

# Ultrashort pulse train synthesized by light waveform control

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AMO Seminar,  
National Tsing Hua University  
Sep. 27, 2010

# Outline

- Introduction
- Review of basic concepts
- High Harmonic Generation
- Molecular Modulation
- Multicolor synthesized
- Outlook

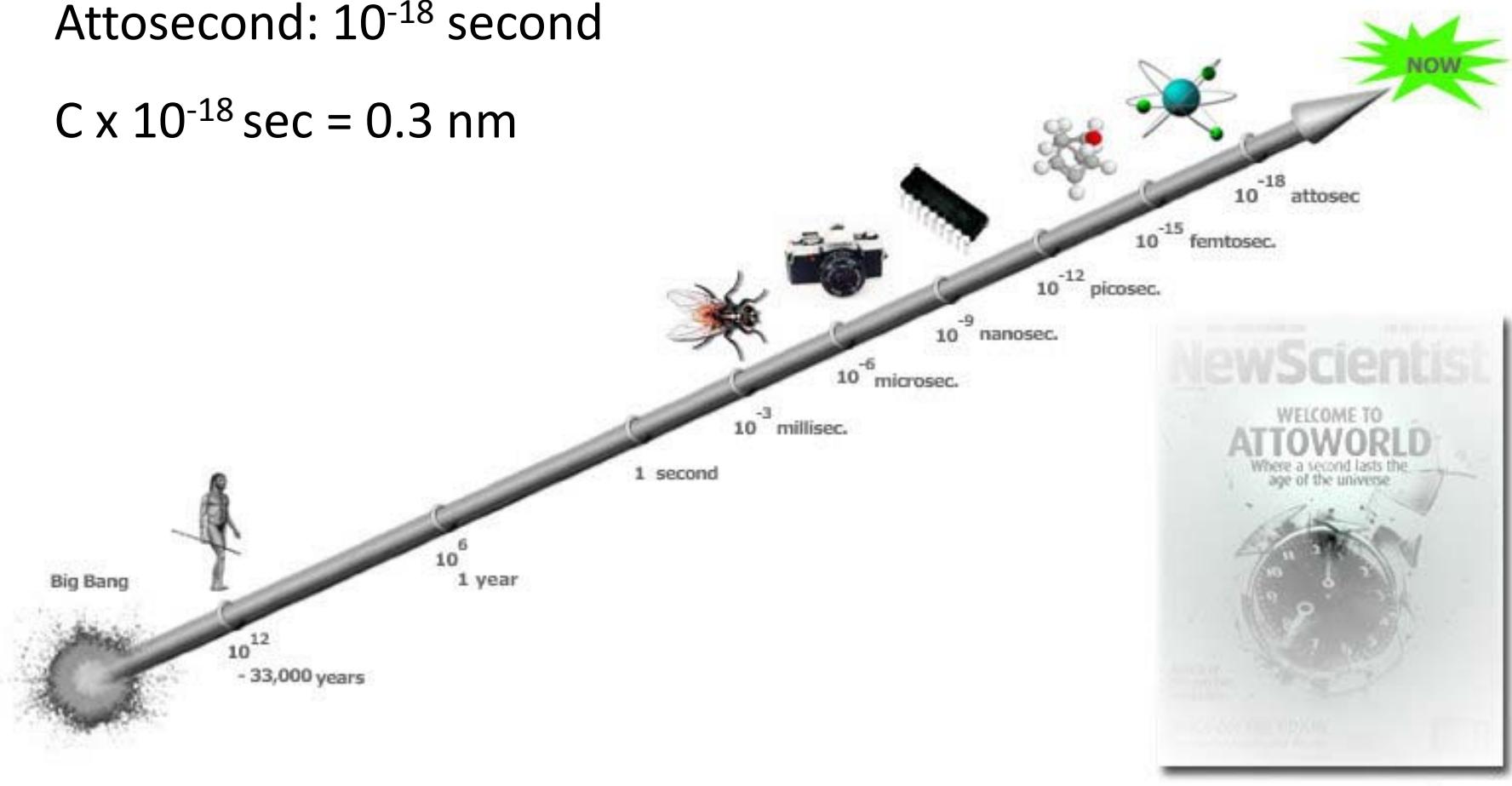
# Outline

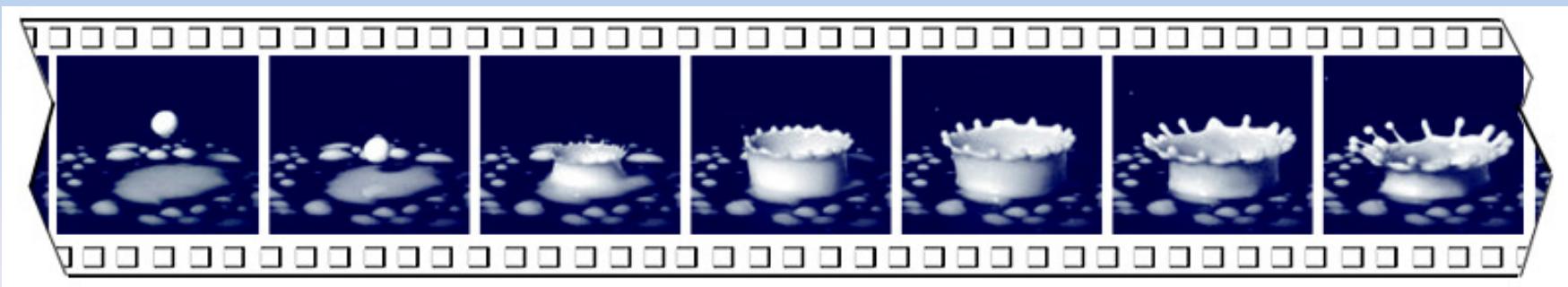
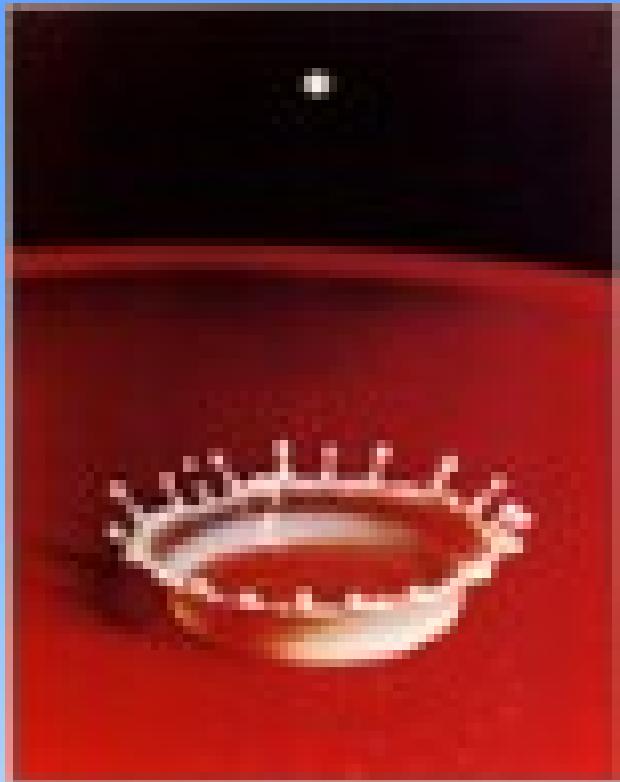
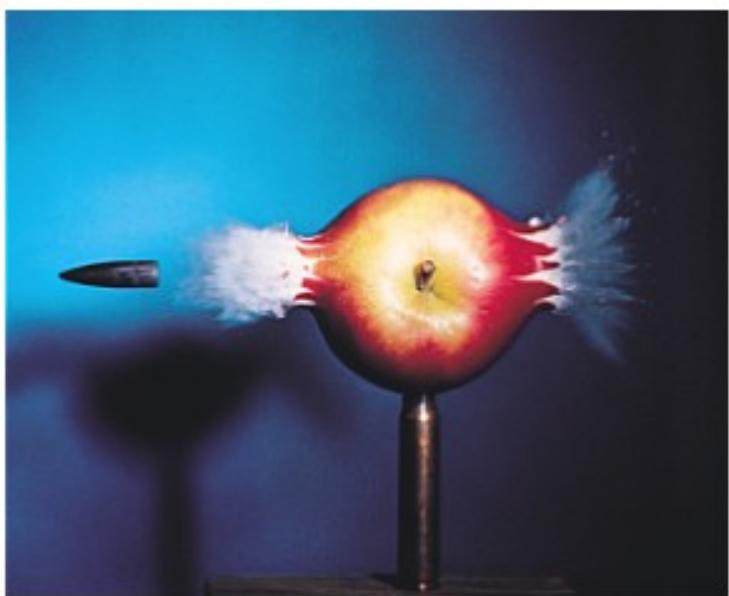
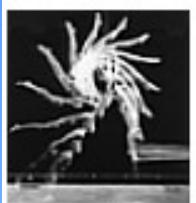
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# Attoworld

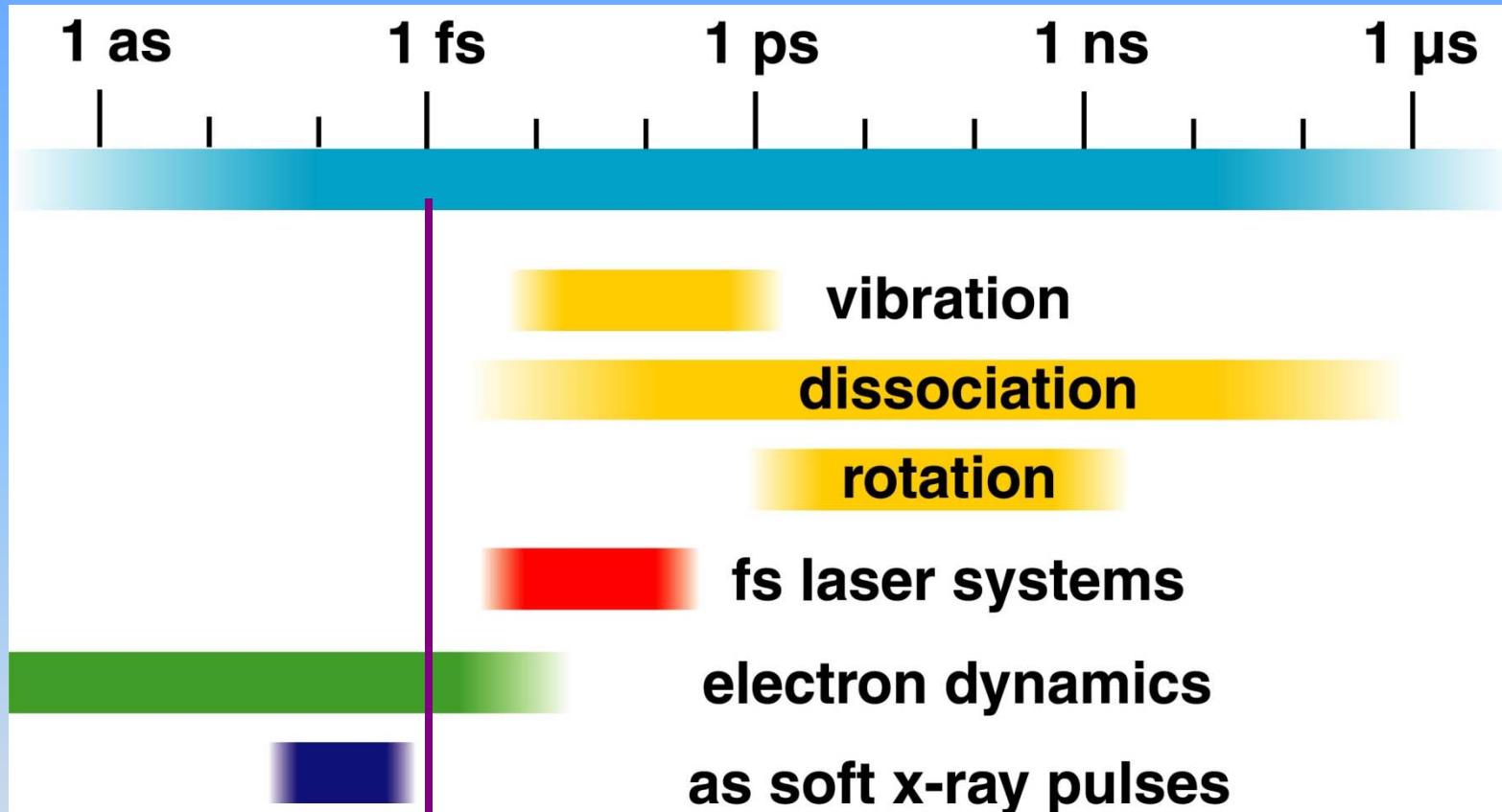
Attosecond:  $10^{-18}$  second

$$C \times 10^{-18} \text{ sec} = 0.3 \text{ nm}$$



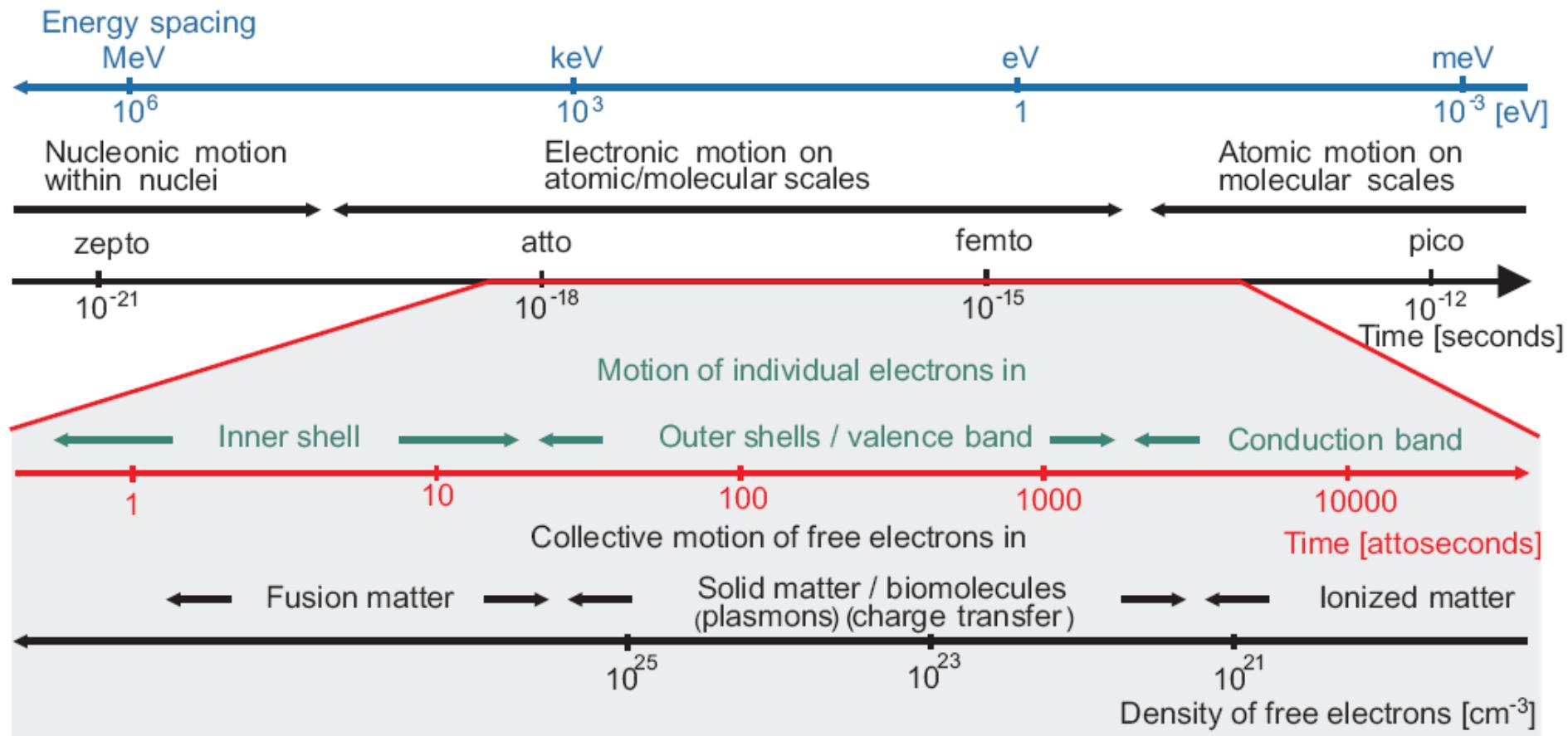


# Request for Ultrashort Pulse

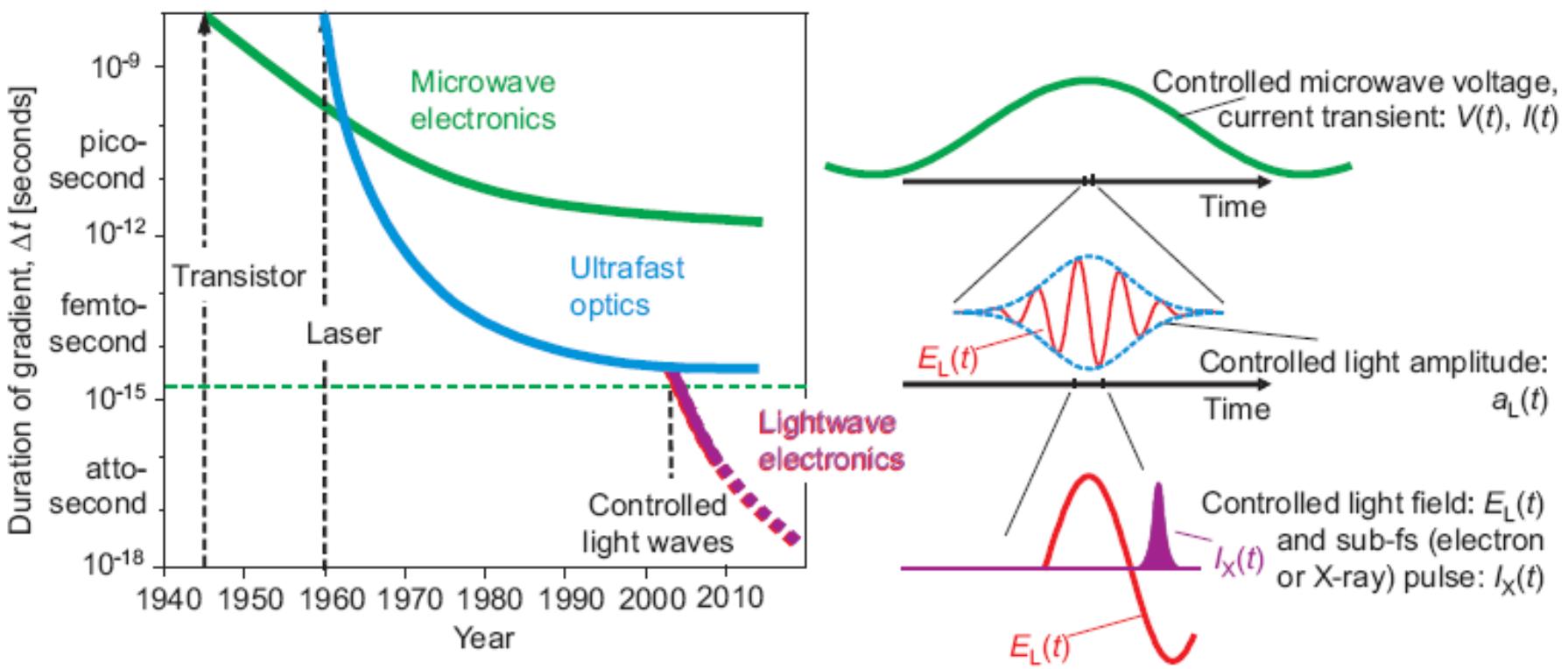


Short pulses can be used to monitor and control  
**molecular** and **electronic** motion

