

MAGNETO-OPTICAL TRAPPING OF CADMIUM ATOMS

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PHYSICS
UNIVERSITY OF MICHIGAN

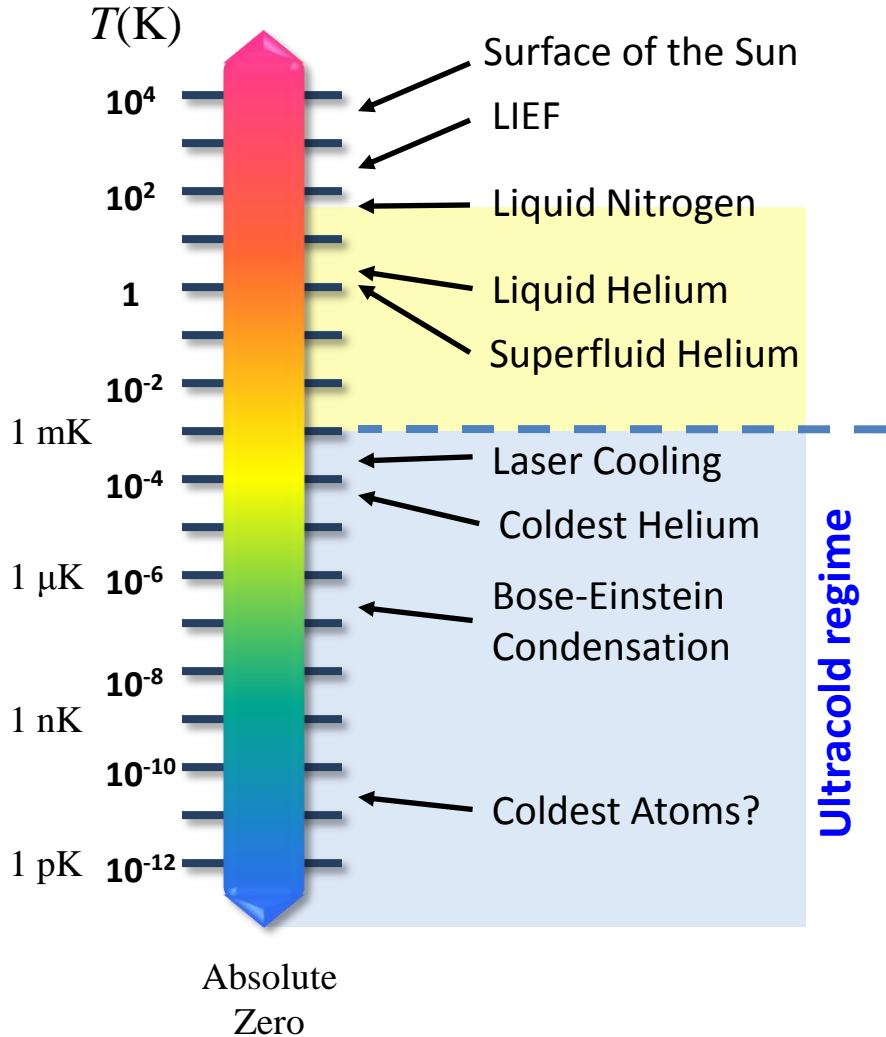


NSF PFC

Outline

- Introduction to ultracold atomic physics
- How does laser cooling work
- Cadmium MOT
- Outlook

Define the “Ultracold”



- Laboratory energy scales

- $1 \text{ peV} < \text{energy} < 1 \text{ TeV}$

BEC

Tevatron,
Fermilab

Atomic velocities

room temperature gas:

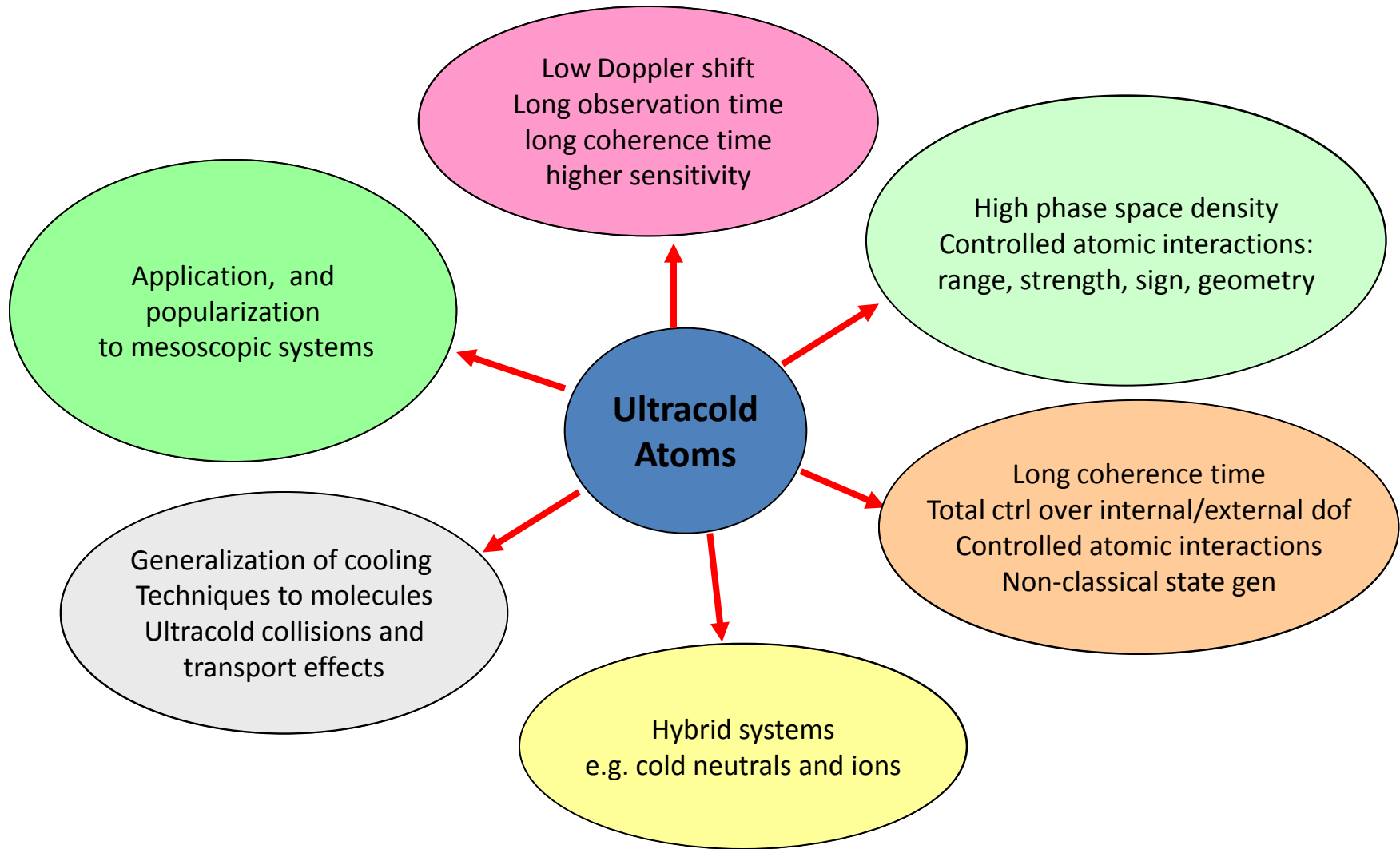
300 meters/sec

ultracold gas:

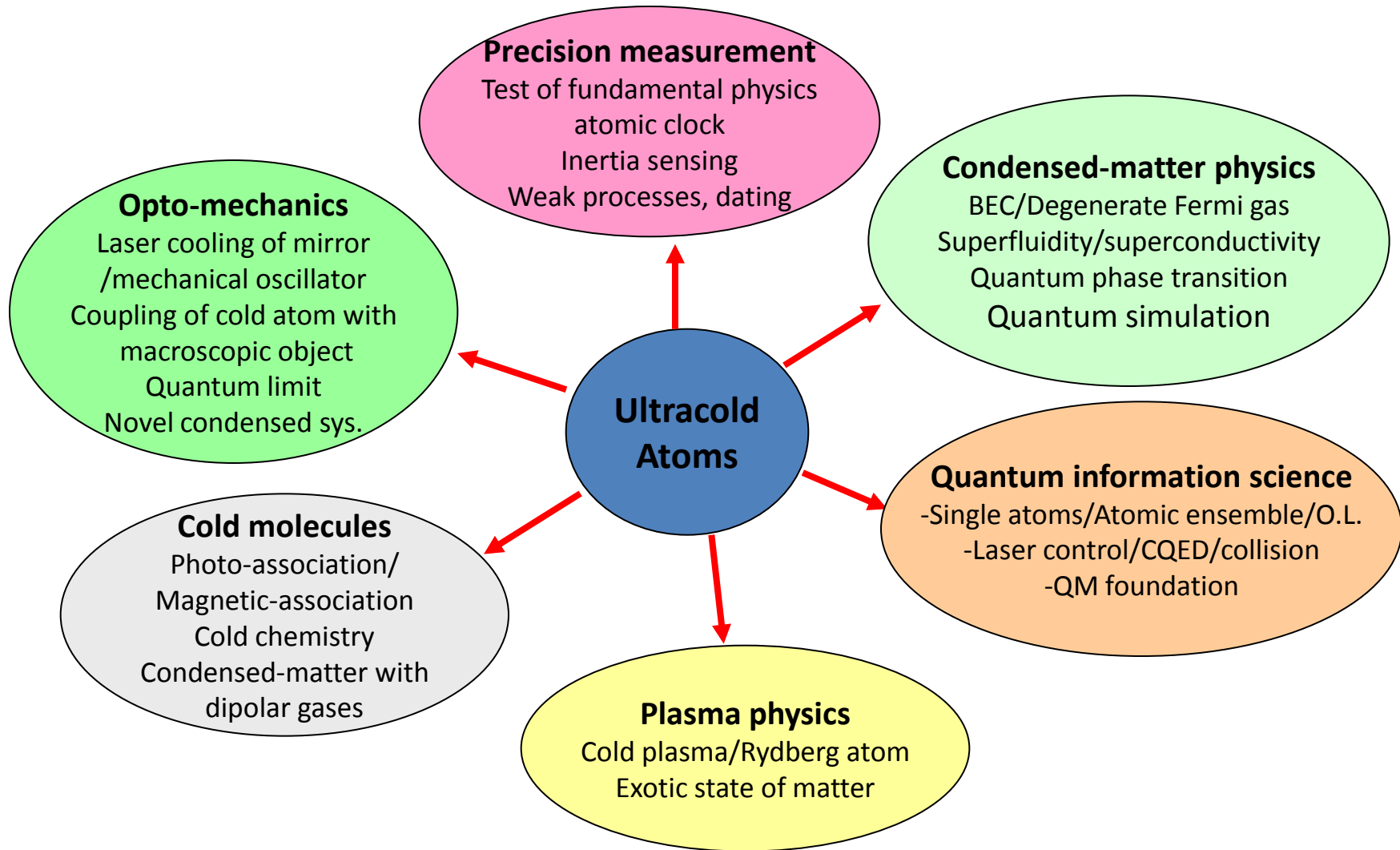
6 meters/hour

$$\frac{1}{2}mv^2 = k_B T$$

Cold atoms: much more than just cool atomic physics



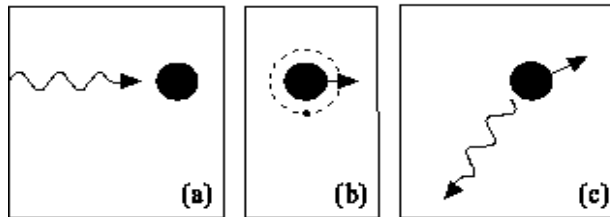
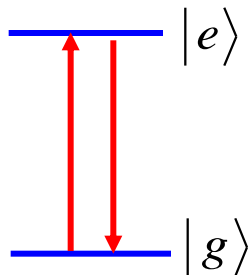
Cold atoms: much more than just cool atomic physics



How does lasers cooling work?

Manipulating atoms with light - I

Photons carry momentum: can be used to accelerate/decelerate an object



$$E = \hbar\omega_i$$

$$E' = \hbar\omega_s$$

$$\vec{p} = \hbar\vec{k}_i$$

$$\vec{p}' = \hbar\vec{k}_s$$

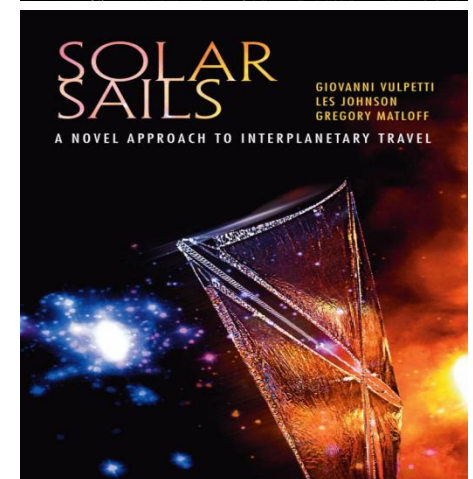
$$\langle \vec{k}_i \rangle = \vec{k}$$

$$\langle \vec{k}_s \rangle = 0$$

Photon energy $E = \hbar\omega \sim \text{eV}$

Photon recoil energy $E_r = (\hbar\vec{k})^2 / 2m \sim 10^{-7} \text{ eV}$

Thermal energy (@ 293K) $E_{R.T.} \sim 25 \times 10^{-3} \text{ eV}$

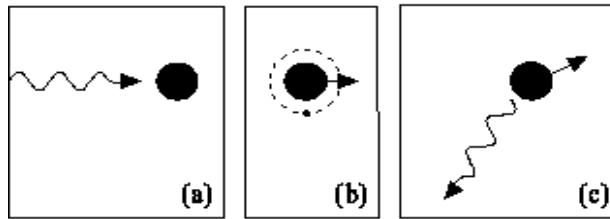
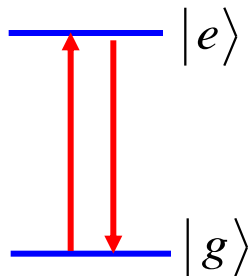


Laboratory applications:

1. Laser cooling
2. Raman cooling
3. Coherent control of Motional D.O.F.

Manipulating atoms with light - I

Photons carry momentum: can be used to accelerate/decelerate an object



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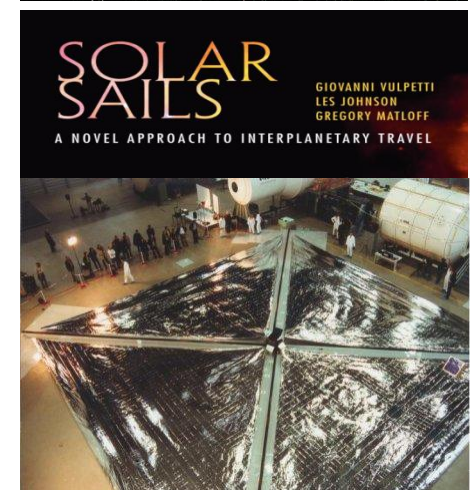
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Laboratory applications:

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Manipulating atoms with light - II

When external motional-states are spectroscopically resolved and quantized, light can be used to control the quantum states of the external degrees of freedom (DOF).

