



# The Application of X-ray Scattering in the Studies of Nanomaterials

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Introduction of X-ray scattering

The growth of ZnO on Si using a  $Y_2O_3$  buffer layer

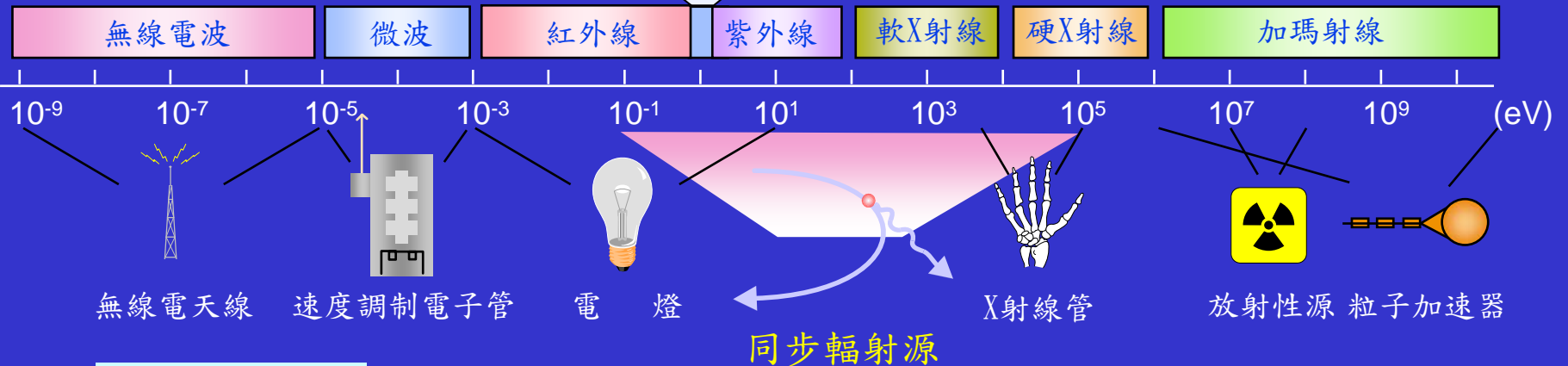
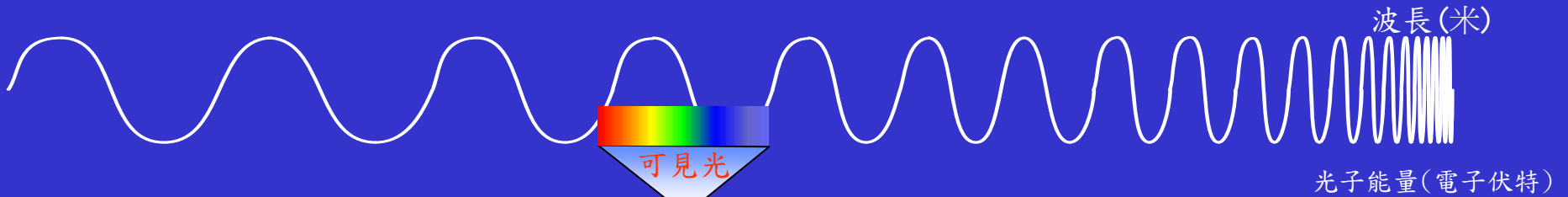
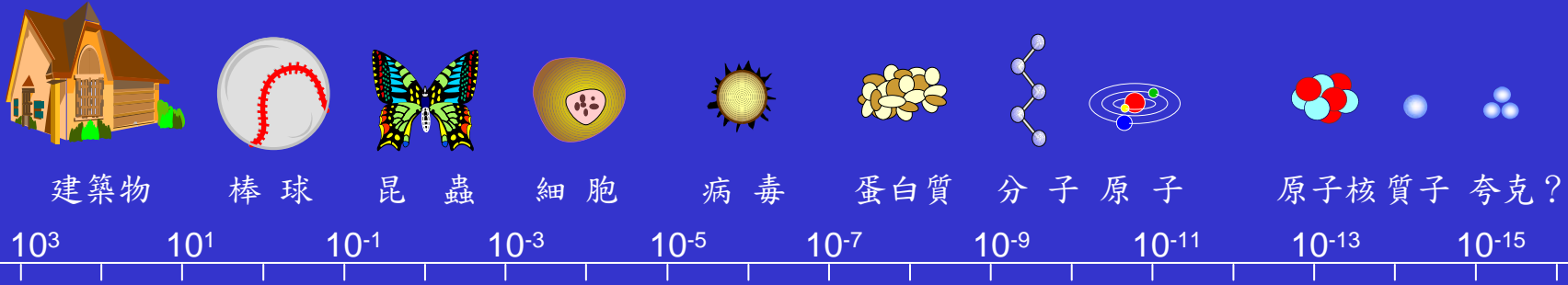
Domain Matching Epitaxy

Summary

NSRRC



可探測到的物體



輻射源

# The Properties of Synchrotron Radiation

- High Intensity

$$I_{SR} > 10^6 * I_{tube}$$

- Continuous Spectrum

(NSRRC  $35 \text{ keV} > E > 0.05 \text{ eV}$ )

- Excellent Collimation

- Low Emittance

- Pulsed-time Structure (NSRRC)

