



JIAN's LABORATORY, NCHU, Taichung, Taiwan (2003)  
Moved to NCTU, Hsinchu, Taiwan (2004)

Magnetic Properties of  
Nanowires and  
Nanoparticles  
PbSe Nanocrystals,  
ZnCoO Nanowires

1. J. Chem. Phys. 124, 064711 (2006).
2. J. Appl. Phys. 99, 08N708 (2006).
3. Phys. Rev. B 73, 233308 (2006).
4. Nanotechnology 17, 5511 (2006).
5. J. Nanosci. Nanotechnol. 8, 202 (2008).
6. New J. Phys. 10, 033017 (2008).
7. J. Phys. Chem. C. 112, 9168 (2008).

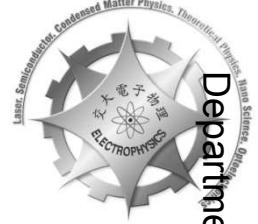
Electrical Properties of  
Nanowire Based  
Nanoelectronics  
ZnO, InP, GaP, RuO<sub>2</sub>  
Nanowires

1. Appl. Phys. Lett. 90, 013105 (2007).
2. Appl. Phys. Lett. 90, 223117 (2007).
3. **Nano Lett. 8, 3146 (2008).**
4. Chem.-Eur. J. 15, 4546 (2009).
5. Adv. Funct. Mater. submitted (2009).

Electronic Structures of  
Nanocrystals by Using  
LTSTM  
PbSe Nanocrystals, Au  
Nanoparticles

1. J. Phys. Chem. C (ASAP, 2009).  
**Cover Art of Issue 18**
2. Nanotechnology accepted (2009).





Department of Electrophysics, National Chiao Tung University, Hsinchu, Taiwan

# Size Effects in Collective Transport at Coupled PbSe Quantum Dot Arrays

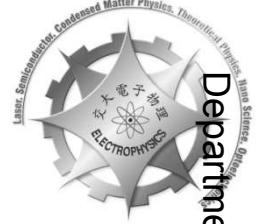
Yi-Ching Ou<sup>1</sup>, Jiun-Ji Wu<sup>2</sup>, Jiye Fang<sup>3</sup>, and Wen-Bin Jian<sup>2</sup>

<sup>1</sup>Institute of Physics, National Chiao Tung University, Hsinchu 30010 Taiwan

<sup>2</sup>Department of Electrophysics, National Chiao Tung University, Hsinchu 30010 Taiwan

<sup>3</sup>Department of Chemistry, State University of New York at Binghamton

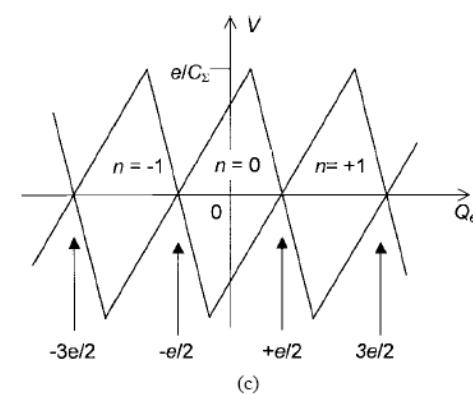
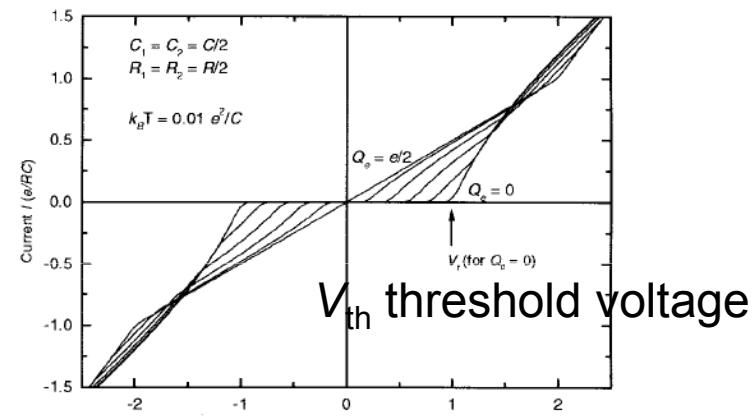
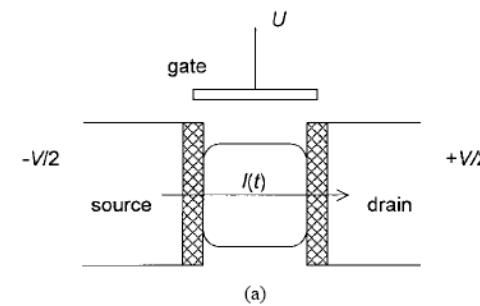
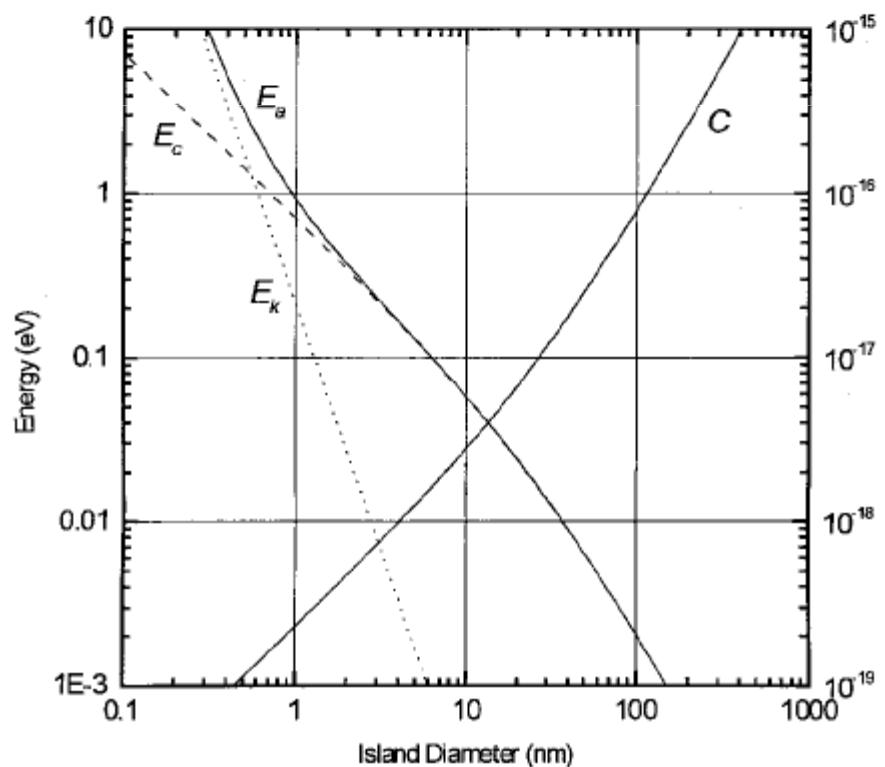
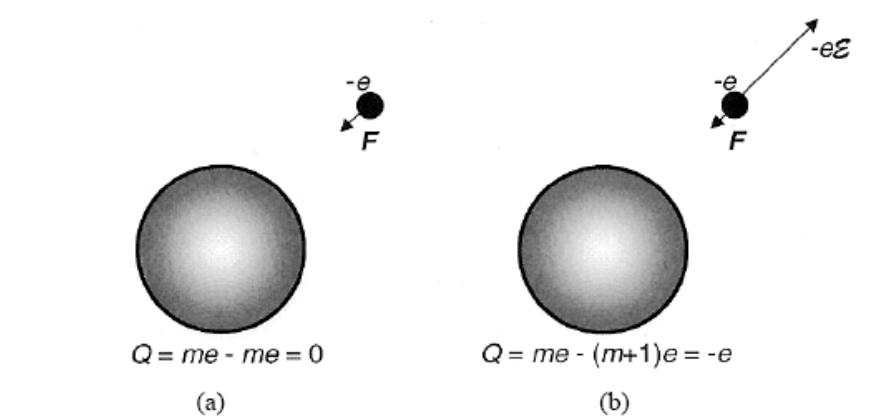
Binghamton, NY 13902-6000



