



NTHU AMO seminar, 3/19/2012



Precision Measurement of Lithium Hyperfine Structure

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- Historical review: spectroscopy of simple atoms
- Examples (H, He, Li)
- What physics to study?
- Experiment in NTHU
- Our results and outlook



- To the extent **atomic structure** is calculable, precision measurement test fundamental physics
- **Electromagnetic** interaction well known
- Advances in atomic theory
- Simple atoms, e.g.: H, He, Li, etc...
- What **fundamental physics** to study

Hydrogen



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- non-relativistic

$$E_n = -\alpha^2 mc^2 \left(\frac{1}{2n^2} \right) = \frac{-13.6 \text{ eV}}{n^2}$$

- relativistic correction

$$-\alpha^4 mc^2 \frac{1}{4n^2} \left[\frac{2n}{(l+1/2)} - \frac{3}{2} \right]$$

- spin-orbit interaction
(L·S, fine structure)

$$-\alpha^4 mc^2 \frac{1}{4n^2} \left[\frac{2n}{(j+1/2)} - \frac{3}{2} \right]$$

- QED effect (Lamb shift)

$$\alpha^5 mc^2 \frac{1}{4n^3} \left\{ k(n, l) \pm \frac{1}{\pi(j+1/2)(l+1/2)} \right\}$$

- nuclear magnetic moment
(hyperfine structure)

$$\left(\frac{m}{m_p} \right) \alpha^4 mc^2 \frac{4\gamma_p}{3n^2} [f(f+1) - 3/2]$$

- nuclear size effect

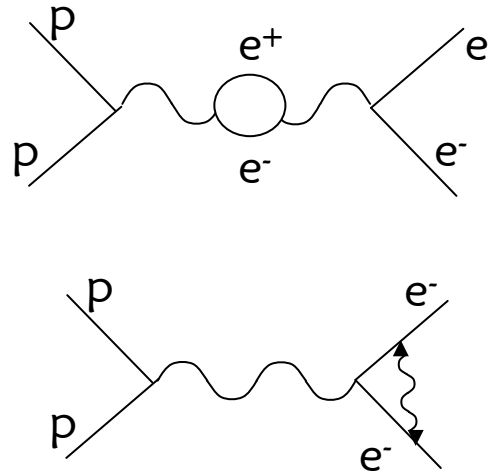
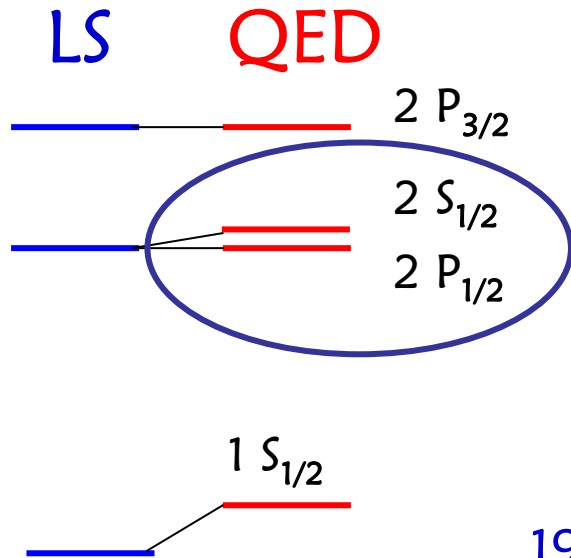
$$\frac{2\pi}{3} Ze^2 |\psi(0)|^2 \langle r^2 \rangle_{\text{proton}}$$

$$E = E_{\text{Bohr}} + E_{\text{rel}} + E_{\text{ls}} + E_{\text{Darwin}} + E_{\text{HF}} + E_{\text{QED}} + E_{\text{nuclear}}$$

The Lamb Shift



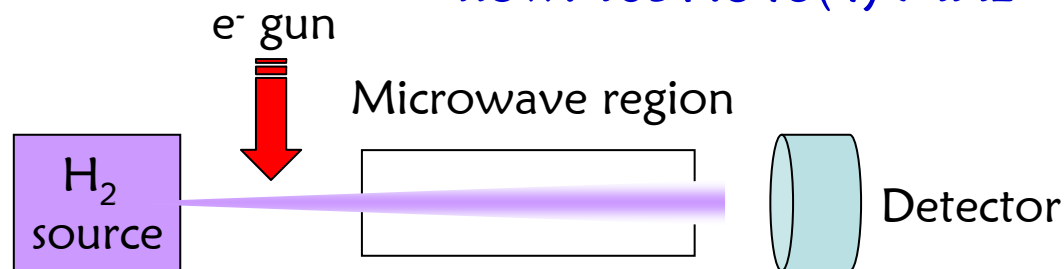
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1947 by Lamb ~ 1060 MHz
now: 1057.846(4) MHz

Willis Eugene Lamb
Nobel Prize in Physics 1955

"for his discoveries concerning the fine structure of the hydrogen spectrum"



g-2 experiment of electron and muon:

$g_e(\text{exp}) = 2.0023193043617(15)$, $g_e(\text{th})$ to determine fundamental constant

$g_\mu(\text{exp}) = 2.0023318416(12)$

$g_\mu(\text{th}) = 2.0023318367(13)$

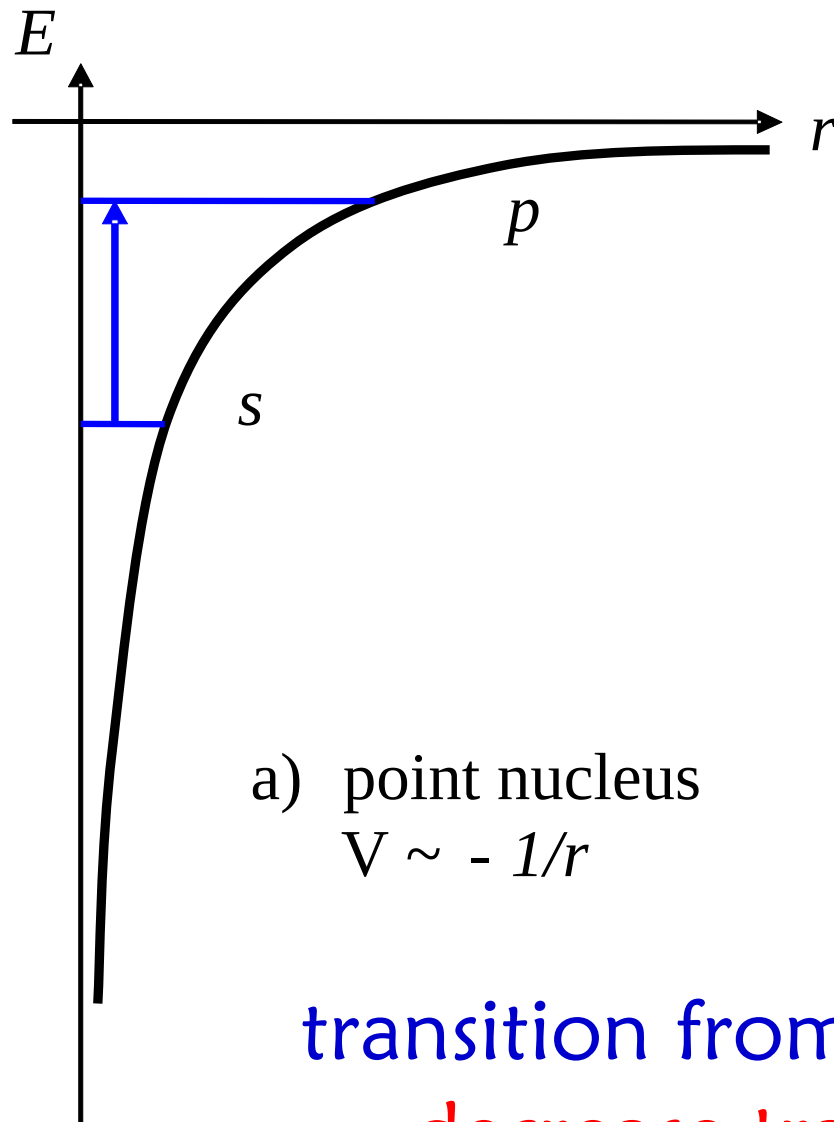
G.W. Bennett et al., *Phys Rev Lett.* **92**, 161802 (2004)

B. Odom et al., *Phys. Rev. Lett.* **97**, 030801 (2006)

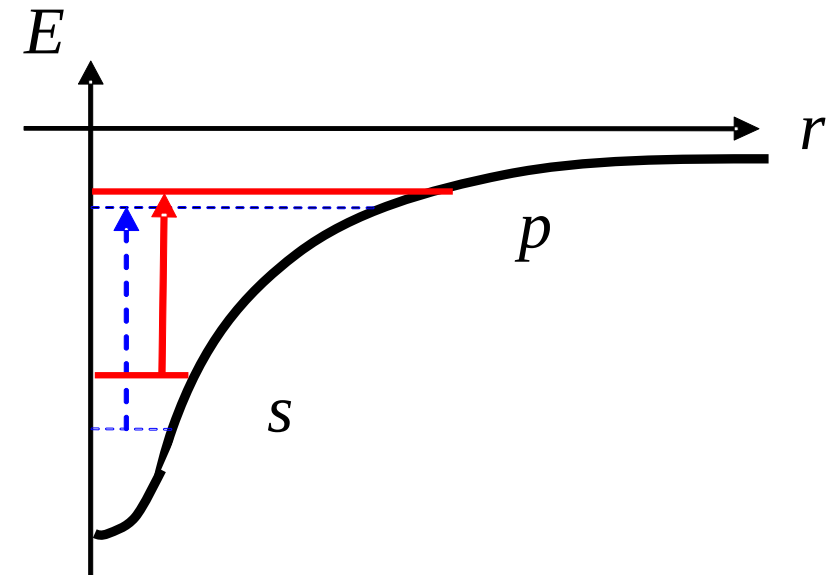
Nuclear size effect



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a) point nucleus
 $V \sim -1/r$



b) finite size nucleus

transition from s to p state

→ decrease transition frequency

- Measure total transition frequency:
uncertainty: theory ~ 10 kHz, experiment ~ 20 kHz
→ charge radius of proton
 $R_p = 0.883(14)$ fm [1, 2]
 $= 0.890(14)$ fm [3]

Reference:

- [1] C. Schwob et al., Phys. Rev. Lett. **82**, 4960 (1999).
- [2] Kirill Melnikov and Timo van Ritbergen, Phys. Rev. Lett., **84**, 1673(2000).
- [3] T. Udem et al. Phys. Rev. Lett. **79**, 2646, (1997).