bunch length: 25 ps

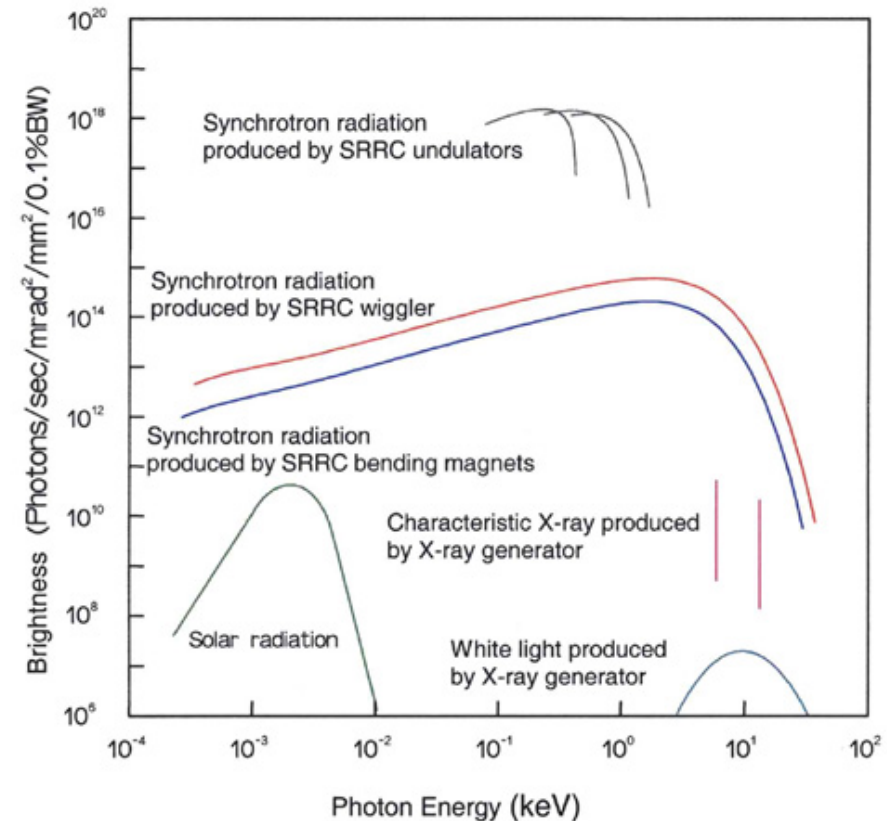
pulse separation: 2 ns

no. of buckets: 200

- Polarization

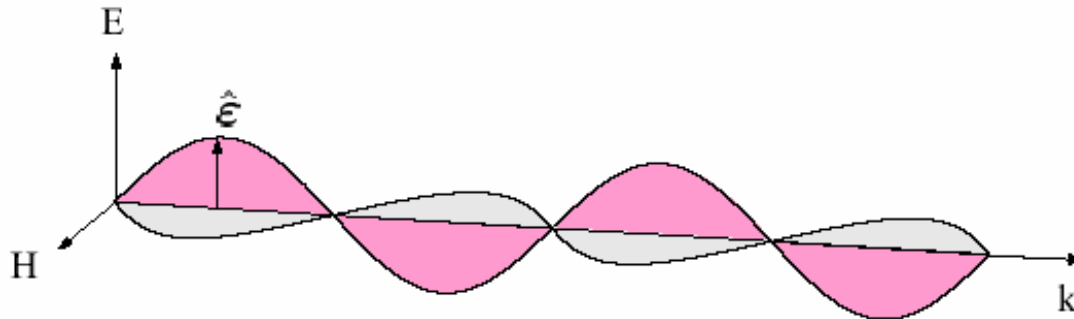
linear polarization, elliptical pola

- Coherence (laser)



# (Elastic) X-ray Scattering

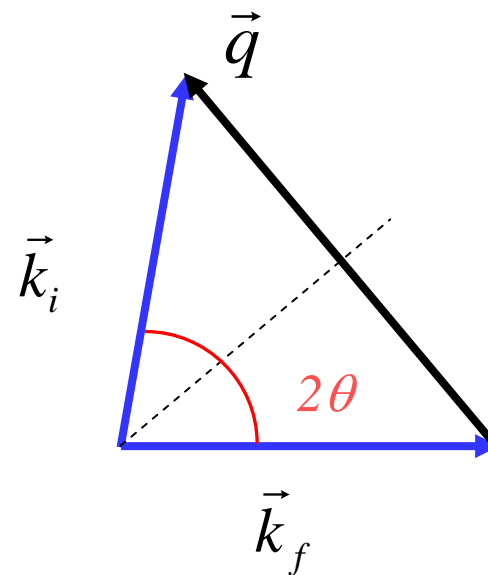
X-ray: Electromagnetic wave  $E = hc/\lambda$



$E_i = E_f$  i.e.  $\lambda_i = \lambda_f$  (elastic scattering)

wave vector  $k = 2\pi/\lambda$  ;  $|k_i| = |k_f|$

wave vector (energy), amplitude, phase

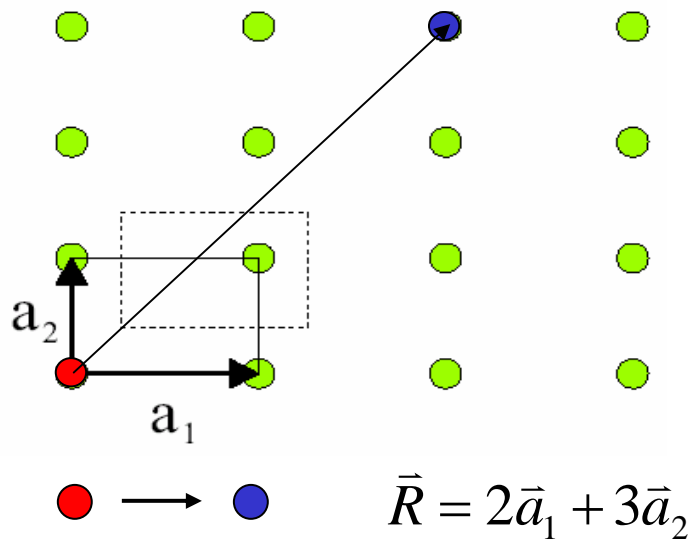
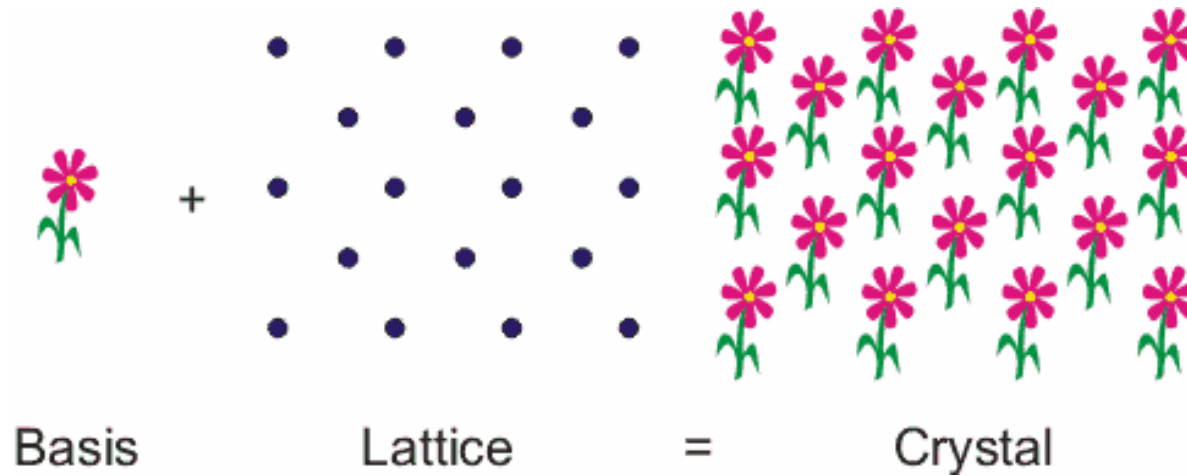