# OUTLINE

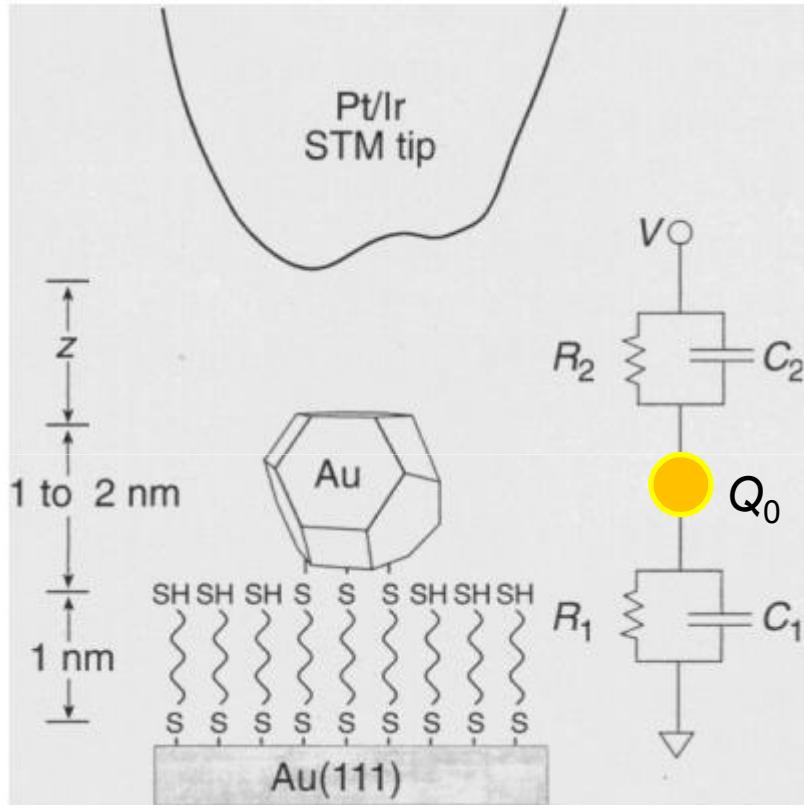
1. Introduction to Phenomena of Colloidal Quantum Dot
  - a) Single Electron Tunneling (orthodox theory)
  - b) Memory Effects
  - c) Collective Transport (Middleton & Wingreen model)
  - d) Artificial Atom States
2. Experiment
3. Results and Discussions
  - a) The Array Is Regarded As An Island
  - b) The Array Is Regarded As Coupled Quantum Dots
4. Conclusion

## 1. Introduction – a) single electron tunneling

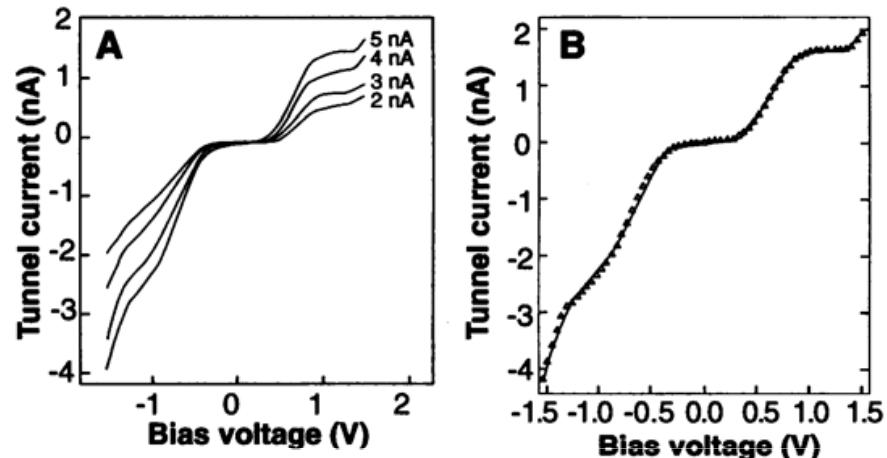


K. K. Likharev, Proc. IEEE 1999, 87, 606.

## 1. Introduction – a) single electron tunneling



Double-ended aryl dithiol [ $\alpha,\alpha'$ -xylyldithiol (XYL) and 4,4'-biphenyldithiol] formed SAM.  
Semiclassical model (orthodox theory) of Coulomb blockade.