Let's assume no spontaneous decay from $|e\rangle$

$$\hat{H}_I = \hbar\Omega\hat{\sigma}^+ e^{-i\delta t} e^{ik\hat{x}} + h.c.$$

When $kx_0 \ll 1$, (Lamb-Dicke regime)

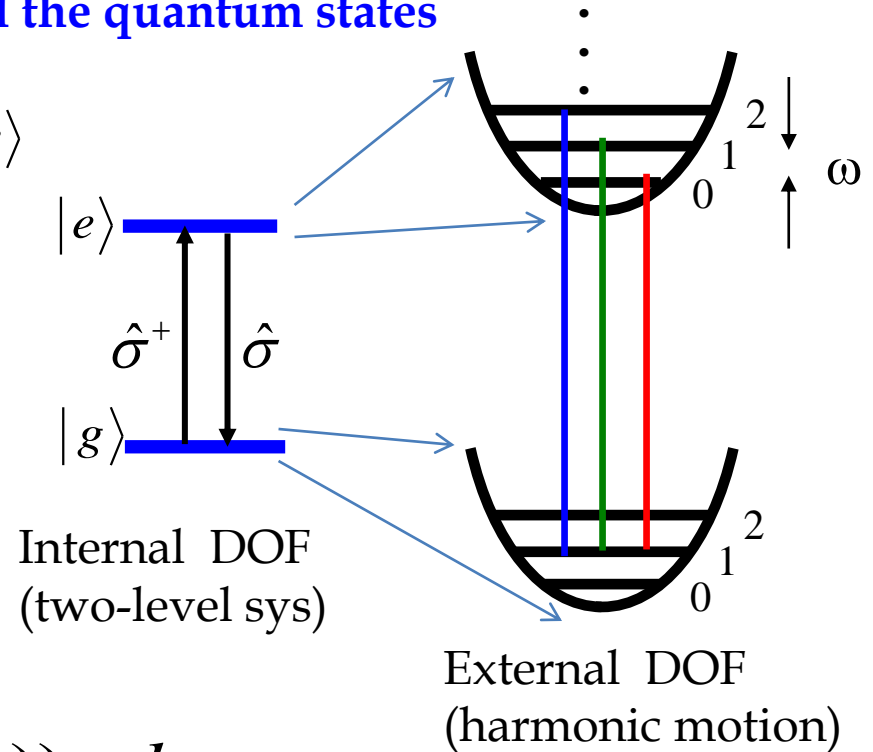
$$e^{ik\hat{x}} \sim 1 + ik\hat{x} \\ = 1 + ikx_0 (\hat{a} + \hat{a}^+).$$

$$\hat{H}_I \sim \hbar\Omega e^{-i\delta t} \hat{\sigma}^+ (1 + ik(\hat{a} + \hat{a}^+)) + h.c.$$

detuning

carrier

Motional sidebands { red sideband
blue sideband



Valid when
Lamb-Dicke Parameter

$$\eta = kx_0 \propto \frac{x_0}{\lambda} \ll 1$$

Doppler cooling

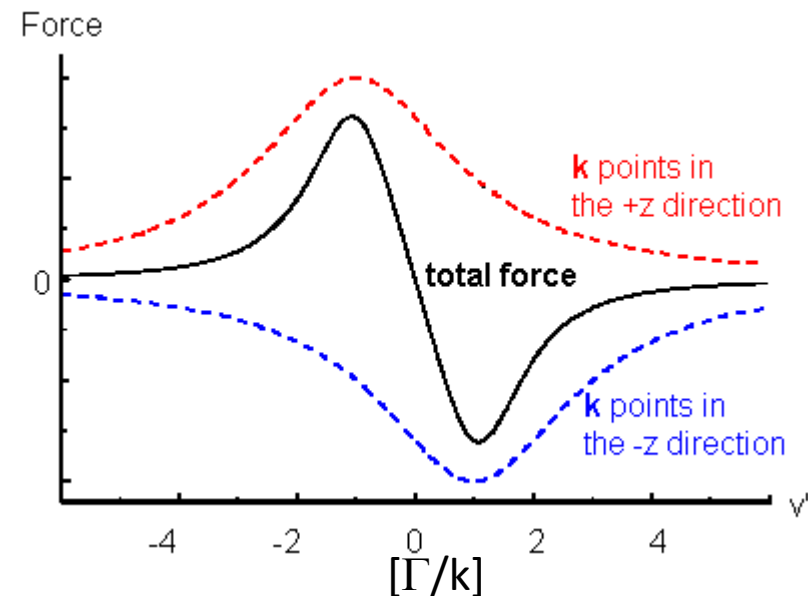
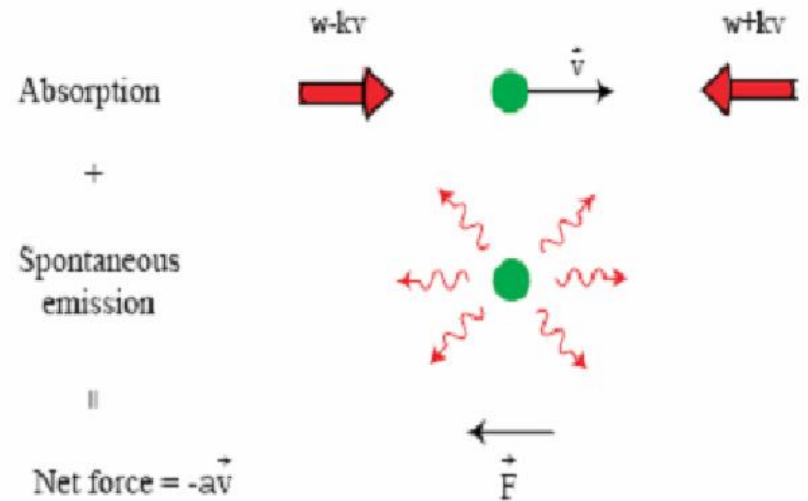
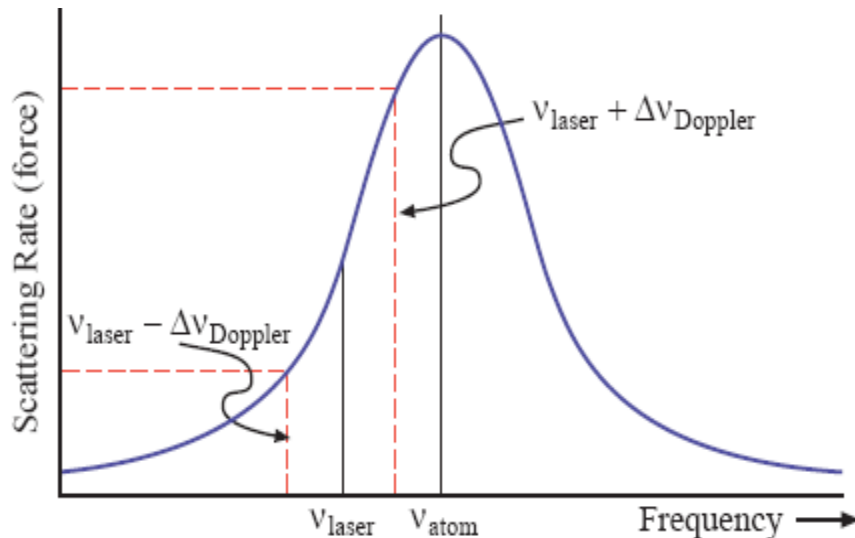
Doppler shift $\omega_D = 2\pi \frac{v}{c} f = \frac{2\pi v}{\lambda} = kv$

$$\vec{F} = \vec{F}_+ + \vec{F}_-$$

$$\vec{F}_\pm = \pm \frac{\hbar k \Gamma}{2} \frac{s_0}{1 + s_0 + [2(\delta \mp kv)/\Gamma]^2}$$

$$F \approx \frac{8\hbar k^2 \delta s_0 \vec{v}}{\Gamma(1 + s_0 + (2\delta/\Gamma)^2)^2} \equiv -\beta \vec{v}, \text{ if } \left(\frac{kv}{\Gamma}\right)^2 \ll 1$$

For a **red-detuned** ($\delta < 0$) laser, the force damps the velocity.



How to make a MOT?

VOLUME 59, NUMBER 23

PHYSICAL REVIEW LETTERS

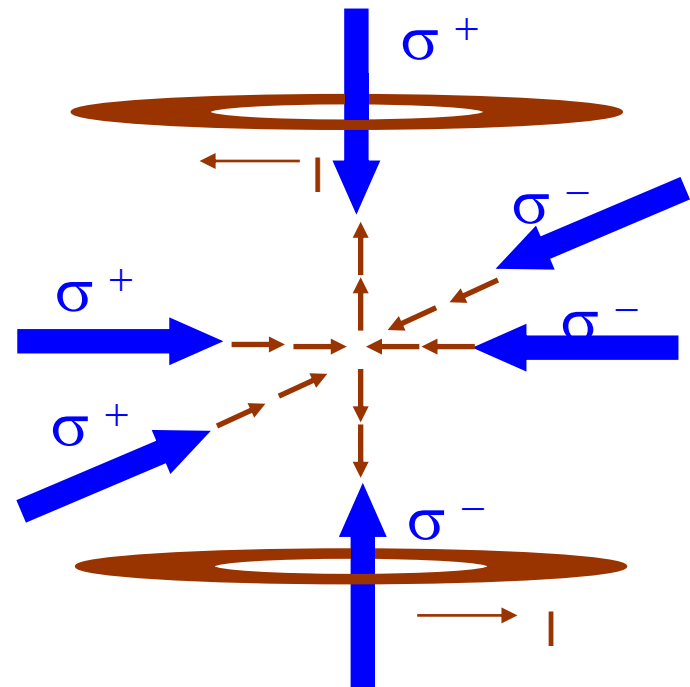
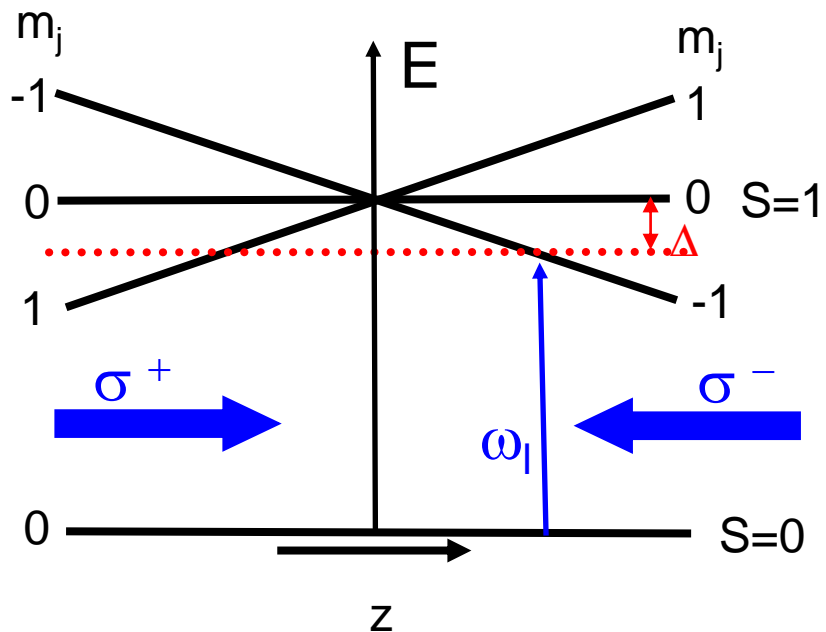
7 DECEMBER 1987

Trapping of Neutral Sodium Atoms with Radiation Pressure

E. L. Raab,^(a) M. Prentiss, Alex Cable, Steven Chu,^(b) and D. E. Pritchard^(a)

AT&T Bell Laboratories, Holmdel, New Jersey 07733

(Received 16 July 1987)



3D Monte-Carlo simulation of a MOT

Initial position: uniform distribution, initial velocity: Boltzmann distribution

Acceleration:

$$a_x(\vec{r}, v_x) = \frac{\hbar k \gamma}{2m} s_x(\vec{r}) \left[\sum_q \frac{p_{+,q}(\vec{r})}{1 + s_{\text{tot}}(\vec{r}) + (2\delta_{+,q}(\vec{r}, v_x))^2} - \sum_q \frac{p_{-,q}(\vec{r})}{1 + s_{\text{tot}}(\vec{r}) + (2\delta_{-,q}(\vec{r}, v_x))^2} \right]$$

Saturation parameter:

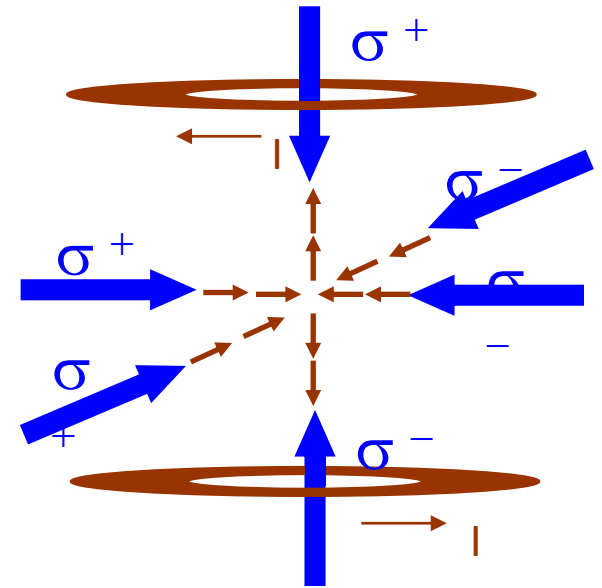
$$s_x(\vec{r}) = \frac{I_x}{I_{\text{sat}}} e^{-\frac{2(y^2+z^2)}{w_0^2}},$$

$$s_{\text{tot}}(\vec{r}) = 2s_x(\vec{r}) + 2s_y(\vec{r}) + 2s_z(\vec{r}),$$

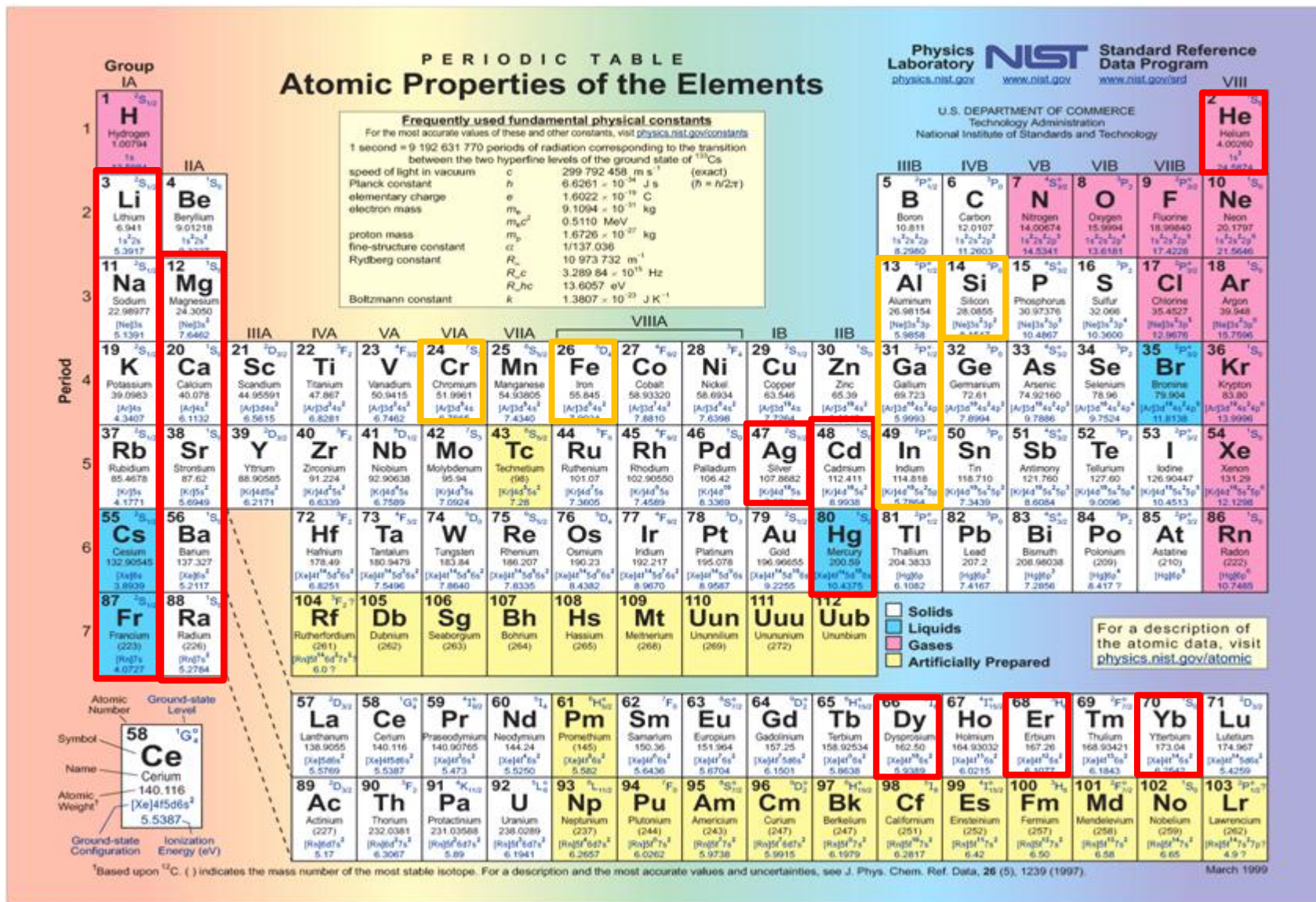
Polarization:

$$p_{\pm,q}(\vec{r}) = \begin{cases} \left(\frac{1}{2}\left[1 \mp \frac{x B'}{2 B(\vec{r})}\right]\right)^2, & q = -1 \quad (\sigma^-) \\ \left(\frac{1}{2}\left[1 \pm \frac{x B'}{2 B(\vec{r})}\right]\right)^2, & q = +1 \quad (\sigma^+) \\ 1 - (p_{\pm,-1} + p_{\pm,+1}), & q = 0 \quad (\pi) \end{cases}$$

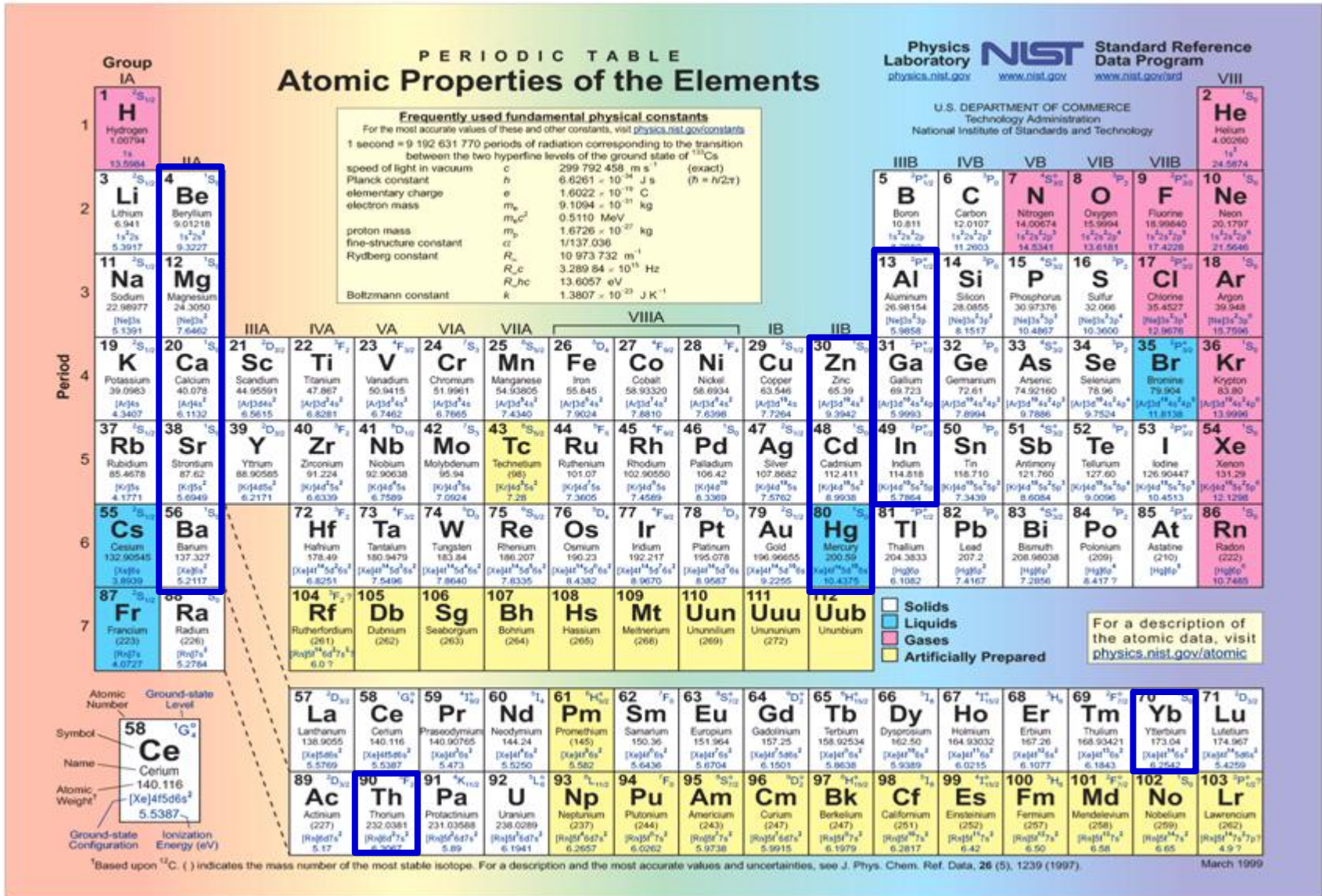
Effective detuning: $\delta_{\pm,q}(\vec{r}, v_x) = (\Delta \mp k v_x)/\gamma + q \frac{\mu_B g_F B(\vec{r})}{\gamma \hbar}$



Demonstrated laser cooling of neutral atoms

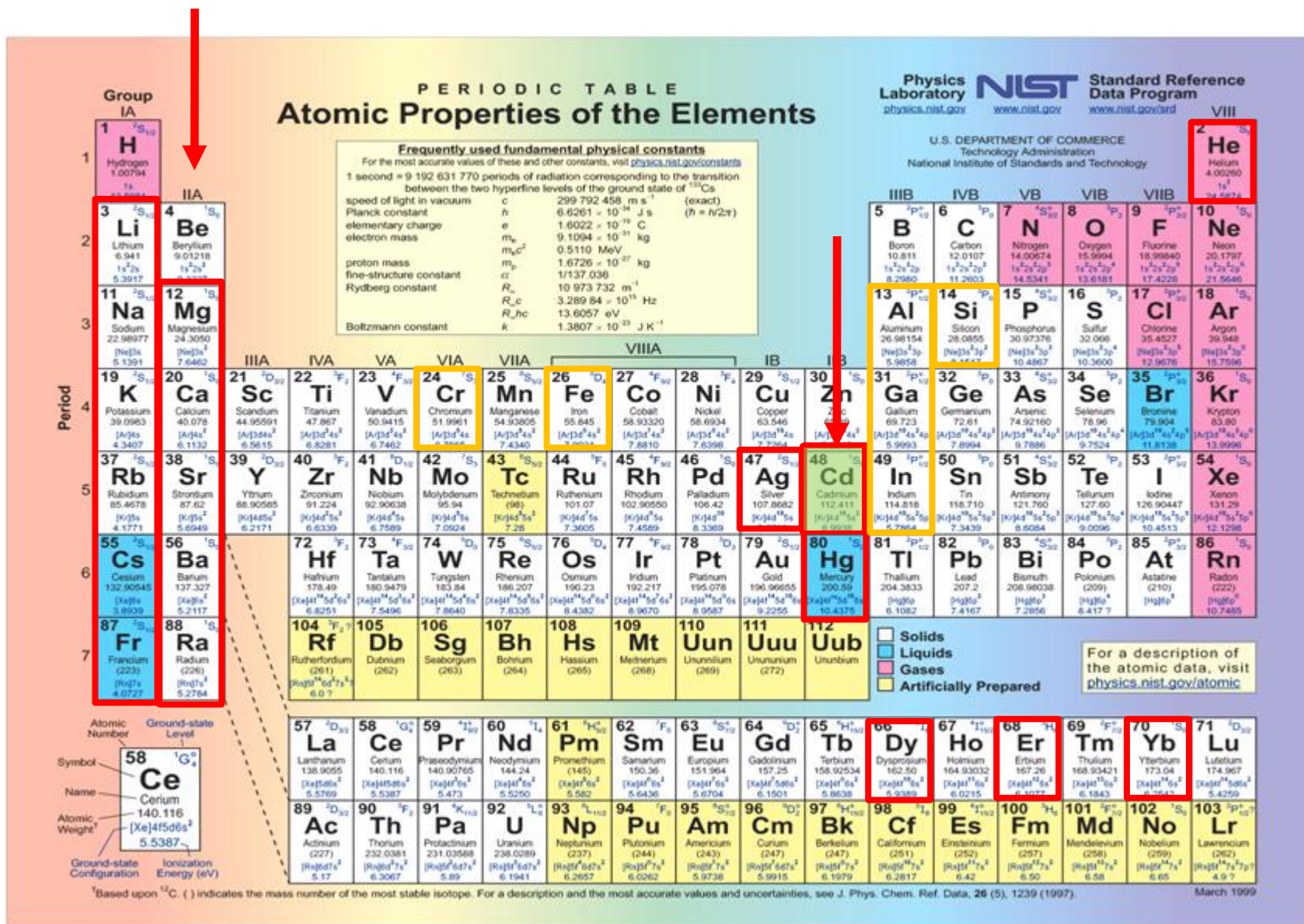


Demonstrated laser cooling of ionic atoms



Magneto-Optical Trapping of Cadmium

Demonstrated laser cooling of neutral atoms

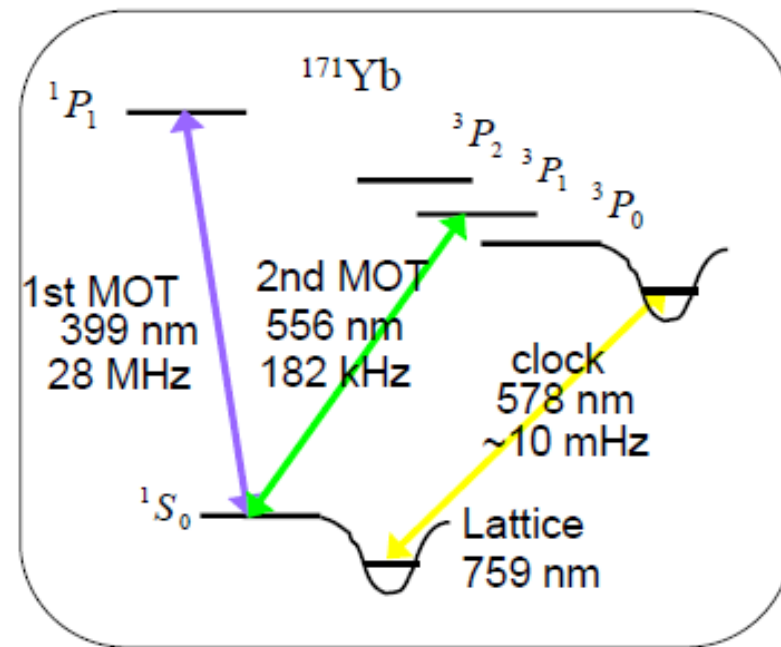


Why two-electron atoms?