$$\vec{q} = \vec{k}_f - \vec{k}_i$$

$$q = 4\pi \sin(\theta)/\lambda$$



# Crystal Structure



in 3-D

basis vectors:  $a_1, a_2, a_3$

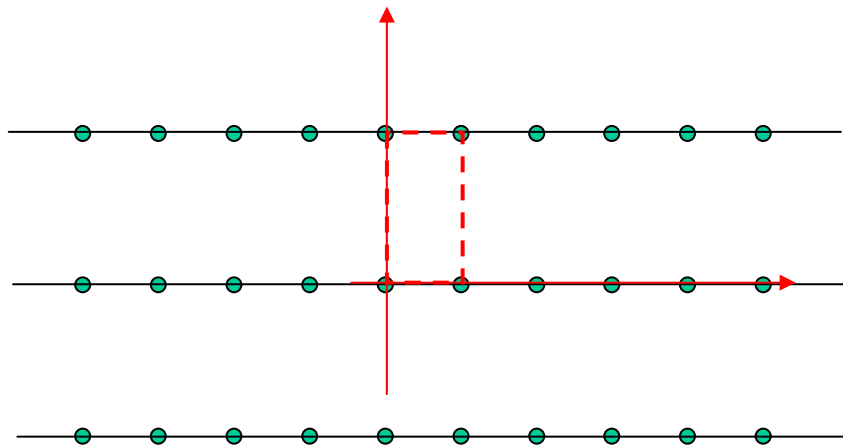
Any lattice point  $\vec{R}$  can be obtained by translation

$$\vec{R} = n_1\vec{a}_1 + n_2\vec{a}_2 + n_3\vec{a}_3$$

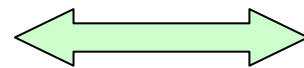
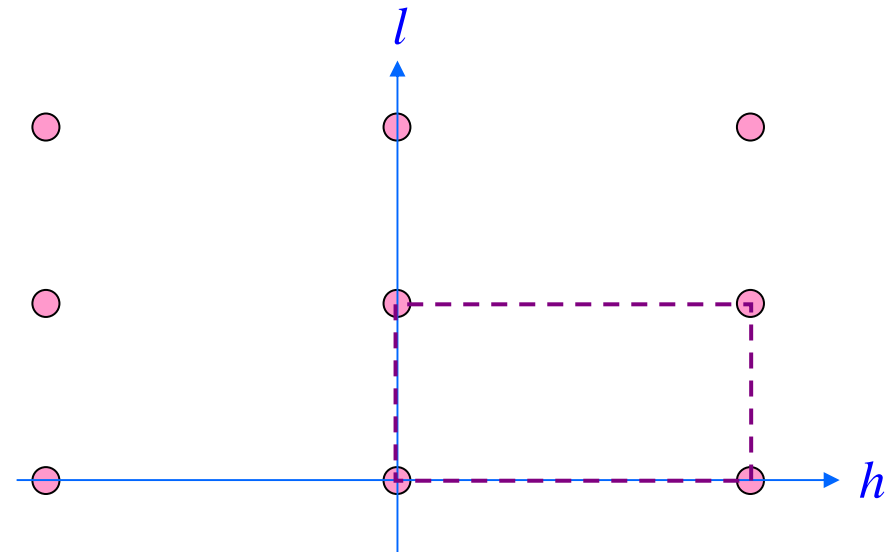