Coulomb staircase at **room temperature** in a self-assembled molecular (SAM) nanostructure by using STM in a ultra-high vacuum.

$$C_2 = 0.13 \text{ aF}, C_1 = 0.08 \text{ aF}$$

$$R_2 = V/I, R_1 = 1.8 \text{ M}\Omega$$

$$Q_0 = -0.2 \text{ e} \text{ (polarization charge)}$$

## 1. Introduction – b) memory effects

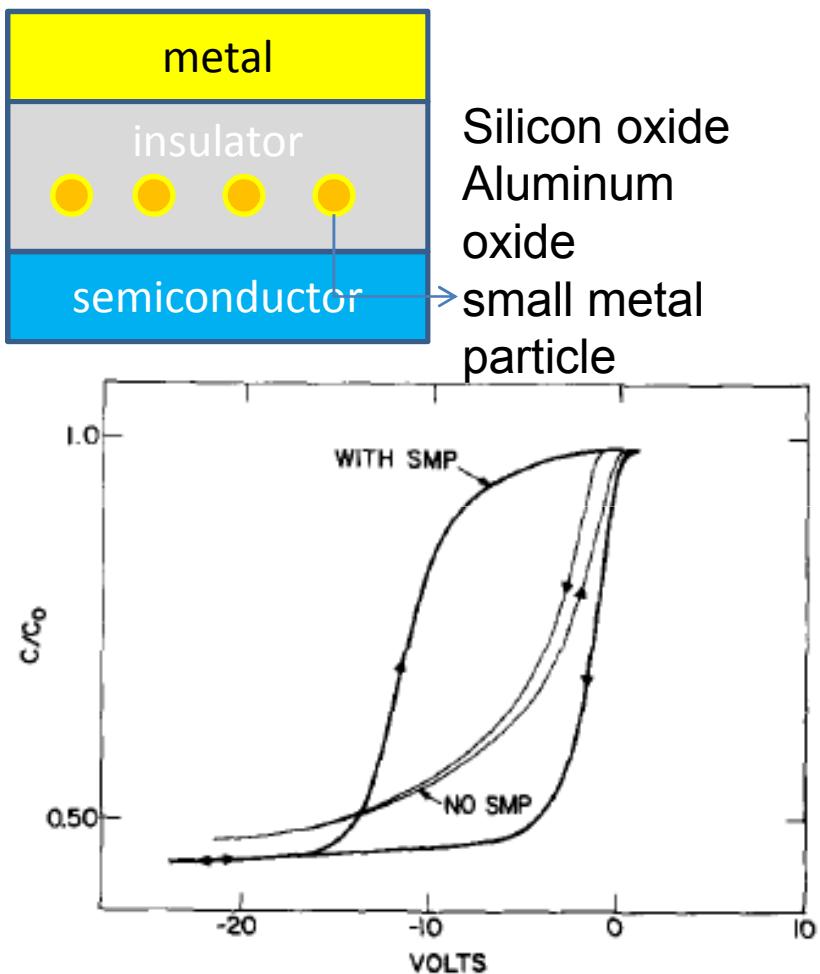
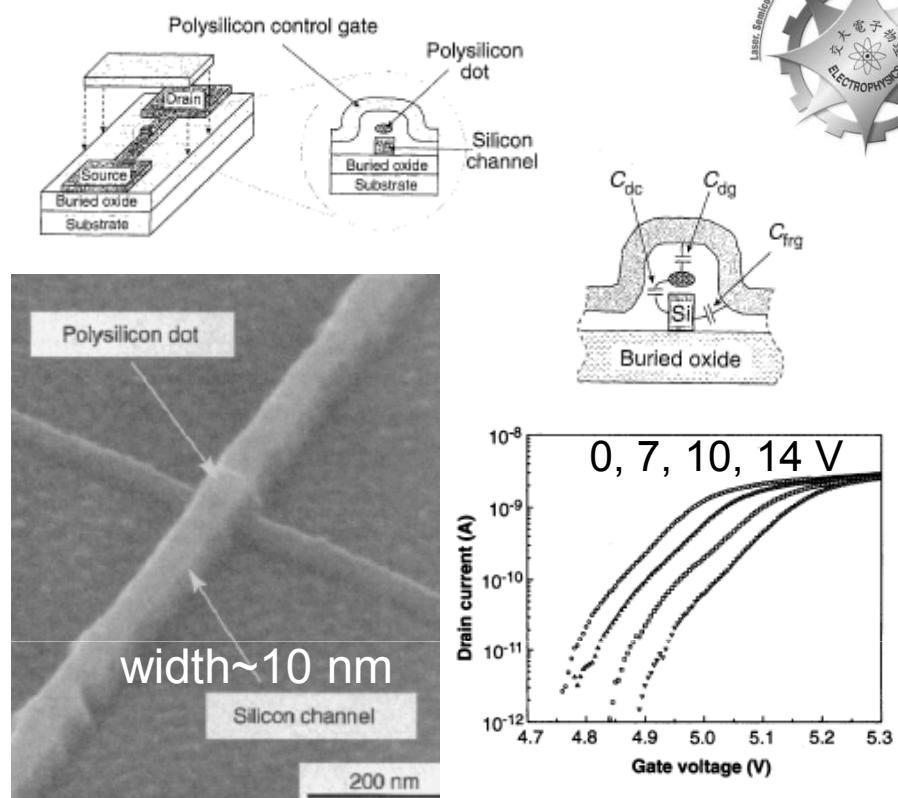


FIG. 1. Capacitance-voltage characteristics for similar samples with and without SMP.

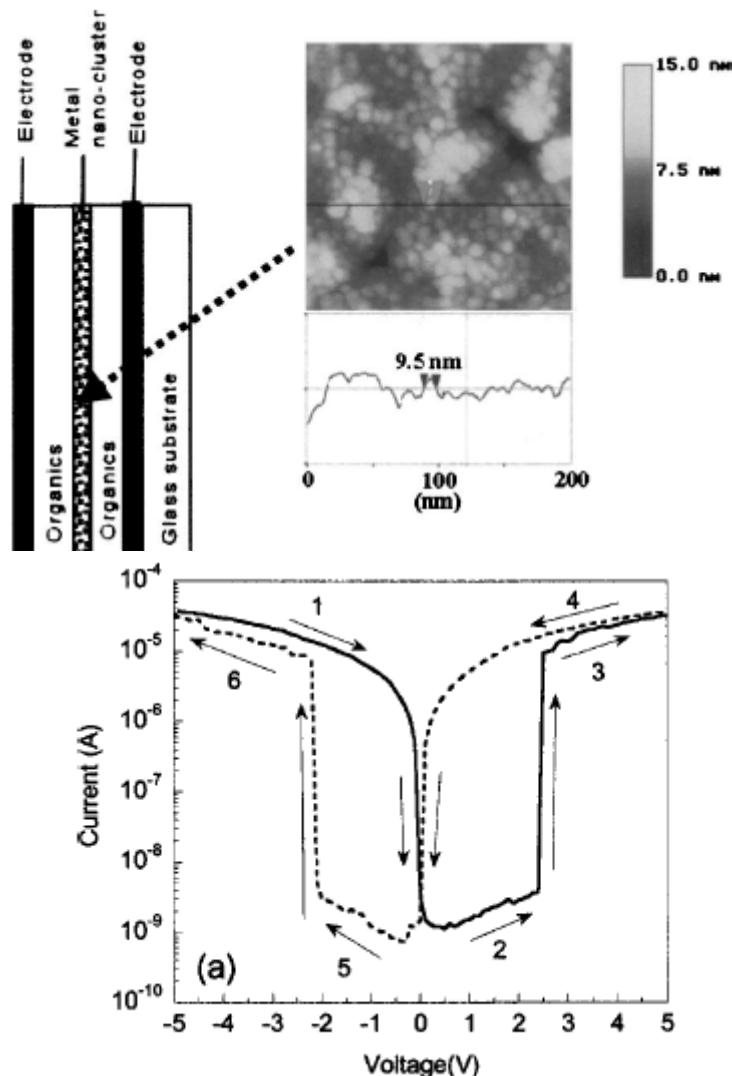
R. B. Laibowitz and P. J. Stiles, *Appl. Phys. Lett.* **1971**, *18*, 267.