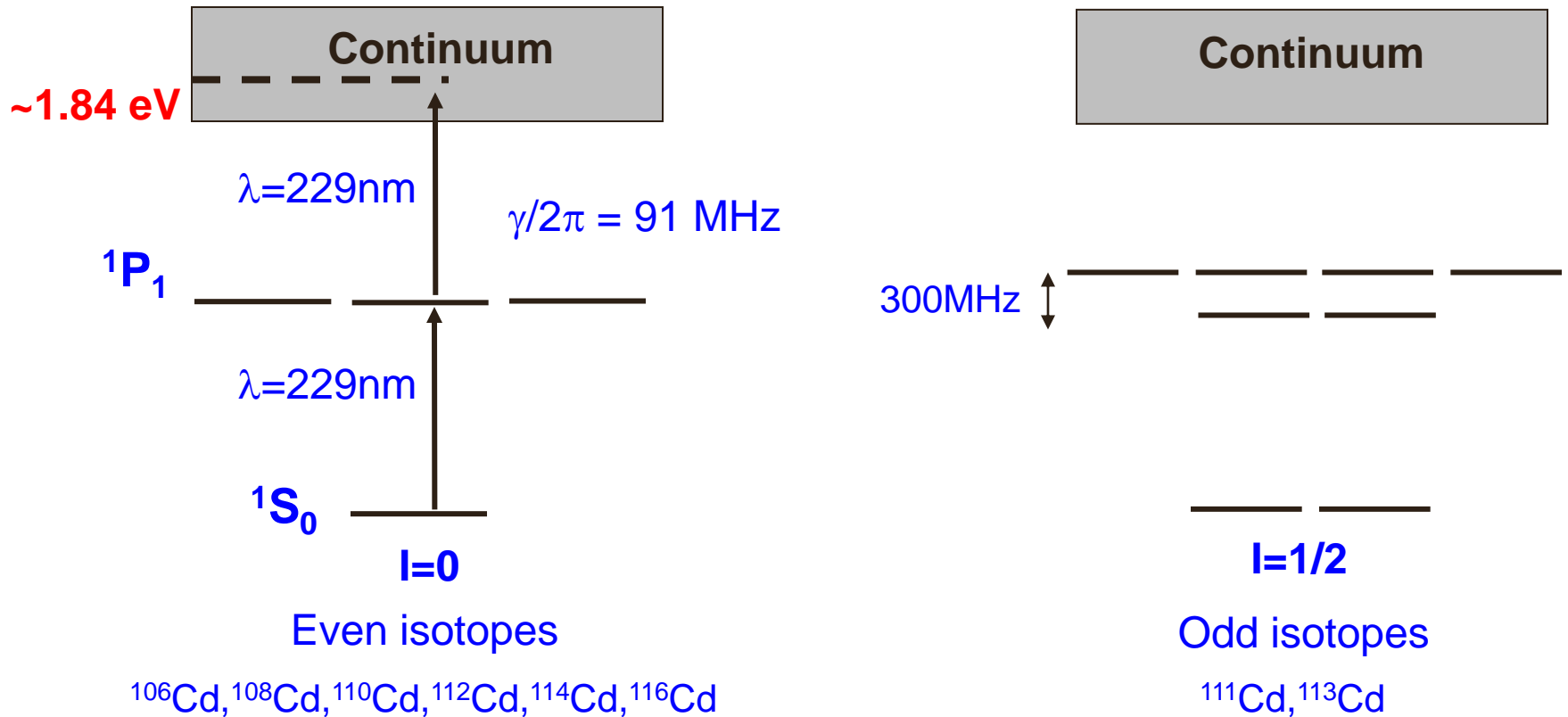
- Textbook two-level atom
- Possess intercombination transition lines
 - Lower Doppler limit temperature
 - atomic clock: Sr, Mg, Hg, Yb
- EDM, T/CP violation: ^{225}Ra , ^{199}Hg
- Trappable neutrals and ions
 - Build a hybrid system

Intercombination lines:

$$^1S_0 - ^3P_{0,1,2}$$

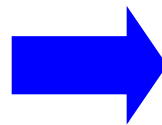


Cadmium overview



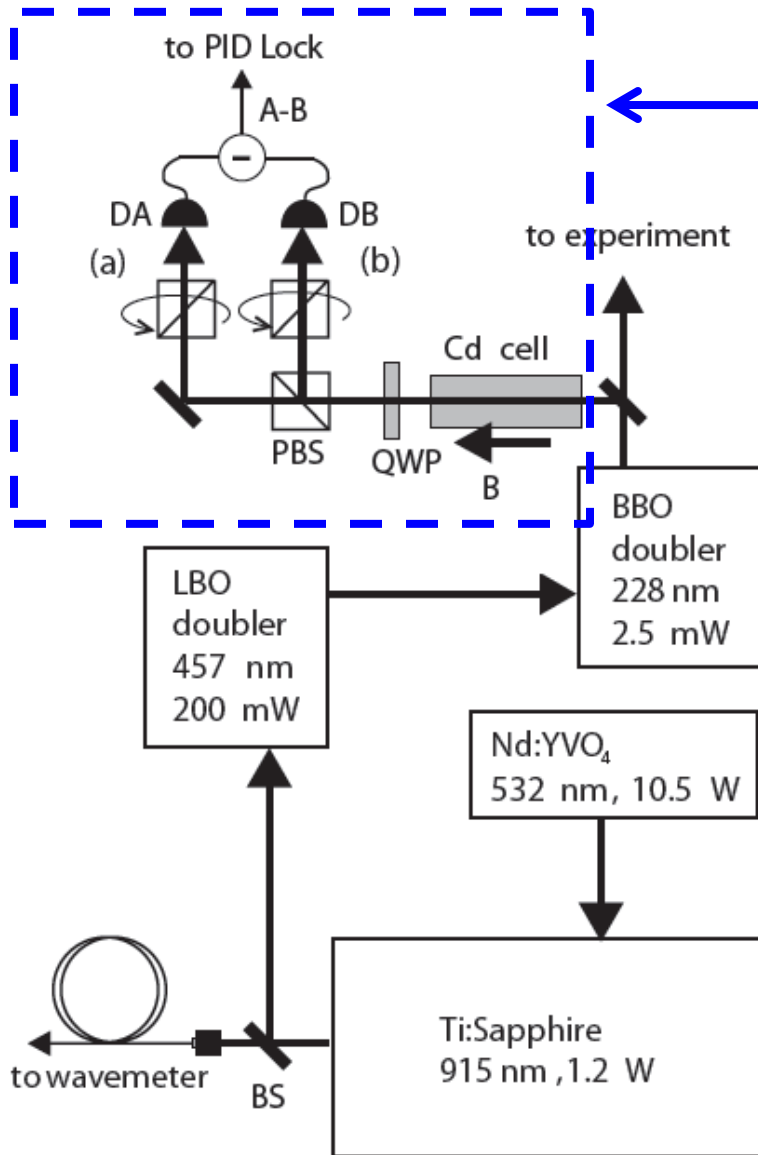
Large $k=2\pi/\lambda$

- **Large linewidth**
- **Photo-ionization**



- **Large I_{sat} (1.0 W/cm^2)**
- **Large photon recoil acceleration ($\sim 50x \text{ Rb}$)**
- **Large B-field gradients**

Laser System and freq stabilization



DAVLL lock:

$$\Delta\nu \sim 30 \text{ MHz} \sim \gamma/3$$

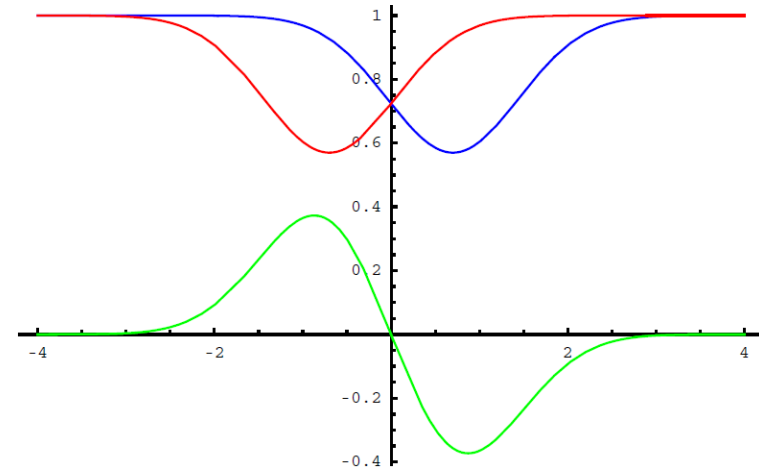
1.5 GHz capture range

DA

(sig. from Detector A)

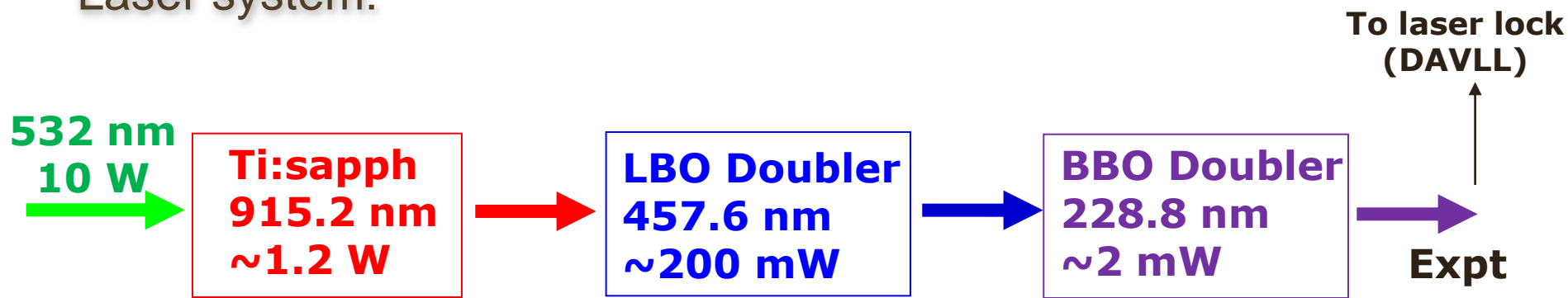
DB

(sig. from Detector B)

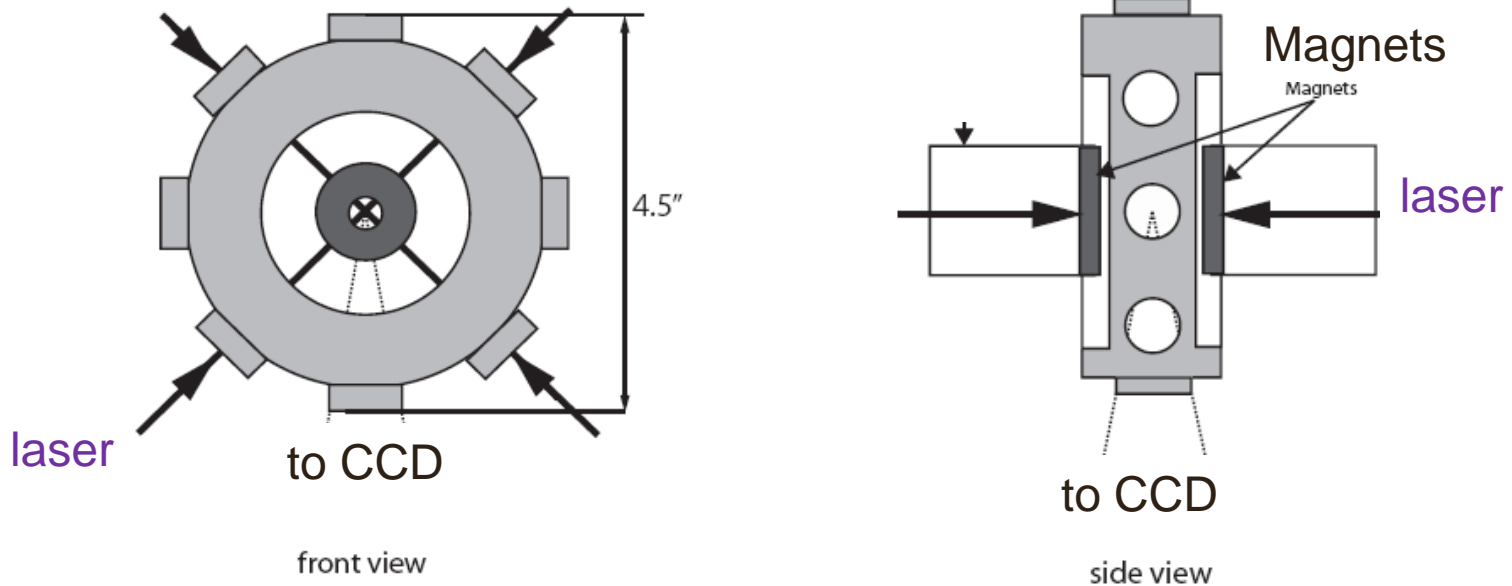


DB - DA

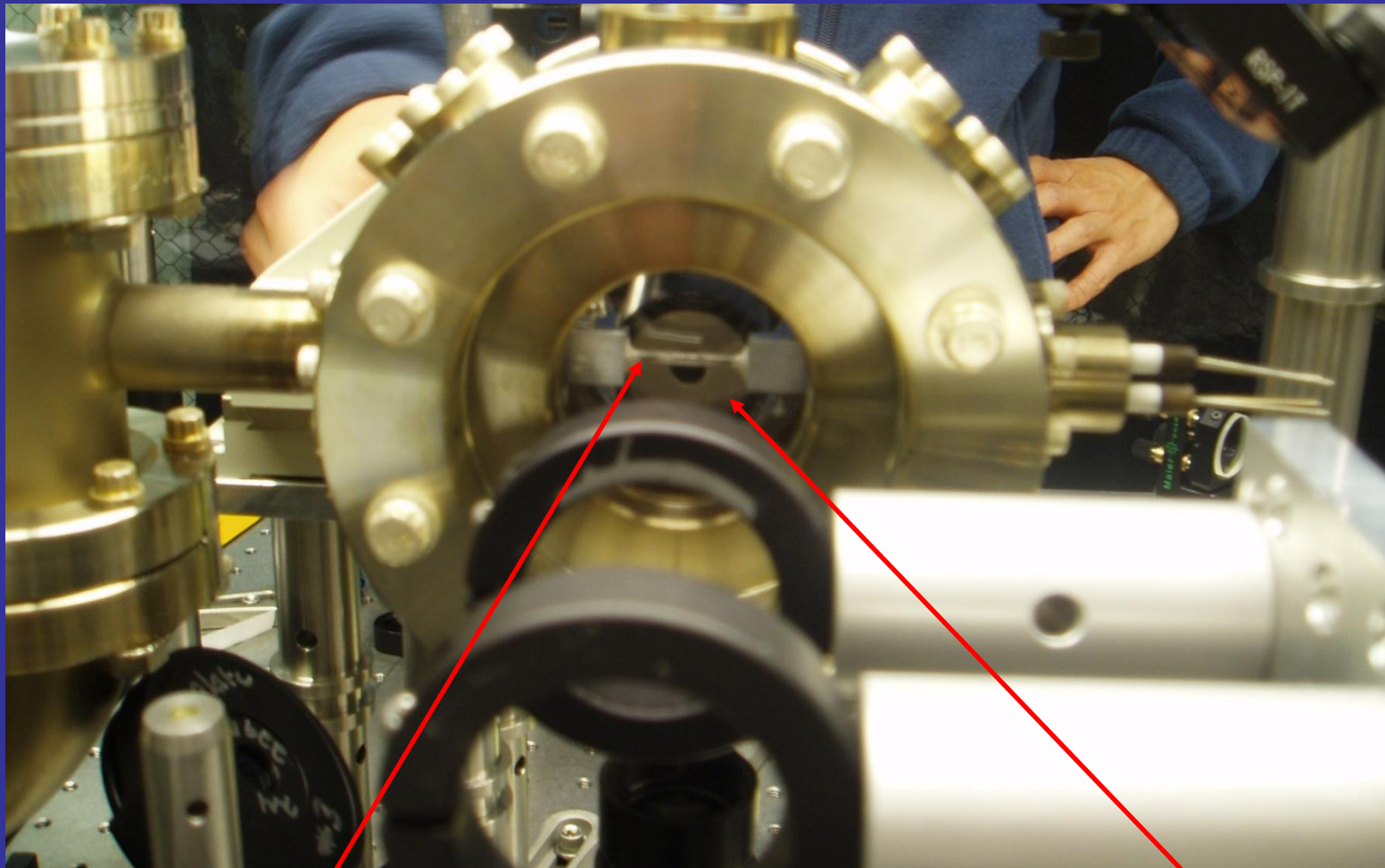
Laser system:



Vacuum chamber:



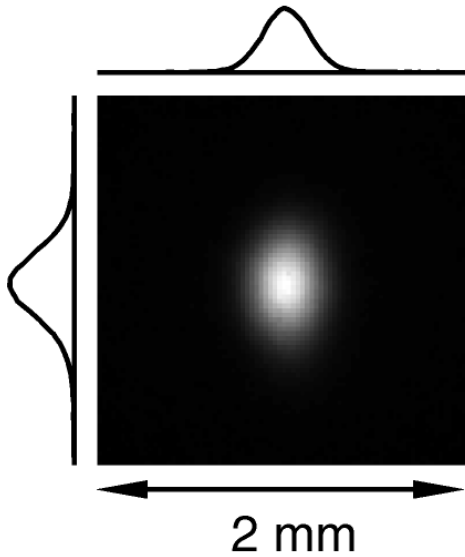
Cd vapor pressure $P \sim 10^{-11}$ Torr at 300K



Ion trap: Four-rod linear Paul trap

Permanent magnets give large magnetic field gradients:
 $B' \sim 300-1500 \text{ G/cm}$

Cadmium MOT parameters



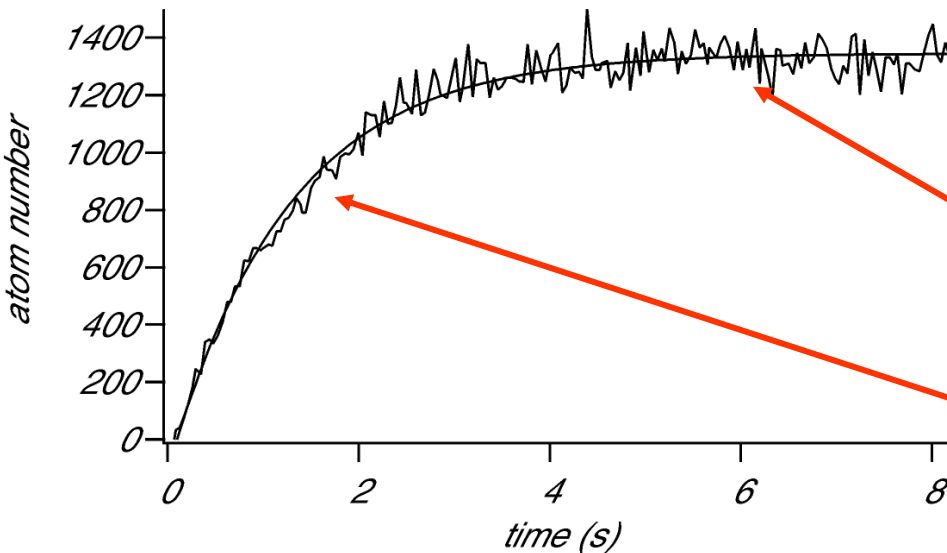
- MOT Atom Number (N): $\sim 10 - 10000$
- MOT Density: $\sim 10^8 - 10^9 \text{ cm}^{-3}$
- Beam waist (w_0): $0.5 - 1.5 \text{ mm}$
- Beam power: $0.7 - 2.5 \text{ mW}$
- Saturation parameter (s): $0.02 - 0.77$
- Magnetic field gradient (B'): $300 - 1200 \text{ G/cm}$
- Gaussian cloud shape: temperature limited
- Thus not density limited: **two-body collision loss ignored**

In a vapor cell:

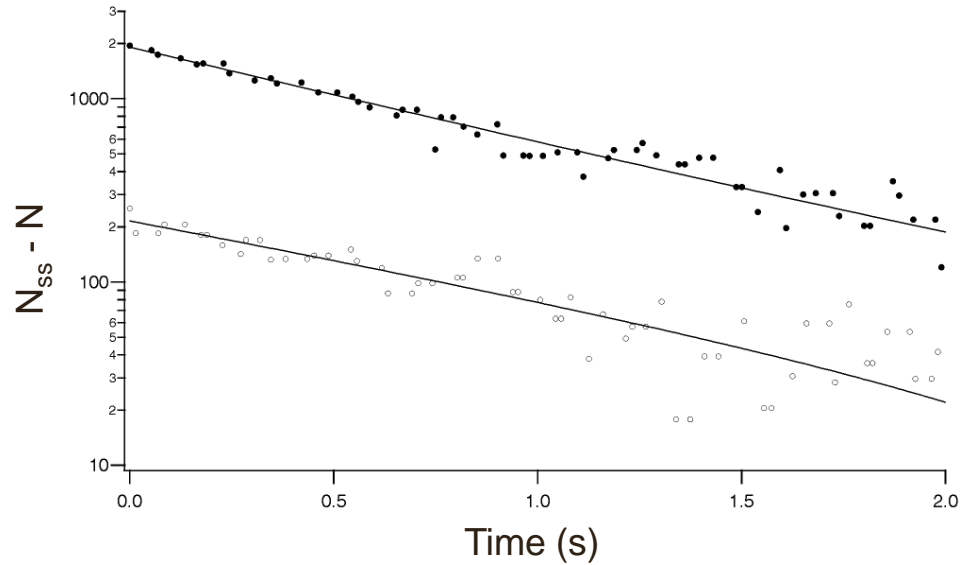
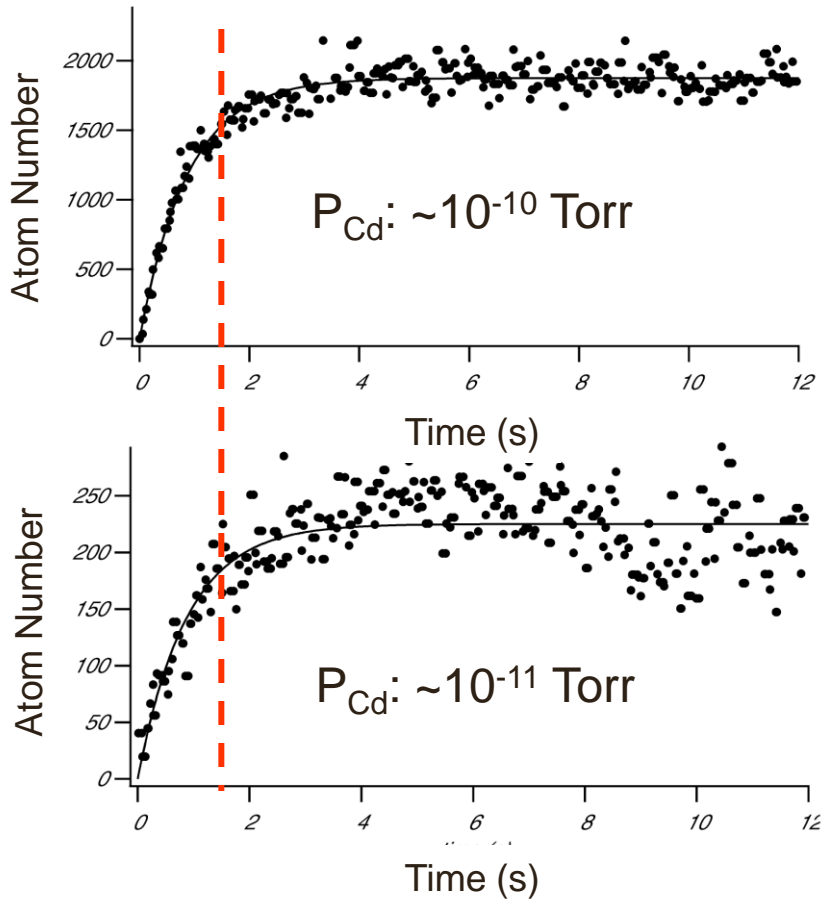
$$\frac{dN}{dt} = L - \Gamma_{\text{eff}} N - \beta \frac{N^2}{V}$$

$$N_{ss} = \frac{L}{\Gamma_{\text{eff}}} \Rightarrow L = \Gamma_{\text{eff}} N_{ss}$$

$$\Gamma_{\text{eff}} = \Gamma_0 + \Gamma_{PI}$$



Dominant loss: photoionization



MOT growth rate independent of the vapor pressure: one-body collision loss is small and ignored.

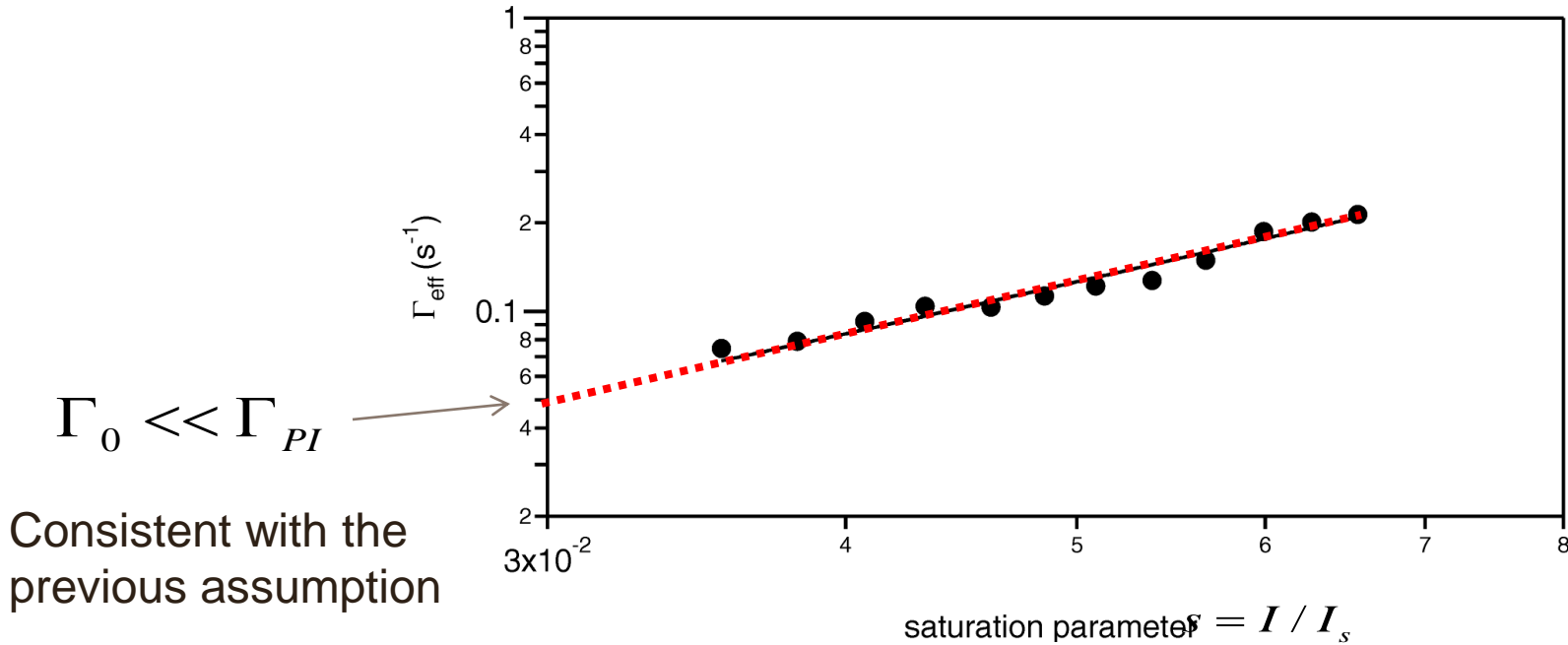
$$\Gamma_{eff} = \cancel{\Gamma_0} + \Gamma_{PI}$$

$$\Gamma_{PI} = \frac{\sigma_{PI} I \text{Pr}(I, \delta)}{\hbar \omega}$$

$$\text{Pr}(s, \delta) = \frac{s/2}{1 + s + 4(\frac{\delta}{\gamma})^2}$$

σ_{PI} : Photoionization cross-section from P state

Photoionization cross-section



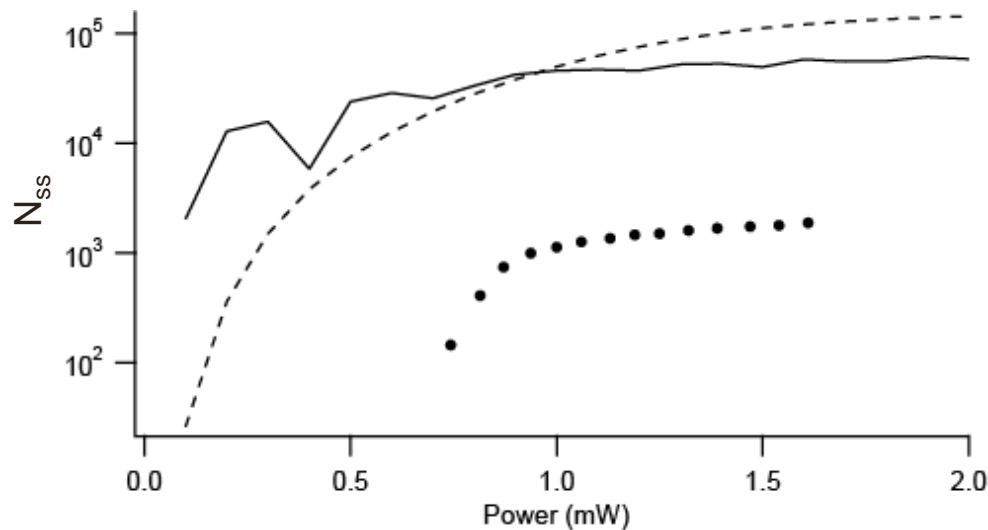
$$\Gamma_{PI} = \frac{\sigma_{PI} I \text{Pr}(s, \delta)}{\hbar \omega} \quad \text{Pr}(s, \delta) = \frac{s/2}{1 + s + 4(\frac{\delta}{\gamma})^2}$$

$$\sigma_{PI} = 2(1) \times 10^{-16} \text{ cm}^2$$

σ_{PI} : Photoionization cross-section from P state

Limited by intensity and detuning uncertainty

Power / intensity:



- 3-D Monte Carlo
- - - 1-D Analytical
- Expt Data

Optimum intensity is lower than that of typical MOTs due to photoionization

Parameters:

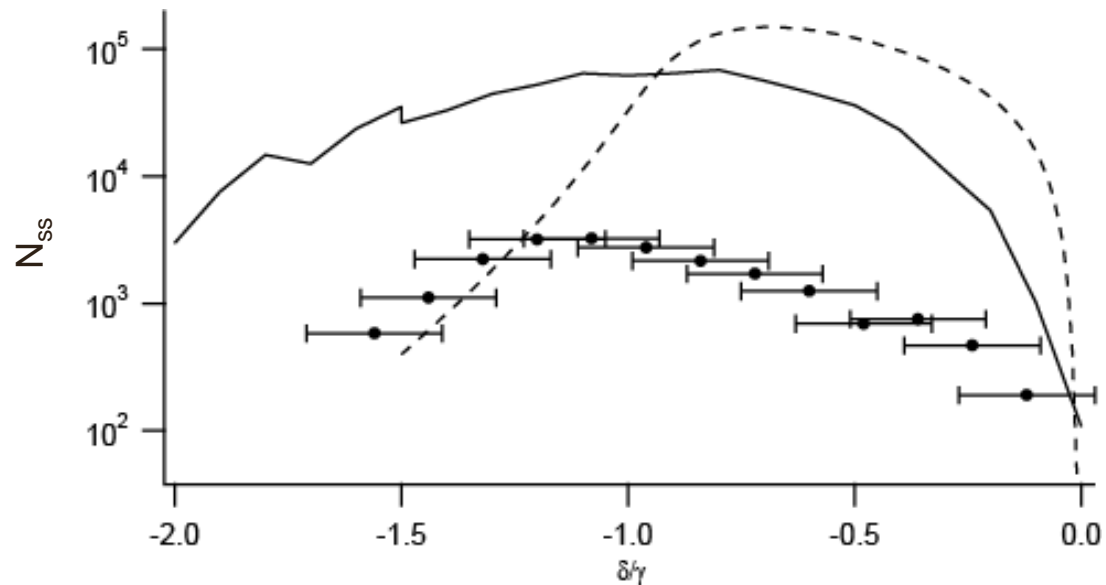
- $w_0 = 1.25$ mm
- $\delta = -0.6\gamma$
- $B' = 500$ G/cm

Detuning:

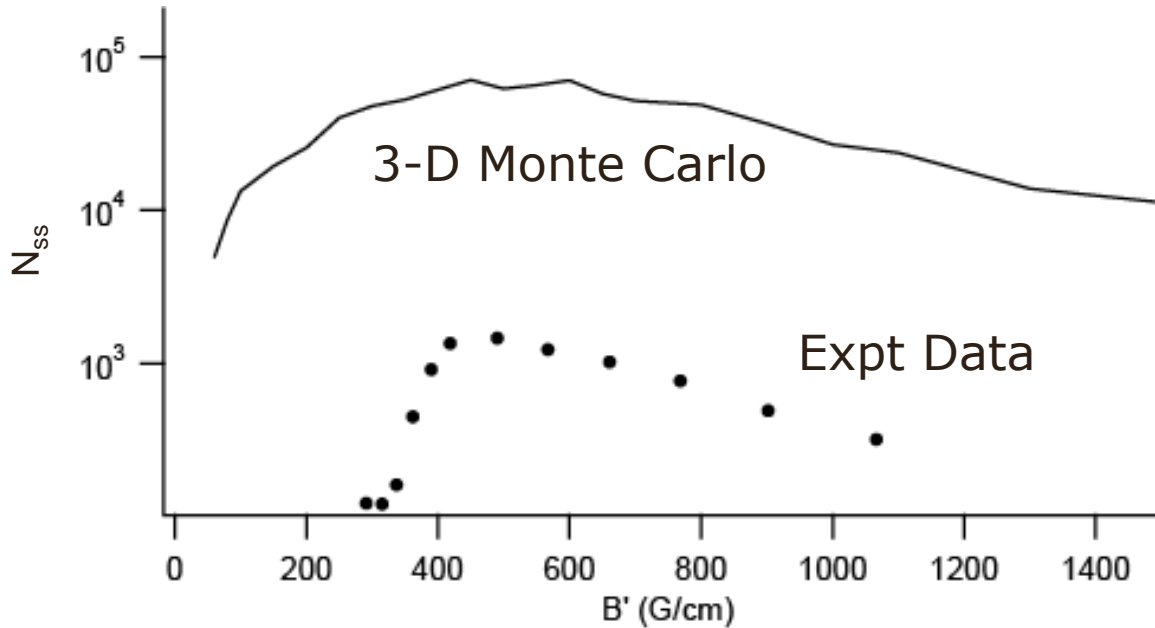
Large DAVLL capture range leads to uncertainty in detuning

Parameters:

- $P = 1.8$ mW
- $w_0 = 1.25$ mm
- $B' = 500$ G/cm



Magnetic field gradient



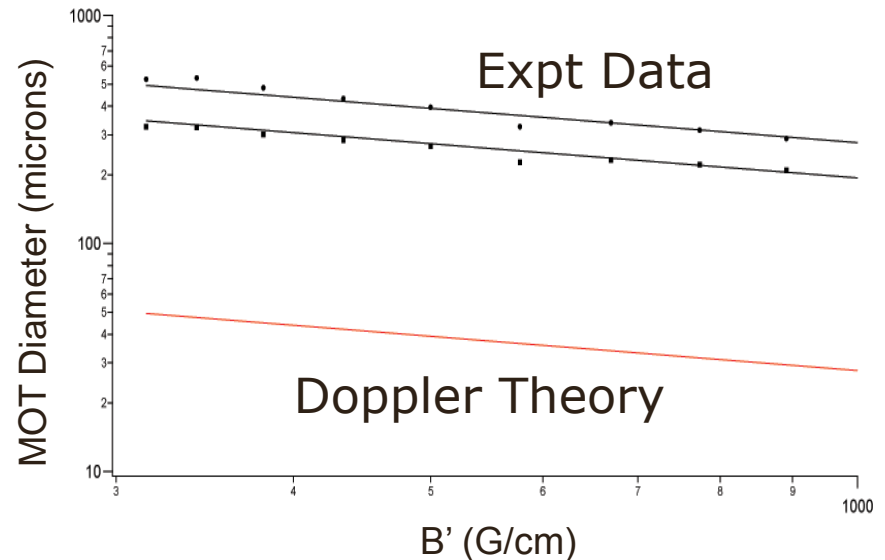
Optimal B-field gradient
when Zeeman shift at
beam waist = linewidth

Parameters:

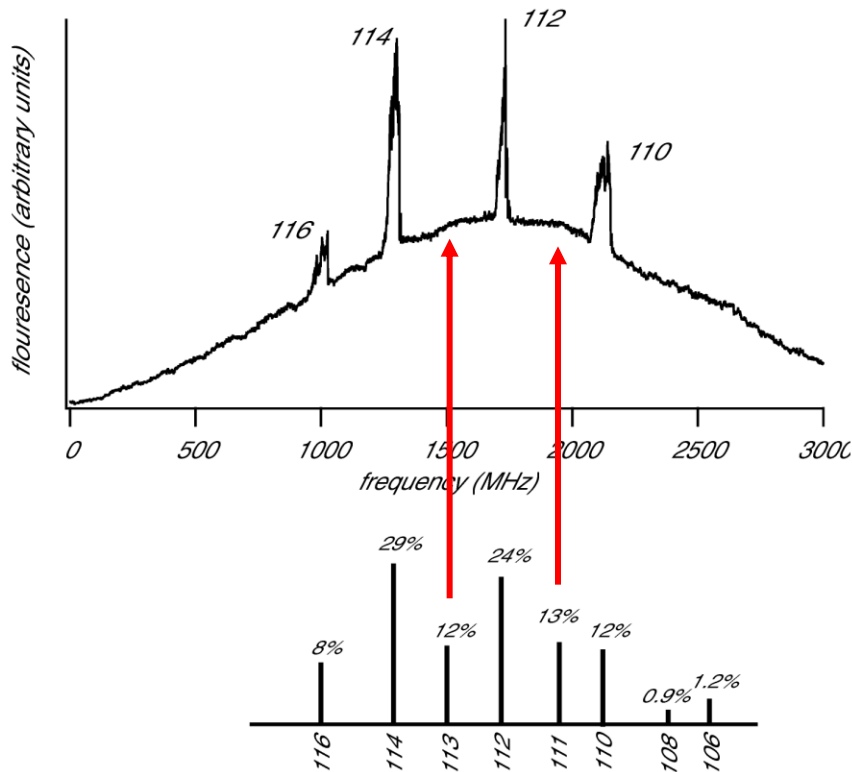
- $P=1.8$ mW
- $w_0=1.25$ mm
- $\delta=-0.6\gamma$

MOT size scales as $1/\sqrt{B'}$
(temperature-limited regime),
but absolute size is $\sim 10\times$
Doppler-expected size

Similar results observed in Sr:
X. Xu, et. al, PRA **66**, 011401 (2002)



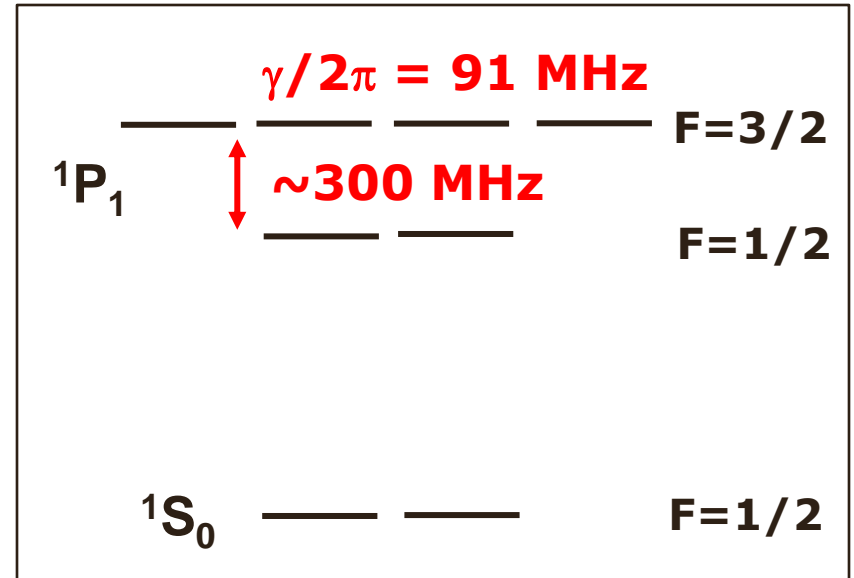
Odd vs. even isotopes



MOT for odd isotopes were not observed.

Similar results observed in Yb:
H. Katori, et. al, PRL **82**, 1116 (1999)

Odd isotopes of Cd ($I=1/2$):

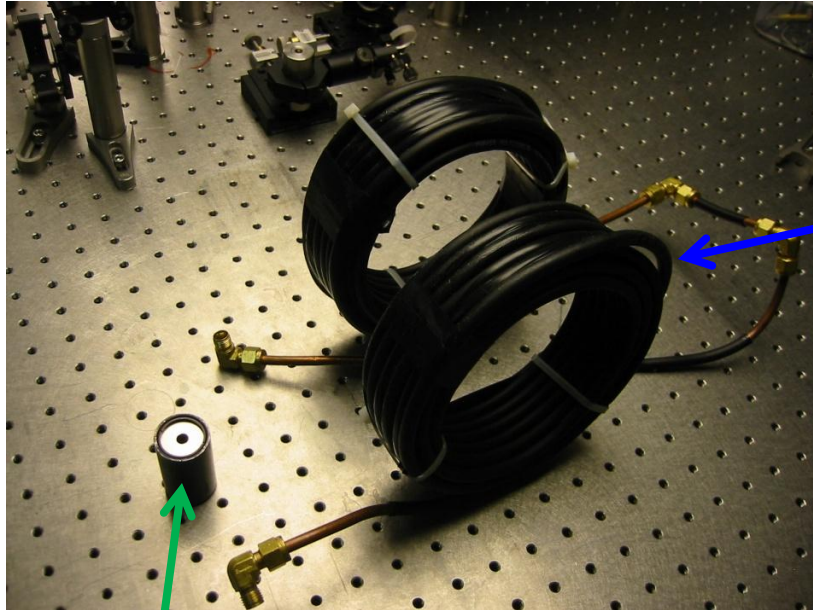


Linewidth \sim the $1P_1$ state hyperfine splitting: bad for laser cooling.