# Lattice

Real space lattice



Reciprocal space lattice



Fourier Transfer



# Condition for Bragg reflection

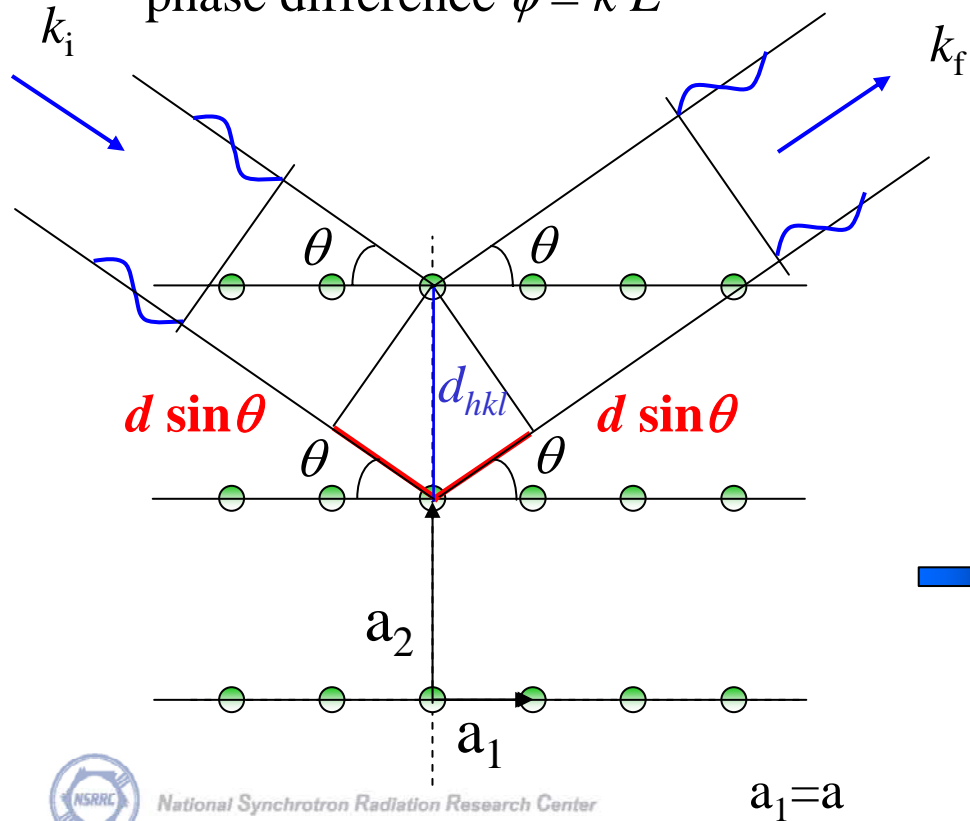
## Real space

Bragg Law  $2d \sin\theta = \lambda$

Path Difference  $L = 2d_{hkl} \sin\theta$

Constructive interference:  $L = n\lambda$

phase difference  $\phi = kL$

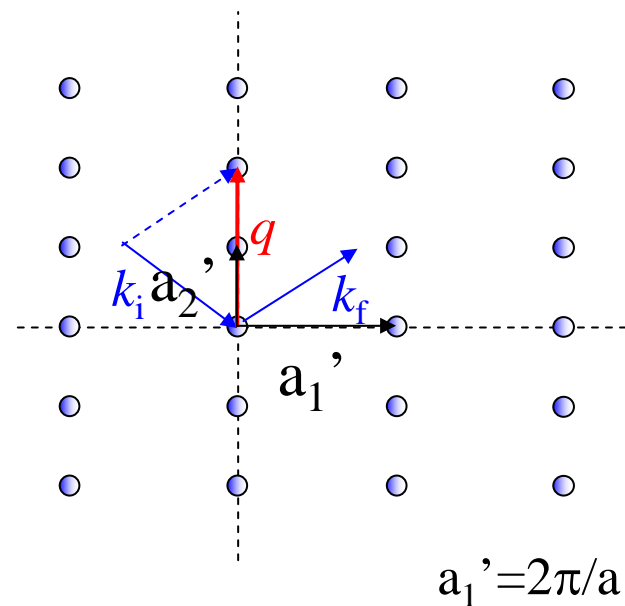


## Reciprocal space

$$2 \frac{2\pi}{\lambda} \sin\theta = \frac{2\pi}{d_{hkl}}$$

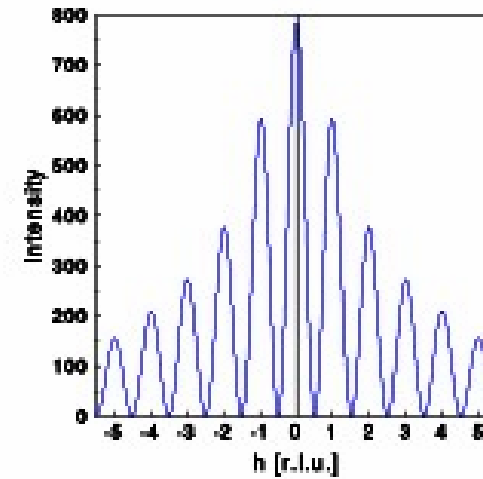
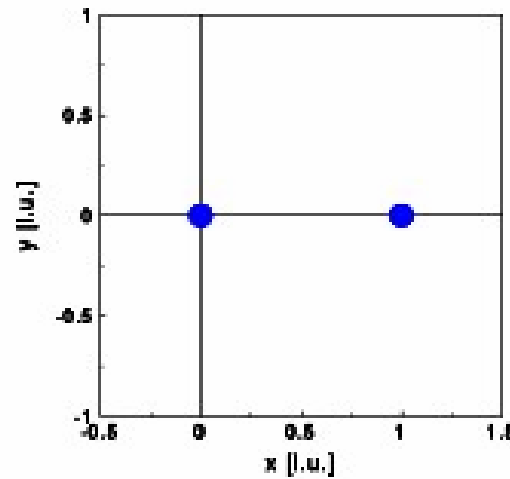
$$\vec{q} = \frac{4\pi}{\lambda} \sin\theta \hat{q} = \frac{2\pi}{d_{hkl}} \hat{n} = \vec{G}_{hkl}$$

FT  
→



# Size Effect - Diffraction Pattern of A Row of Atoms

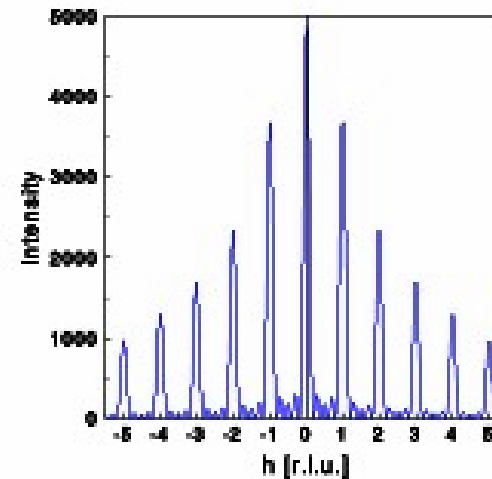
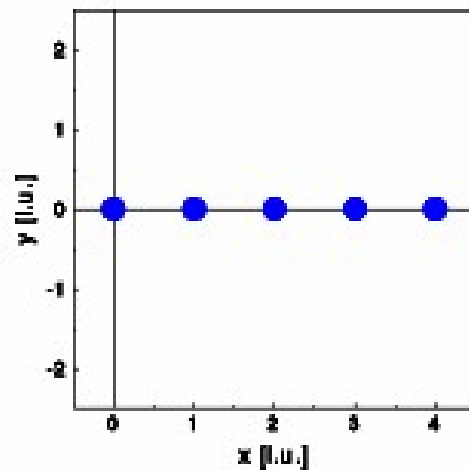
2 atoms



1 l.u. = a Å

1 r.l.u. =  $2\pi/a$  Å<sup>-1</sup>

5 atoms



Scherrer's equation

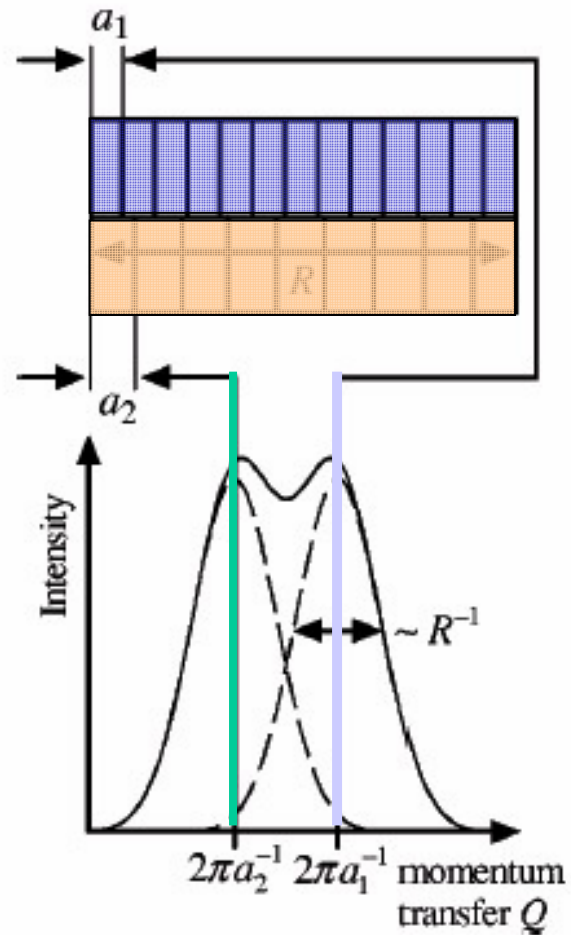
$$L \approx \frac{2\pi}{FWHM(q)}$$

$$L \approx \frac{0.9\lambda}{FWHM(2\theta) \cos \theta_B}$$





## Effect due to Lattice Constant Change (Strain Effect)



$$2\pi (a_2^{-1} - a_1^{-1}) \geq R^{-1}$$





**National Synchrotron Radiation Research Center**

## **Structural and Optical Properties of ZnO films Grown on Si with a Y<sub>2</sub>O<sub>3</sub> Buffer Layer**

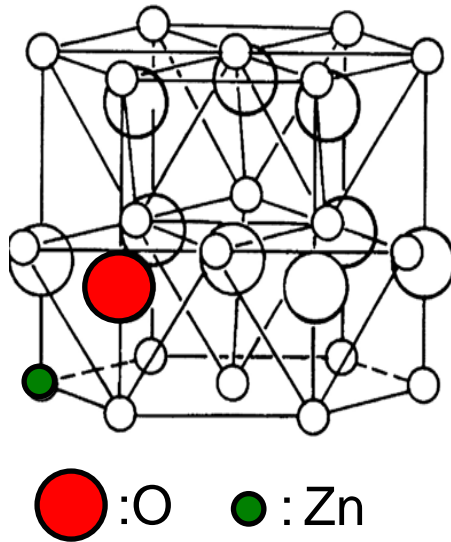
劉維仁	李岳勳	謝文峰	交大光電
李威縉	李毅君	洪銘輝	清大材料
	郭瑞年		清大物理
林碧軒	楊智凱	徐嘉鴻	同步輻射

