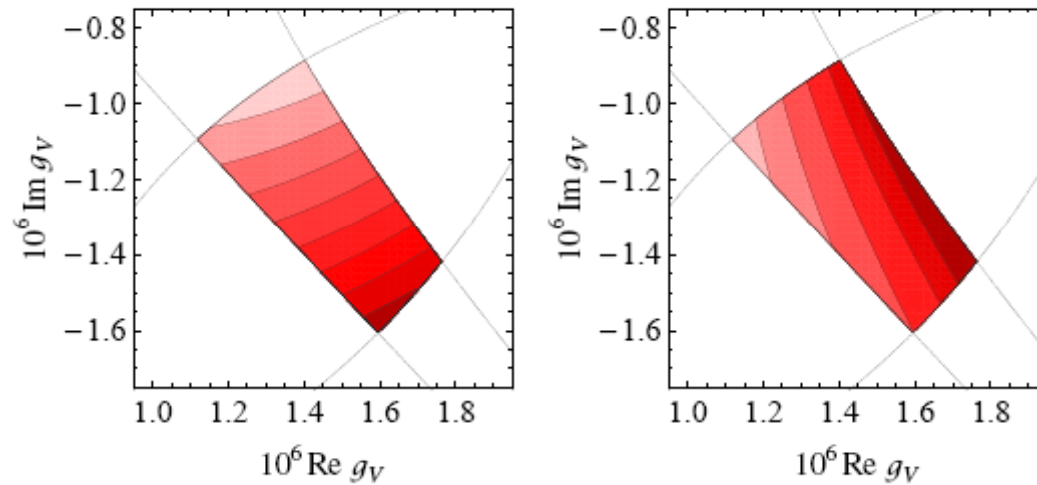


FIG. 3: Values of $|\Gamma_s^{12}|$ (left plot) and $\sin \phi_s$ (right plot) for $m_X = 4 \text{ GeV}$ and the $(\text{Re } g_V, \text{Im } g_V)$ overlap region in the fourth quadrant of the lower-right plot in Fig. 2 allowed by all the constraints, with $\Gamma(b \rightarrow sX) < 0.15 \text{ ps}^{-1}$. In the left plot, from darkest to lightest, the differently shaded (red colored) areas correspond to $|\Gamma_s^{12} / \Gamma_s^{12,SM}| > 3.1, 2.9, 2.7, \dots, 1.5$, respectively, with each region including the area of the next darker region and $|\Gamma_s^{12,SM}|$ being its central value. Similarly, in the right plot, from darkest to lightest $\sin \phi_s < -0.99, -0.98, -0.96, -0.93, -0.89, -0.85$.

$$a_{sl}^{s, \text{exp}}, (\Delta M_s^{\text{exp}} \Delta \Gamma_s^{\text{exp}}), \Gamma(b \rightarrow sX)$$

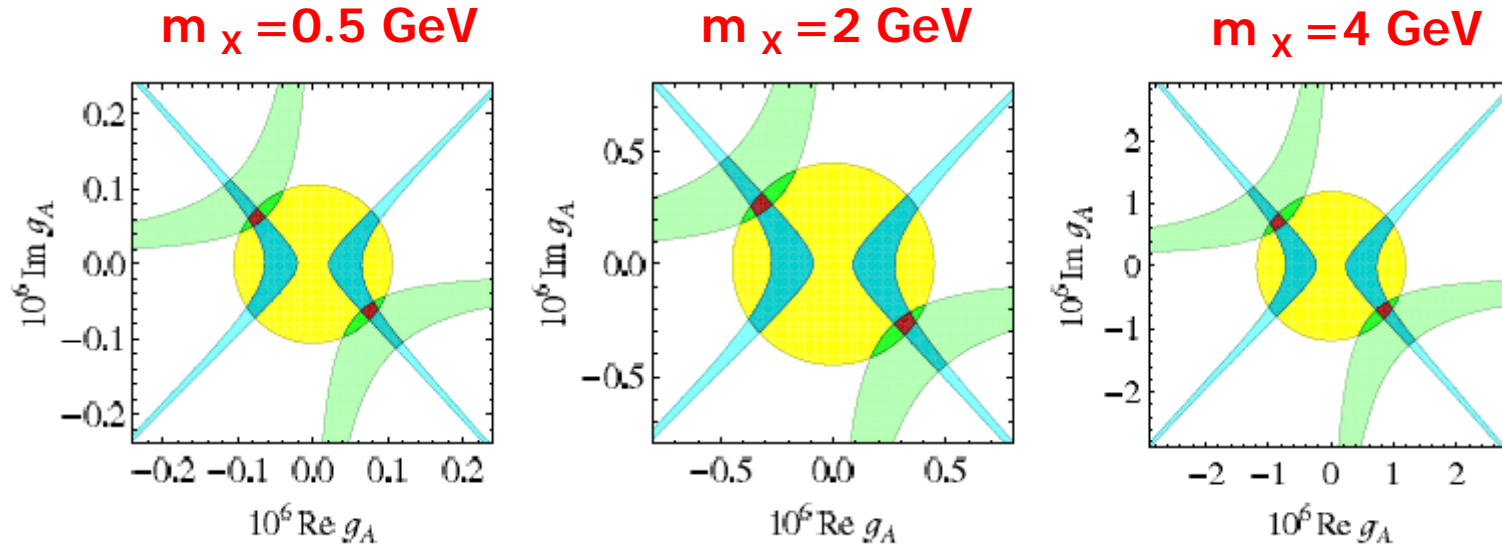


FIG. 4: Regions $\text{Re } g_A$ and $\text{Im } g_A$ allowed by $a_{sl}^{s, \text{exp}}$ constraint (green), $\Delta M_s^{\text{exp}} \Delta \Gamma_s^{\text{exp}}$ constraint (blue), $\Gamma(b \rightarrow sX) < 0.1 \text{ ps}^{-1}$ (yellow), and all of them (dark red) for $m_X = 0.5 \text{ GeV}$ (left plot), 2 GeV (middle plot), and 4 GeV (right plot), under the assumption $g_V = 0$.

Summary

- ◆ We have investigated the possibility that the D0 anomaly arises from the contribution of a light spin-1 particle to the B_s mixing.
- ◆ In contrast to a heavy Z' particle, X can be produced as a physical particle in B_s decay, and so it affects not only M_s^{12} , but also Γ_s^{12} .
- ◆ Under constraints from available experimental data, the effect of X can increase $|\Gamma_s^{12}|$ to become **a few times larger** than its SM value, and enlarge the size of $\sin\phi_s$ by a factor of **a few hundred**.
 - Can explain the D0 anomaly.
 - But, $m_X \sim 0.2 \text{ GeV}$ is unlikely allowed.

Thank you!