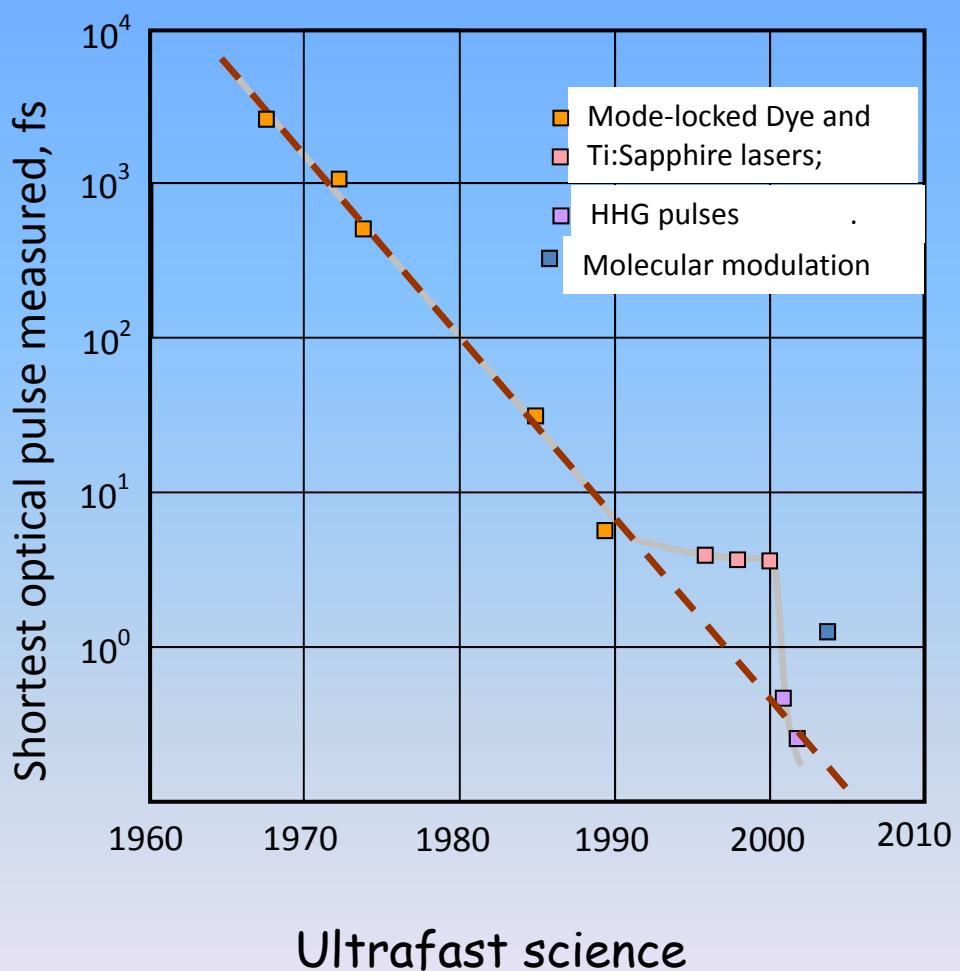
# Electronic Motion



# Evolution of Ultrafast Science

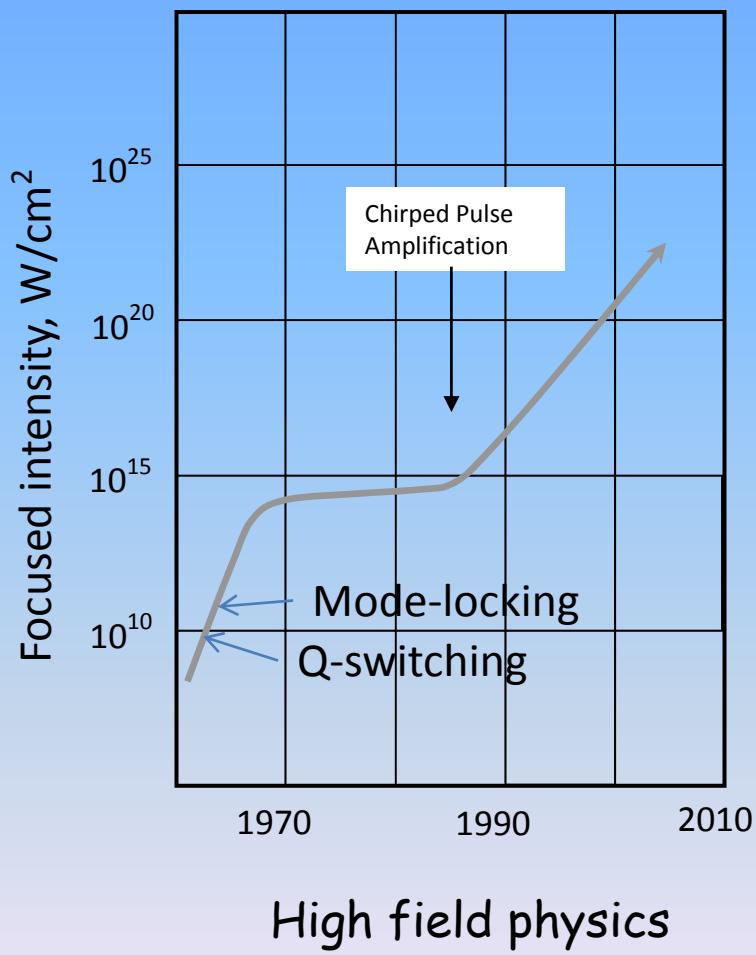


## Laser pulses got shorter over the years



Ultrafast science

## Peak intensity increased



High field physics

# Outline

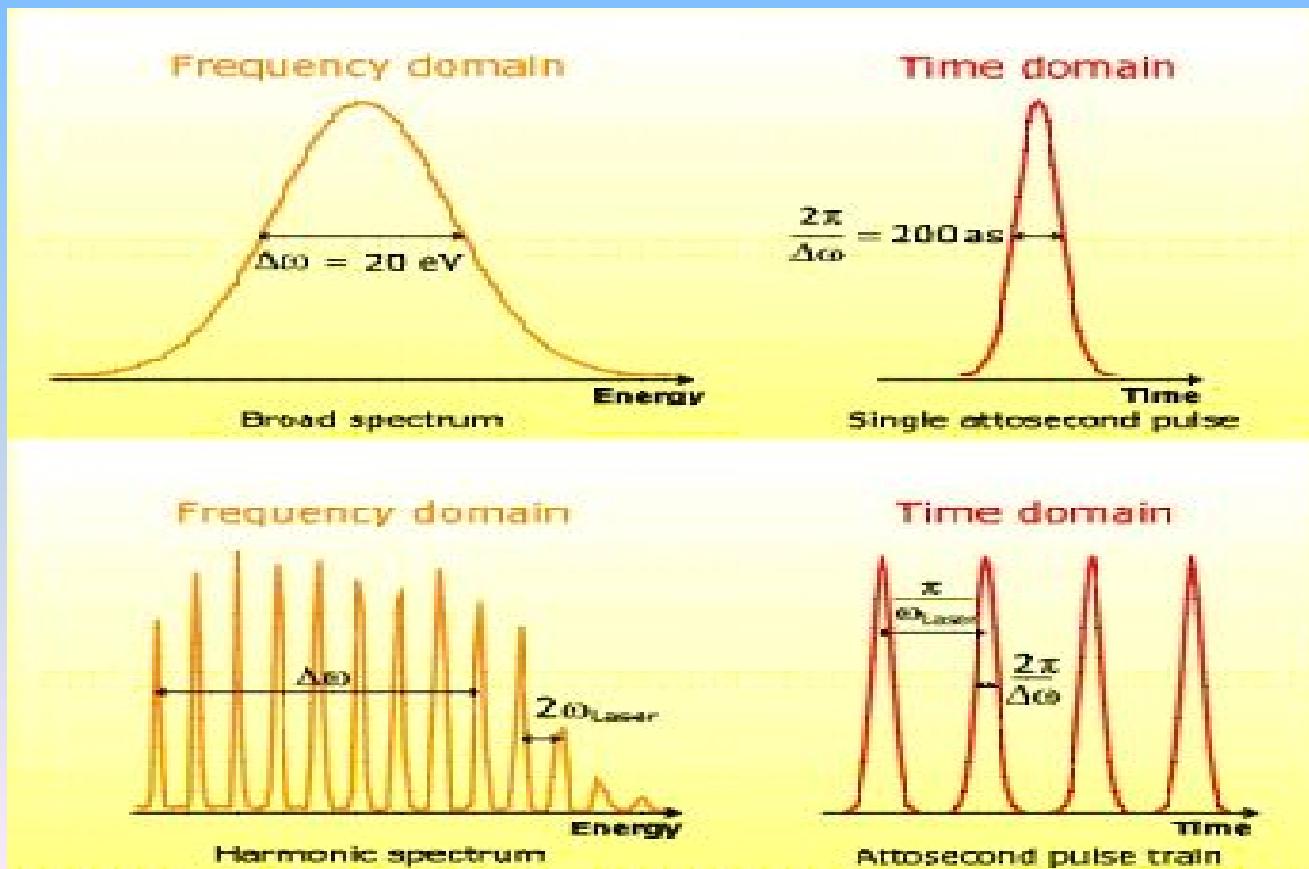
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# Correlation Between Time and Frequency

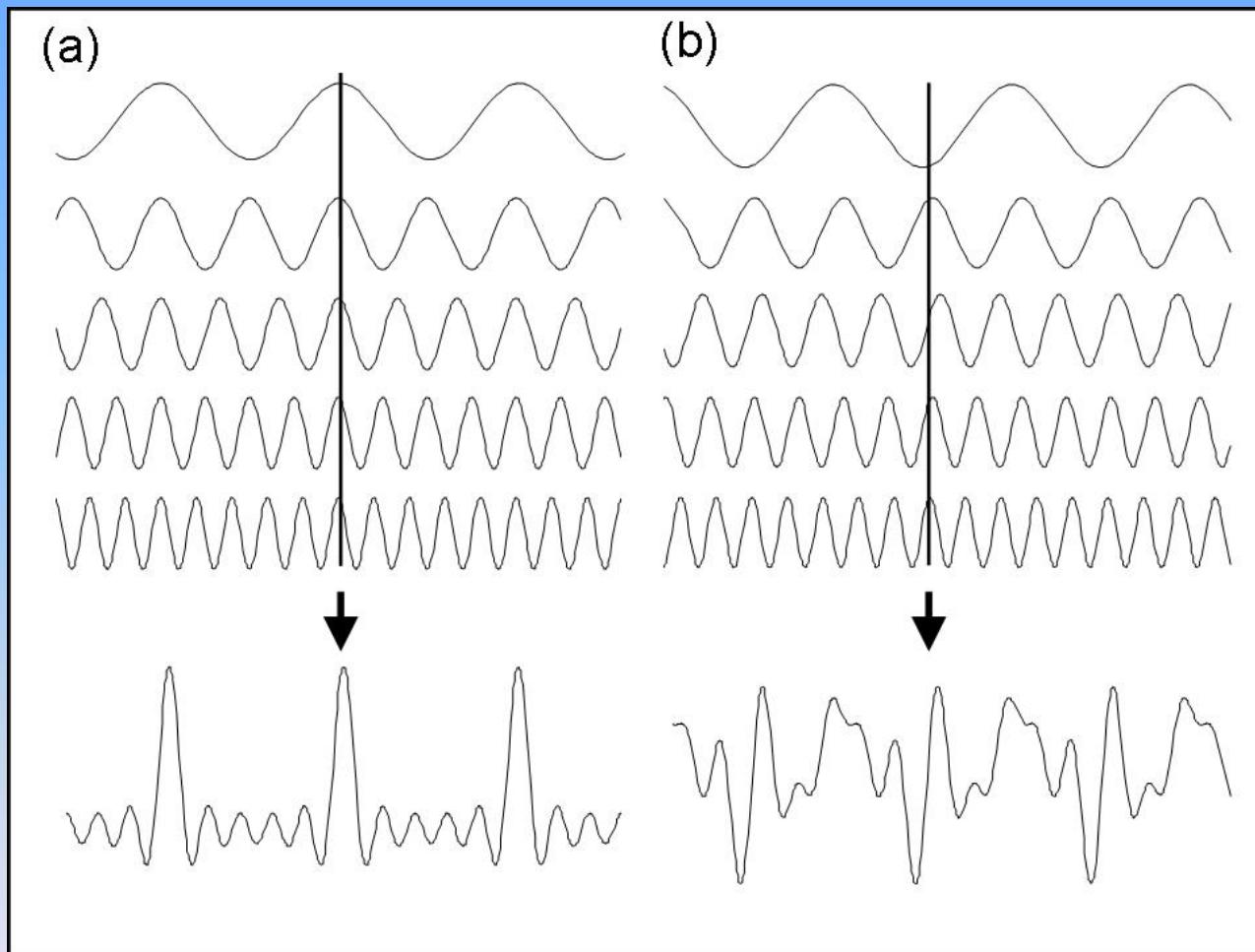
$$x(t - t_0) \xleftrightarrow{FT} e^{-j\omega t_0} X(\omega)$$

Fourier transform:

$$X(\omega) = \int_{-\infty}^{\infty} x(t) e^{-i\omega t} dt$$



# Principle of optical interference of coherent light fields



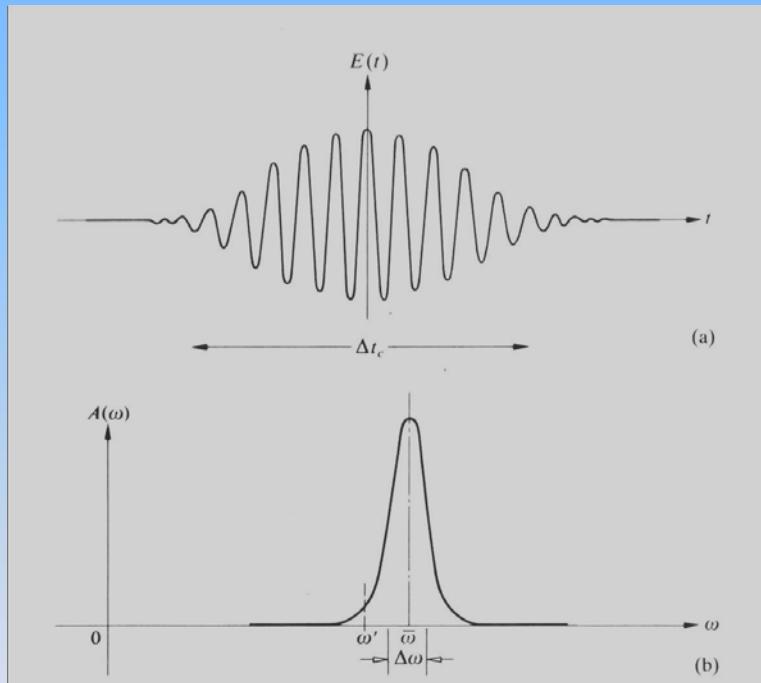
In phase

Random phase

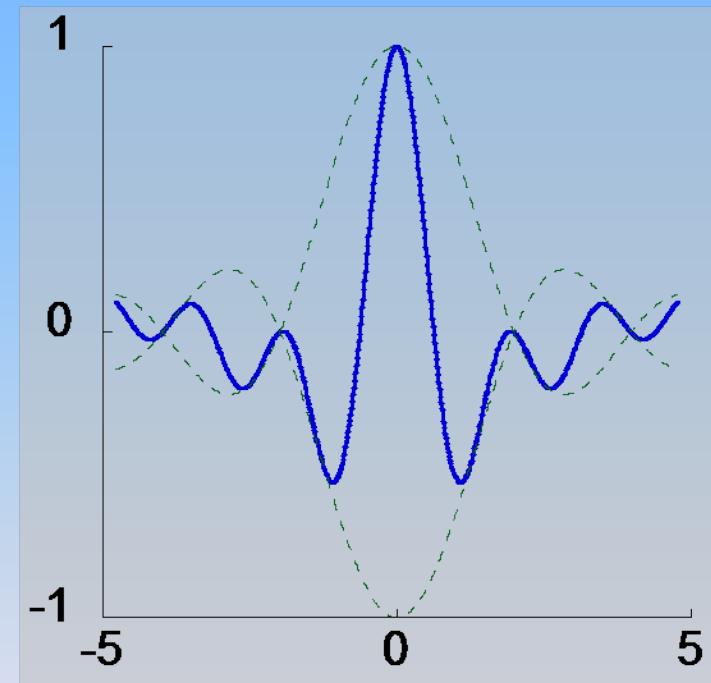
# What is a single cycle optical pulse

(a) Many waves propagating to form a wave packet (left)

(b) Ultimate wavepacket is a single-cycle and sub-cycle pulse (right)



(a)



(b)

# Optical cycle

$$E(t) = \tilde{E}(t) + c.c.$$

$$\tilde{E}(t) = A(t)e^{i(\omega_0 t + \phi)}$$

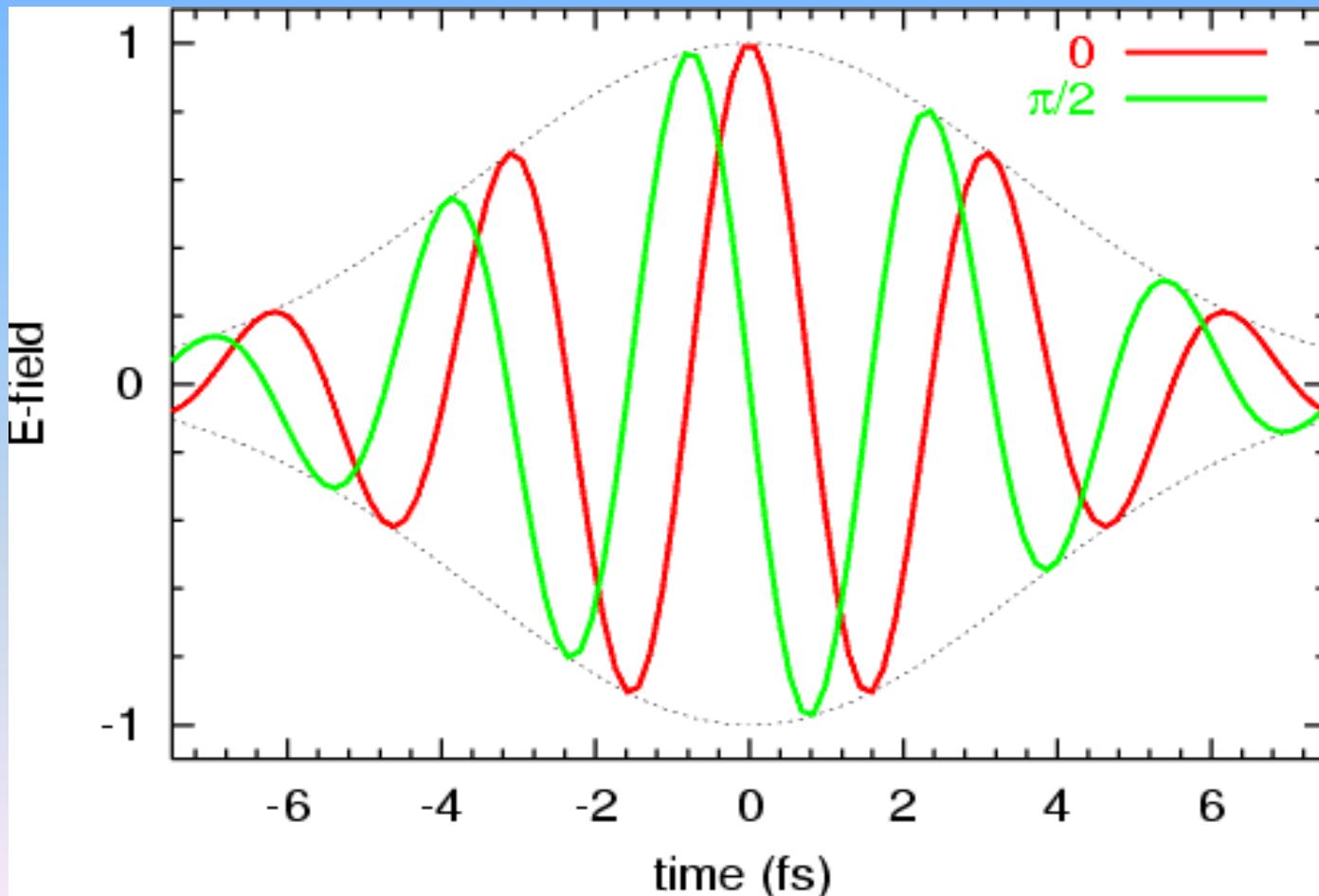
$$\omega_0 = \frac{\int_0^\infty \omega |E(\omega)|^2 d\omega}{\int_0^\infty |E(\omega)|^2 d\omega}$$