Electron scattering



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● Electron beam on nucleus

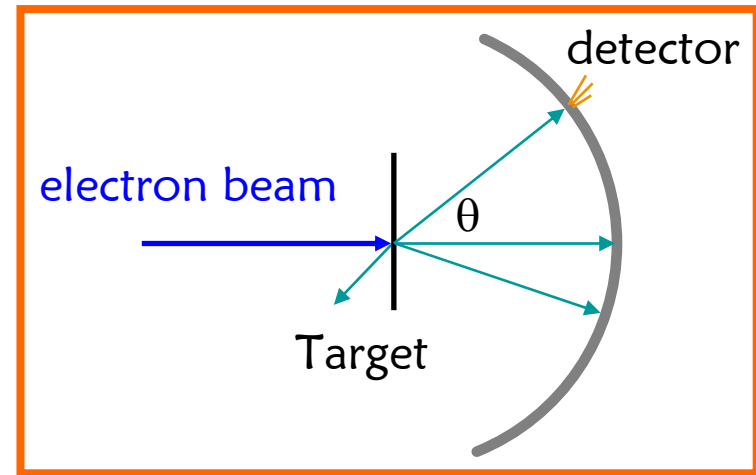
$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Rutherford}} = \frac{Z^2 \alpha^2 (\hbar c)^2}{4 E^2 \sin^4 \frac{\theta}{2}}$$

Nuclei with finite size:

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{exp}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Rutherford}} * \cos^2 \frac{\theta}{2} * |G_E(q^2)|^2$$

$$\langle r^2 \rangle = -6\hbar^2 \left. \frac{dG_E(q^2)}{dq^2} \right|_{q^2=0}$$

Note: not the shape to fit,
but the slope at $q^2=0$



Discrepancy



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2σ deviation

$$R_p = 0.862(12) \text{ fm}$$

G.G. Simon et.al. Nucl. Phys. A, 333, 381, (1980).



$$R_p = 0.883(14) \text{ fm [1, 2]} \\ = 0.890(14) \text{ fm [3]}$$

0.895(18) fm, re-analysis of world data

I. Sick, Phys. Lett. B 576, 62-67 (2003).

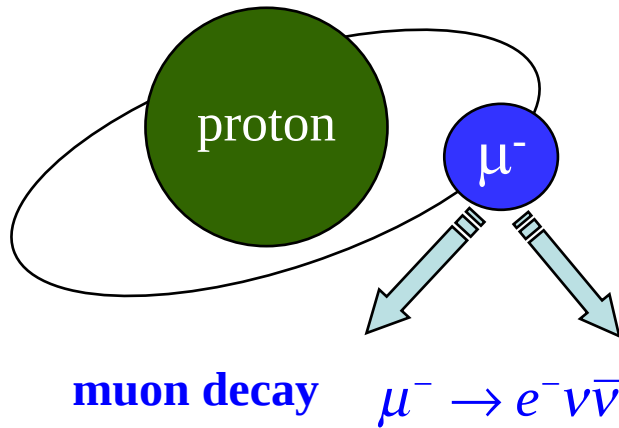
0.879(8) fm, new experiment by GSI

J. C. Bernauer et al., Phys. Rev. Lett. 105, 242001 (2010)

Muonic hydrogen



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- $m_\mu/m_e \sim 200$

- Bohr radius

$$a_0 = \frac{4 \pi \epsilon_0 \hbar^2}{m_e e^2}$$

- Energy level

$$E_n = - \frac{m_e}{2 (4 \pi \epsilon_0 \hbar)^2} \frac{1}{n^2}$$

- Wave function

$$\Psi(r) \sim a_0^{-3/2} e^{-r/a_0}$$

- Energy shift due to nuclear size ~

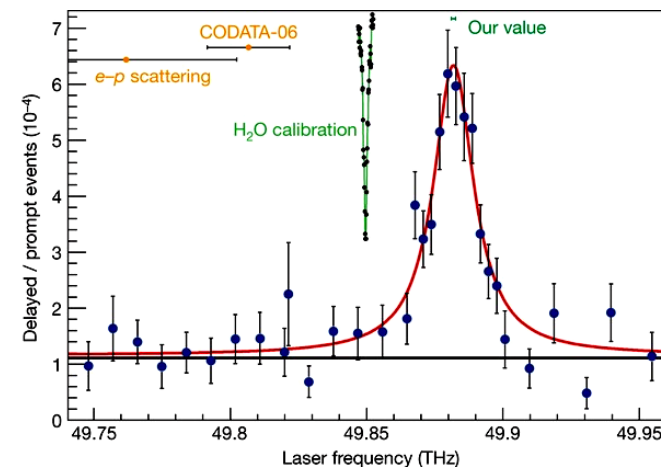
$$|\Psi(0)|^2 \langle r^2 \rangle$$

- Sensitivity $\sim (m_\mu/m_e)^2$

at PSI, reaching 0.1 % precision

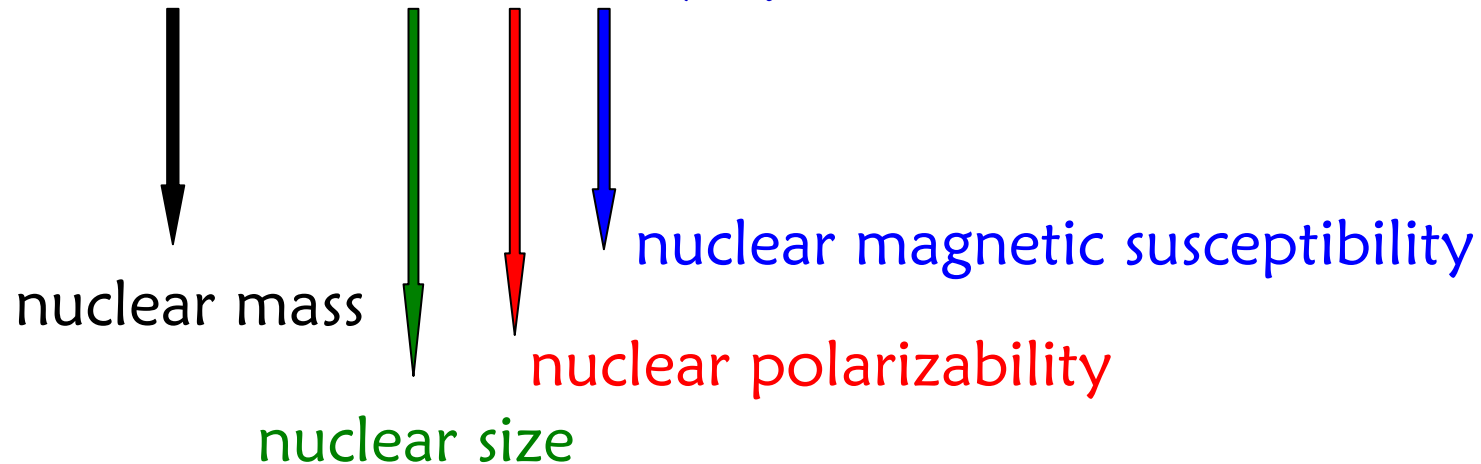
$$R_{\text{rms}} = 0.84184(67) \text{ fm}$$

Nature 466, 213–216, 2010



- Measure **isotope shift**, $1s \rightarrow 2s$ at 121 nm

$$\Delta\nu = 670\,994.33464(15) \text{ MHz}$$



A. Huber et al., Phys. Rev. Lett. 80, 468 (1998)



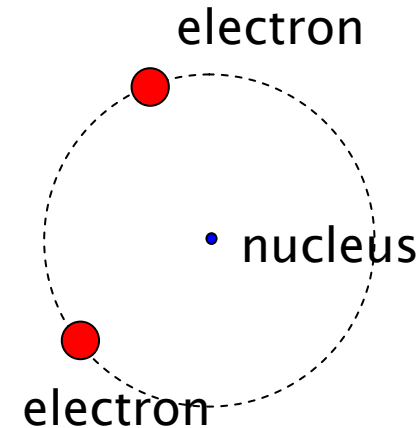
- H: 10 kHz, He: 1 MHz, Li: > 10 MHz
- Typical nuclear effect: several MHz
- G. Drake: QED uncertainty largely cancel in isotope shift (IS) and fine structure (FS) splitting measurement
- Uncertainty in isotope shift:
H: <1 kHz, He: <10 kHz, Li: 100 kHz
- Total transition frequency: test QED calculation
- Isotope shift: nuclear property
- FS and HFS: nuclear moment and many-body calculation

Two-electron system



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- non-relativistic ($\sim 1/n^2$)
- relativistic correction
- spin-orbit interaction
- nuclear magnetic moment
- QED effect
- nuclear size effect (e- inside the nucleus)
- nuclear polarizability
- many-body (e^2/r_{12})
- recoil correction ($p_1 p_2$)