NSRRC



# ZnO

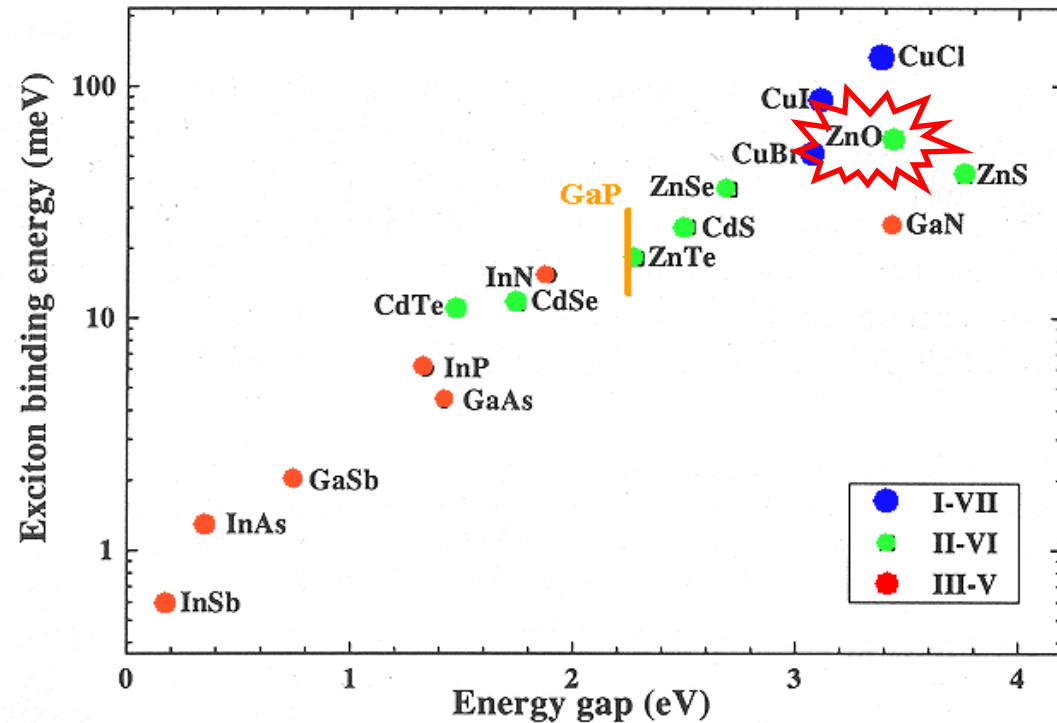
Wurtzite (hexagonal)



ZnO bulk:  $a = 3.24382 \text{ \AA}$   
 $c = 5.20364 \text{ \AA}$

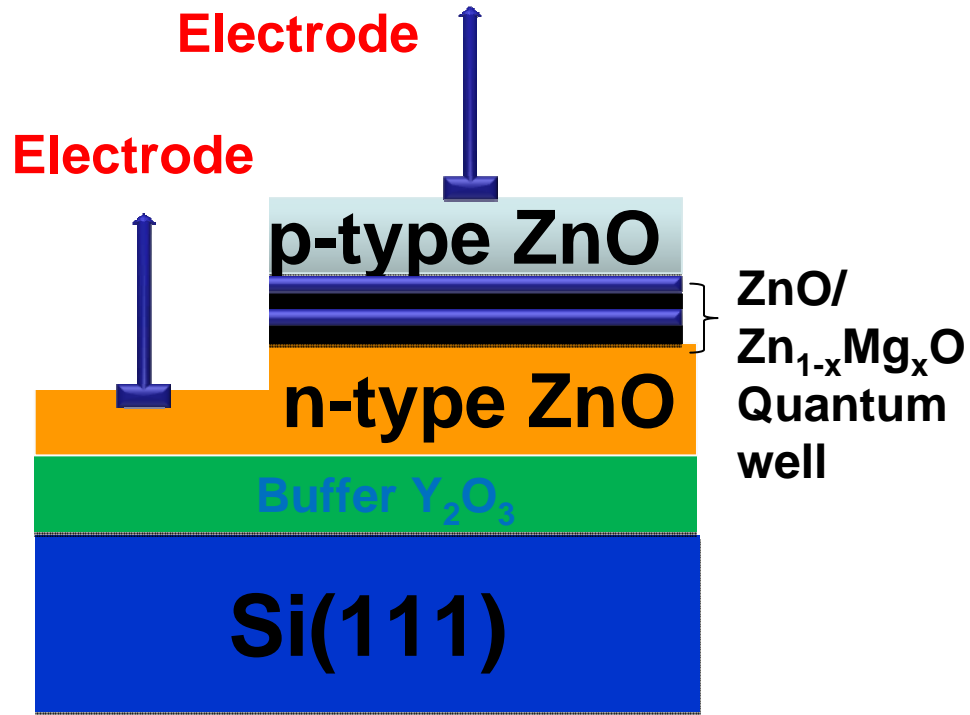
- II-VI wide direct band gap (3.37eV) wurtzite-type semiconductor
- Large binding energy of free exciton (60 meV)
- Free exciton emission at room temperature

Thermal Energy (26 meV)

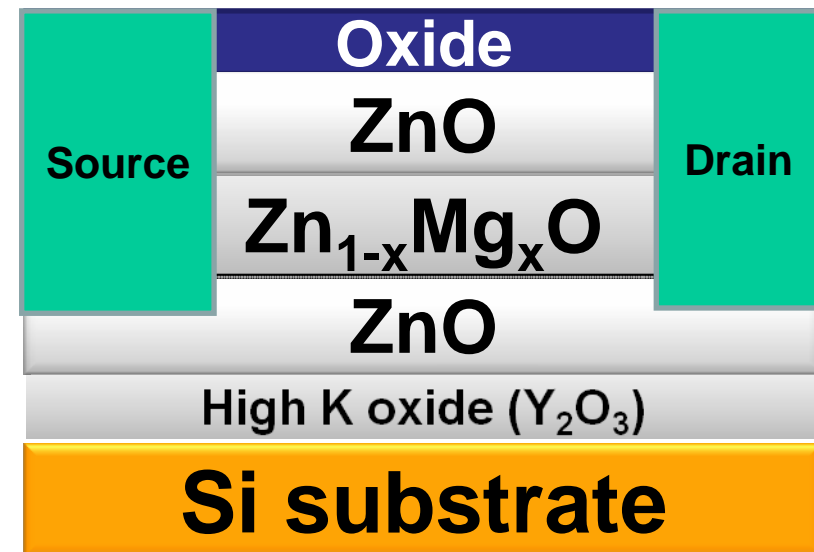


# Why ZnO on Si

## Silicon-based blue/UV LED



## ZnO/ZnMgO FET



or being an buffer for GaN on Si (small lattice mismatch between GaN and ZnO)



# Obstacles for the growth of high quality ZnO on Si

Large lattice mismatch (-15%) between ZnO ( $a = 3.24 \text{ \AA}$ ) and Si ( $a\sqrt{2} = 3.84 \text{ \AA}$ )