Carrier frequency

$E(\omega)$  : Fourier transform of  $E(t)$

# Carrier envelope phase

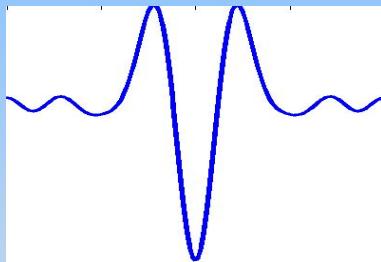
$$E(t) = E_0(t) \cos(\omega_0 t + \underline{\phi})$$



# Single cycle waveforms

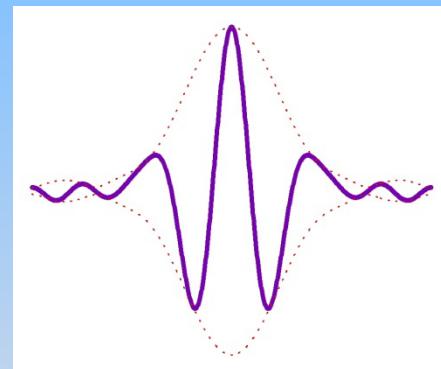
Inverted cosine

$$\phi_n = \pi$$



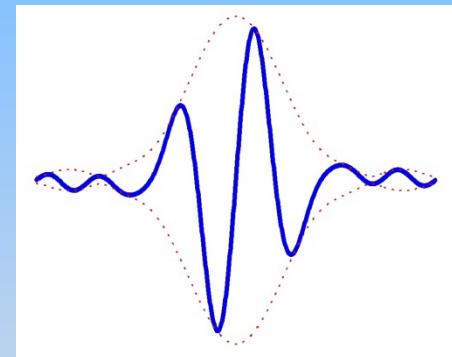
cosine pulse

$$\phi_n = 0$$



sine pulse

$$\phi_n = \pi/2$$



780 nm



12,820 cm<sup>-1</sup>

200 nm

50,000 cm<sup>-1</sup>



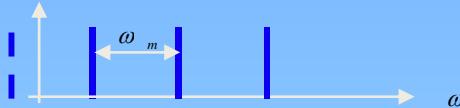
2.6 fs

684 as

# Constant carrier envelope phase

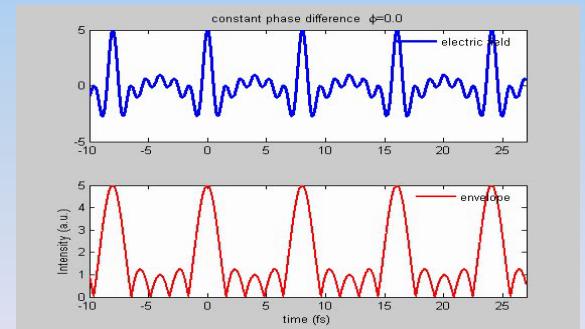
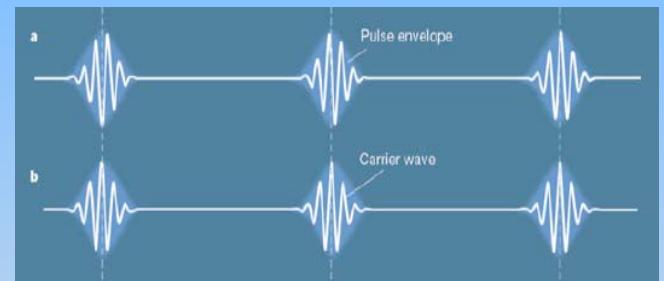
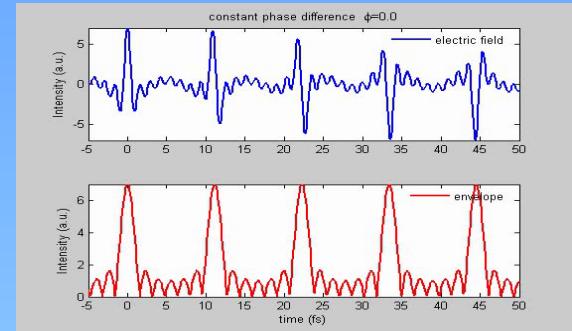
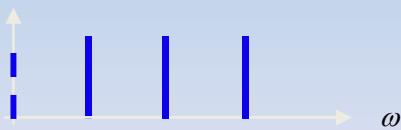
$$E(t) = \sum_n E_n(t) \cos(\omega_n t + \phi_n)$$

**incommensurate**     $\omega_n = n\omega_m + \omega_{ceo}$      $\phi_n = \omega_{ceo}t + \phi'_n$



**commensurate**     $\omega_q = n\omega_m$      $\phi_n = \phi_{CEP} + n\phi_m$

$$E(t) = \sum_n A_n(t) \cos(n\omega_m(t + \phi_m/\omega_m) + \phi_{CEP})$$



Constant CEP requires that the frequencies are commensurate and the relative phases form an arithmetic series

# Ingredients of an attosecond single-cycle optical pulse:

1. Broad spectrum - 2 or more octaves
2. In phase condition
3. Constant carrier envelope phase:
  - Commensurate frequencies
  - Constant phase difference between adjacent spectral components
4. Stable and controllable carrier envelope phase

Light Waveform Control

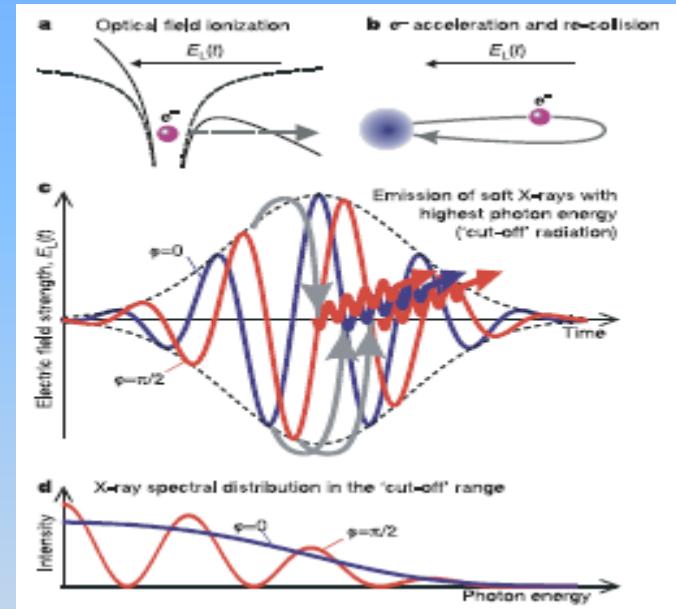
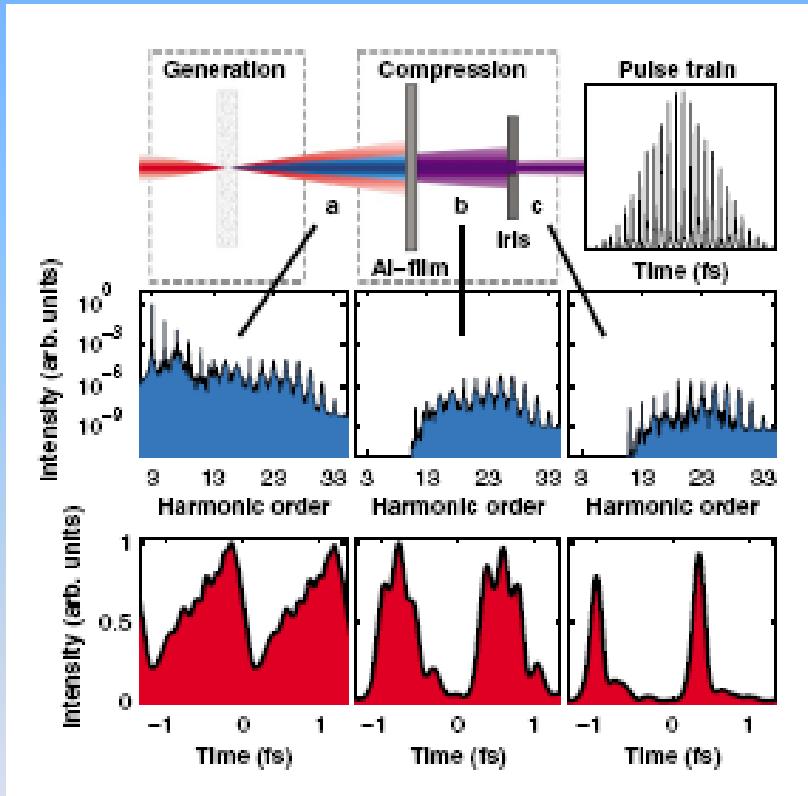
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# Methods of Generating Attosecond Pulses

A

High-order harmonic generation of phase-stabilized femtosecond pulse

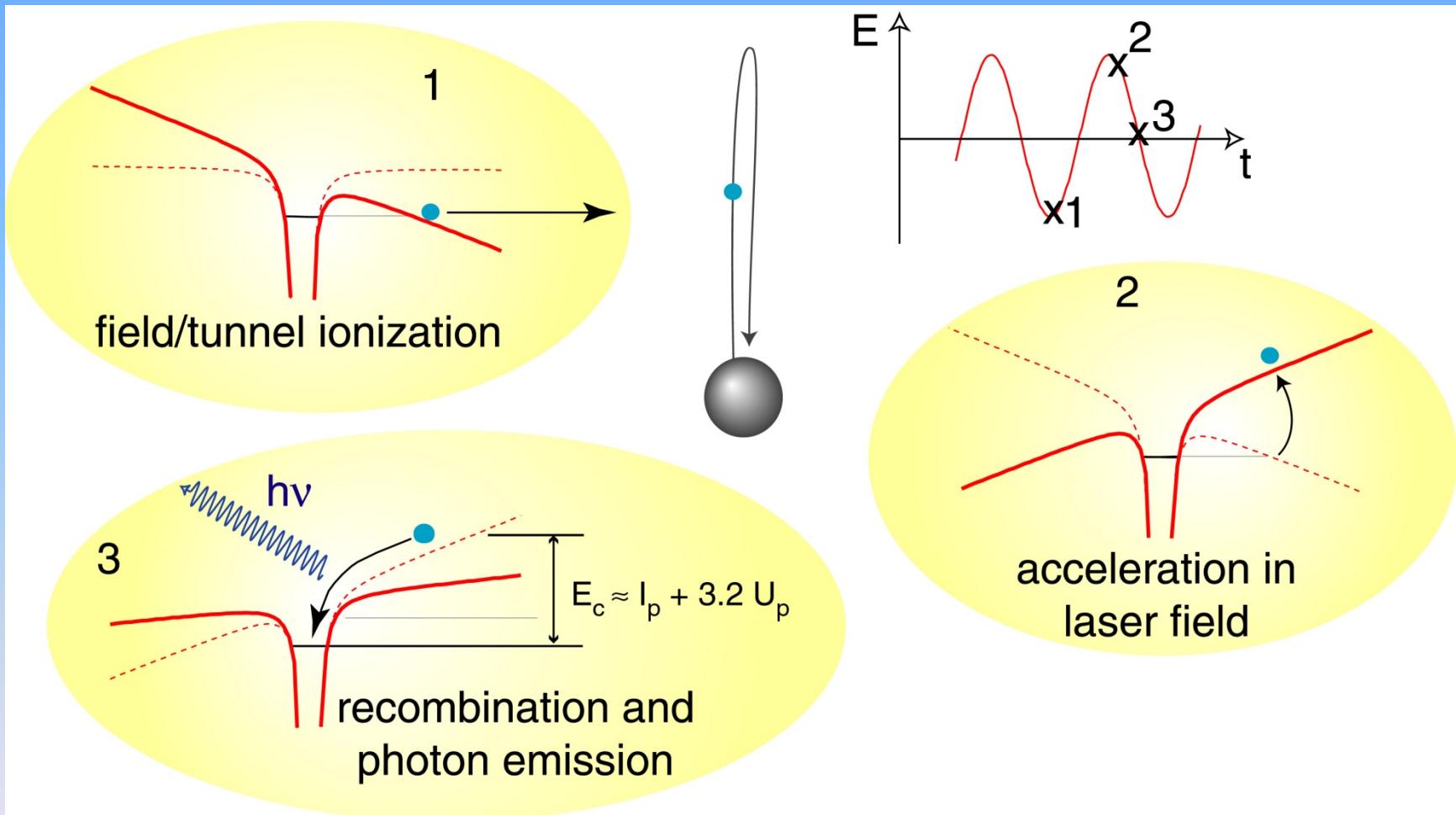


single pulse 100 attosecond  
30-100 eV photons  
very low power  
constitutes a few cycles

Krause et.al., Nature 421, 611 (2003)

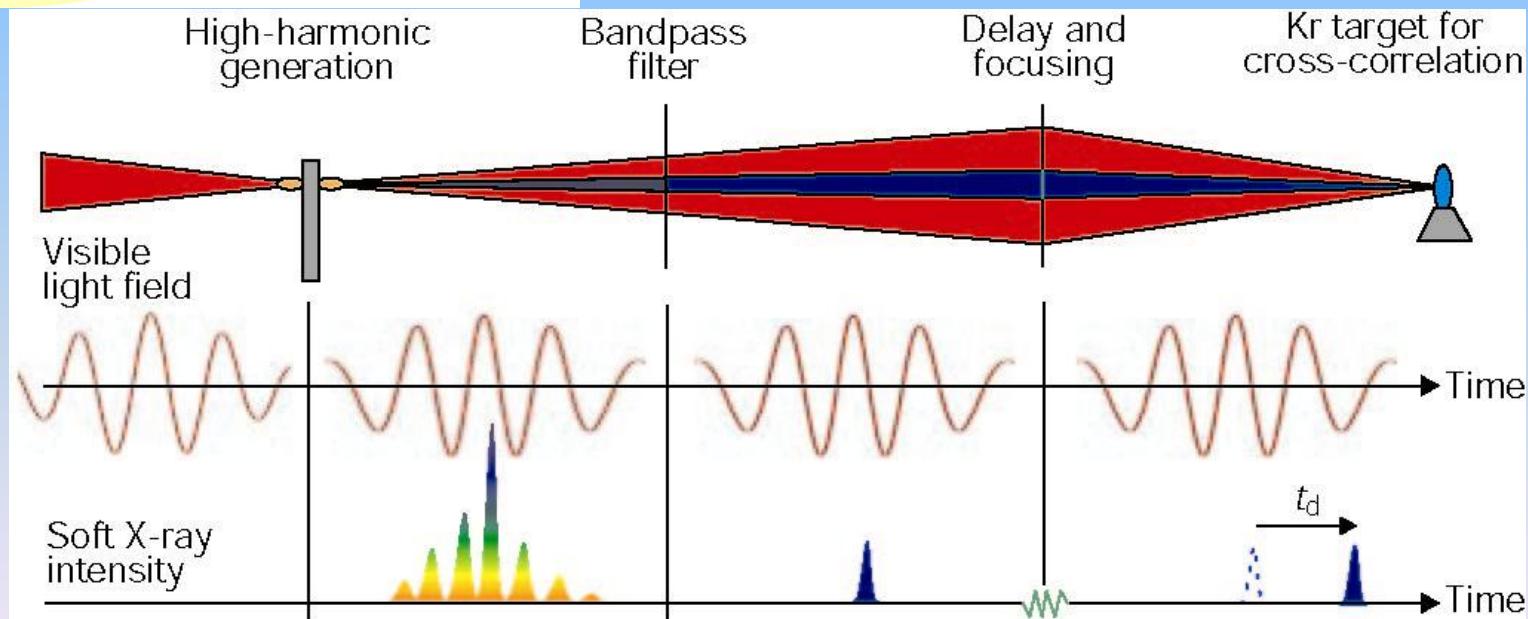
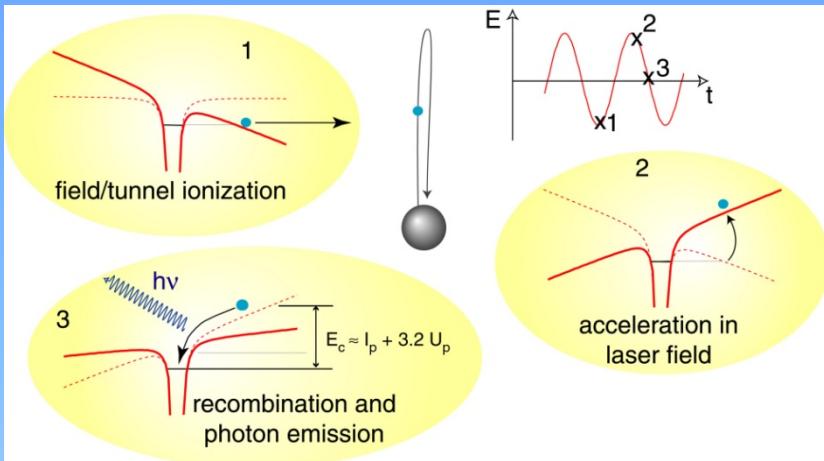
R. Lopez-Martens et. al., PRL 94, 033001 (2005)

# Three-step model



P. Corkum, Phys. Rev. Lett. **71**, 1994 (1993)

# Isolated Attosecond-pulse production



# Attosecond spectroscopy in condensed matter

A. L. Cavalieri<sup>1</sup>, N. Müller<sup>2</sup>, Th. Uphues<sup>1,2</sup>, V. S. Yakovlev<sup>3</sup>, A. Baltuška<sup>1,4</sup>, B. Horvath<sup>1</sup>, B. Schmidt<sup>5</sup>, L. Blümel<sup>5</sup>, R. Holzwarth<sup>5</sup>, S. Hendel<sup>2</sup>, M. Drescher<sup>6</sup>, U. Kleineberg<sup>3</sup>, P. M. Echenique<sup>7</sup>, R. Kienberger<sup>1</sup>, F. Krausz<sup>1,3</sup>  
& U. Heinzmann<sup>2</sup>