The I-V changes after the control gate is pulsed by charging voltage ranging from 0 to 14 V.

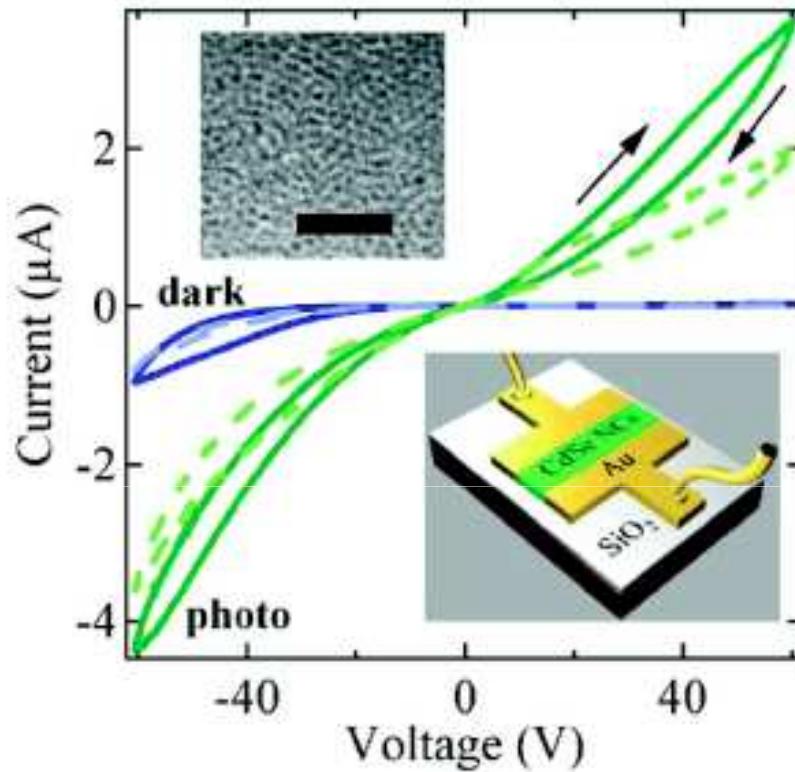
L. Guo, E. Leobandung, and S. Y. Chou, *Science* **1977**, *275*, 649.

## 1. Introduction – b) memory effects



Nonvolatile electrical bistability.

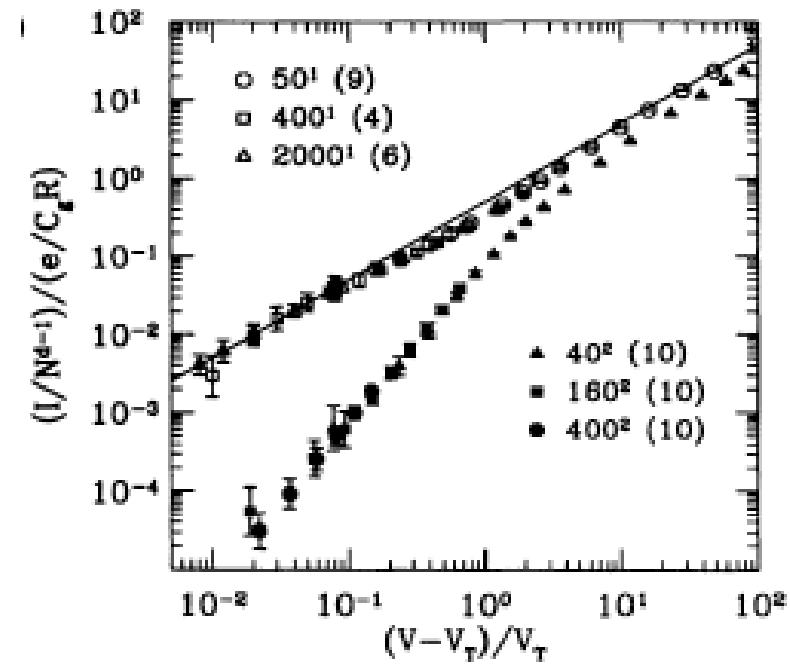
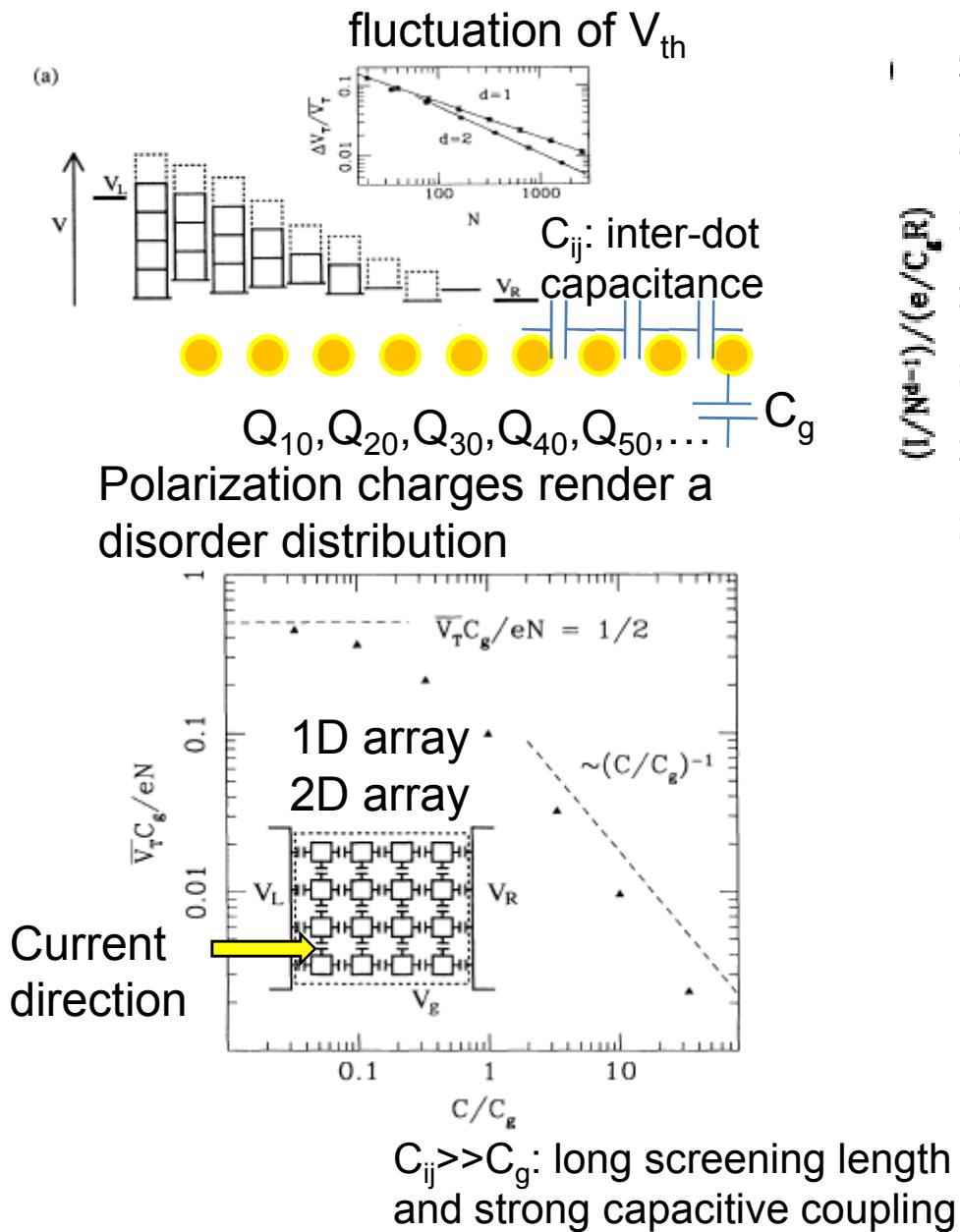
L. Ma, S. Pyo, J. Ouyang, Q. Xu, and Y. Yang, *Appl. Phys. Lett.* **2003**, *82*, 1419.