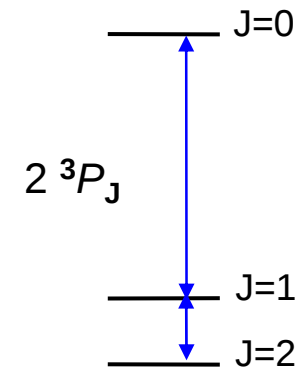
Previous attempt for helium



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Fine structure of helium-4

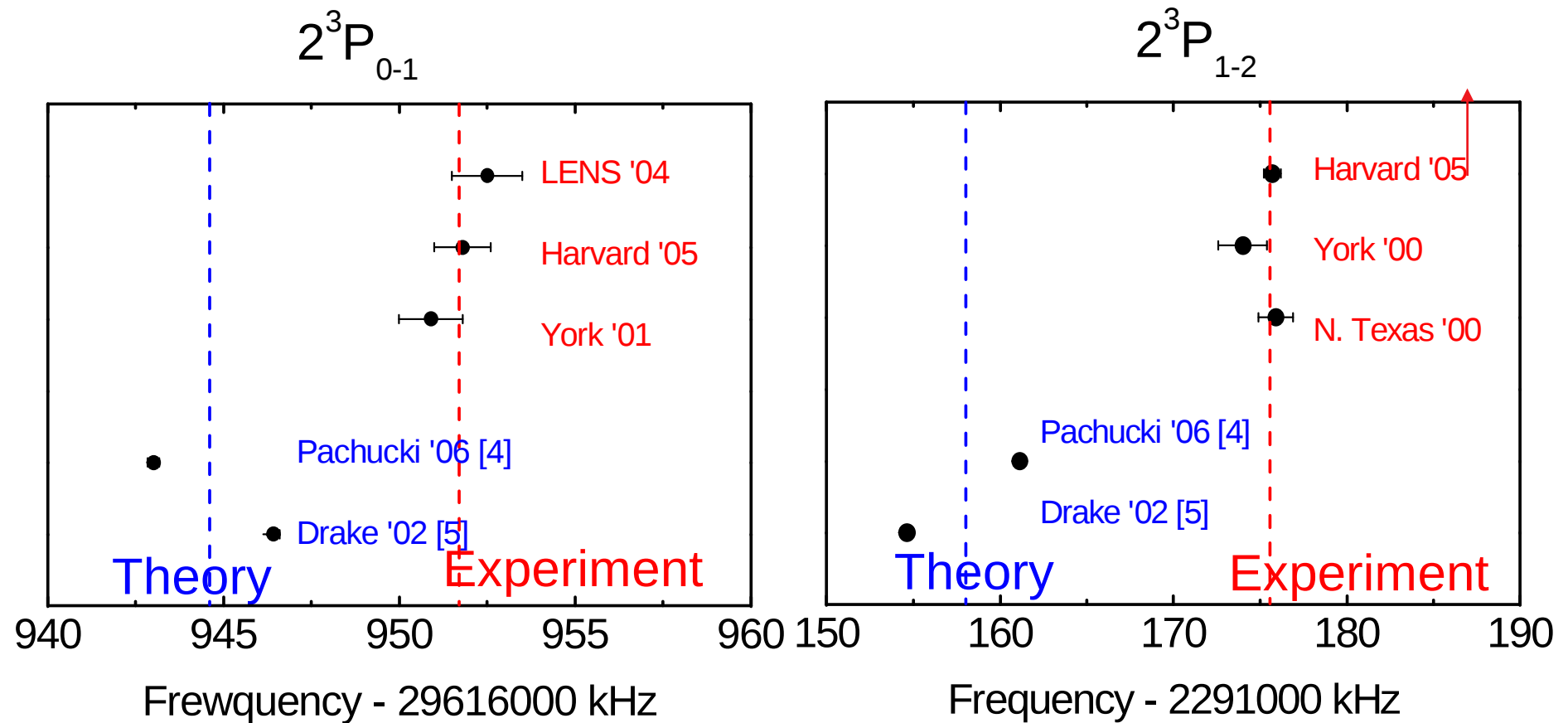
- Interval 29 GHz and 2.3 GHz
- Use one for constraining fine structure constant α ; another one for checking theory calculation



Previous attempt for helium



- uncertainty of theory and exp < 1 kHz
- difference = 10 kHz and 20 kHz





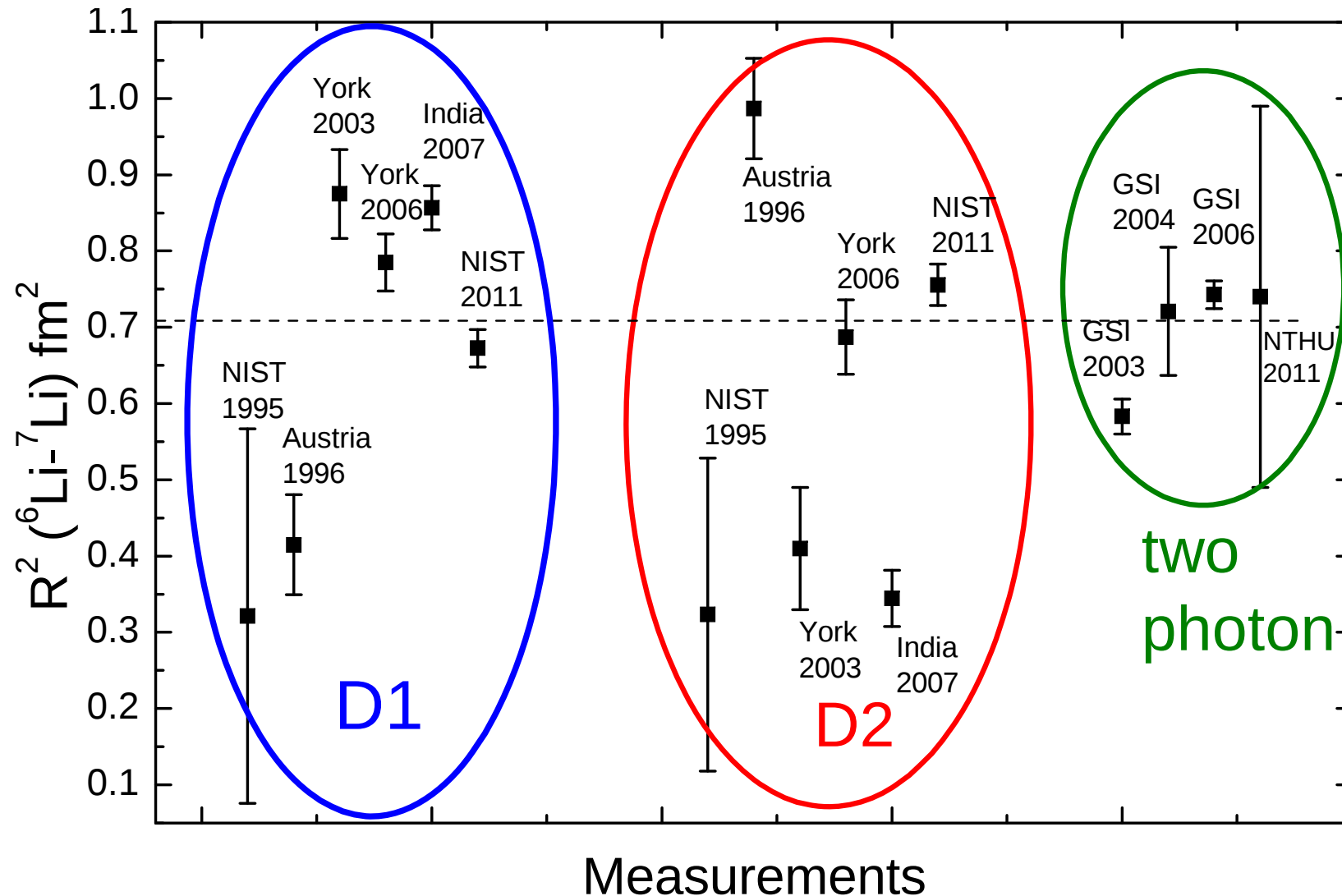
- Lithium, more complicated
- Experimental discrepancy between York and Austria measurement