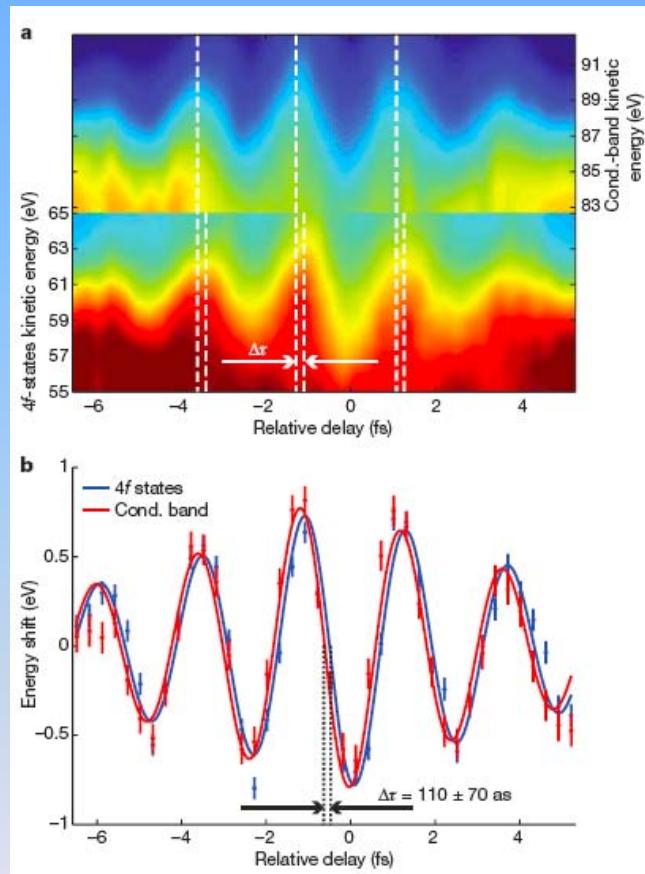
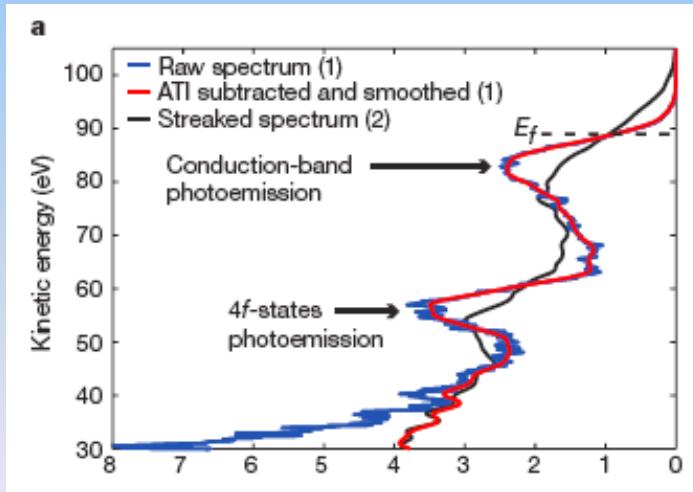
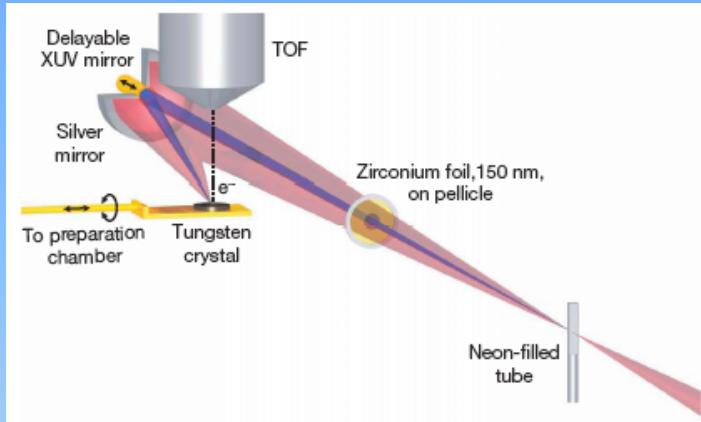


Figure 3 | Evidence of delayed photoemission. a, The 4f and conduction-band spectrograms, following cubic-spline interpolation of the measured data

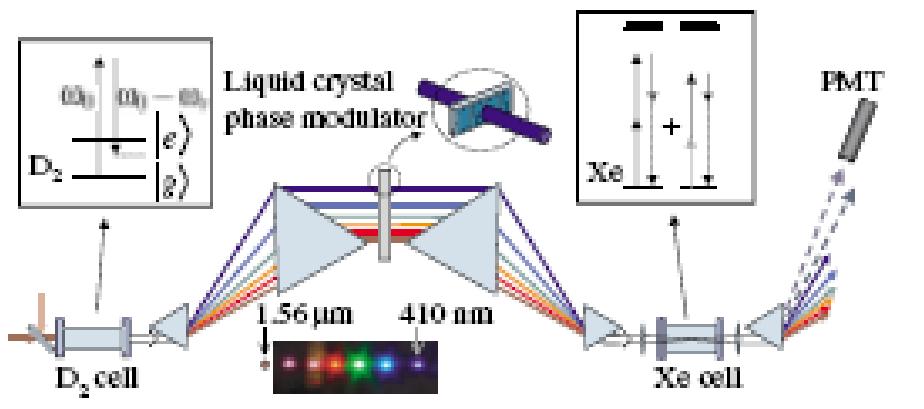
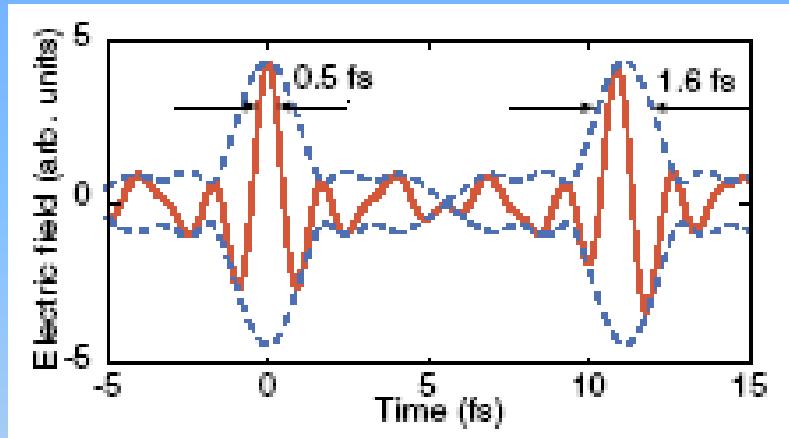
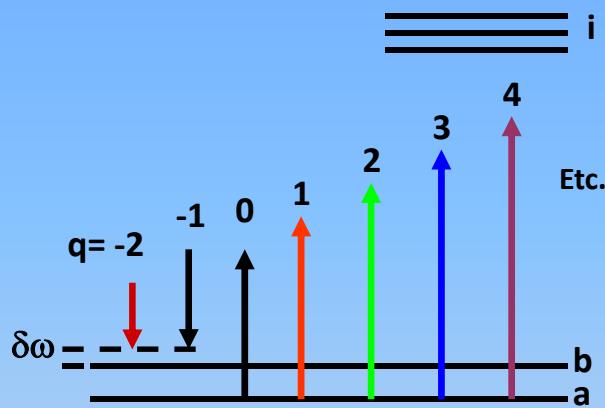
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# Methods of Generating Attosecond Pulses

B

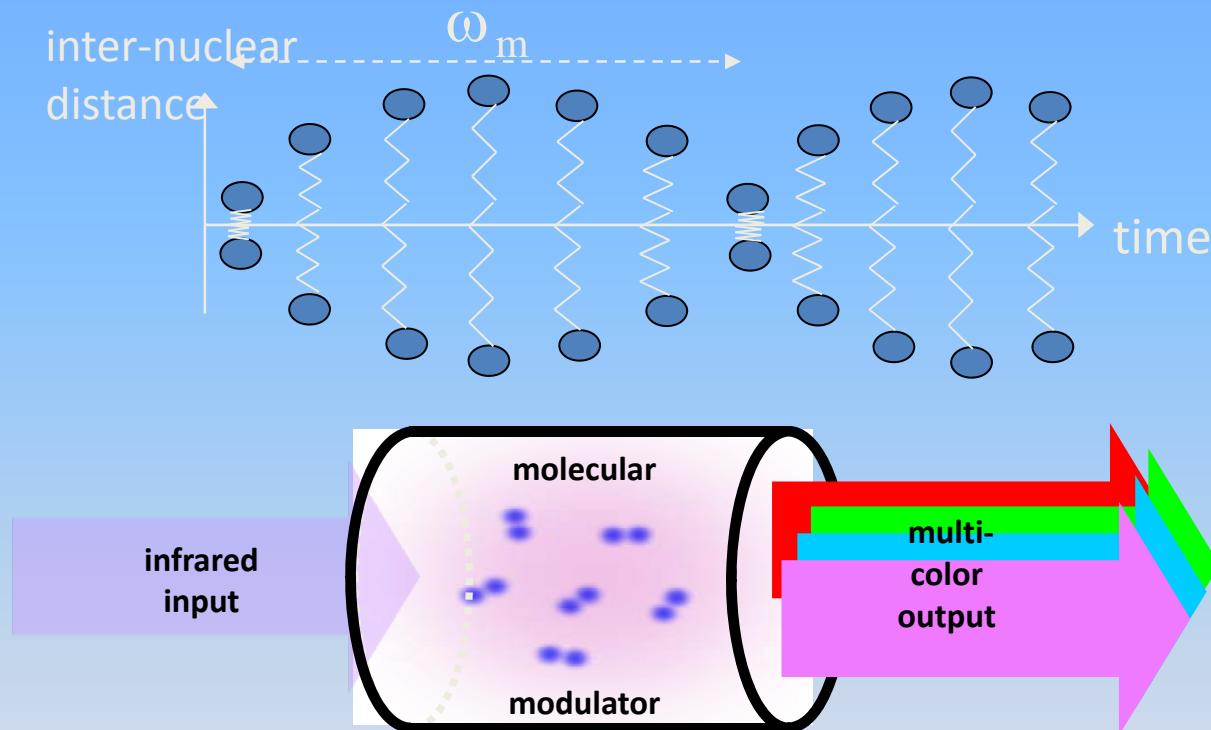
High-order stimulated Raman scattering using molecular modulation



IR-UV region  
good power  
single-cycle  
8-50 fs pulse spacing  
limited to  $\sim 300-500$  as

# Molecular Modulation

Molecular modulation is analogous to electro-optic modulation



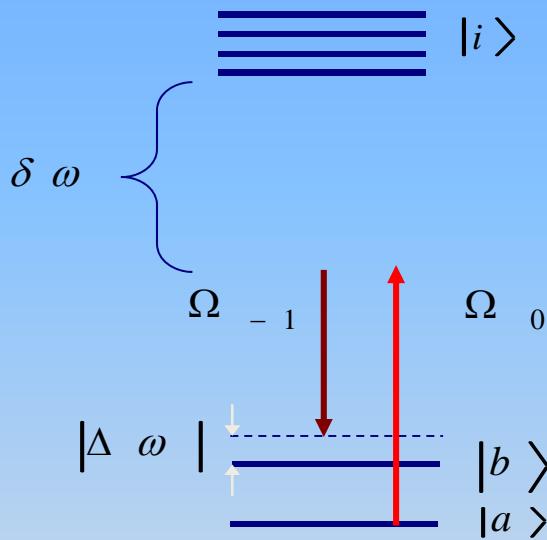
Refractive Index

$$n = n_0 + \delta \cos \omega_m t$$

$$\omega_q = \omega_0 + q\omega_m \quad q = -2, -1, 0, 1, 2, 3, \dots$$

# Coherent Molecular Excitation

- Two strong laser fields adiabatically drive the molecules into a maximally coherent state.



Maximal coherence,  $\rho_{ab} = 0.5$

$$\frac{\partial \rho_{aa}}{\partial \tau} = i(\Omega_{ab}\rho_{ba} - \Omega_{ba}\rho_{ab}) + \gamma_{||}\rho_{bb}$$

$$\frac{\partial \rho_{bb}}{\partial \tau} = -i(\Omega_{ab}\rho_{ba} - \Omega_{ba}\rho_{ab}) - \gamma_b\rho_{bb}$$

$$\frac{\partial \rho_{ab}}{\partial \tau} = i(\Omega_{aa} - \Omega_{bb} + \delta + i\gamma_{\perp})\rho_{ab} + i\Omega_{ab}(\rho_{bb} - \rho_{aa})$$

$$\Omega_{aa} = \frac{1}{2} \sum_q a_q |E_q|^2$$

$$\Omega_{bb} = \frac{1}{2} \sum_q b_q |E_q|^2$$

$$\Omega_{ab} = \Omega_{ba}^* = \frac{1}{2} \sum_q d_q E_q E_{q+1}^*$$



Coherence:

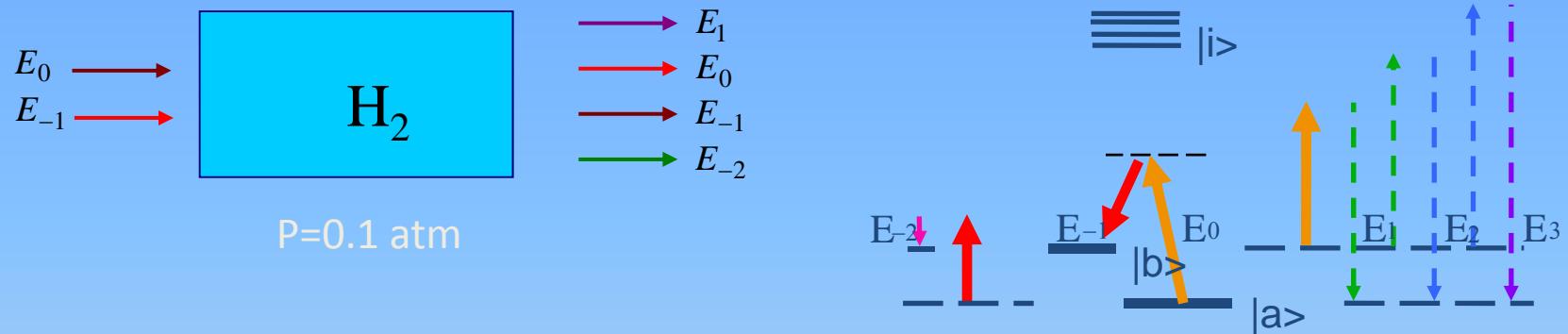
$$\rho_{ab}^{(\pm)} = \frac{1}{2} e^{i\varphi} \sin 2\theta^{(\pm)} = \pm \frac{\Omega_{ab}}{\sqrt{(\Omega_{aa} - \Omega_{bb} + \delta)^2 + 4|\Omega_{ab}|^2}}$$

$$|\rho_{ab}| = 0.5$$

$$|\Omega_{ab}| \gg |\Omega_{aa} - \Omega_{bb} + \delta|$$

# Sideband Generation and Propagation

- Adiabatically prepared molecules modulate the driving fields producing a wide comb

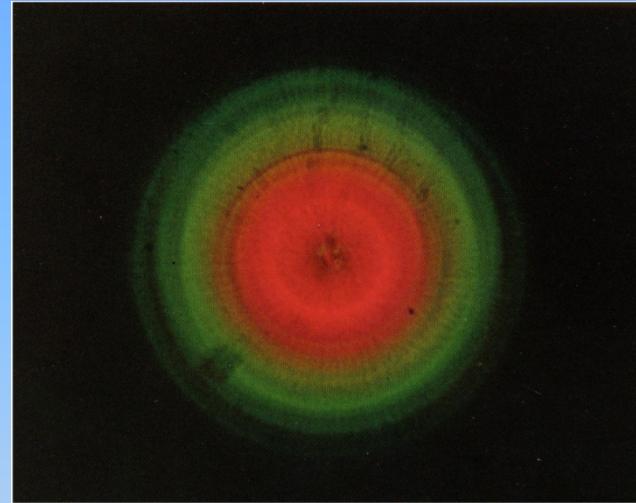
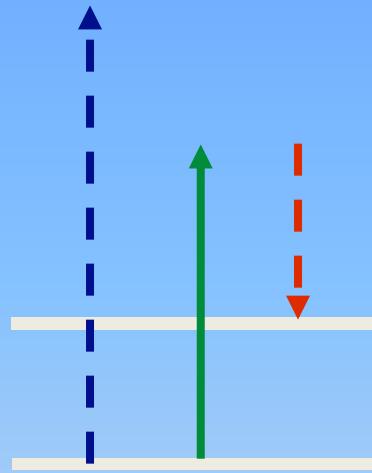


- Propagation equation for the  $q$ th sideband:  $\omega_q = \omega_{q-1} + \omega_0 - \omega_{-1}$

$$\frac{\partial E_q}{\partial z} = -j\eta\hbar\omega_q N \left( \underbrace{a_q \rho_{aa} E_q + d_q \rho_{bb} E_q}_{\text{dispersion}} + \underbrace{b_q^* \rho_{ab} E_{q-1} + c_q^* \rho_{ab}^* E_{q+1}}_{\text{coupling}} \right)$$

At maximum coherence,  $\rho_{ab} = 0.5$  the dispersion and coupling terms become comparable. Phase-matching is then not important, and generation is collinear.

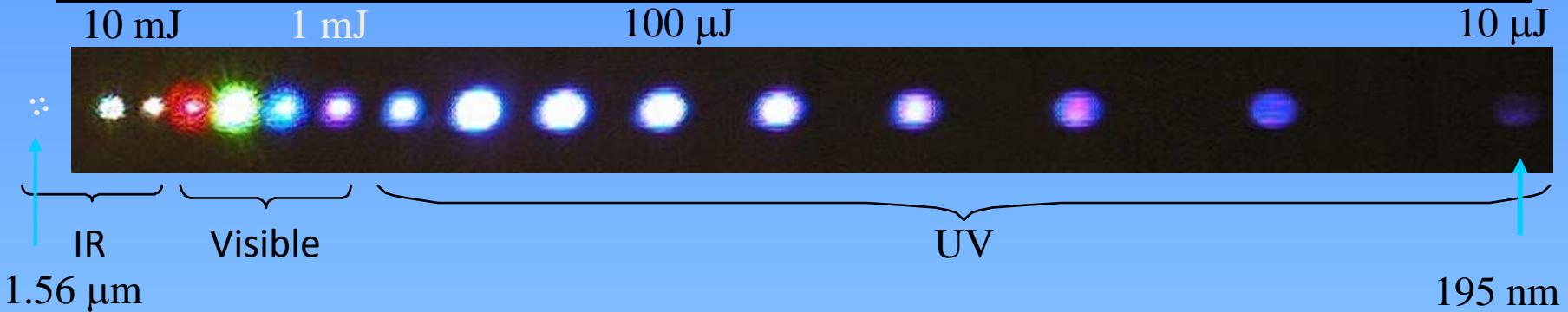
# Stimulated Raman Scattering



Traditional SRS:

- ★ Generation occurs at **high gas pressure**
- ★ Molecular excitation occurs **on-resonance**
- ★ Anti-Stokes generation occurs **off-axis**
- ★ **Few** Stokes and anti-Stokes orders are observed.