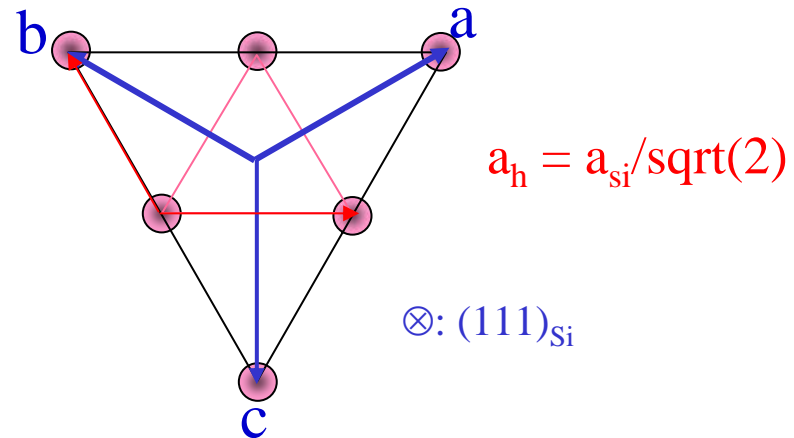
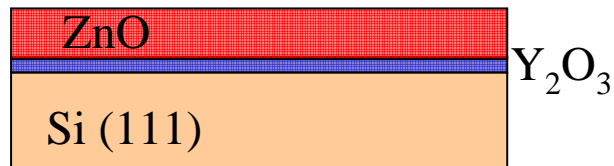
Large thermal mismatch between ZnO ( $\alpha = 4.75 \times 10^{-6} \text{ K}^{-1}$ ) and Si ( $\alpha = 2.56 \times 10^{-6} \text{ K}^{-1}$ )

thermal stress  $\rightarrow$  the formation of cracks

Formation of an amorphous  $\text{SiO}_2$  layer  $\rightarrow$  polycrystalline or textured ZnO layer

(  $\Delta H_{\text{SiO}_2} = -910.7 \text{ kJ/mole}$ ,  $\Delta H_{\text{ZnO}} = -350.5 \text{ kJ/mole}$ ,  $\Delta H_{\text{Y}_2\text{O}_3} = -1905.31 \text{ kJ/mole}$ )

Possible solution: buffer layer



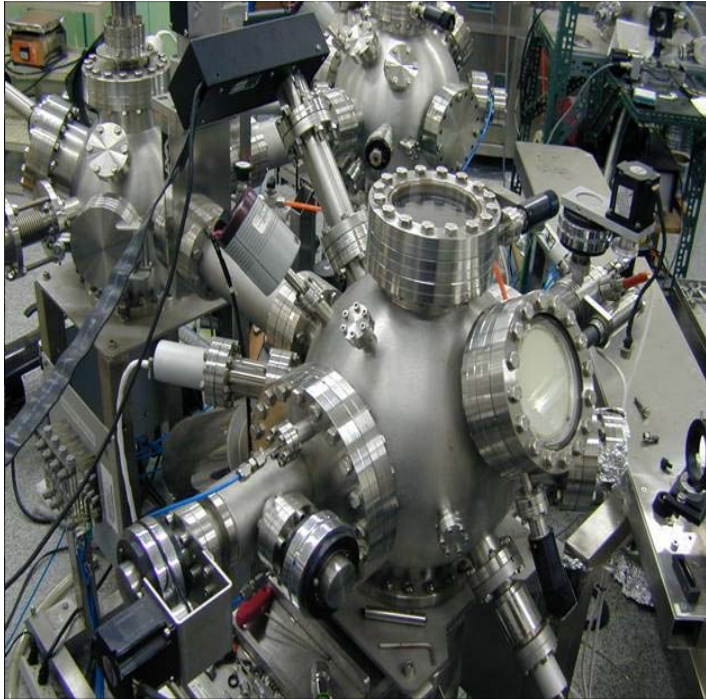
ZnO:  $a = 3.244 \text{ \AA}$ ,  $c = 5.204 \text{ \AA}$

$\text{Y}_2\text{O}_3$ :  $a = 10.606$ ; on (111)  $a_h = 7.50 \text{ \AA}$

Si:  $a = 5.431 \text{ \AA}$ ; on (111)  $a_h = 3.84 \text{ \AA}$



# Sample preparation and characterization



## Growth condition

Pulsed laser deposition (PLD) or laser MBE

KrF pulsed excimer laser: 248 nm, 10 Hz,  $7 \text{ J/cm}^2$

Substrate :  $\text{Y}_2\text{O}_3/\text{Si}(111)$  (grown by MBE);

Target : 5N ZnO target

Growth rate and sample thickness:  $0.27 \text{ \AA/s}$  and  
 $\sim 0.21 \text{ \mu m}$

Chamber basic pressure:  $2.4 \times 10^{-8}$  torr

## Characterization

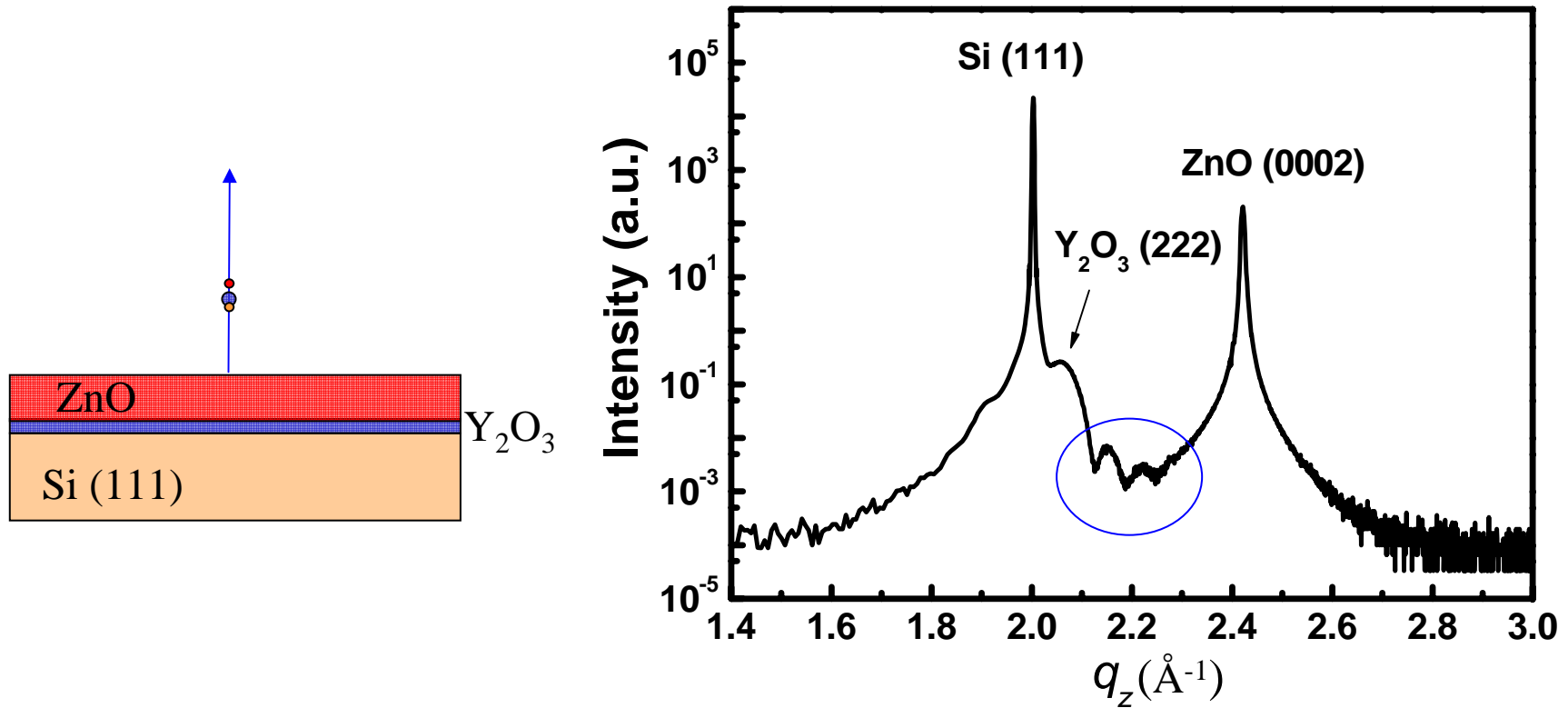
**XRD** : 4-circle diffractometer at BL17A, NSRRC