Discrepancy in lithium



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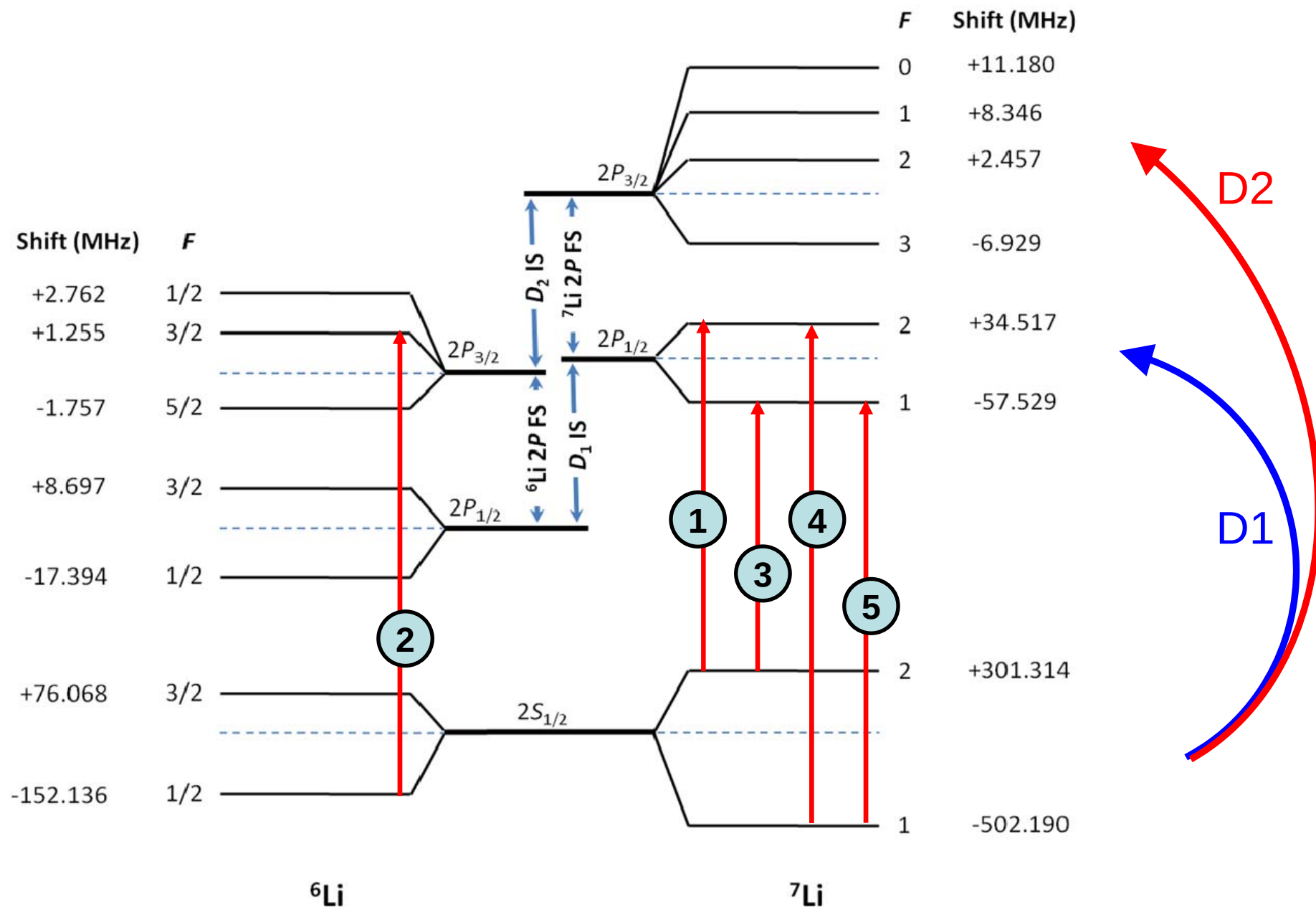
- Test QED calculation, but discrepancy also exist



Energy level of Li-6,7



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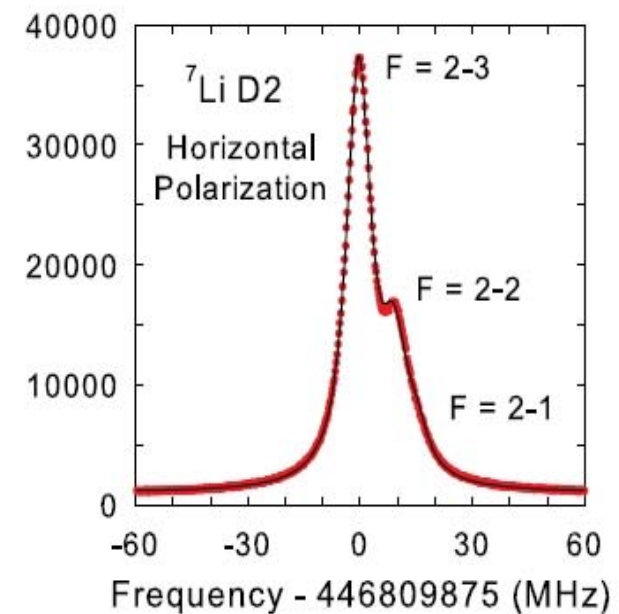
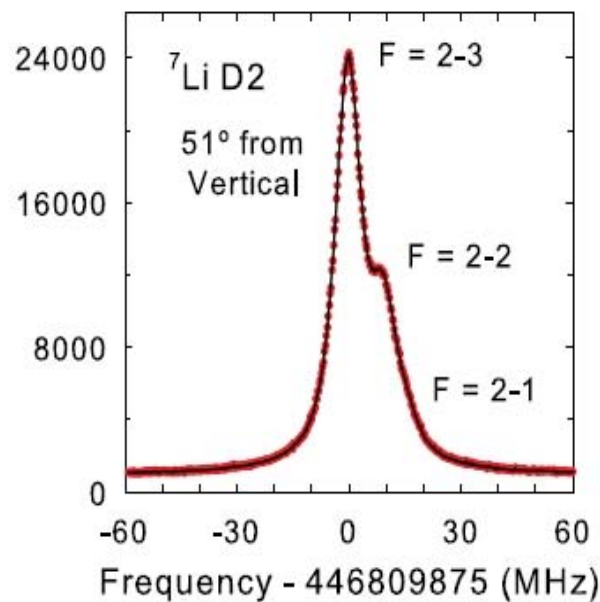
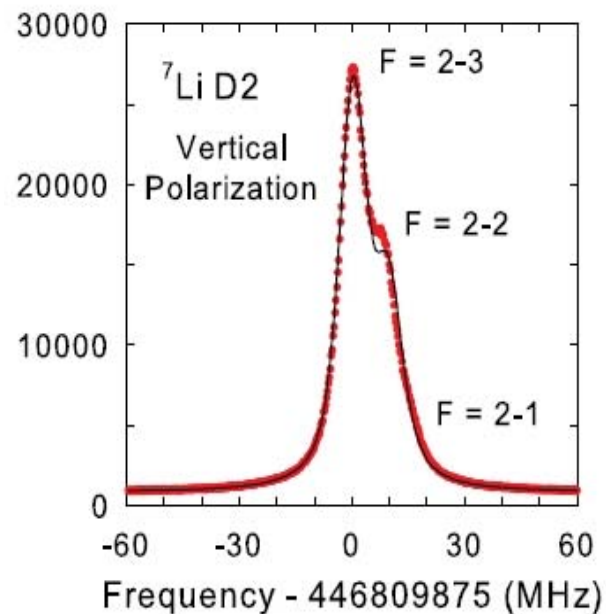


Explanation for D2 by NIST 2011



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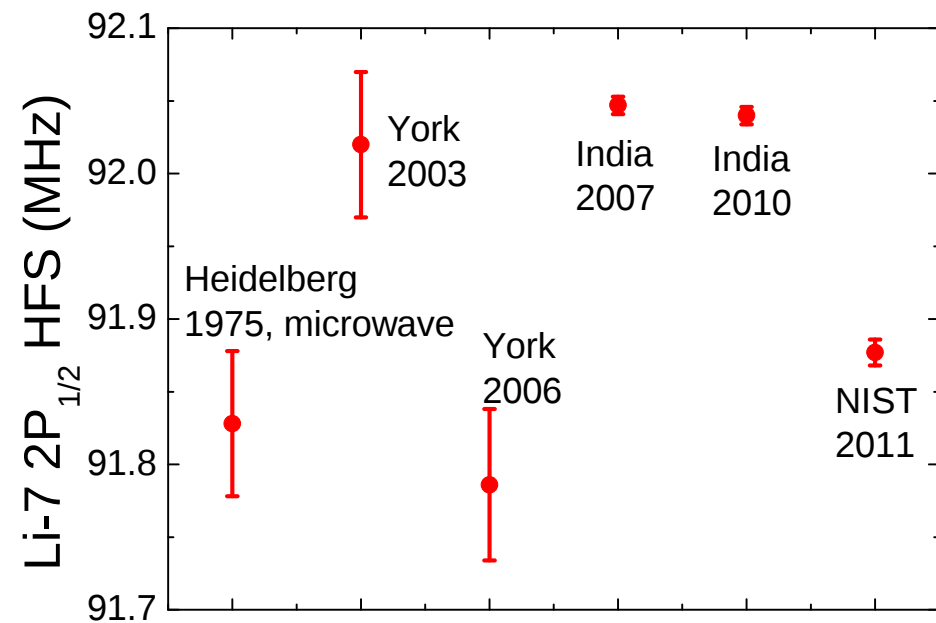
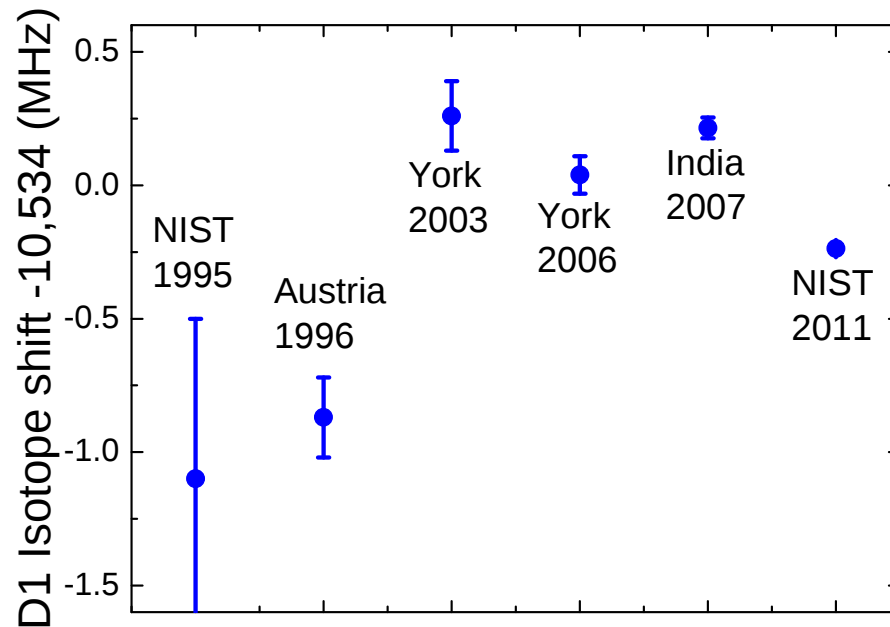
- D2 line not well resolved
- Exhibit quantum interference
- Large polarization dependence