# $D_2$ Vibration Spectra: 16 sidebands, spaced by $2994\text{ cm}^{-1}$

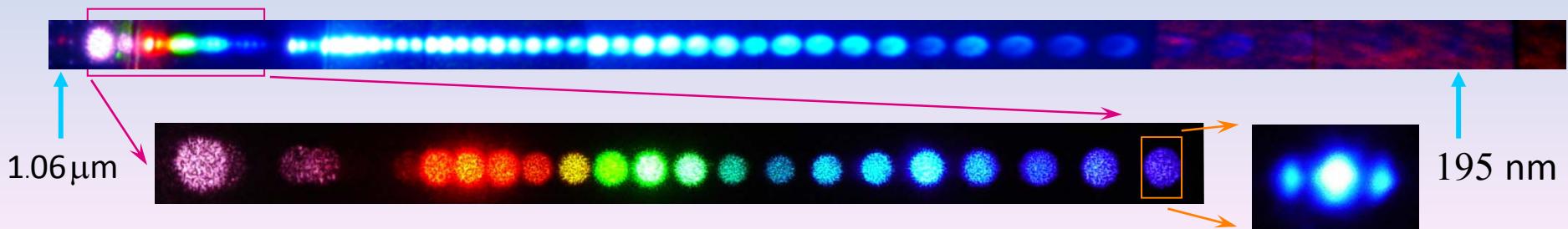


## $H_2$ Rotation Spectra: 29 sidebands, spaced by $587\text{ cm}^{-1}$

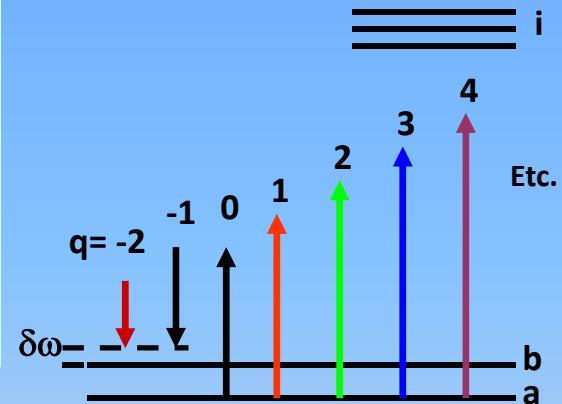
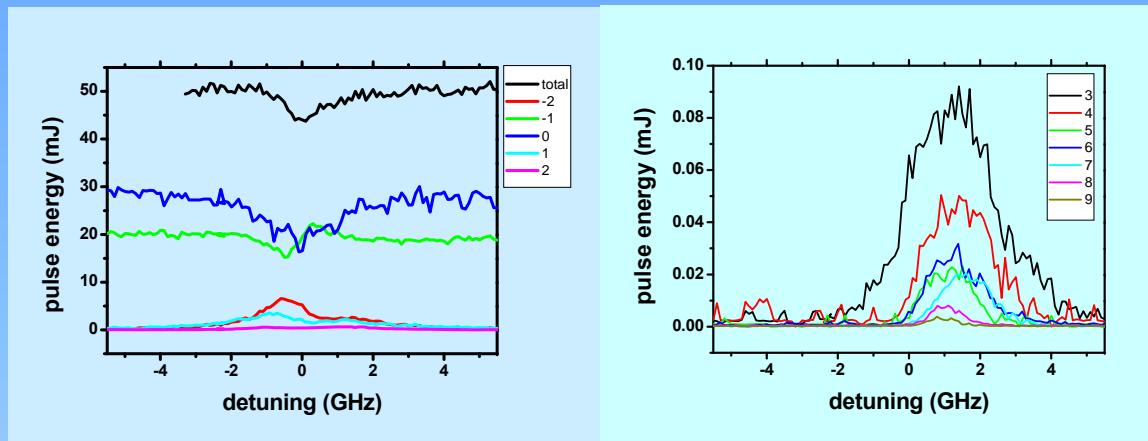


Phys. Rev. A (R) (1997)  
Phys. Rev. Lett. 81 (1998)  
Opt. Lett. 24 (1999)  
Phys. Rev. Lett. 84 (2000)  
Phys. Rev. Lett. 85 (2000)  
Phys. Rev. A 63 (2001)  
Phys. Rev. Lett. 91 (2003)  
Phys. Rev. Lett. 93 (2005)

## Multiplicative Spectra: $\sim 200$ sidebands, spaced by $< 587\text{ cm}^{-1}$



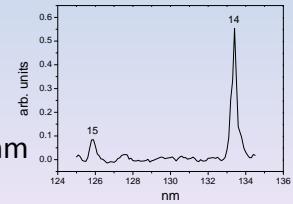
# Raman Spectrum



$q = 3, \lambda = 339.6$	nm
6	238.6 nm
9	183.9 nm
12	149.6 nm
14	133.0 nm

Total spectral span >70,000 cm<sup>-1</sup>  
(~500 as)

15<sup>th</sup> order at 126 nm  
observed



$$\omega_q = n\omega_m$$

Note:

$589 \text{ nm} \leftrightarrow 16978 \text{ cm}^{-1}$  ( $4 \times 4155.2 = 16621 \text{ cm}^{-1}$ )

$780 \text{ nm} \leftrightarrow 12822.8 \text{ cm}^{-1}$  ( $3 \times 4155.2 \text{ cm}^{-1} = 12465.6 \text{ cm}^{-1}$ )

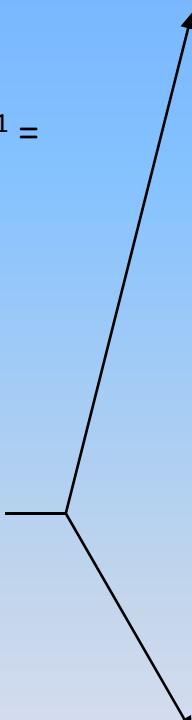
The sidebands are not commensurate.

New input wavelengths:

$$\omega_0 = 16621 \text{ cm}^{-1} (602 \text{ nm})$$

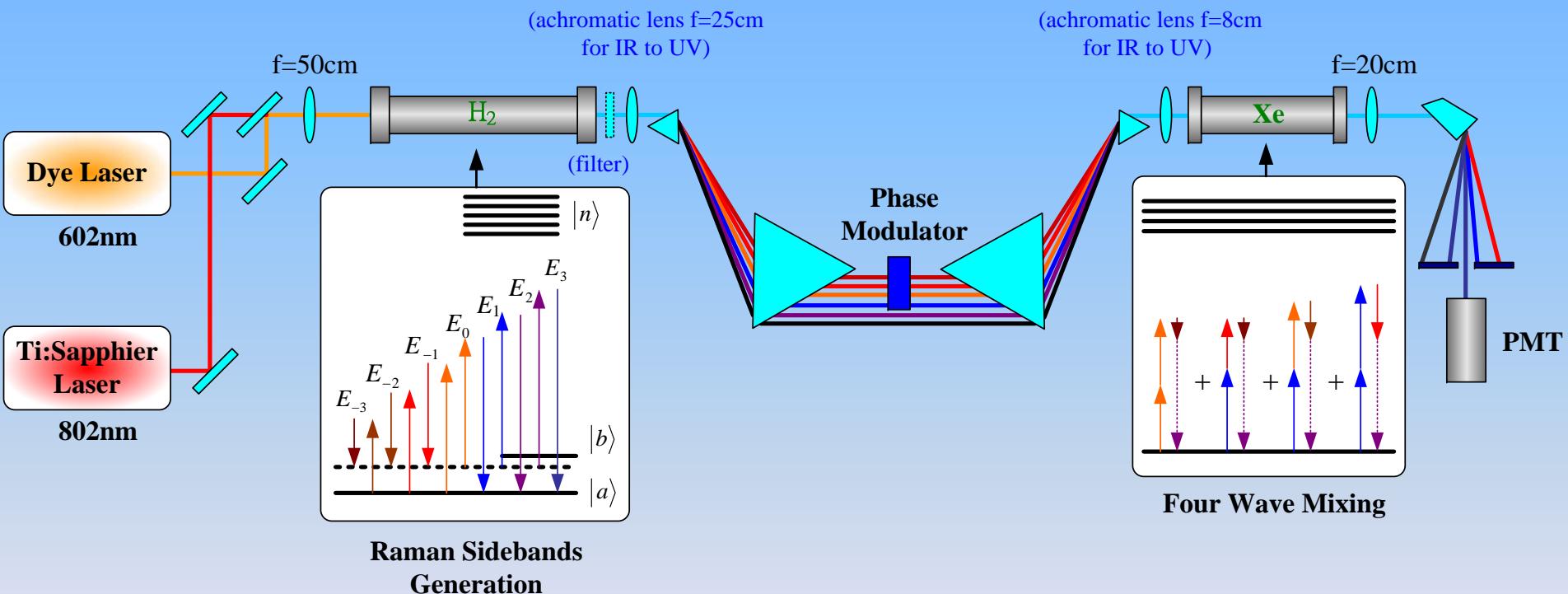
$$\omega_{-1} = 12465.6 \text{ cm}^{-1} (802 \text{ nm})$$

These wavelengths produce a commensurate set of sidebands, as shown on the right:



Raman Order	nm	cm <sup>-1</sup>	4 wave-mixing order
	$\infty$	0	
-3	2407	4155	
-2	1203	8310	1
-1	802	12465	2
0	602	16620	3
1	481	20775	4
2	401	24930	5
3	344	29085	6
4	301	33240	7
5	267	37395	8
6	241	41550	9
7	219	45705	10
8	201	49860	11
9	185	54015	

# Experiment Setup



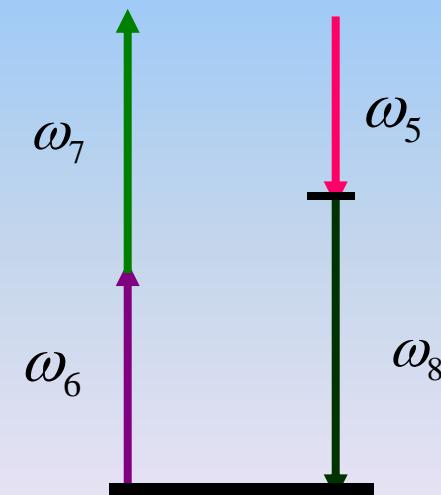
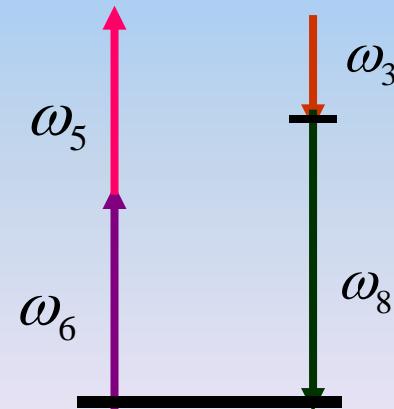
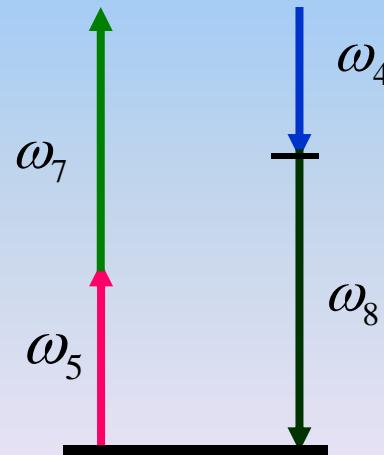
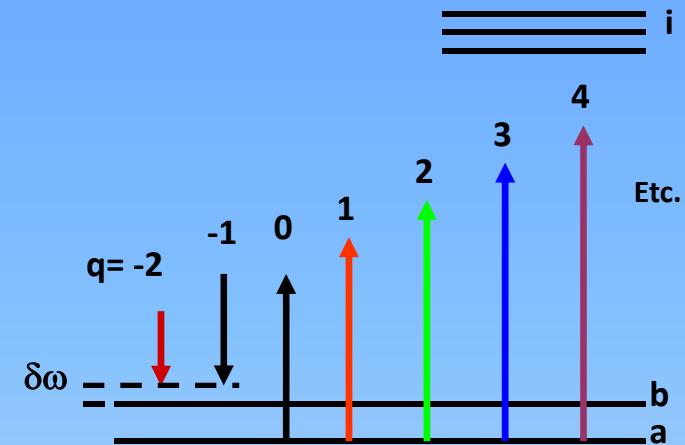
# Multiple quantum paths interference

Four wave mixing:

$$\omega_5 + \omega_7 - \omega_4 = \omega_8$$

$$\omega_6 + \omega_5 - \omega_3 = \omega_8$$

$$\omega_6 + \omega_7 - \omega_5 = \omega_8$$



# In phase condition

7=6+6-5, 6+5-4, 6+4-3, 6+3-2, 6+2-1.

5+5-3, 5+4-2, 5+3-1.

4+4-1

6, 5, 4 : 6+6-5, 6+5-4

$$\Phi_{65} = \Phi_{54}$$

+3 : 6+4-3, 5+5-3

$$\Phi_{65} = \Phi_{54} = \Phi_{43}$$

+2 : 6+3-2, 5+4-2

$$\Phi_{65} = \Phi_{54} = \Phi_{43} = \Phi_{32}$$

+1 : 6+2-1, 5+3-1, 4+4-1  $\Phi_{65} = \Phi_{54} = \Phi_{43} = \Phi_{32} = \Phi_{21}$

1: 1203nm

2: 802nm

3: 602nm

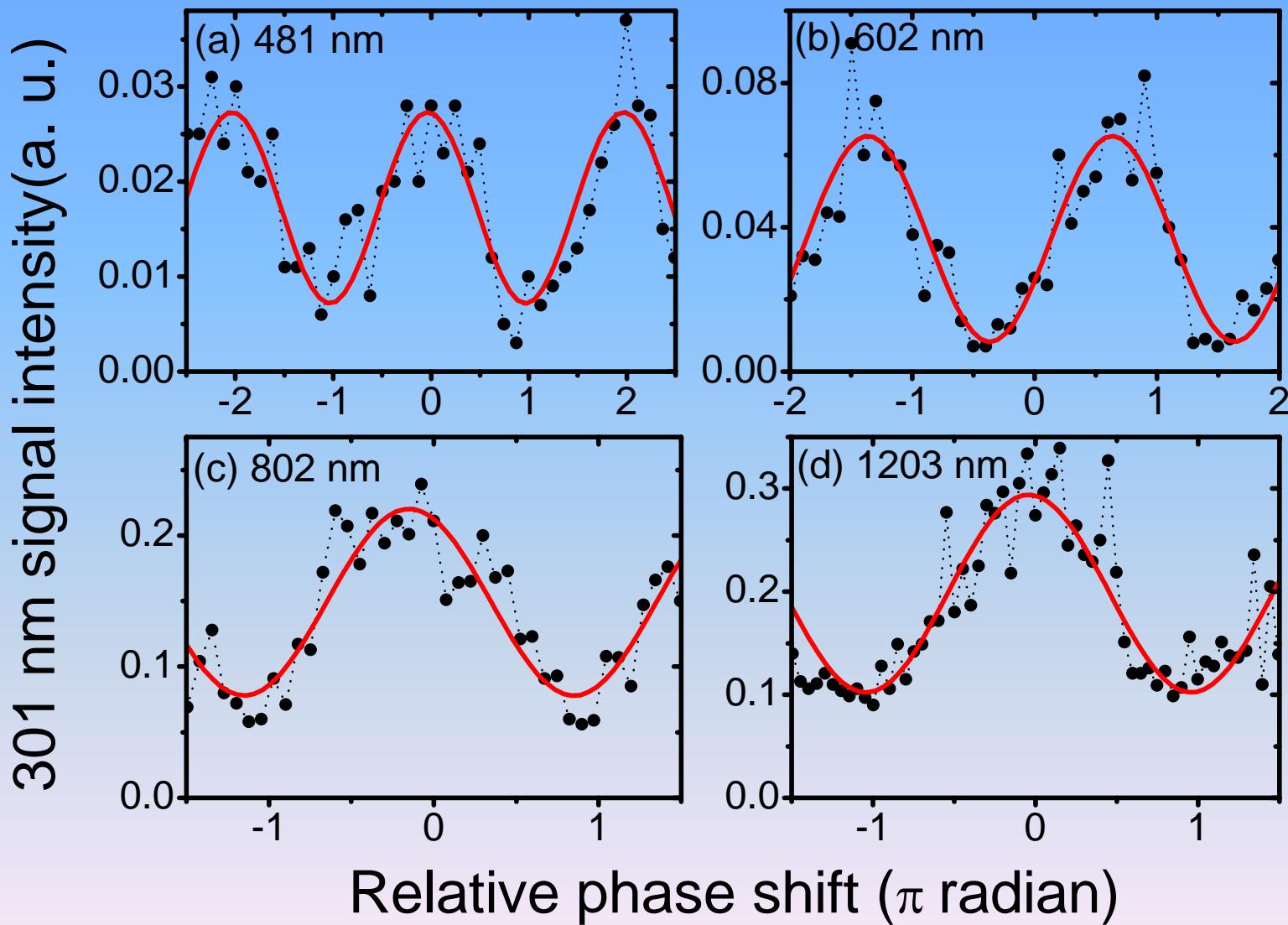
4: 481nm

5: 401nm

6: 344nm

7: 301nm

# Searching in phase condition

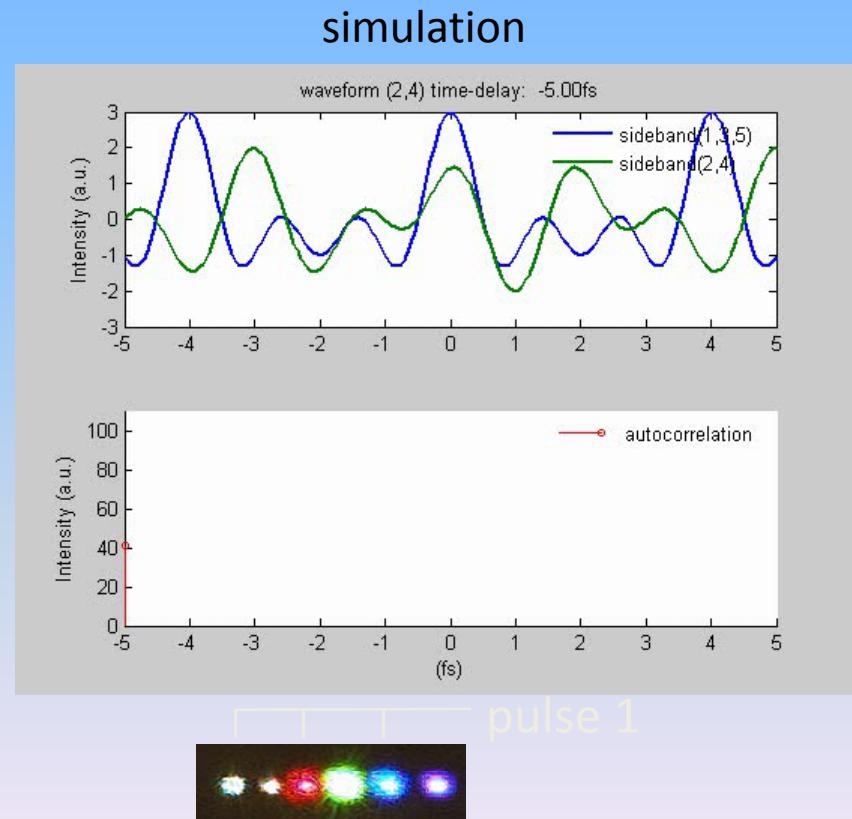


# How to check the pulse shape?

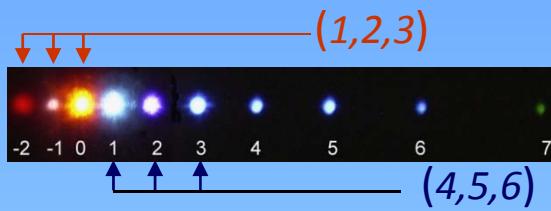
Autocorrelation is standard way to measure ultrafast pulsedwidth. However it could not be done here because of the wide bandwidth.

**Solution:** Correlation using pulses formed by the sidebands themselves.

Synthesize two pulses from the subsets of sidebands and electronically delay one pulse with respect to the other. Measure the resulting four-wave signal with a photomultiplier.