Possible solutions:

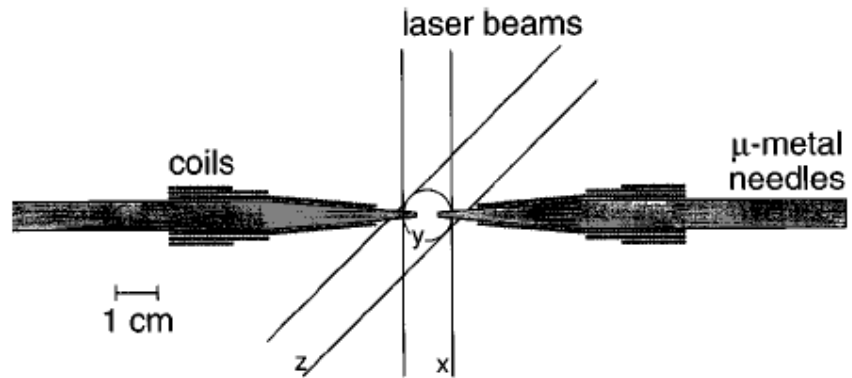
- Dichroic MOT
- Operates in a very high B gradient (Paschen-Bach regime)
- Large laser power with large red detuning

Improve Cd MOT: generate even higher B field gradient



AH coil w/ up to 400 Amp
But ...
bulky
needs water cooling
 B' up to <200 G/cm only

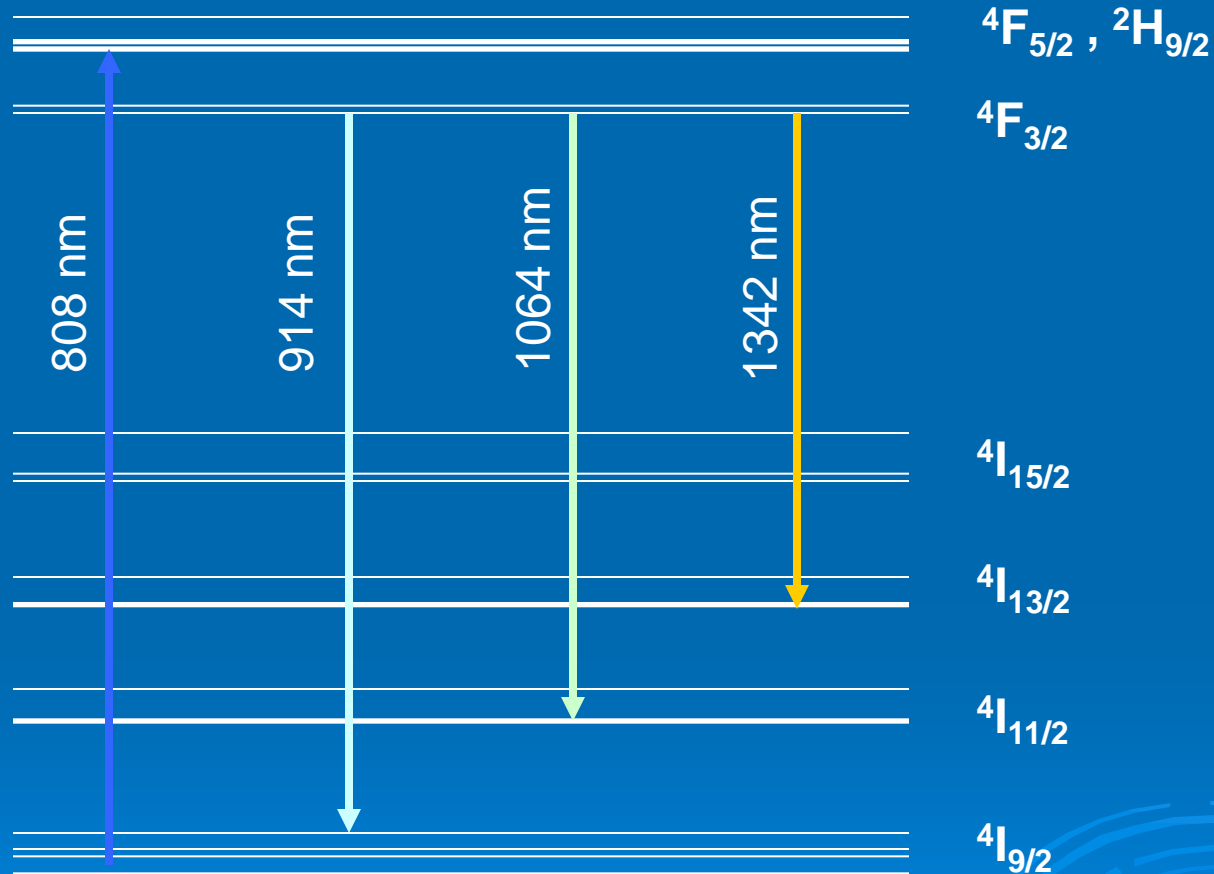
A pair of NdFeB magnets
compact
 B' up to 1500 G/cm !
But ...
not switchable



B' up to 10^4 G/cm
compact
switchable

Improve Cd MOT: generate higher laser power at 229 nm - I

Nd:YVO₄ Crystal Based **RGB** lasers



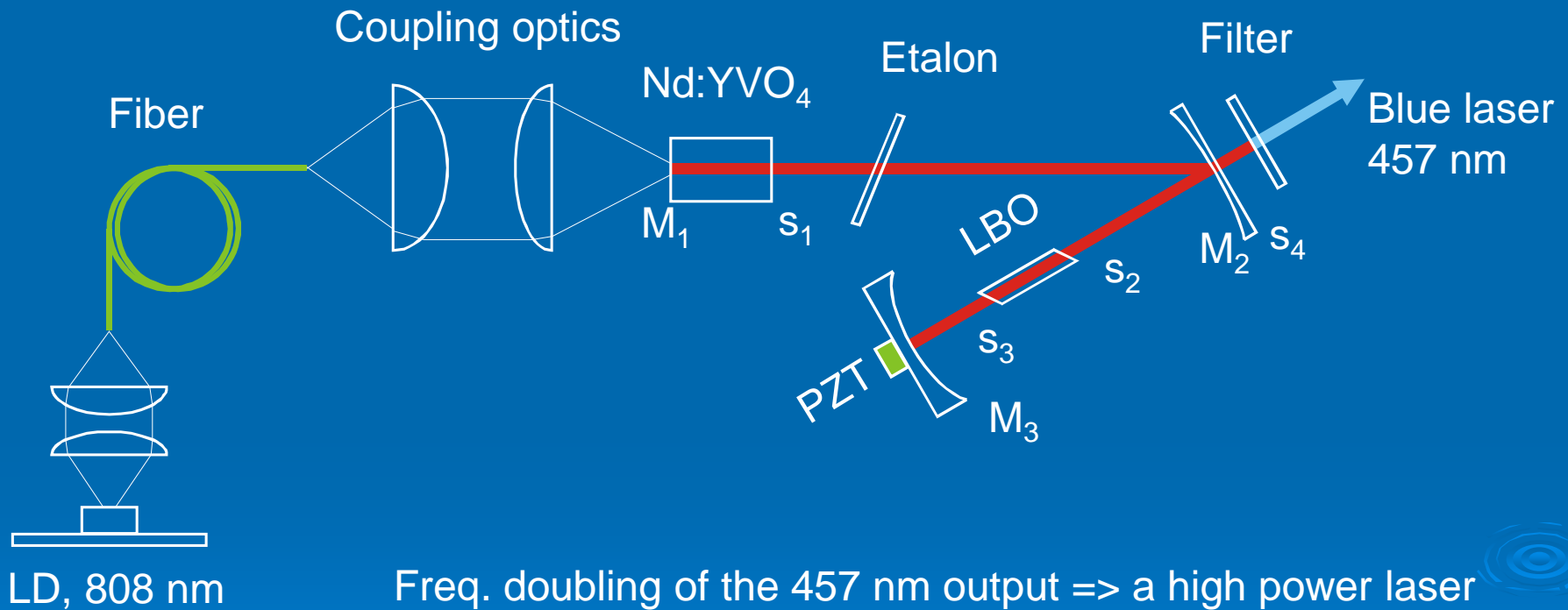
(1342, 1064, 914) nm

x 2

(671, 532, 457) nm

Improve Cd MOT: generate higher laser power at 229 nm - II

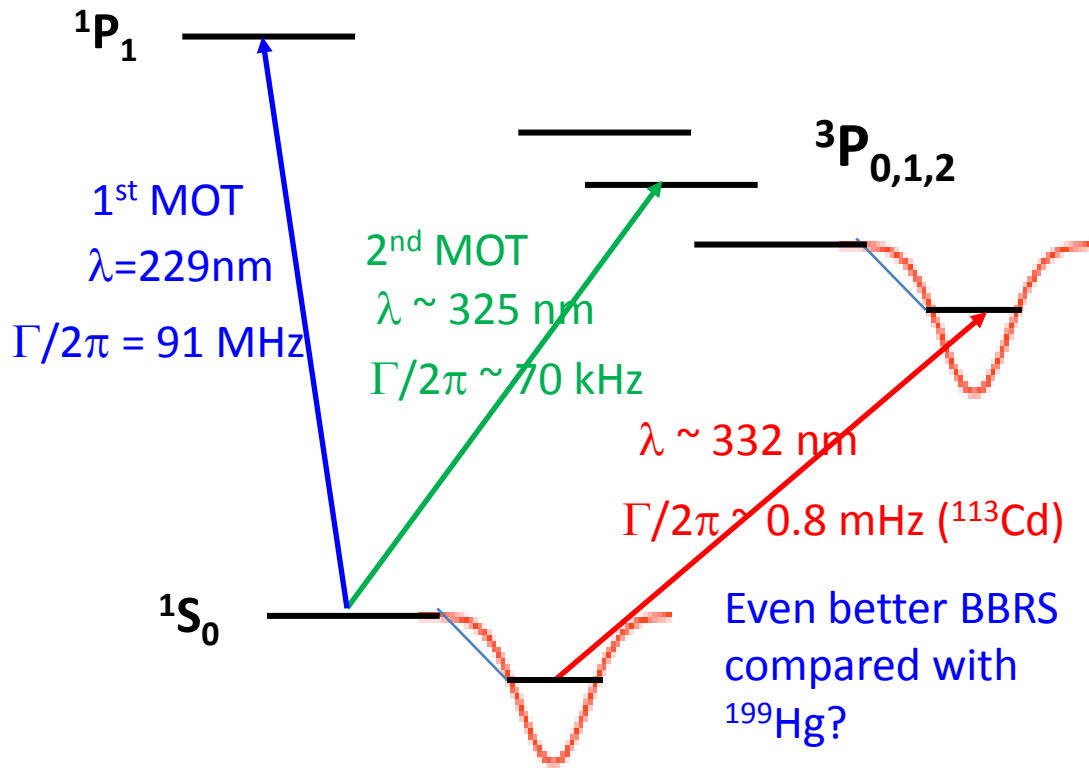
Single Mode 457 nm high power DPSS Laser for Ultracold Atomic Physics



Freq. doubling of the 457 nm output => a high power laser at 229 nm.

What can we do with a Cadmium MOT?

Cadmium for an optical lattice clock?



^{199}Hg

$1S_0 - 3P_1$ (2nd MOT)
 $\lambda \sim 253.7 \text{ nm}$
 $\Gamma/2\pi \sim 1.3 \text{ MHz}$

$1S_0 - 3P_0$ (clock trans.)
 $\lambda \sim 265.6 \text{ nm}$
 $\Gamma/2\pi \sim 111 \text{ mHz}$

Blackbody radiation shift
 $\Delta\nu/\nu$ (T=300 K) $\sim -1.6 \cdot 10^{-16}$
 BBRs better than Yb, Sr.

Currently lowest BBRs: $^{27}\text{Al}^+$ ion.

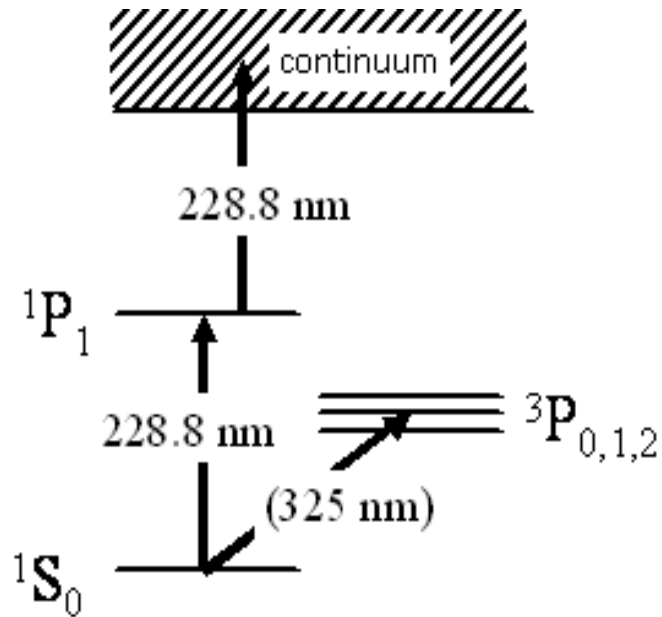
$\Delta\nu/\nu$ (T=300 K) $\sim 8(3) \cdot 10^{-18}$