D1 line



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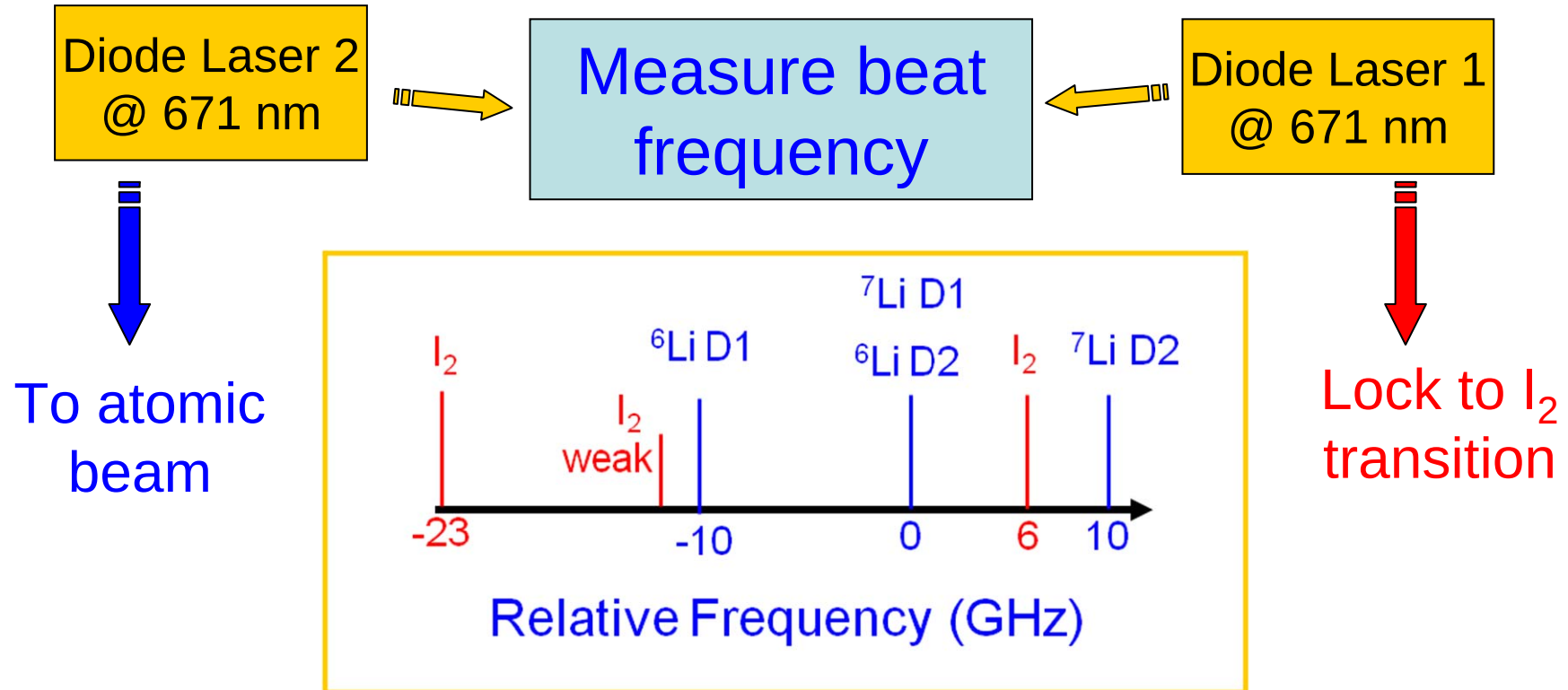


- Isotope shift: different velocity may cause systematic effect
- FS and HFS in one isotope: almost immune to beam alignment

Our approach



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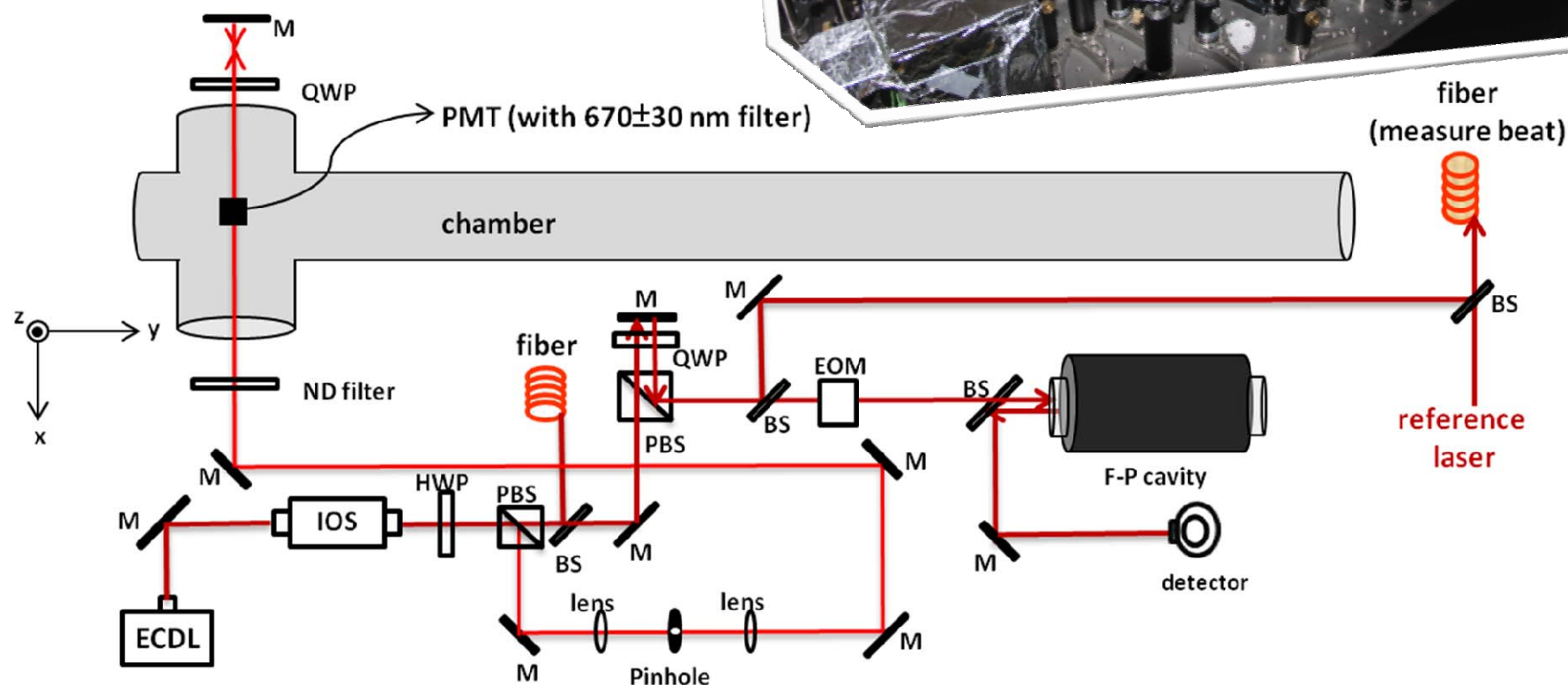
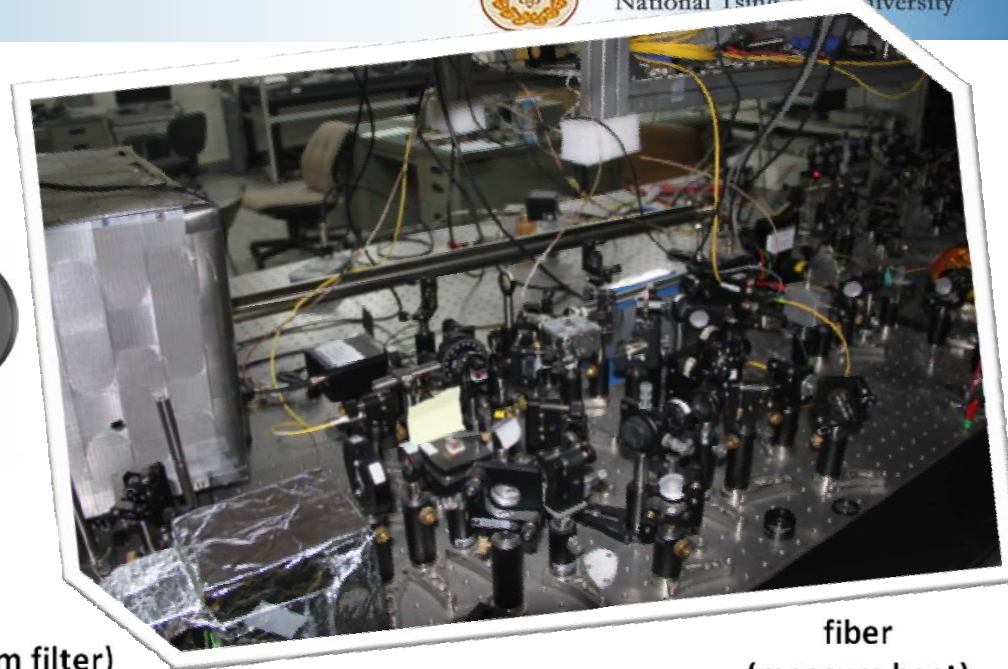