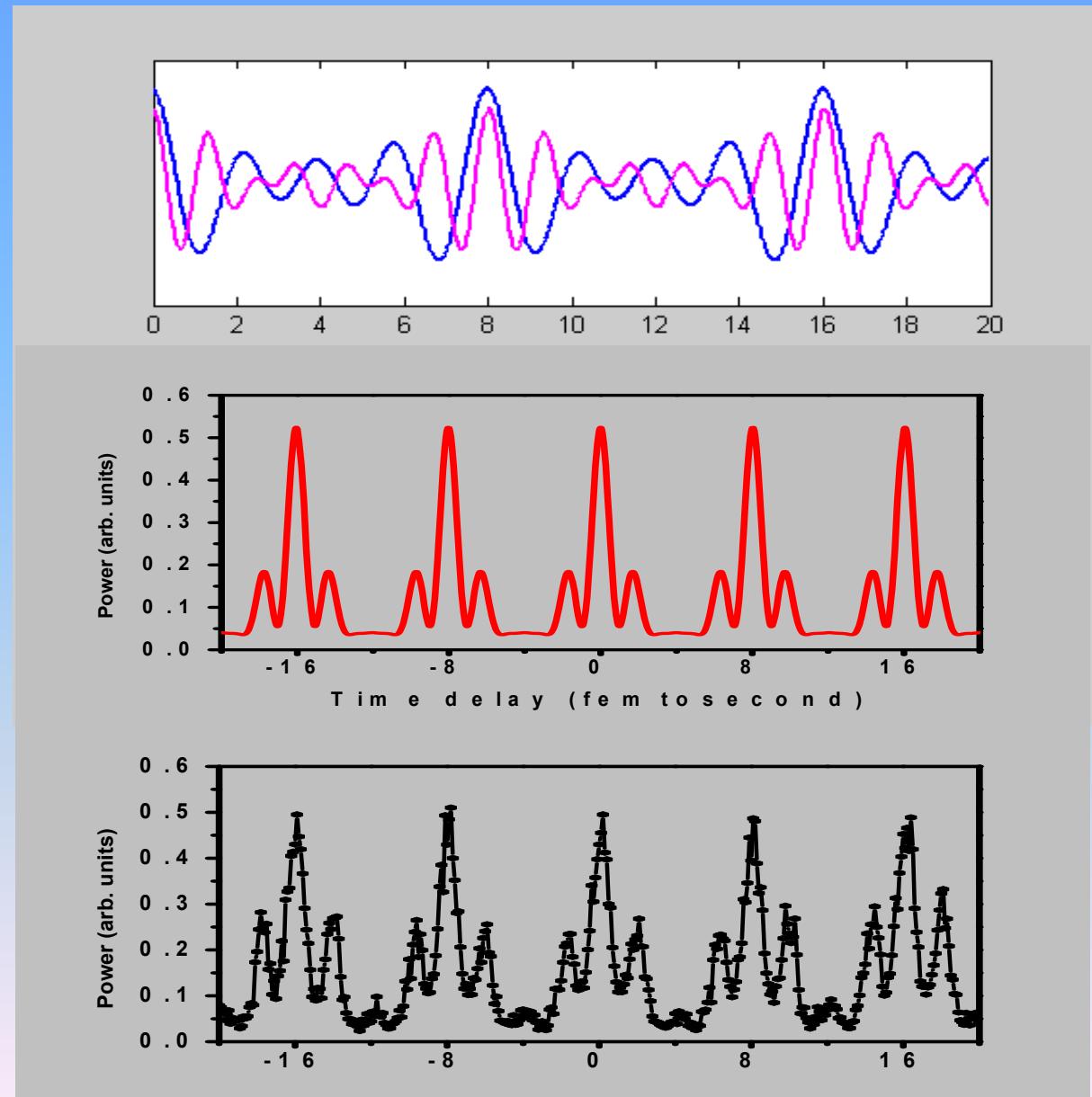
# Cross Correlation of Single Cycle Pulse Train



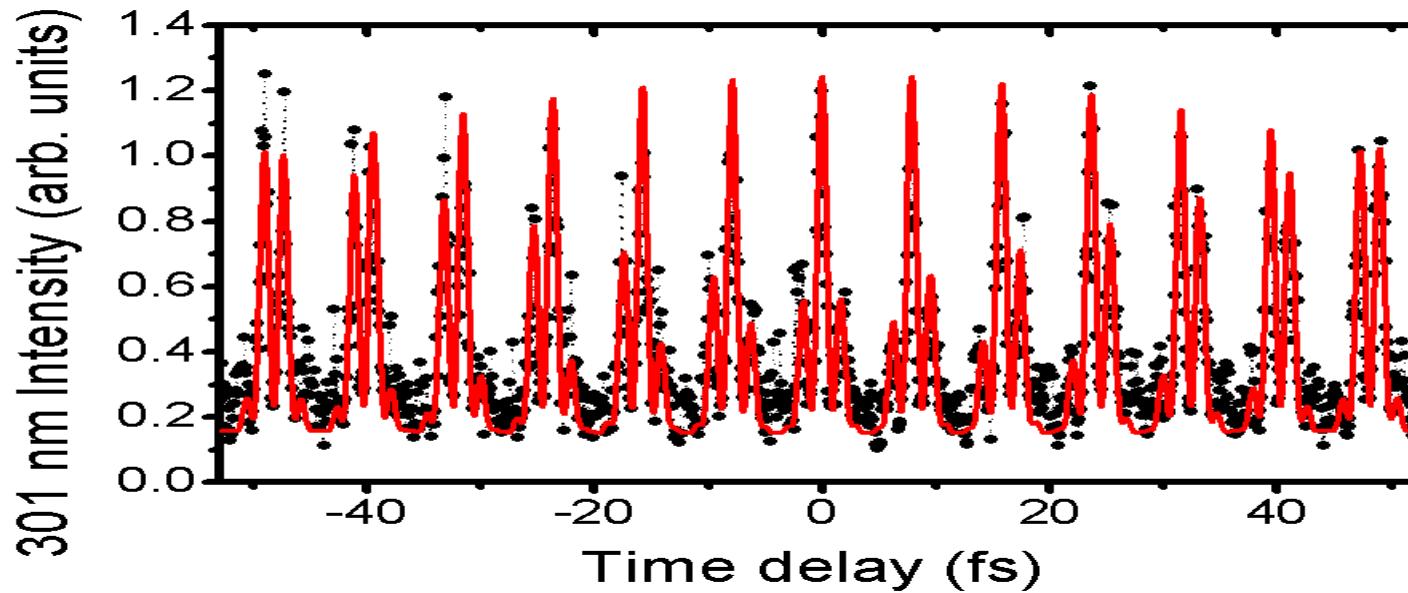
Sideband Orders

Simulation →

Experiment →

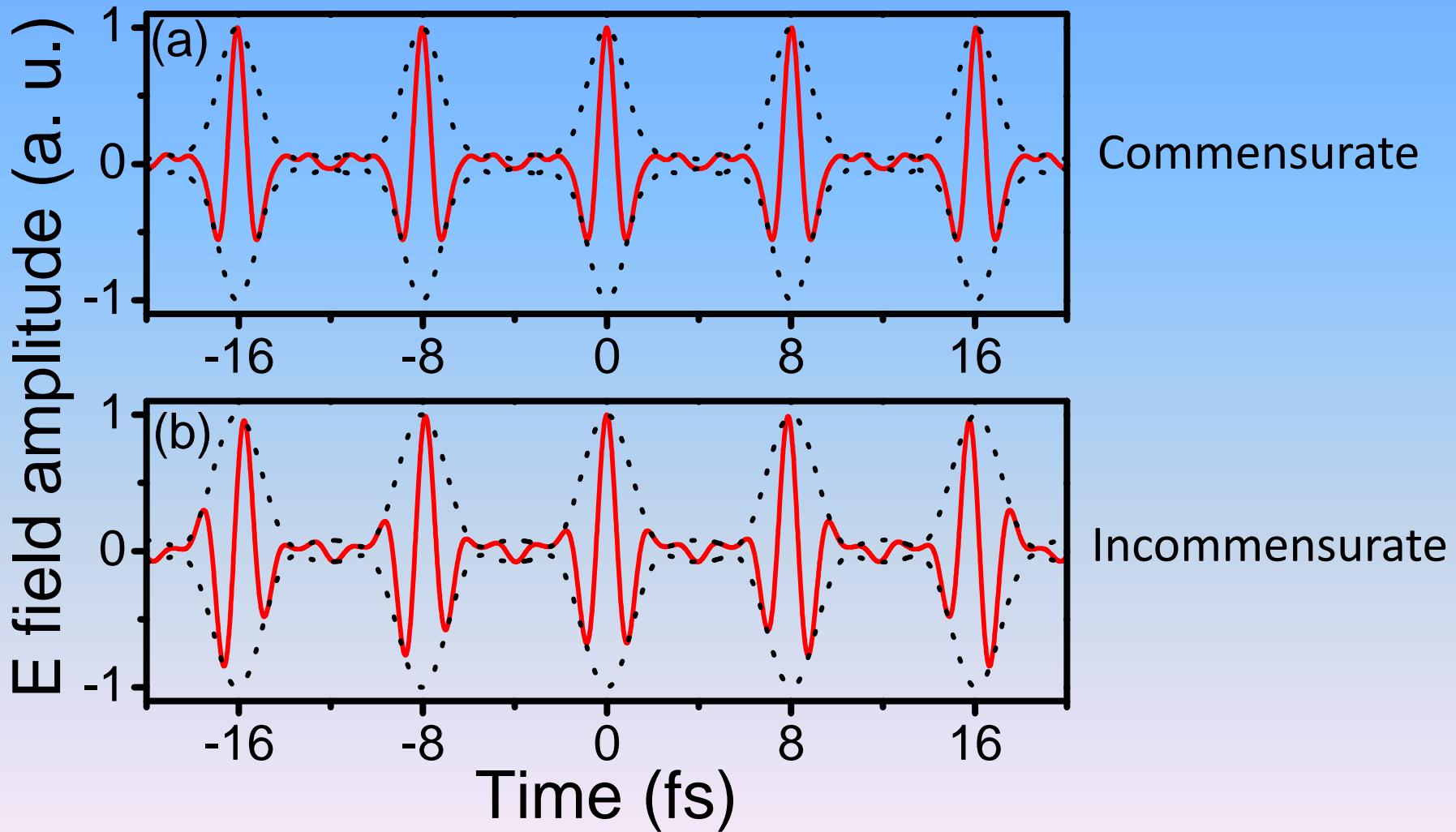


## Cross correlation signal of incommensurate pulses

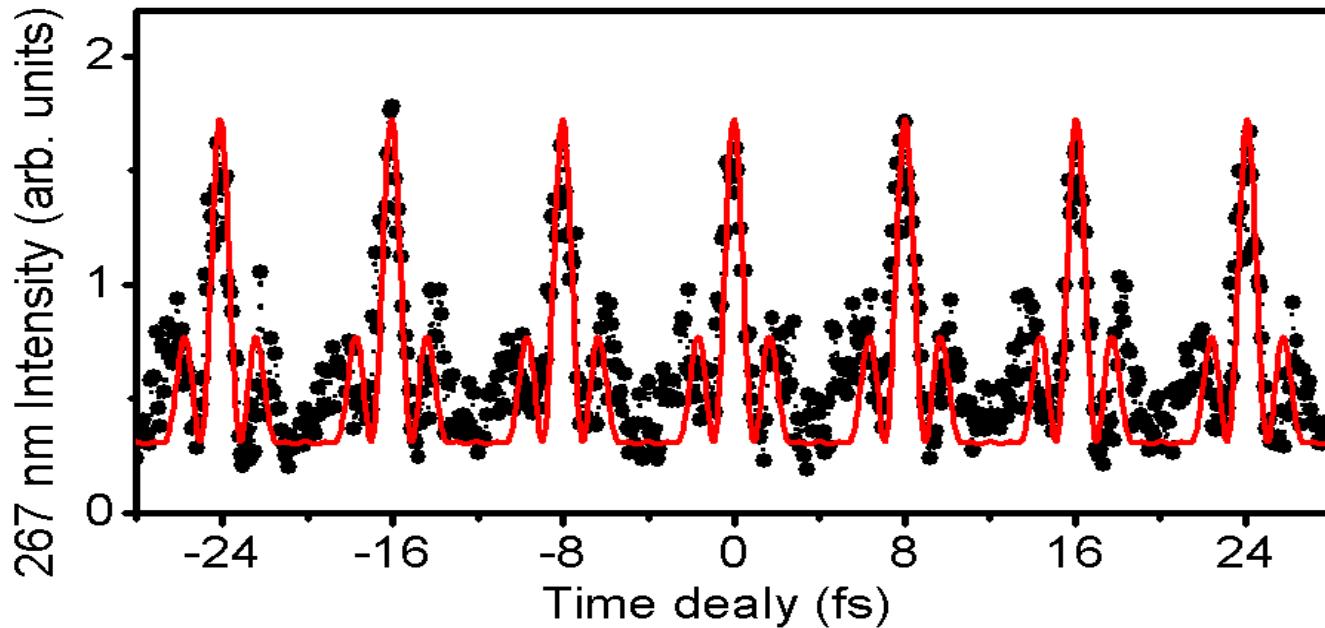


CEO frequency  $\sim 349 \text{ cm}^{-1}$   
Waveform repeats every 96 fs

# Pulse train



## 7 beam correlation in Xe



Carrier envelope phase is constant to  $\sim 2.5$  part in  $10^6$

Total phase slip of <0.18 cycles over 1 million pulses

# Status of sub-cycle optical pulse generation by molecular modulation

IAMS sub-cycle source

**0.833 cycle per pulse**

**1.4 fs envelope**

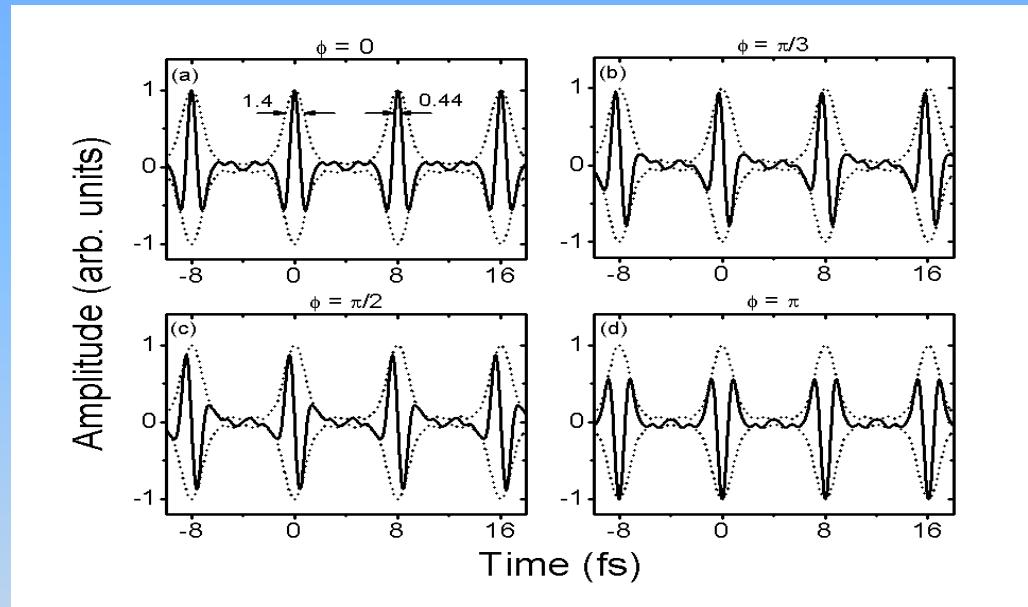
**440 as cycle width**

constant carrier envelope phase

2 ns pulse train duration

8.0 fs pulse spacing

**~1 MW peak power**



Total spectral span  $>70,000 \text{ cm}^{-1}$

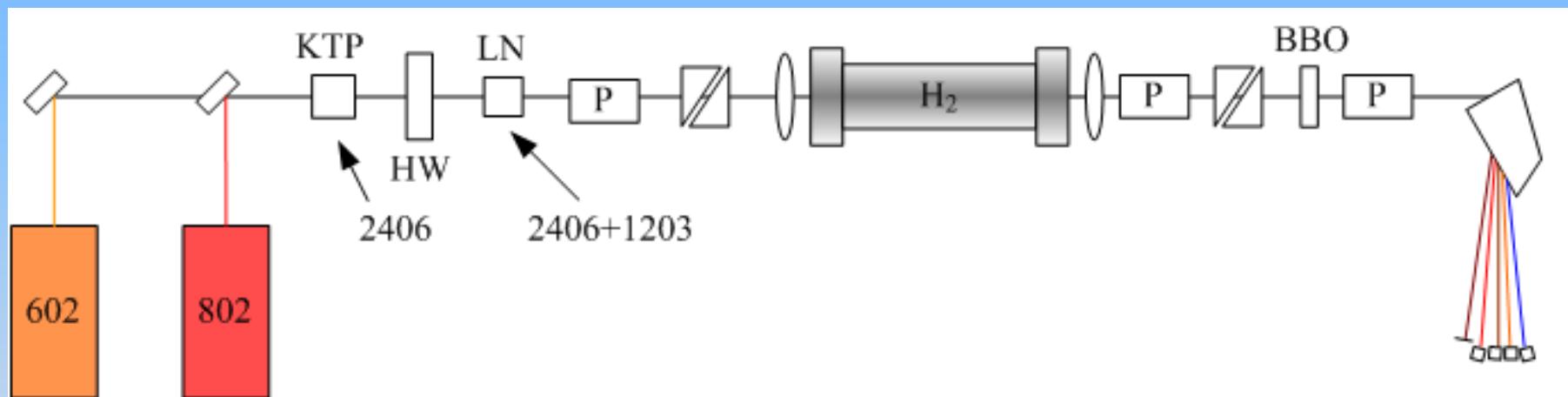
Wei-Jan Chen et al., Phys. Rev. Lett. 100, 163906 (2008)

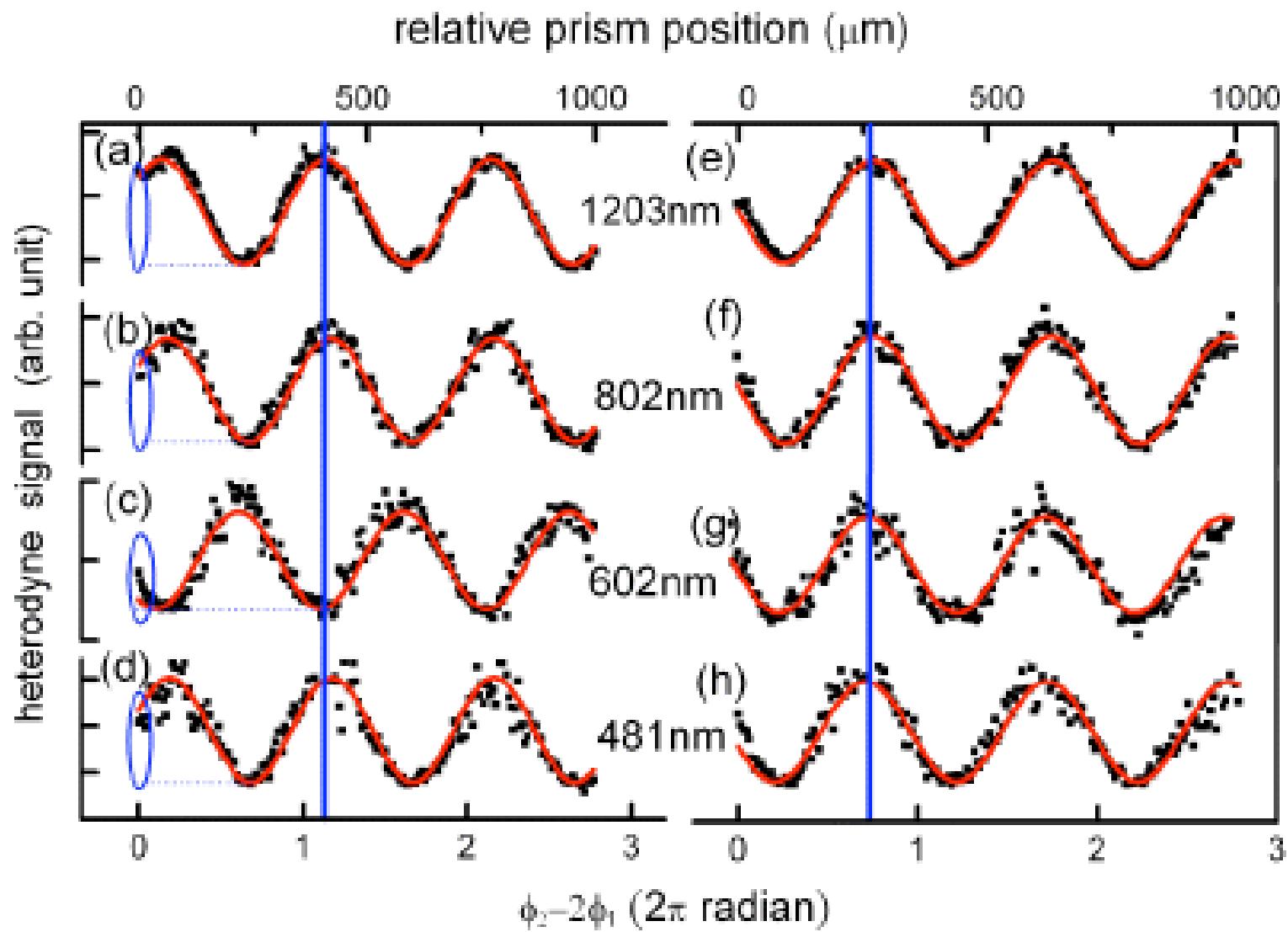
Zhi-Ming Hsieh et al., Phys. Rev. Lett. 102, 213902 (2009)