T. Rosenband *et al.*, *arXiv:physics/0611125*

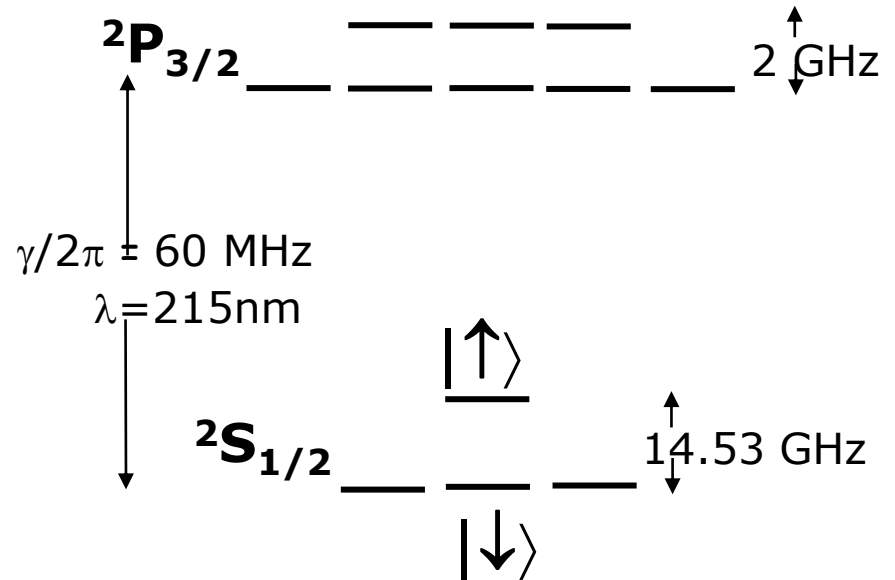
Hg MOT & Opt Lattice Clock

H. Hacish *et al.*, PRL, **100**, 053001 (2008)

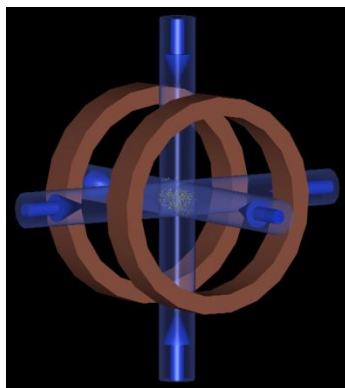
Combining Cd neutrals and ions



Laser cooling works at both 228.8 nm and 325 nm

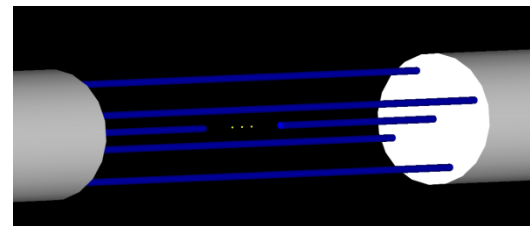


Laser cooling works at 215 nm



MOT

+

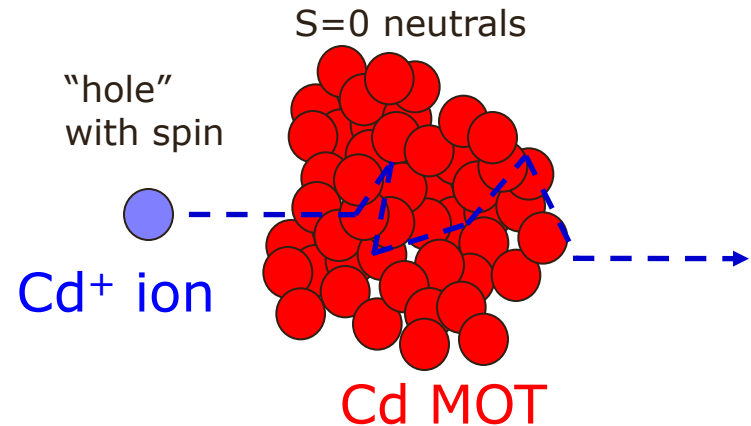


Linear Paul Trap

Combining neutrals and ions

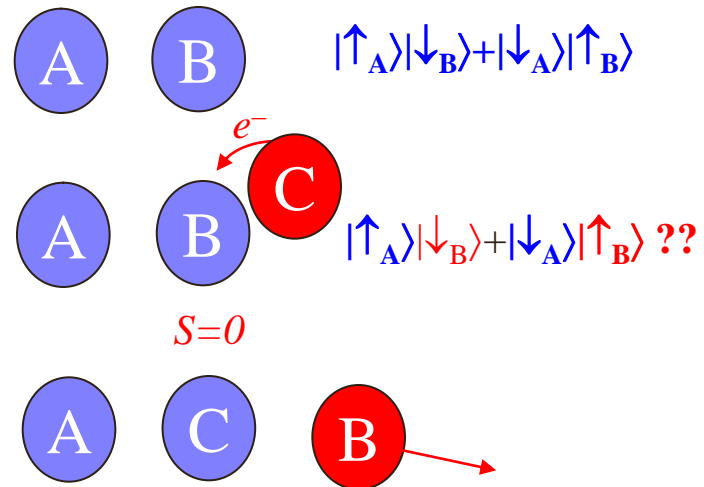
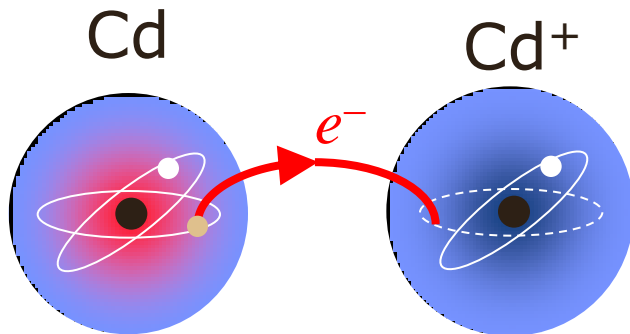
- Transport effects
 - Ultracold charge-exchange collisions
 - "Hole" transport through disordered media
 - Ultracold Quantum chemistry
- Coherence-preserving charge exchange

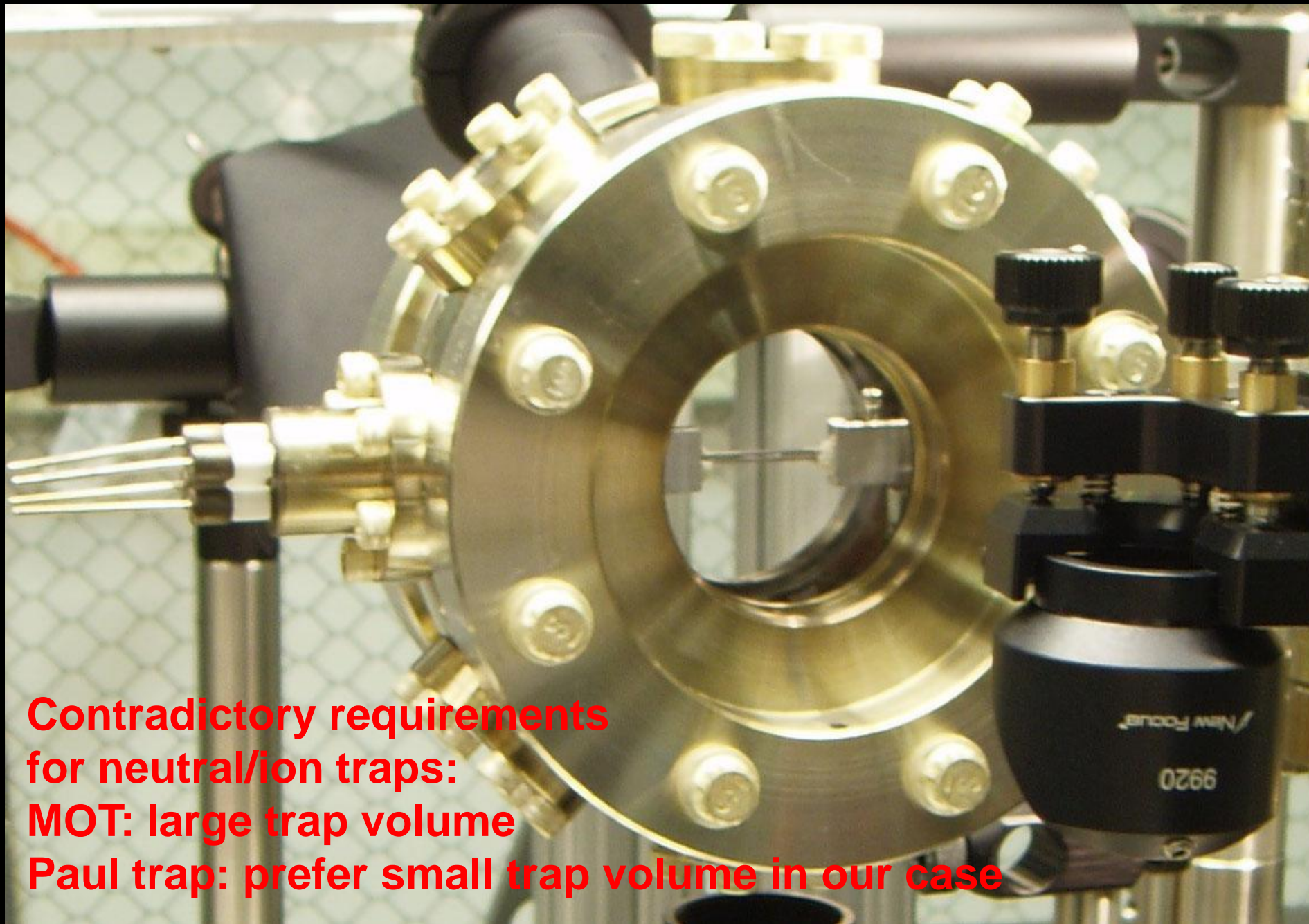
Single ion and a MOT



Ensemble of Yb neutrals and ions:
A. Grier, et al. PRL **102**, 223201 (2009)

Single ion and a single neutral atom





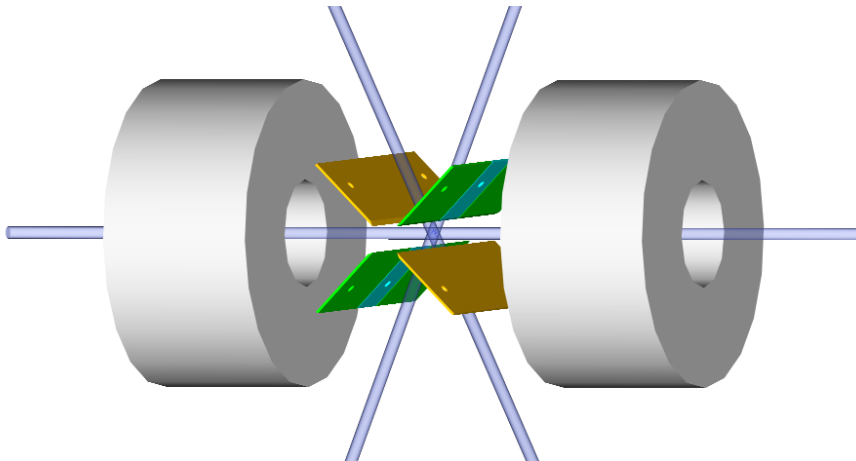
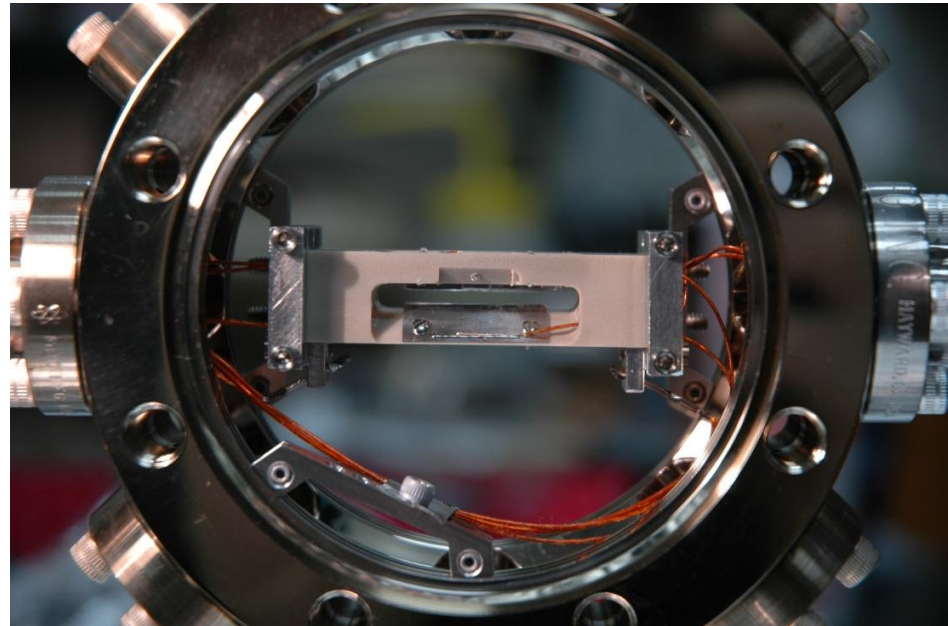
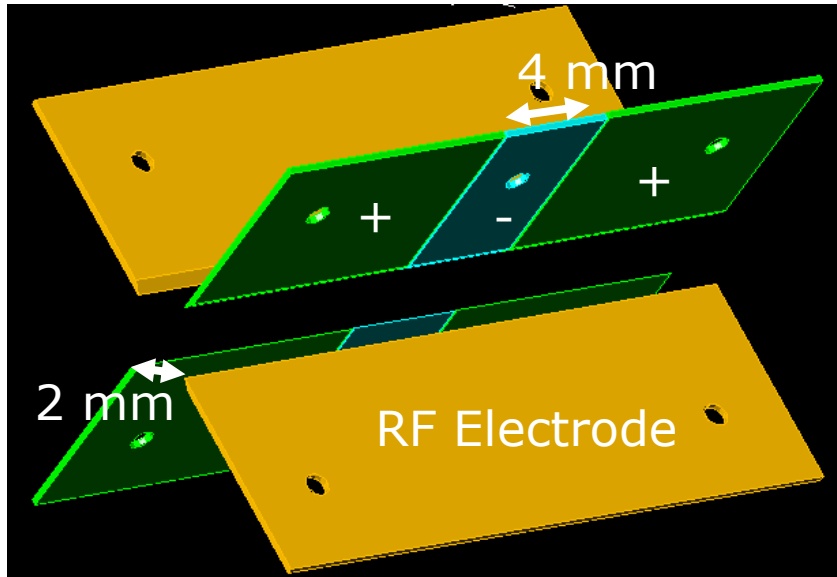
Contradictory requirements

for neutral/ion traps:

MOT: large trap volume

Paul trap: prefer small trap volume in our case

Neutral-Ion hybrid-trap design



Summary

- Realized a magneto-optical trap for Cadmium
 - MOT with extreme trapping parameters:
large linewidth, short wavelength, low laser power, PI loss
 - Determined photo-ionization cross-section
 - Characterized the data with 1D and 3D models
- Outlook
 - Possible research avenues in the future
 - Key enabling techniques for Cd MOT and proposed experiments

University of Michigan

Trapped Ion Quantum Computing

<http://iontrap.physics.lsa.umich.edu/>

Prof. Chris Monroe

Grad Students

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Louis Deslauriers

Patricia Lee

Martin Madsen

David Moehring

Steven Olmschenk

Jon Sterk

Yisa Rumala

Daniel Stick

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Postdocs

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Jacob Burress

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Elizabeth Otto

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Collaborators

Vanderlei Bagnato (Sao Paolo)

Luming Duan (Michigan)

Jim Rabchuk (W. Illinois)

Keith Schwab (Cornell)



University of Maryland

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