No.	Transition energy level	Center(MHz)	Width(MHz)
1	${}^7\text{Li } 2S_{1/2} F=2 \rightarrow 2P_{1/2} F=2$	6285.173(23)	11.060(75)
2	${}^6\text{Li } 2S_{1/2} F=1/2 \rightarrow 2P_{3/2} F=1/2, 3/2$	6345.231(34)	15.103(1.053)
3	${}^7\text{Li } 2S_{1/2} F=2 \rightarrow 2P_{1/2} F=1$	6377.143(18)	10.003(55)
4	${}^7\text{Li } 2S_{1/2} F=1 \rightarrow 2P_{1/2} F=2$	5481.770(15)	11.322(48)
5	${}^7\text{Li } 2S_{1/2} F=1 \rightarrow 2P_{1/2} F=1$	5573.584(45)	9.247(147)

Spectroscopy laser



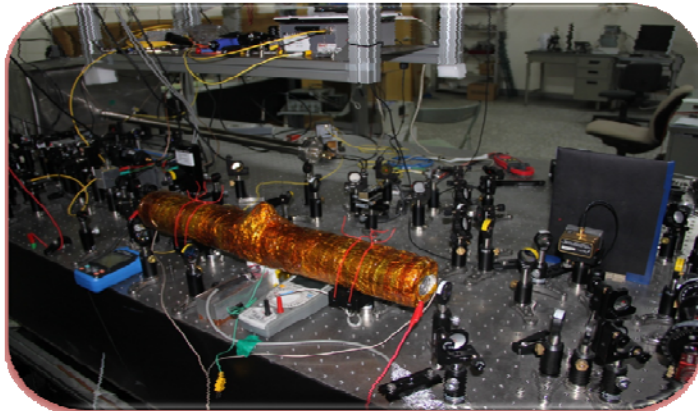
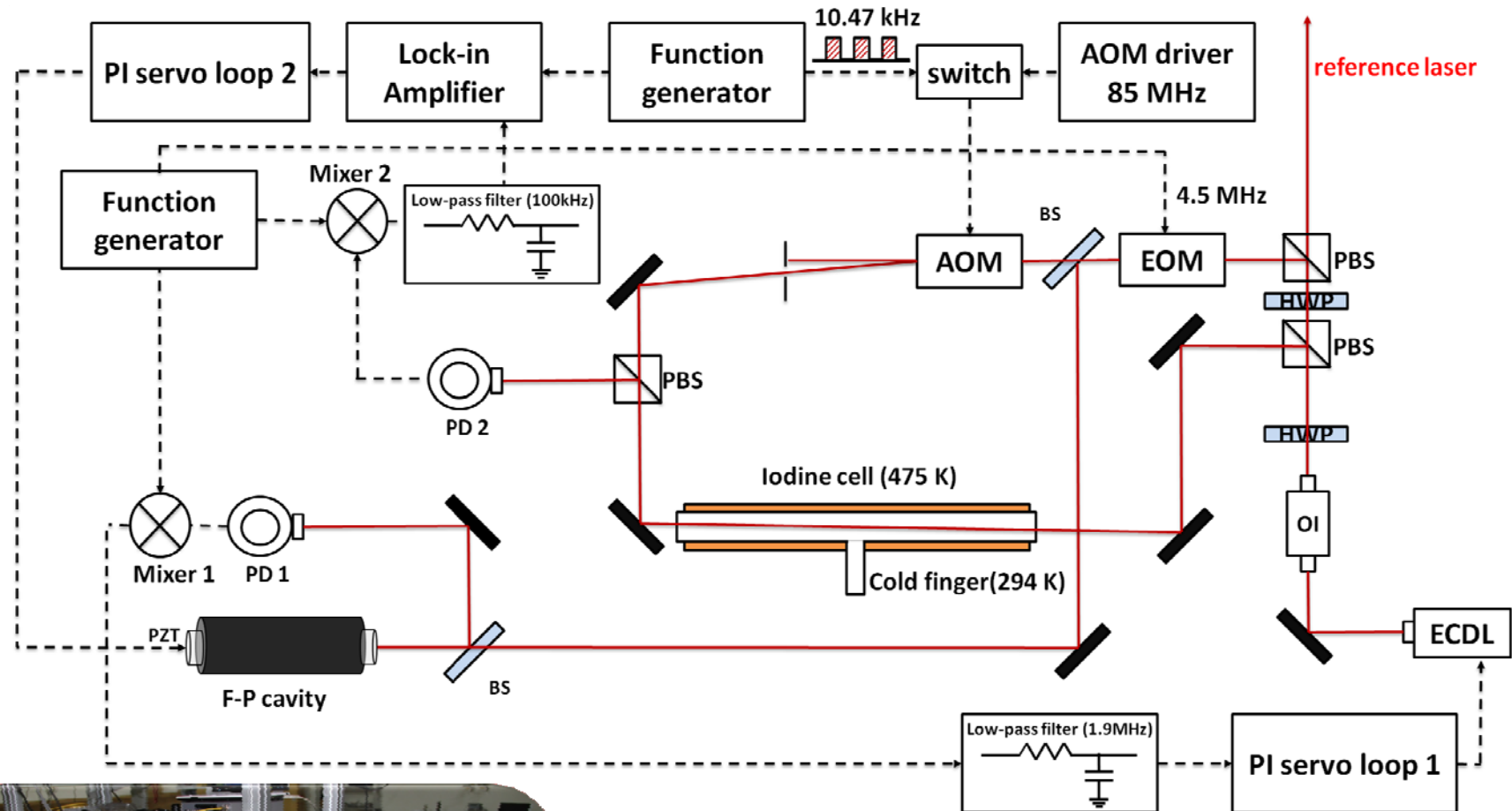
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Reference laser



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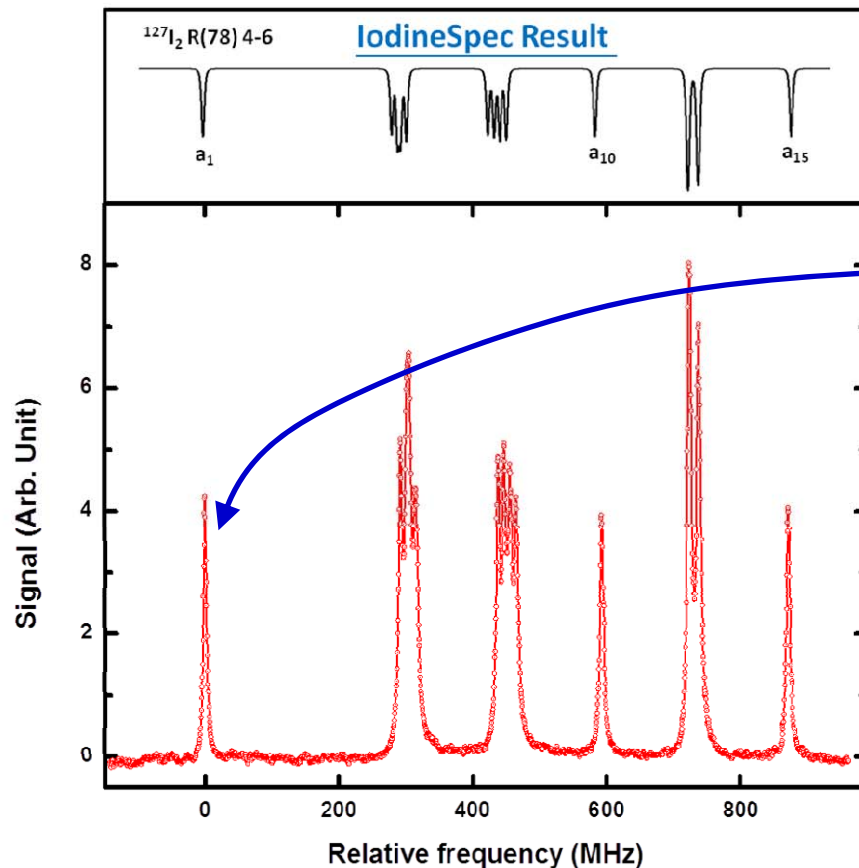


Iodine spectrometer

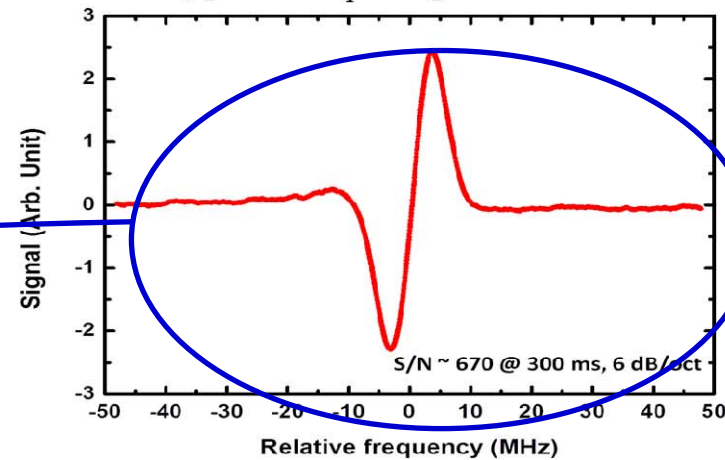


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The transitions and derivative signal of $^{127}\text{I}_2$ at 671 nm:



The hyperfine a_1 component



Parameters

Pump Power = 2.8 mW

Probe Power = < 1 mW

Signal slope: 695 mV/MHz

Signal-to-noise ratio: ~ 670 @ 300 ms



- Frequency-comb measurement of the iodine transition
- Pressure shift, pump power shift, etc.