**TEM** : Philips Tecnai F-20.

**PL** : He–Cd laser (325 nm).



## Radial scan along surface normal



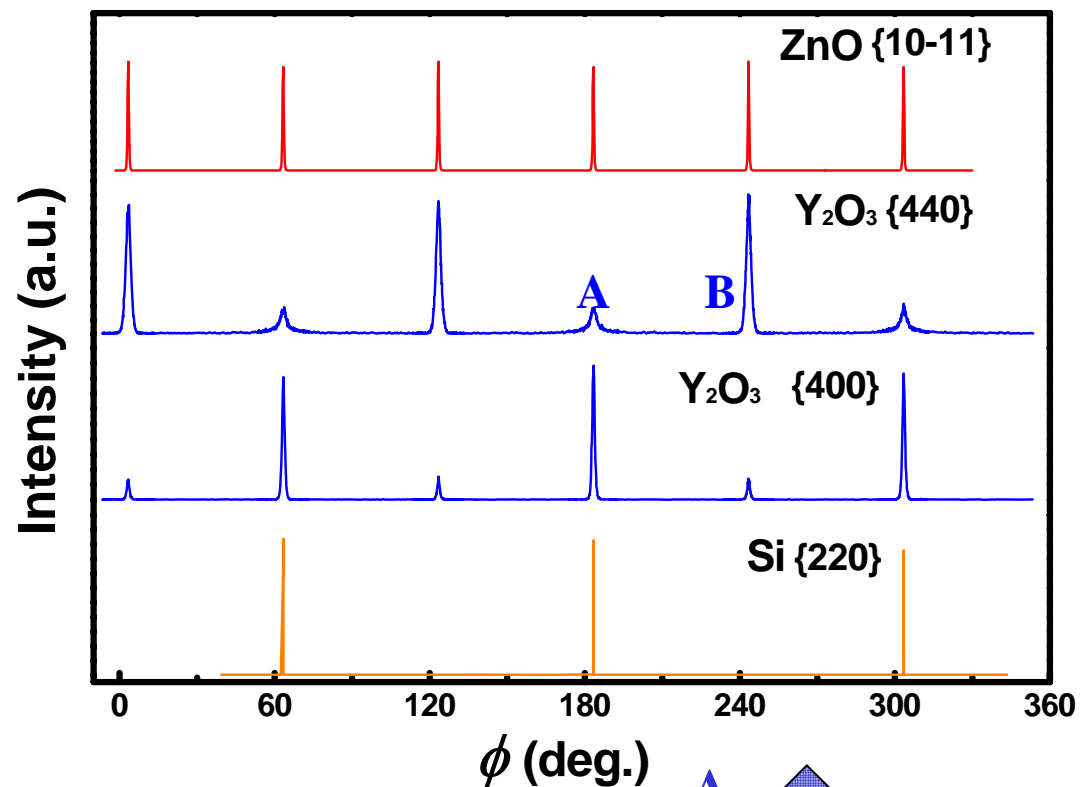
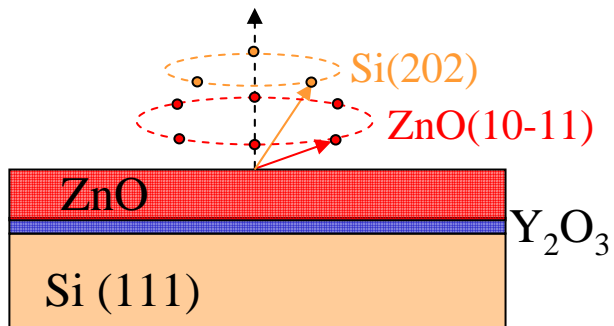
$$(0002)_{\text{ZnO}} \parallel (222)_{\text{Y}_2\text{O}_3} \parallel (111)_{\text{Si}}$$

Thickness fringe: period  $\rightarrow$  Y<sub>2</sub>O<sub>3</sub> layer thickness  $\sim$  9.6 nm