CdSe nanocrystal quantum-dot memory.  
NCs are photoexcited with a 532 nm wavelength (green) diode laser operating at  $1 \text{ mW/cm}^2$ .

M. D. Fischbein and M. Drndic, *Appl. Phys. Lett.* **2005**, *86*, 193106.

## 1. Introduction – c) collective transport

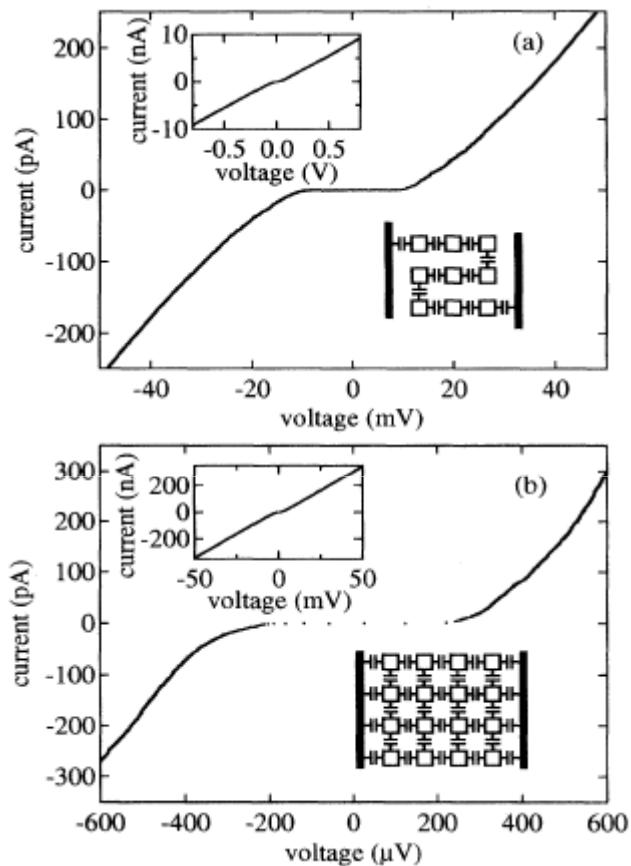


$$I \propto \left( \frac{V}{V_{th}} - 1 \right)^{\zeta}$$

1D:  $\zeta=1$   
2D:  $\zeta=5/3$  or 2...

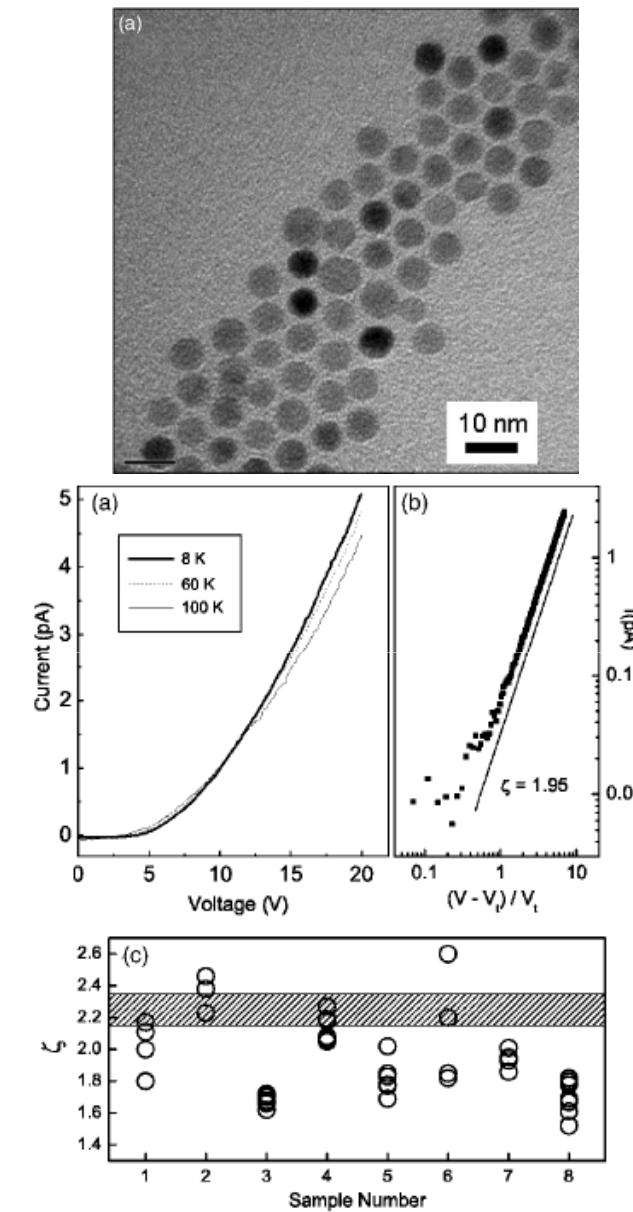
A. A. Middleton and N. S. Wingreen,  
*Phys. Rev. Lett.* **1993**, *71*, 3198.