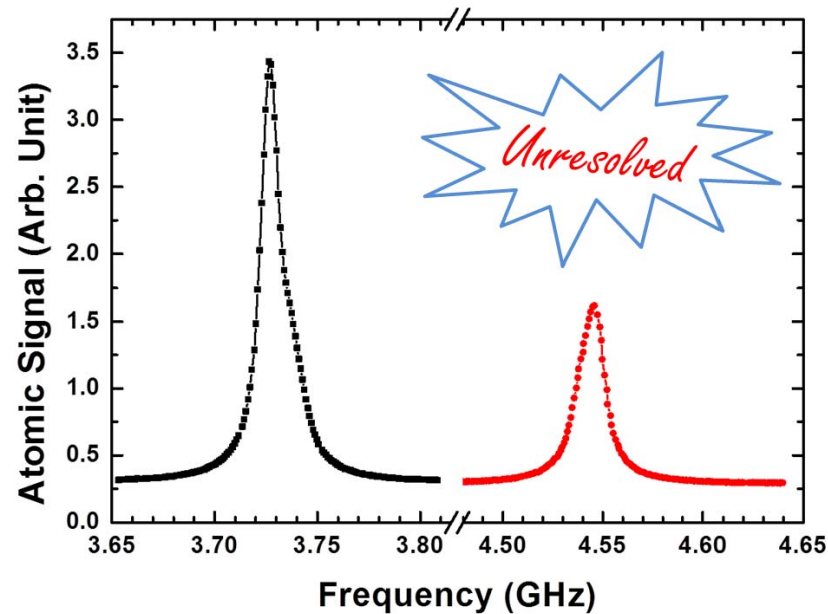
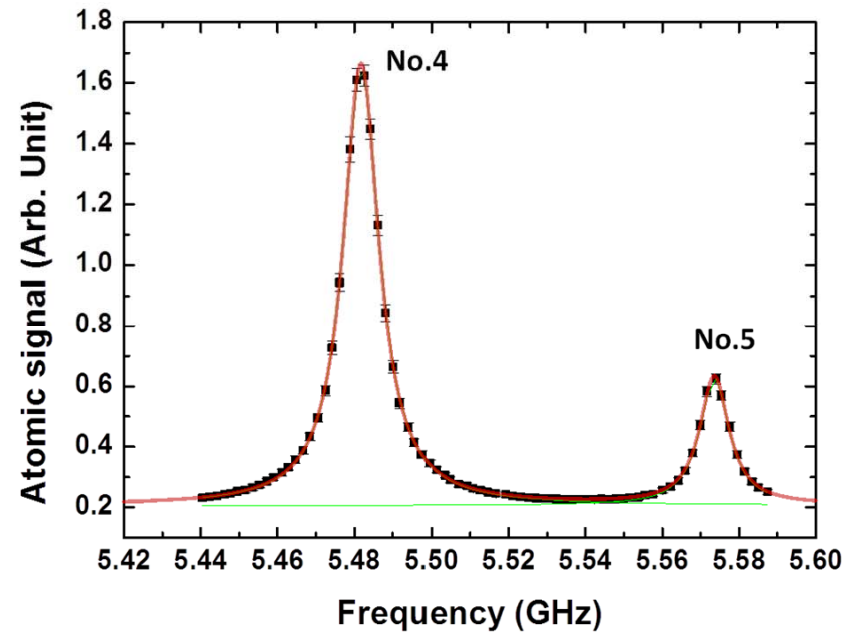
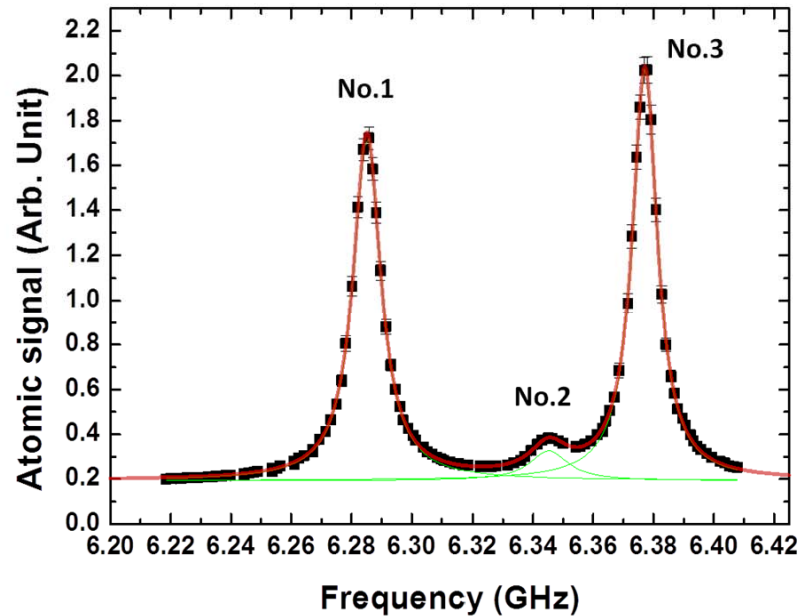
Unit: MHz

line	Result	IodineSpec	Difference
a1	446806191.649(23)	446806194.57	2.92
a10	446806778.709(33)	446806781.53	2.82
a15	446807072.397(33)	446807075.27	2.87

Typical signal for lithium-7



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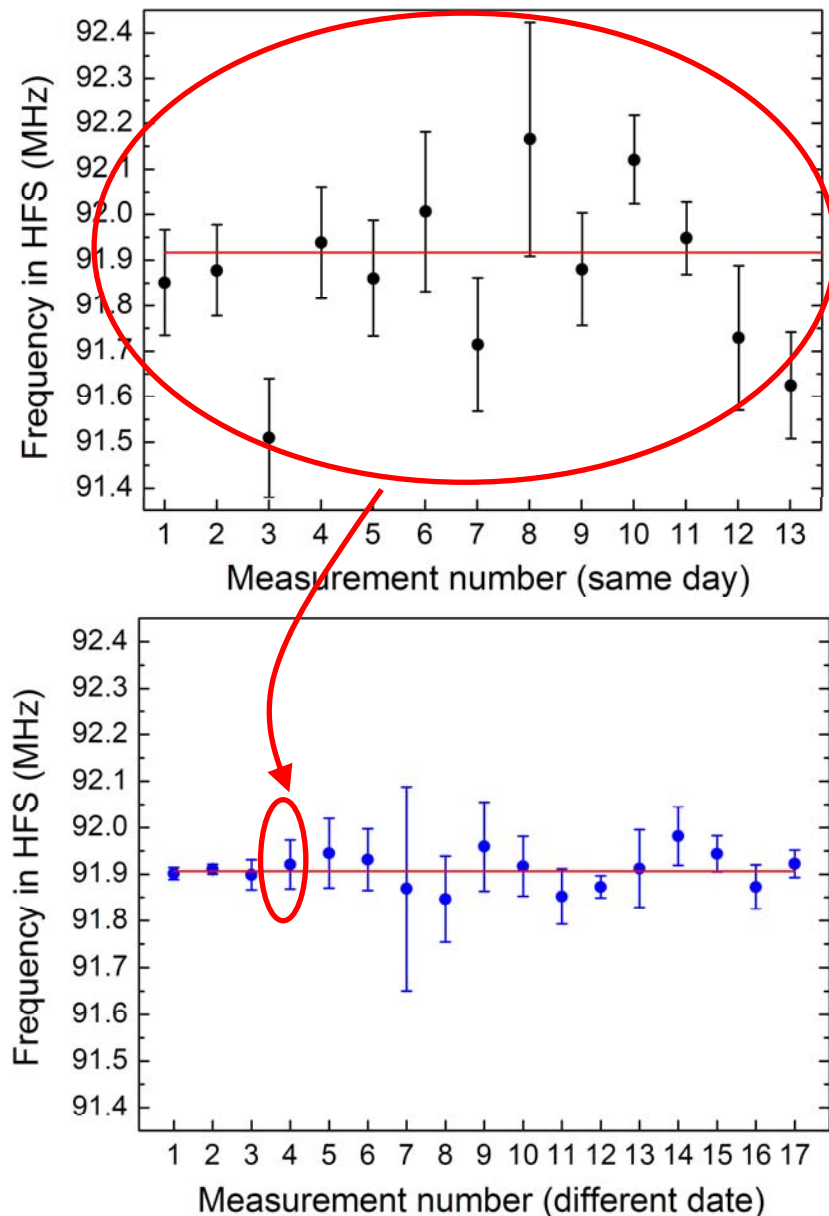
D1 line: hyperfine structure well resolved