Sharp interface and good crystalline quality



# Azimuthal scans across off-normal reflections



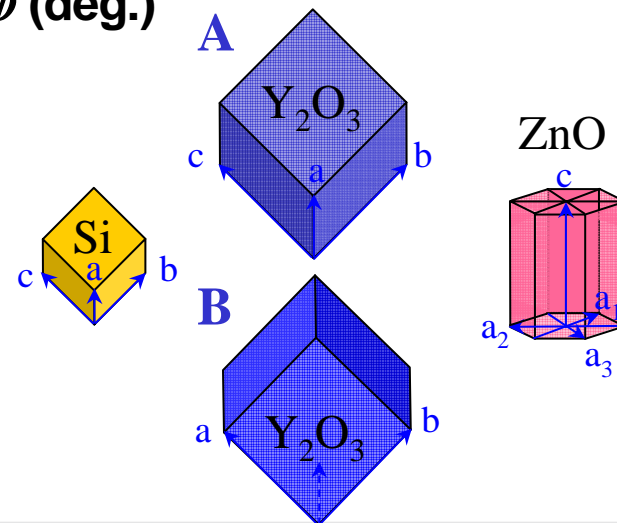
**In-plane orientation**

**A:**  $(10\bar{1}0)_{ZnO} \parallel (11\bar{2})_{Y_2O_3} \parallel (11\bar{2})_{Si}$

$60^\circ$  off

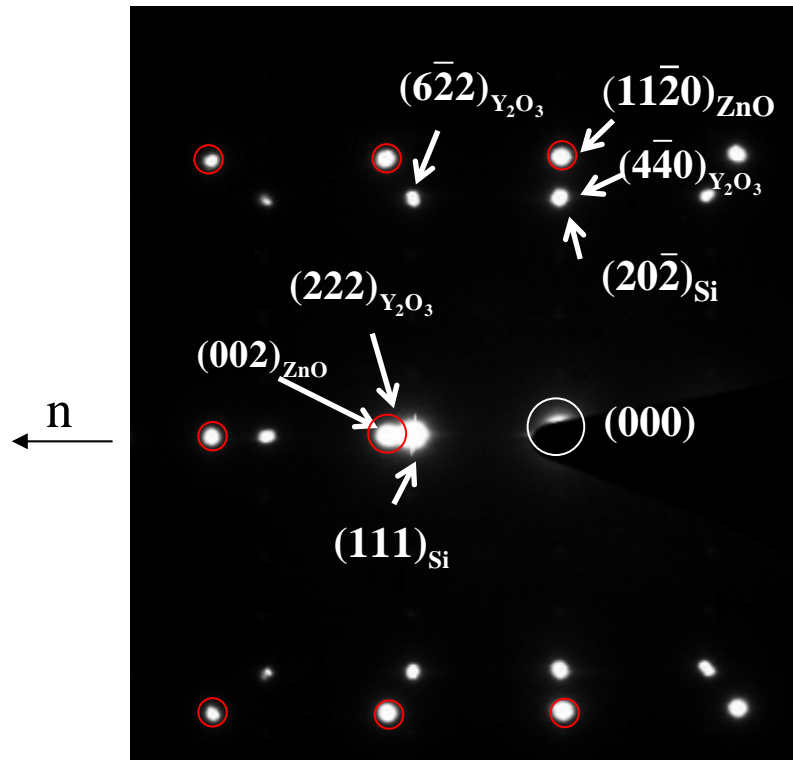
**B:**  $(10\bar{1}0)_{ZnO} \parallel (2\bar{1}\bar{1})_{Y_2O_3} \parallel (11\bar{2})_{Si}$

**dominant**





## Selected Area Electron Diffraction (SAED) Pattern



$$(0001)_{ZnO} \parallel (111)_{Y_2O_3} \parallel (111)_{Si}$$

$$\{11\bar{2}0\}_{ZnO} \parallel \{4\bar{4}0\}_{Y_2O_3} \parallel \{2\bar{2}0\}_{Si}$$

**Lattice mismatch ~ -15.9%**



## Domain Matching Epitaxy (DME)

Strain

$$\varepsilon = \frac{d_f}{d_s} - 1 > \sim 7\%$$

$$(m + \alpha)d_f = (n + \alpha)d_s, \quad m, n : \text{integer}; \alpha < 1$$

Residual strain

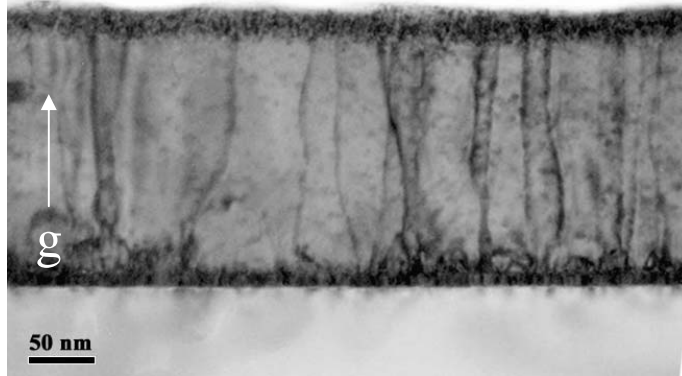
$$\varepsilon_r = \frac{md_f}{nd_s} - 1$$

Residual strain of ZnO grown on Y<sub>2</sub>O<sub>3</sub> reduces down to ~1%

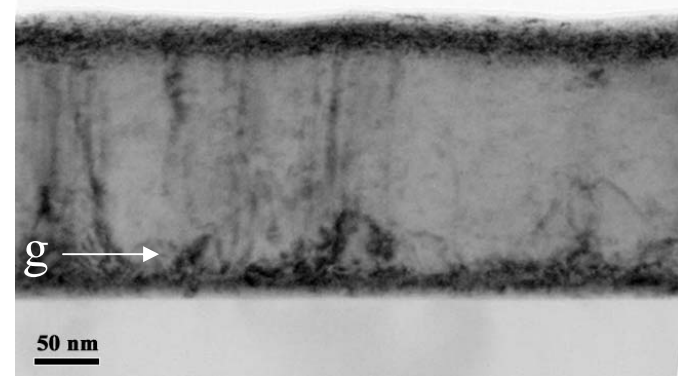


## TEM Contrast Analysis (two-beam condition)

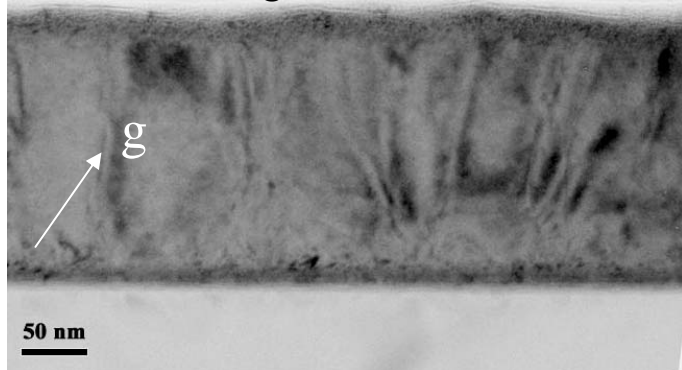
$g=(0002)$  screw + mixed



$g=(11\bar{2}0)$  edge + mixed



$g=(11\bar{2}2)$  edge + screw + mixed



Invisible criterion  $\vec{g} \cdot \vec{b} = 0$

$g$ : diffraction vector

$b$ : dislocation Burgers vector

pure edge  $b_E = 1/3 \cdot \langle 11\bar{2}0 \rangle$

pure screw  $b_C = \langle 0001 \rangle$

Defect structure is predominantly screw and mixed type TDs. Near the interface, there are high density of misfit dislocations.



## Summary

- High quality ZnO epitaxial films have been successfully grown by pulsed-laser deposition on Si (111) substrates with a thin Y<sub>2</sub>O<sub>3</sub> buffer layer.
- Two (111) oriented domains with 60° in-plane rotation coexist in the Y<sub>2</sub>O<sub>3</sub> buffer layer. The in-plane epitaxial relationship between the wurtzite ZnO, cubic Y<sub>2</sub>O<sub>3</sub> and cubic Si follows .
- The growth of ZnO on Y<sub>2</sub>O<sub>3</sub> can be well described by domain matching epitaxy.
- The photoluminescence spectra of ZnO epi-films exhibit superior optical properties at room temperature even for films of thickness as thin as 0.21 μm.