## 1. Introduction – c) collective transport



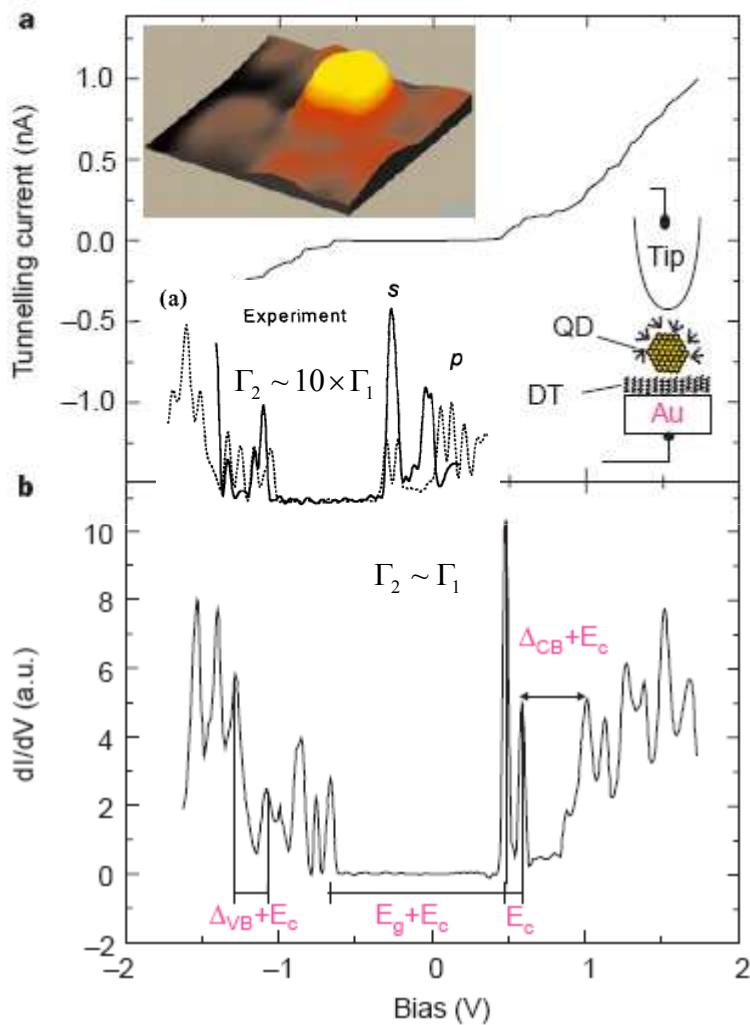
IV of 1- and 2D arrays of small metal islands.

A. J. Rimberg, T. R. Ho, and J. Clarke,  
*Phys. Rev. Lett.* **1995**, 74, 4714.



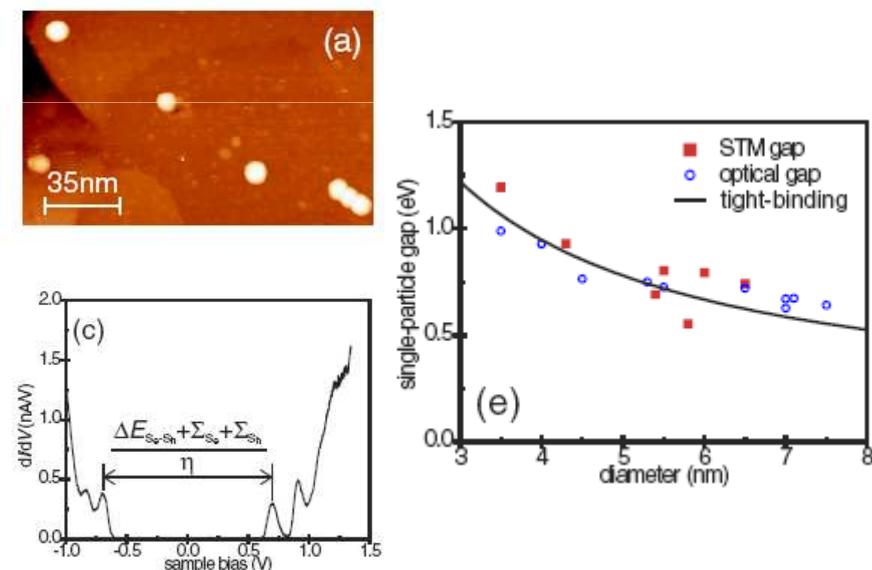
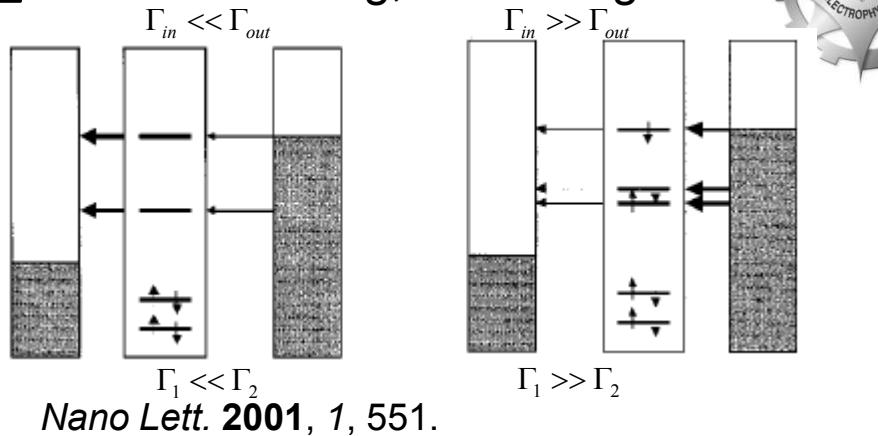
K. Elteto, X. M. Lin, and H. M. Jaeger,  
*Phys. Rev. B* **2005**, 71, 205412.