D2 line: only the ground state hyperfine structure resolved

Data analysis

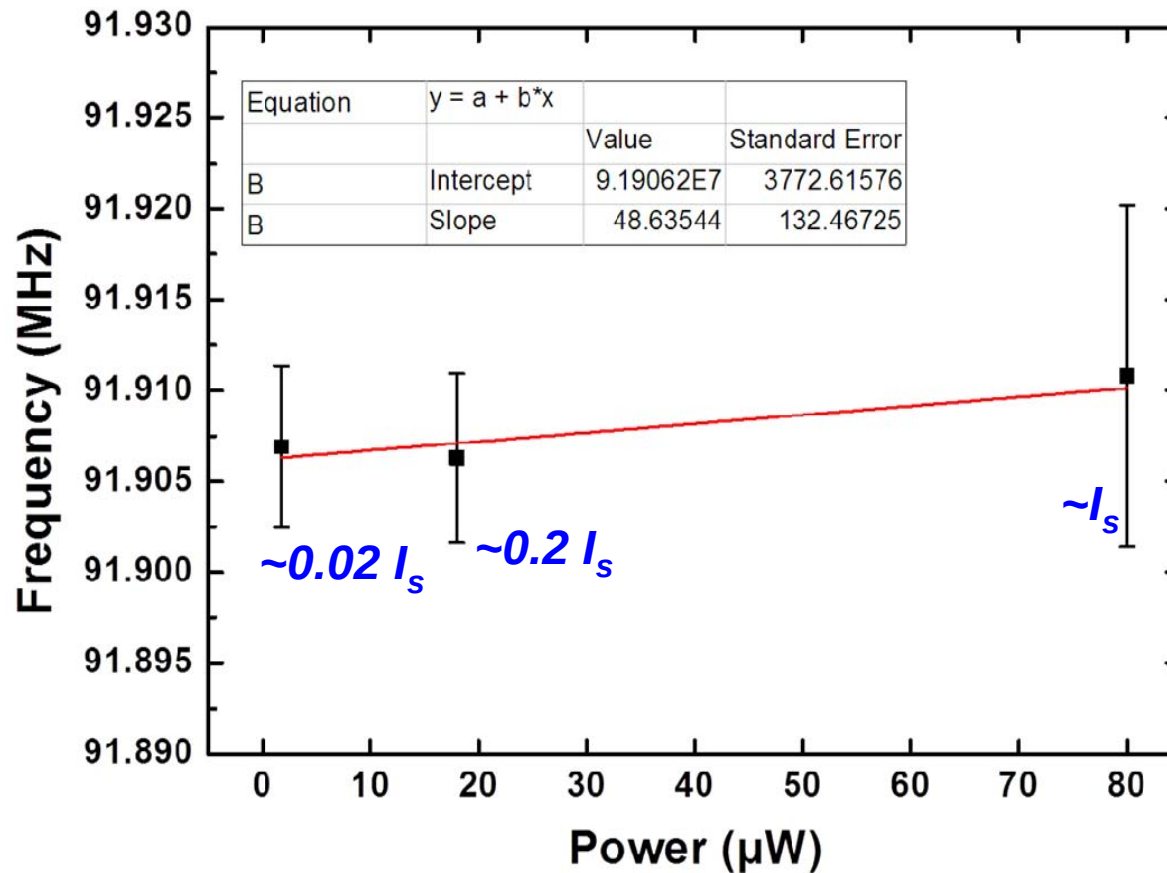


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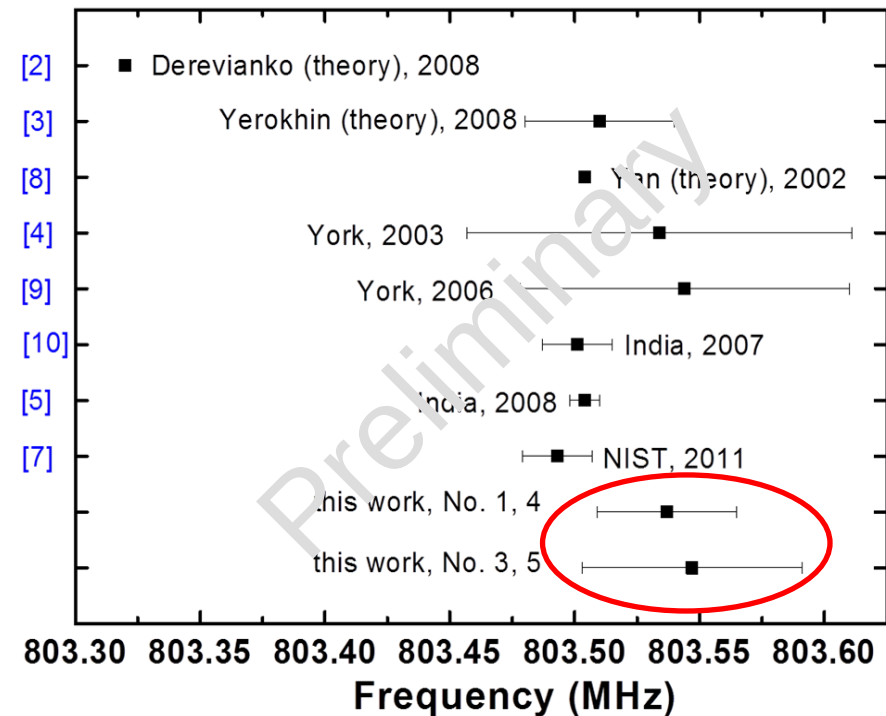
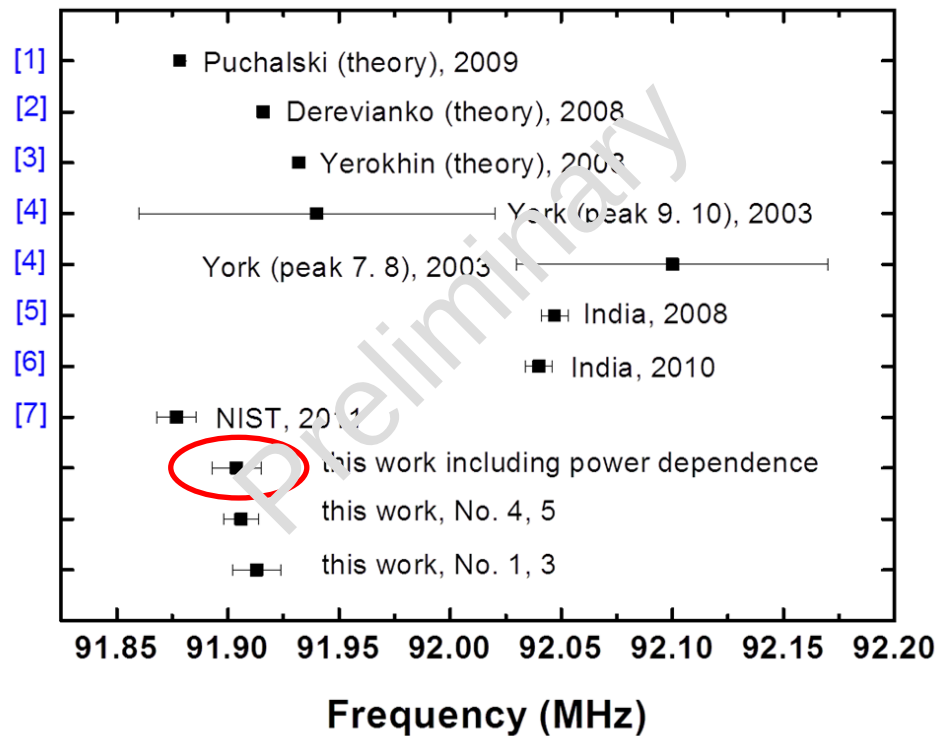
- Difference between two peaks
- Scan up and down
- Quick scan, ~ 1 point/sec
- I_2 instability $\rightarrow \chi^2 > 1$
- Consistent in different dates
- I_2 drift and cavity drift

Laser power dependence



- AC Stark effect from other levels
- Photon momentum → cooling or heating

Results



- [1] M. Puchalski and K. Pachucki, Phys. Rev. A **79**, 032510 (2009).
- [2] A. Derevianko, S.G. Porsev, and K. Beloy, Phys. Rev. A **78**, 010503 (2008).
- [3] V. A. Yerokhin, Phys. Rev. A **78**, 012513 (2008).
- [4] J. Walls, R. Ashby, J. J. Clarke, B. Lu, and W. A. van Wijngaarden, Eur. Phys. J. D **22**, 159 (2003).
- [5] D. Das, and V. Natarajan, Phys. B. **41**, 035001 (2008).
- [6] A. K. Singh, L. Muanzuala, and V. Natarajan, Phys. Rev. A **82**, 042504 (2010).
- [7] C. J. Sansonetti, C. E. Simien, J. D. Gillaspay, J. N. Tan, S. M. Brewer, R. C. Brown, S. Wu, and J. V. Porto, Phys. Rev. Lett. **107**, 023001 (2011).
- [8] Z. C. Yan, and G. W. F. Drake, Phys. Rev. A **66**, 042504 (2002).
- [9] G. A. Noble, B. E. Schultz, H. Ming, and W. A. van Wijngaarden, Phys. Rev. A **74**, 012502 (2006).
- [10] D. Das, and V. Natarajan, Phys. B. **75**, 052508 (2007).

Error Budgets



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Sources	Magnitude (kHz)
Statistical error	5
Laser power effect	5
Beam misalignment	< 1
B field effect	< 3
Total	8

Iodine instability included in statistical error

Note: the hyperfine splitting does not simply relate to A and B coefficients as:

$$\Delta E_{HFS} = \frac{1}{2} AK + \frac{1}{4} B \frac{\frac{3}{2} K(K+1) - 2I(I+1)J(J+1)}{I(2I-1)J(2J-1)}$$

$$\frac{HFS}{2} + 27 \text{ kHz} = A$$

$$HFS = 2A$$

where $K = F(F+1) - J(J+1) - I(I+1)$

2nd order effect
from state mixing

K. Beloy and A. Derevianko, Phys. Rev. A **78**, 032519 (2008).

Summary



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- For H, better theory desired
also muonic hydrogen problem
- For He, discrepancy in fine structure
- Li spectroscopy: (with optical frequency comb)
 - measure Li-6,7 isotope shift and HFS in atomic beam, vapor cell and MOT
 - Li^+ spectroscopy in discharge, ion beam, and trap

People involved Lithium D line: 駱瑋駿, 黃耀欽, 郭彥廷
Iodine spectroscopy: 蕭仔真 Li^+ : 高政揚
Former member: 王宥人, 曾安廷, 陳柏安
Supported by NSC and MOE 5y50b fund