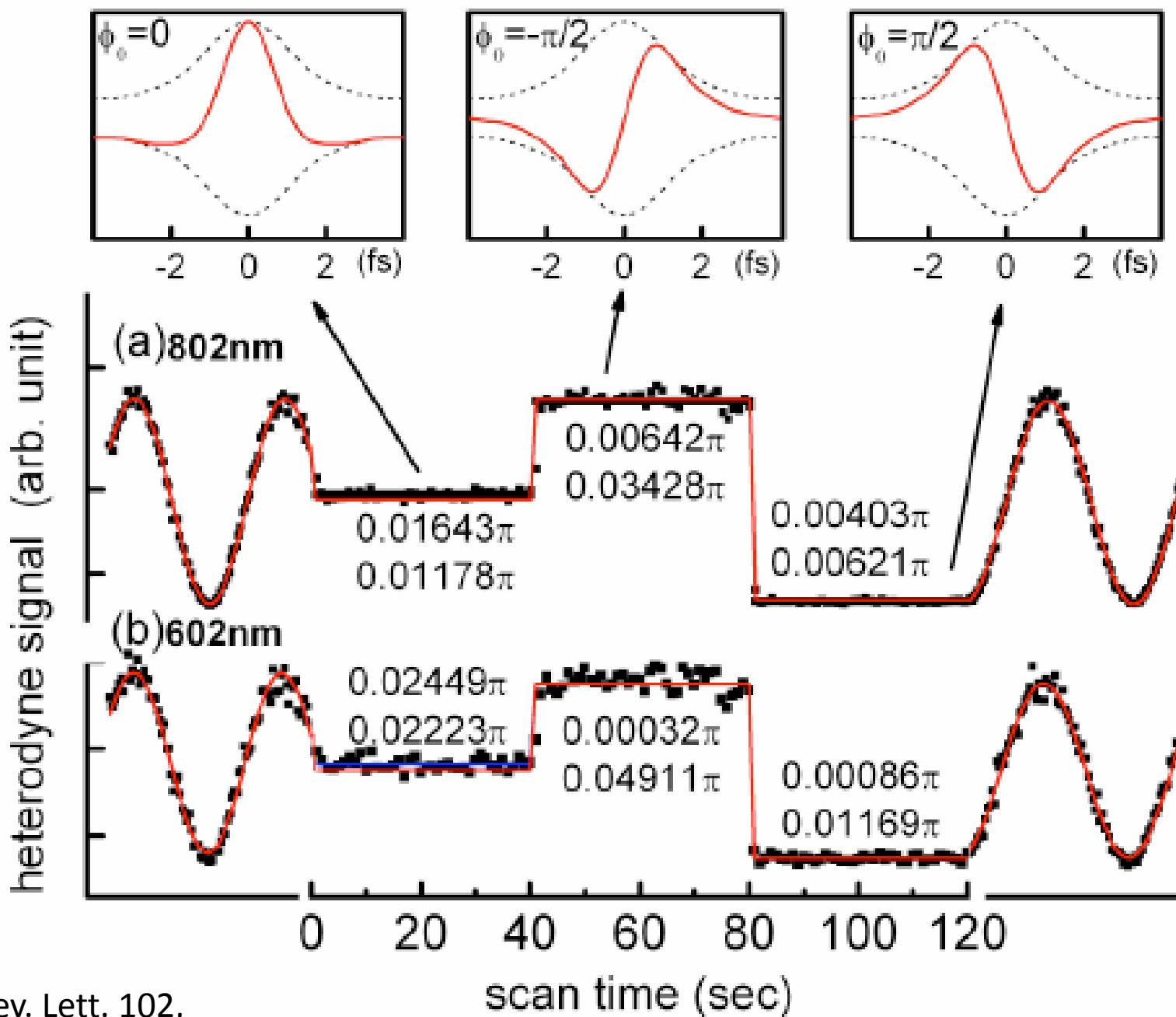
# Ingredients of an attosecond single-cycle optical pulse:

1. Broad spectrum - 2 or more octaves
2. In phase condition
3. Constant carrier envelope phase:
  - Commensurate frequencies
  - Constant phase difference between adjacent spectral components
4. **Stable and controllable carrier envelope phase**

# CEP control







# Brief Summary and Outlook

- Generated commensurate pulse train
  - Single pulse duration 1.4fs
  - Sub-single-cycle pulse: 0.8 cycles
  - CEP (carrier-envelope phase) control
- 
- Sub-femtosecond pulse generation
  - Arbitrary waveform
  - Application for ultra-fast dynamics

# Outline

- Introduction
- Review of basic concepts
- High Harmonic Generation
- Molecular Modulation
- Multicolor synthesized
- Outlook

# Motivation

- Broadband source  
coherent and commensurate
- High peak power enough  
 $10^{13}\text{-}10^{14} \text{ W/cm}^2$
- Simple experiment setup
- Light waveform control

# Methods of Generating Attosecond Pulses

C

## Harmonics Generation

1203

802

602

481

401

344

301

**0.833 cycle per pulse**  
**1.4 fs envelope**  
**440 as cycle width**  
constant carrier  
envelope phase  
2 ns pulse train  
duration  
8.0 fs pulse spacing  
**~1 MW peak power**

$\sim 25,000 \text{ cm}^{-1}$

1064

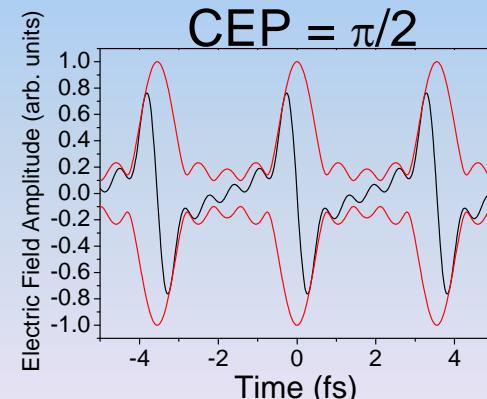
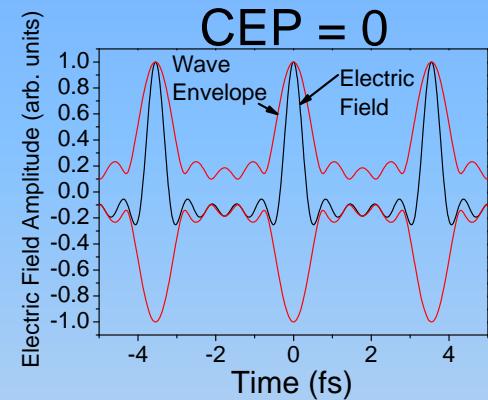
532

355

266

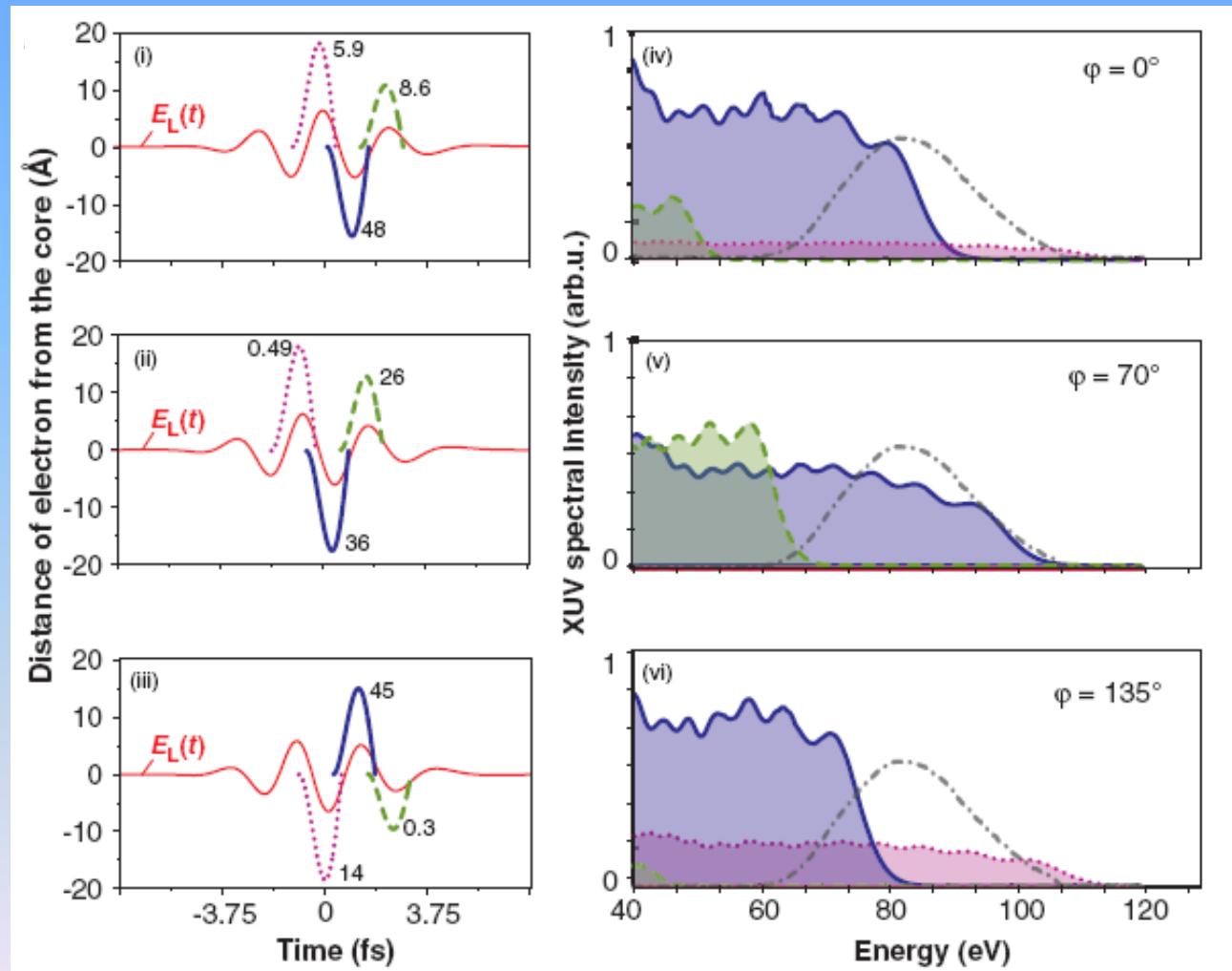
213

$\sim 37,600 \text{ cm}^{-1}$



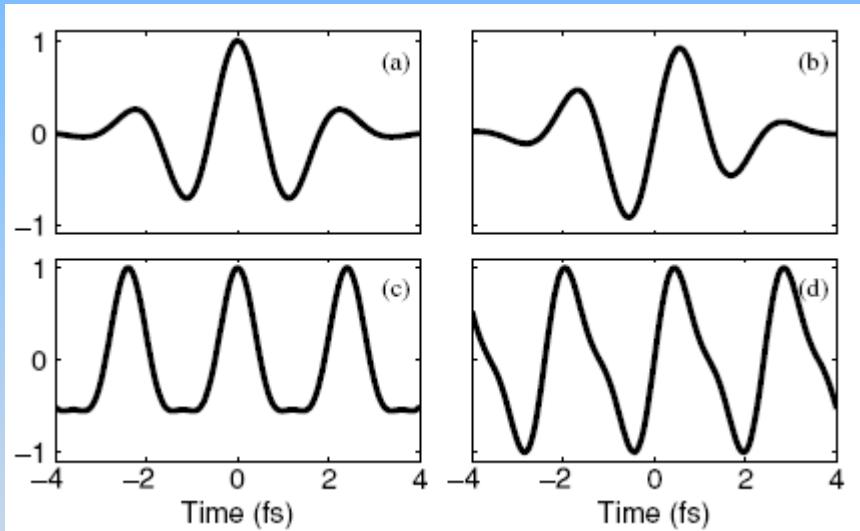
# Single-cycle Nonlinear Optics

Simulation of sub-femtosecond XUV emission from neon atoms ionized by a linearly polarized, sub-1.5-cycle, 720 nm laser field.