## 1. Introduction – d) artificial atom states



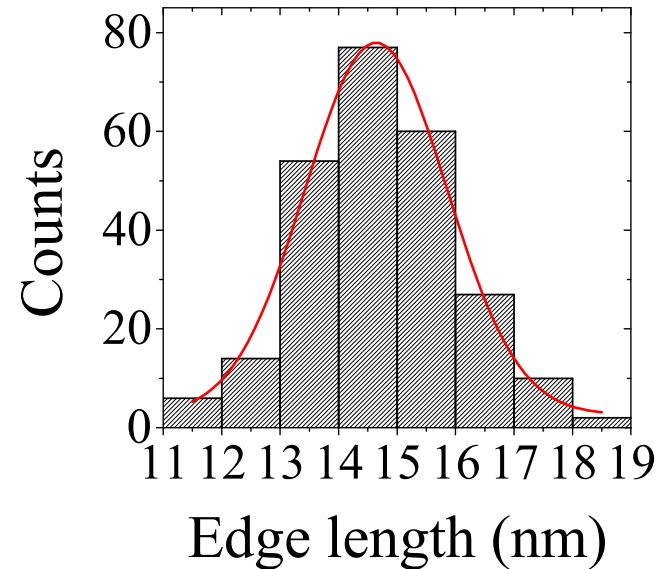
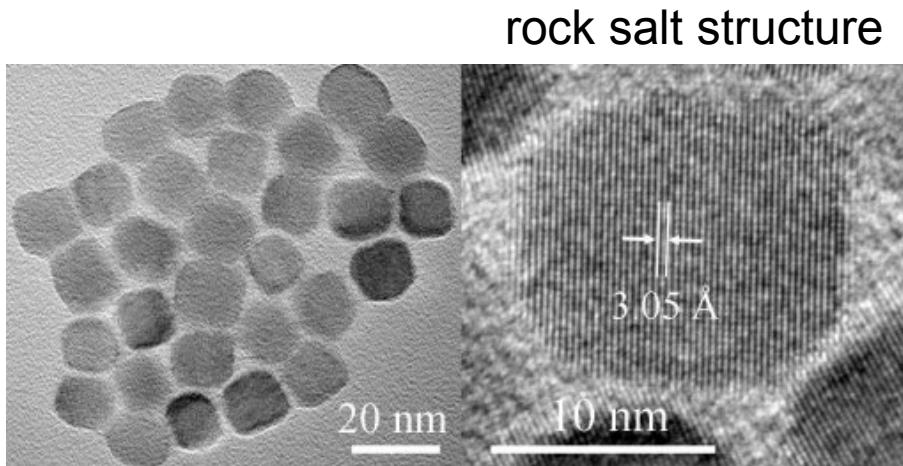
U. Banin, Y. Cao, D. Katz, and O. Millo, *Nature* **1999**, *400*, 542.

## shell tunneling, shell filling



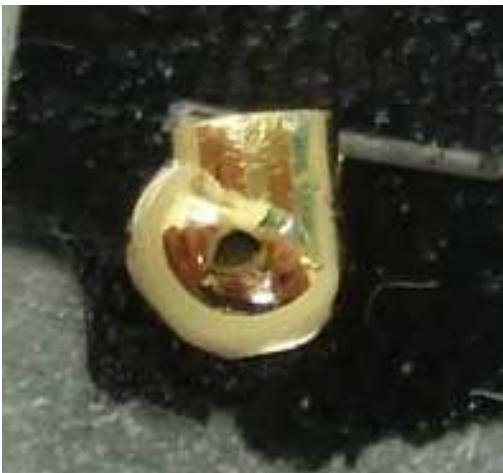
P. Liljeroth, P. A. Z. van Emmichoven, S. G. Hickey, H. Weller, B. Grandidier, G. Allan, and D. Vanmaekelbergh, *Phys. Rev. Lett.* **2005**, *95*, 086801.

## 2. Experiment

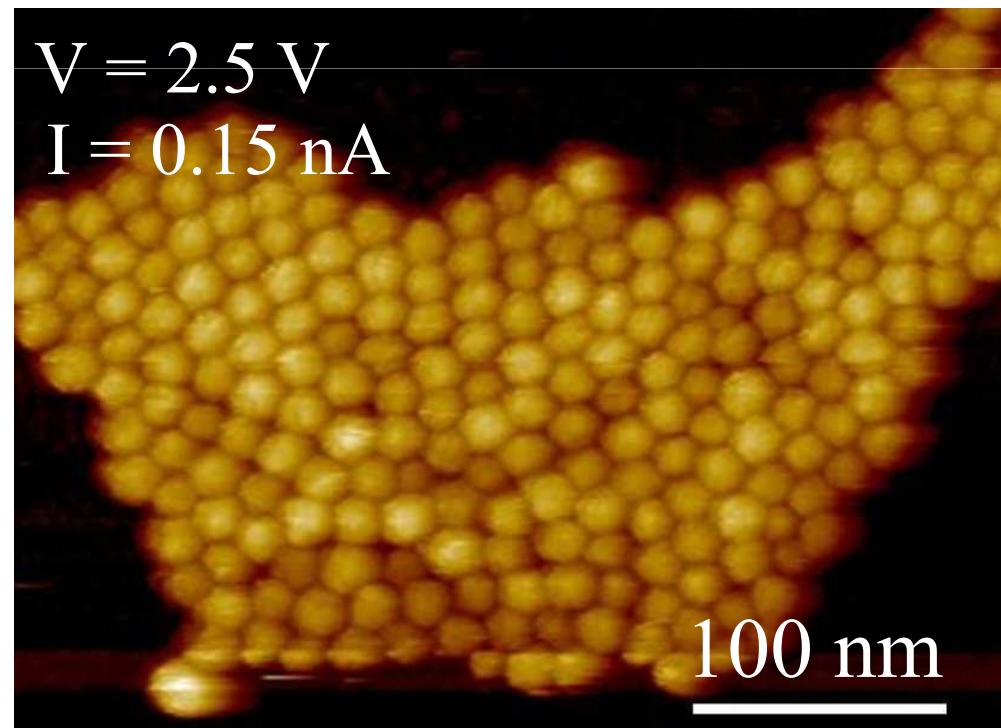
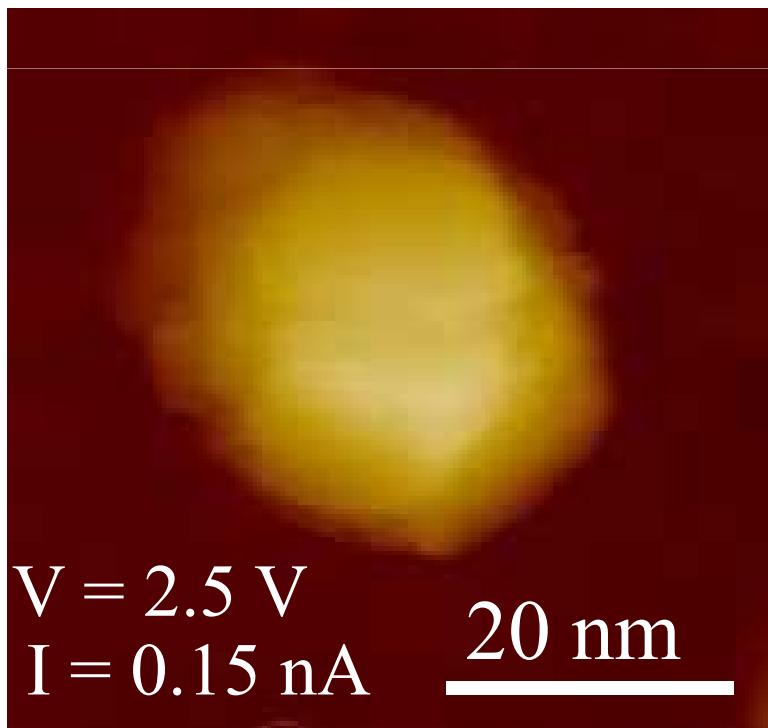