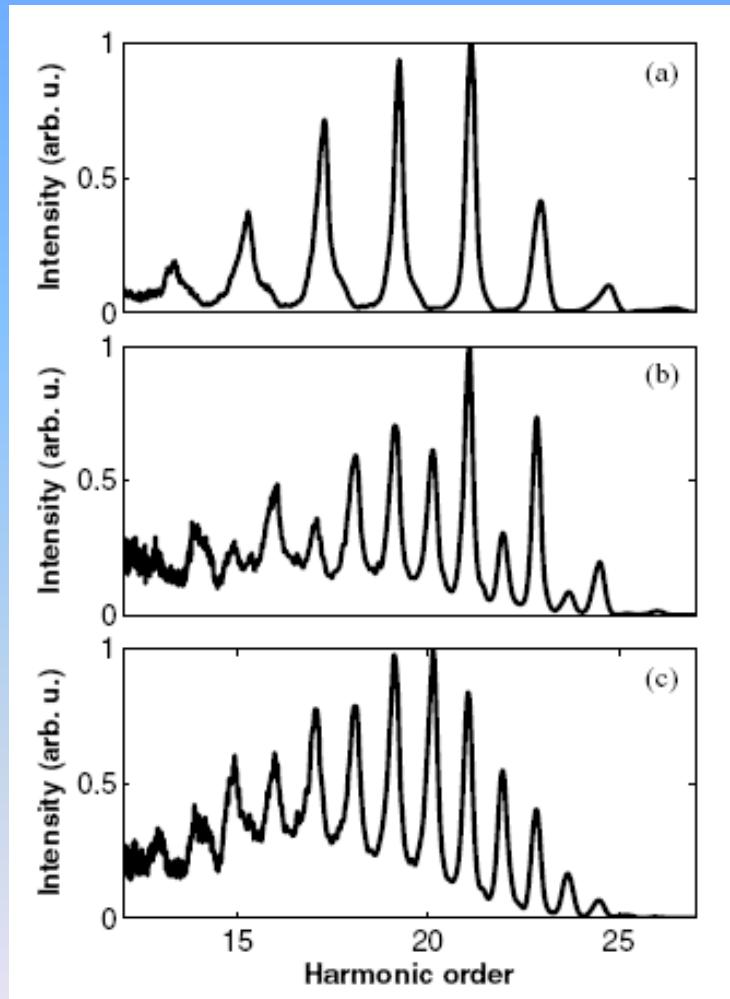


# Two-color multi-cycle field

Few-cycle pulse

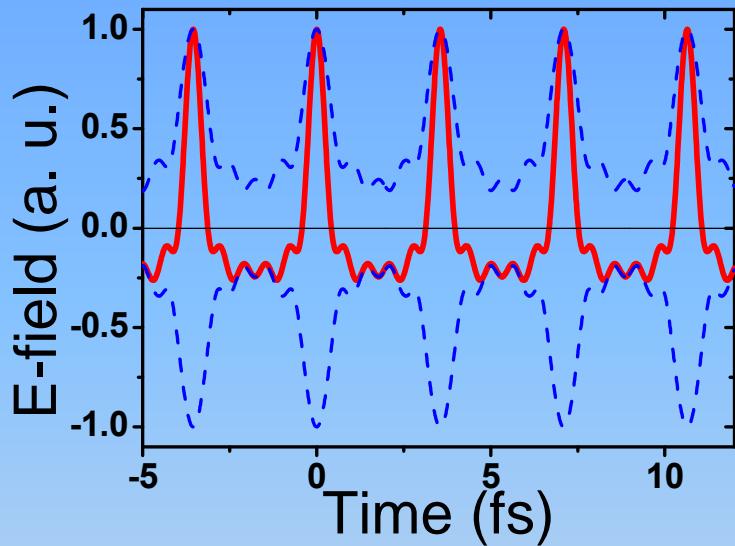


Two-color pulse train

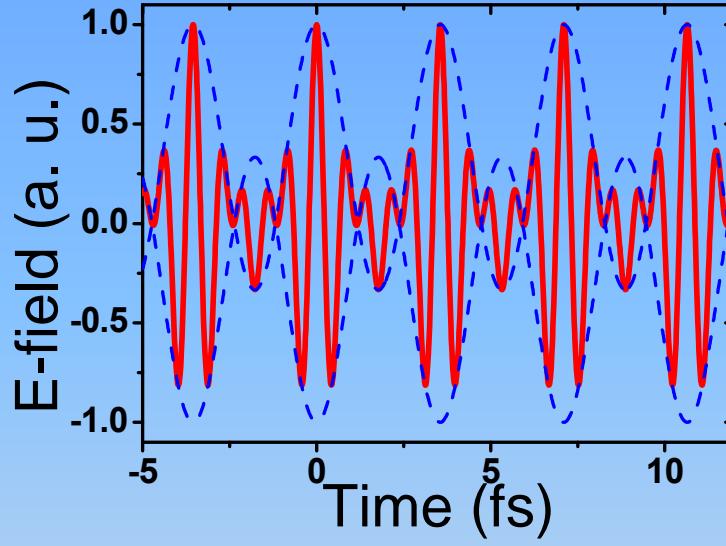


# Waveform by 5 E-field

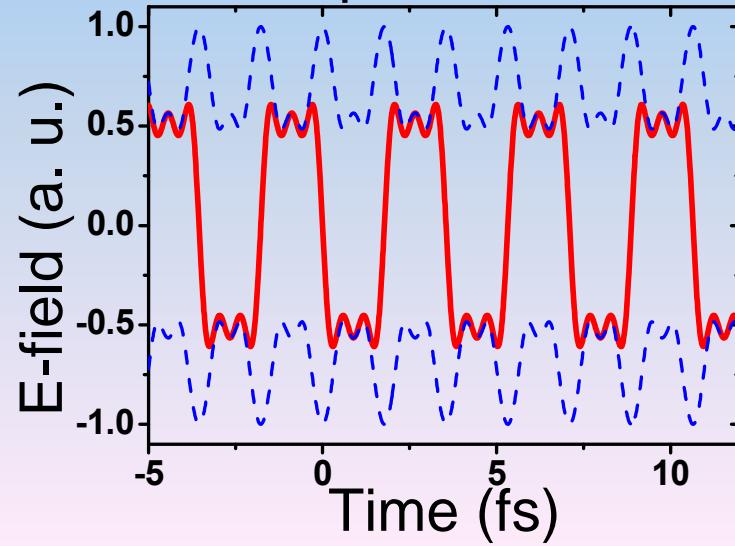
Sub Cycle



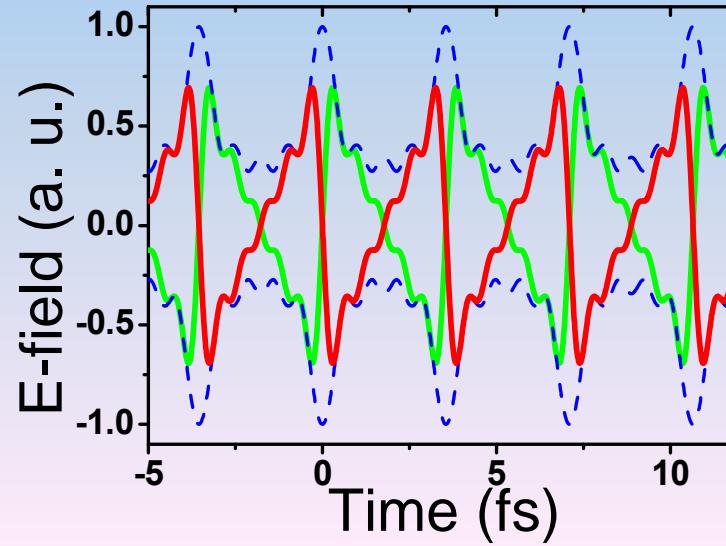
Few Cycle



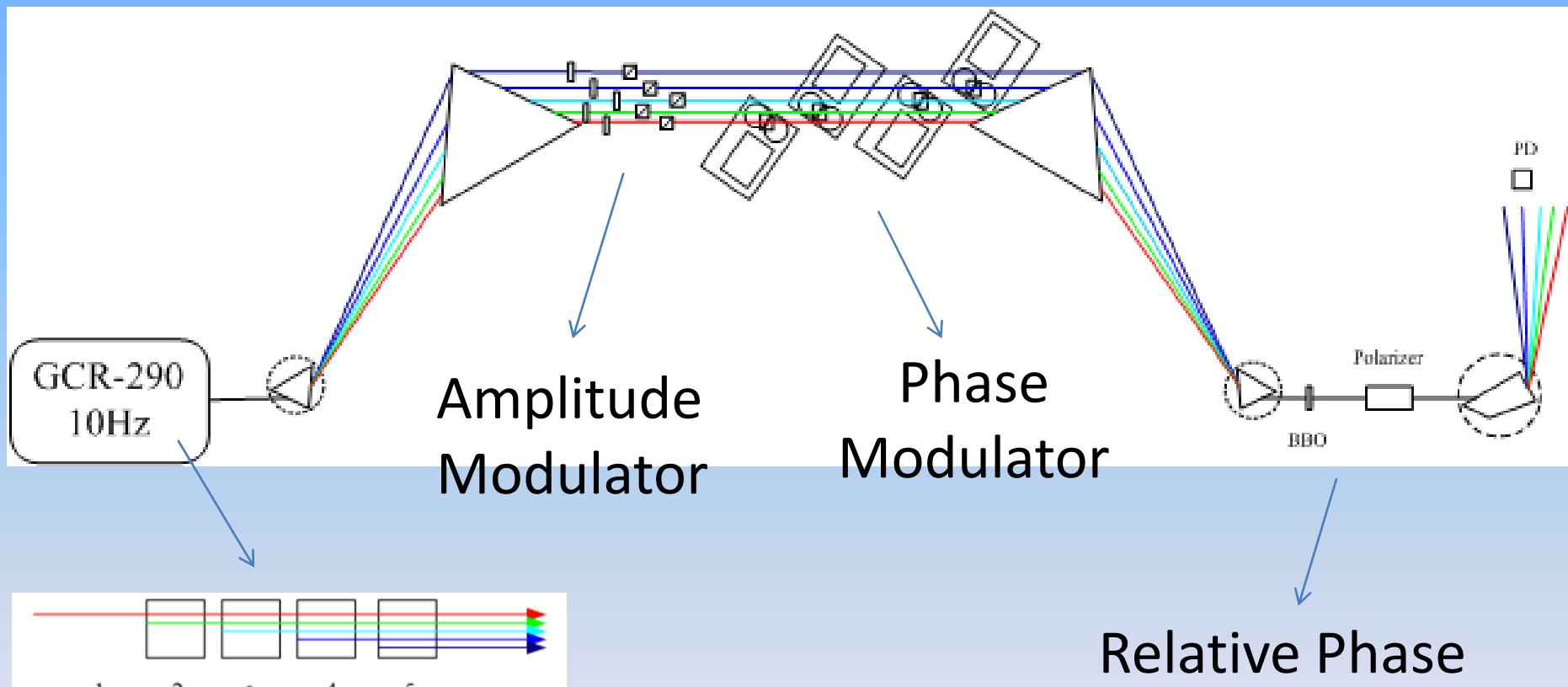
Square Wave



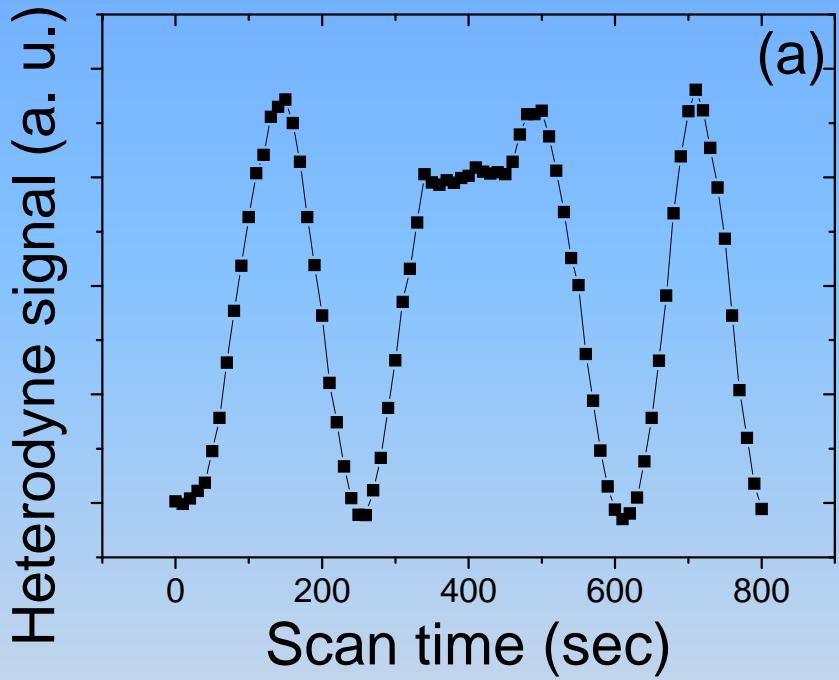
Saw Tooth



# Experimental Setup

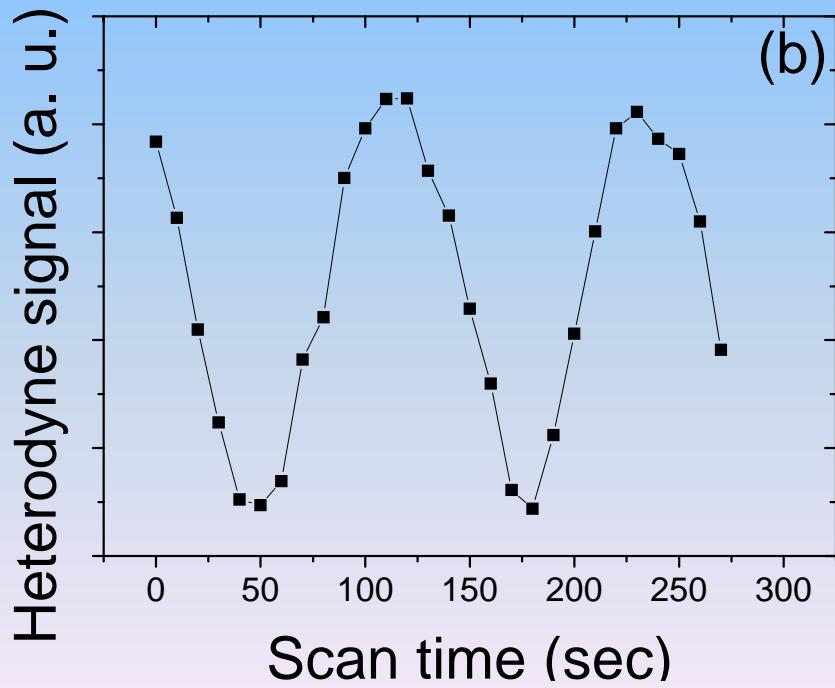


# Relative Phase Measurement

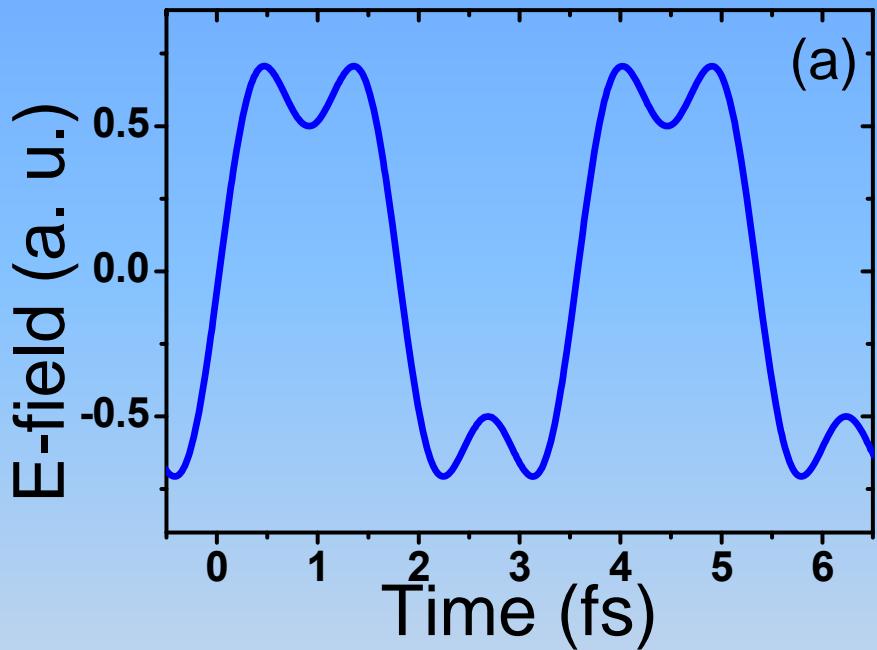


(a) The relative phase between 1064 nm and 532 nm

(b) The relative phase between 1064 nm and 355 nm

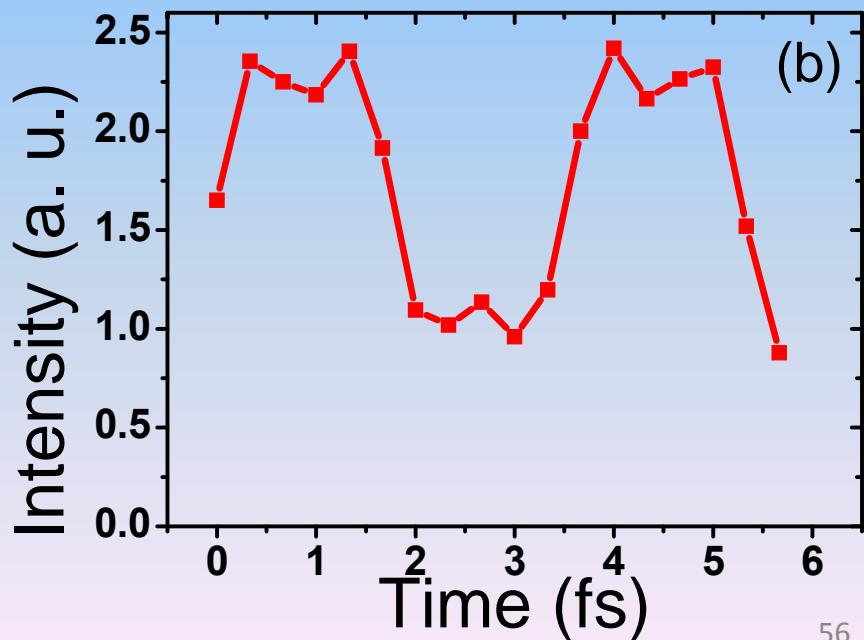


# Waveform by linear cross-correlation



(a) Square wave synthesized by 3 harmonics

(b) Square wave shown by linear cross-correlation process



# Outline

- Introduction
- Review of basic concepts
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- **Outlook**

# The characteristics of the waveform

Pulse train: period 3.55 fs

Pulse energy

1064 nm: 380 mJ

532 nm: 178 mJ

355 nm: 70 mJ

266 nm: 41 mJ

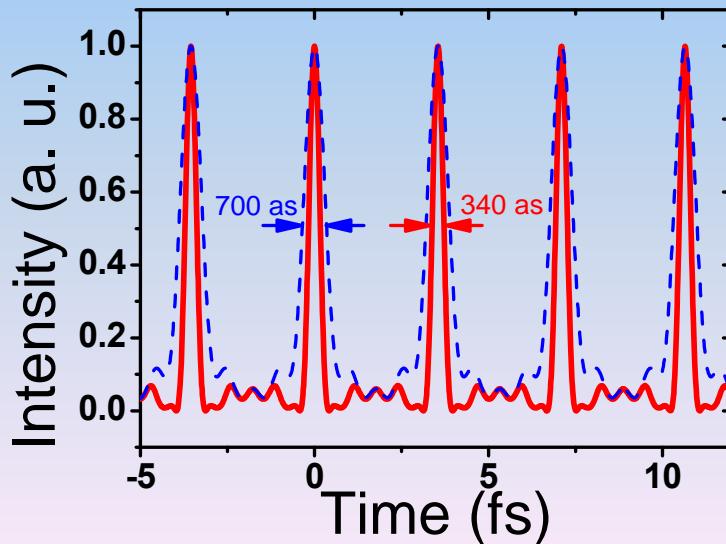
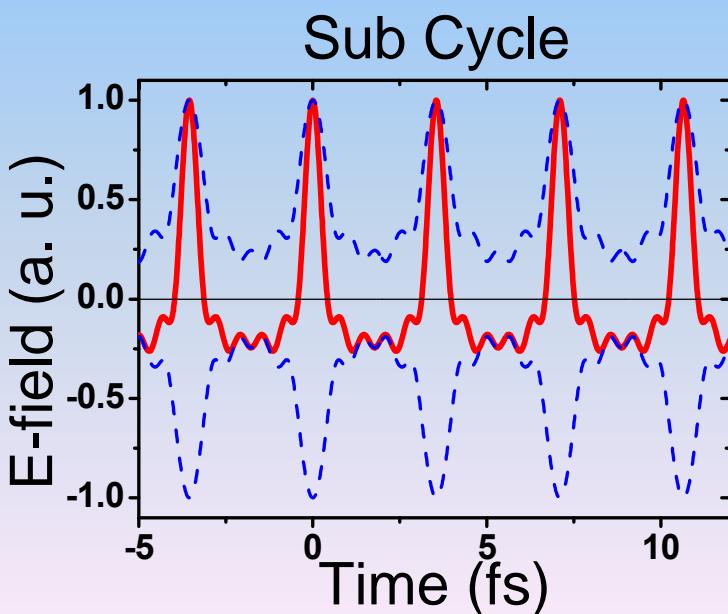
213 nm: 22 mJ

When CEP=0

After these modulator, assume each effective pulse energy is half of original energy

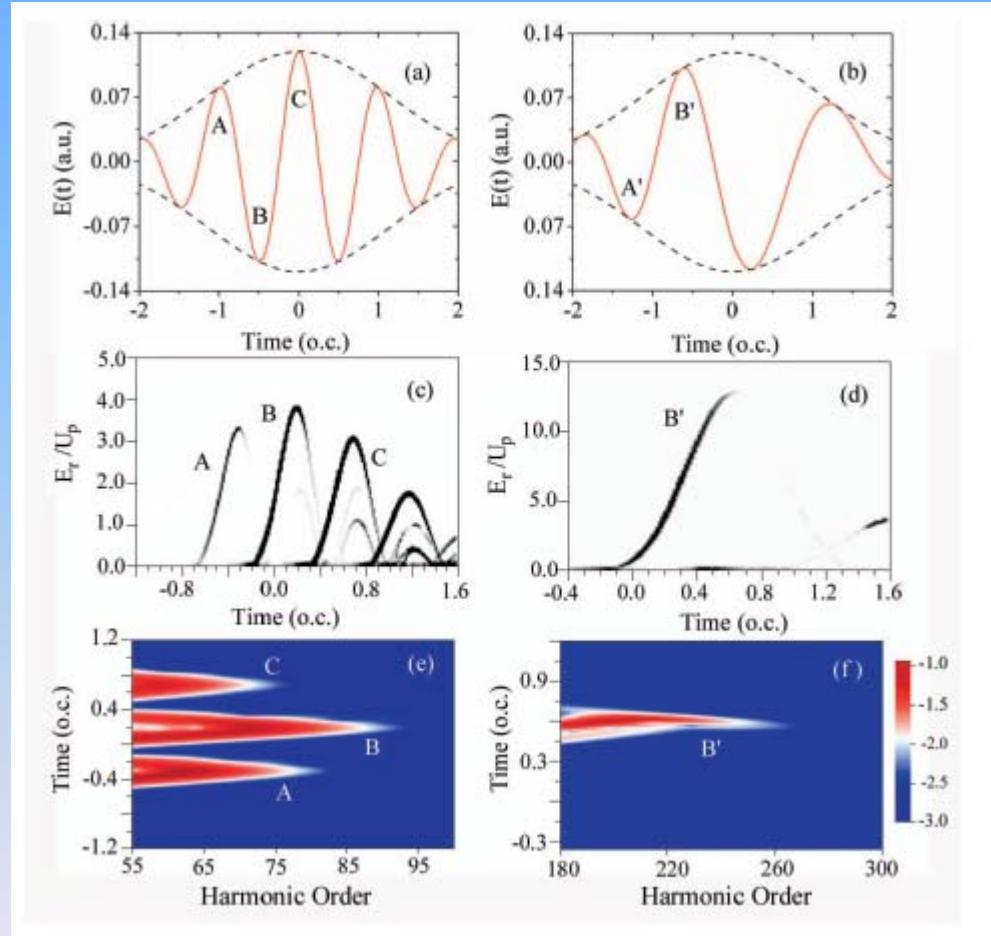
=>The pulse width  $\sim 340$  as

Focusing to a  $\Phi 20\mu\text{m}$  spot, the intensity will reach  $10^{14} \text{ W/cm}^2$ .



# Outlook

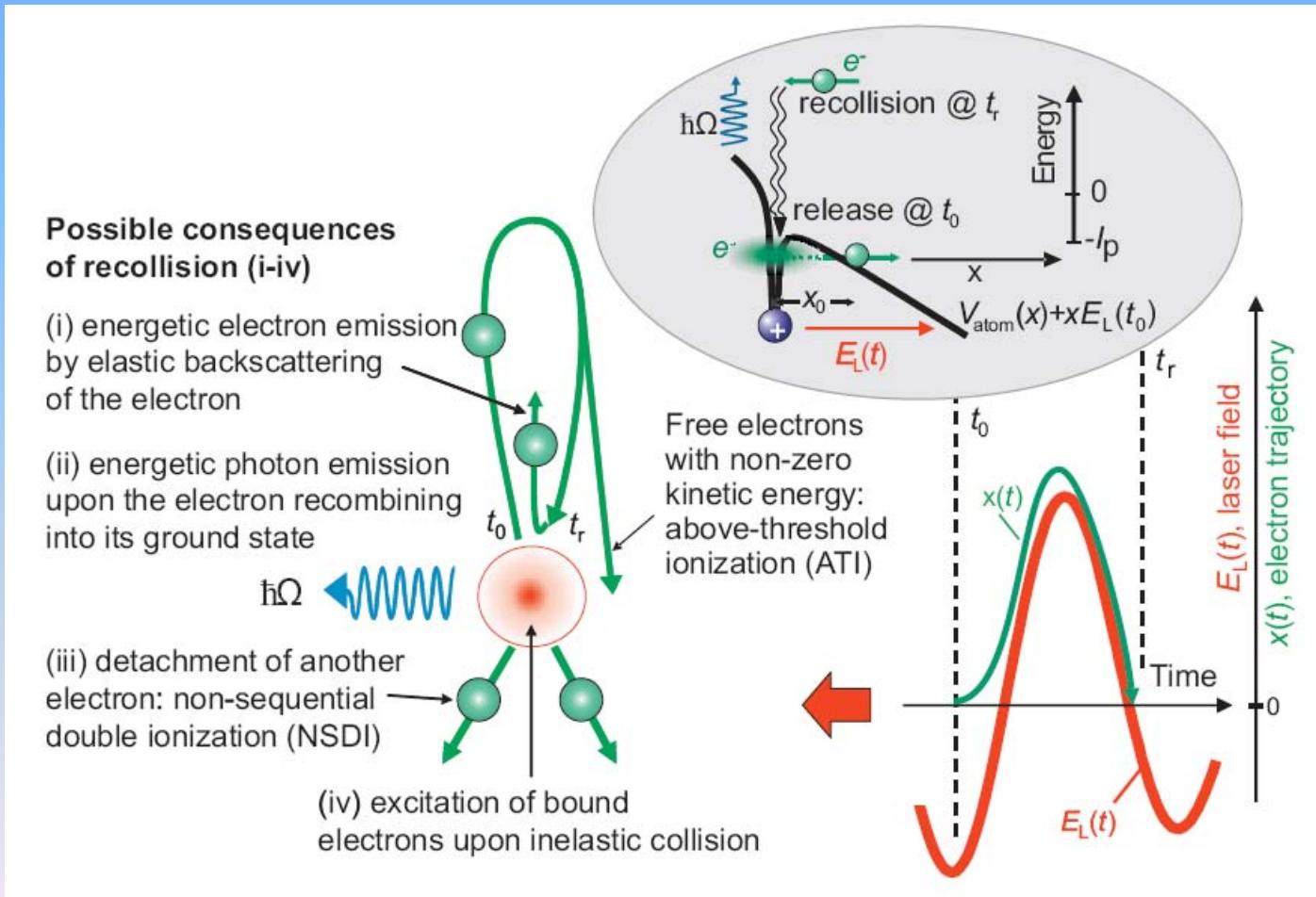
- The further waveform control
- The HHG setup and measurement



Juan J. Carrera and Shih-I Chu, Phys. Rev. A 75, 033807 (2007)

# Outlook

- Photoelectron and/or ion measurement



F. Krausz & M. Ivanov, Rev. Mod. Phys. 81 163 (2009)

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