1. PbSe quantum dots (QDs) were prepared by using a high-temperature organic solution approach.
2. The resultant PbSe QDs were identified using various characterizations including X-ray diffraction study, inductively coupled plasma analysis, transmission electron microscope (TEM, JEOL JEM-2010F) imaging and energy dispersive spectroscopy evaluation.
3. The average diameter and standard deviation of the QDs were estimated to be about **14.6** and 2.4 nm, respectively.

## 2. Experiment

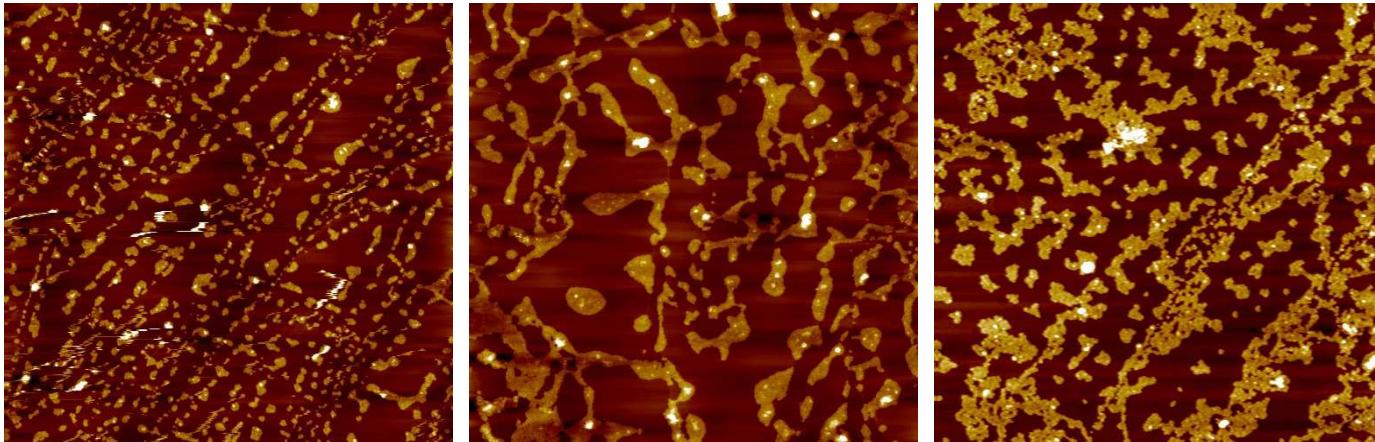


1. The QDs were dispersed in toluene again to make a dilute QD solution.
2. Several drops of the solution were put on atomically flat Au(111) surfaces on the ball prepared by melting a 2-mm wire in a gas flame.
3. The sample was loaded in a **Omicron LTSTM** chamber in an ultra-high vacuum of  $1 \times 10^{-10}$  torr and it was heated up to 100-150°C for more than 10 h.

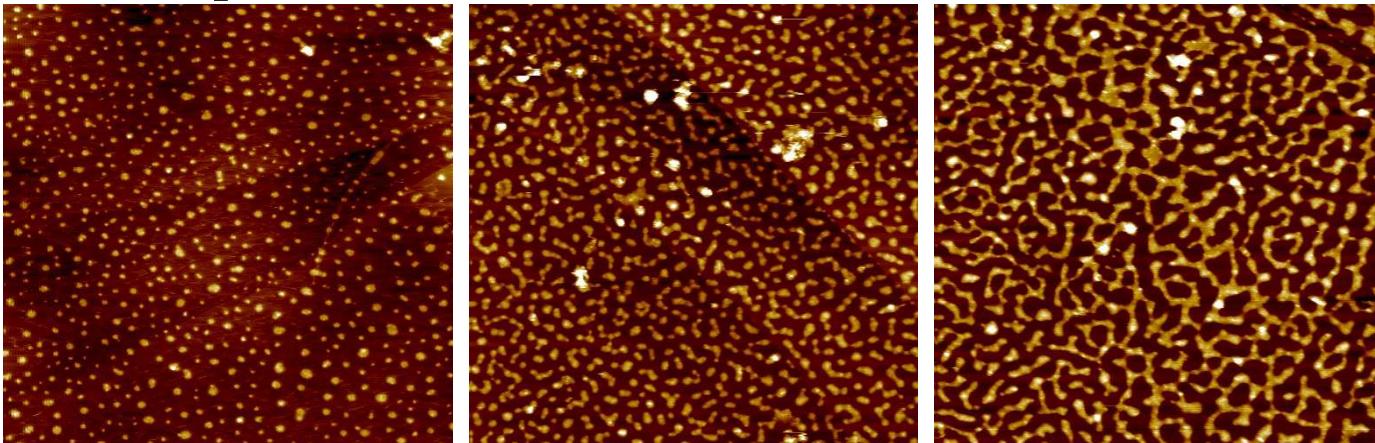


## 2. Experiment

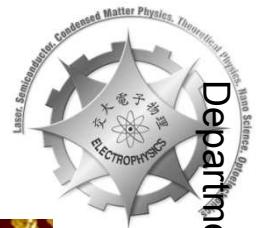
High temperature



Low temperature



1  $\mu\text{m}$

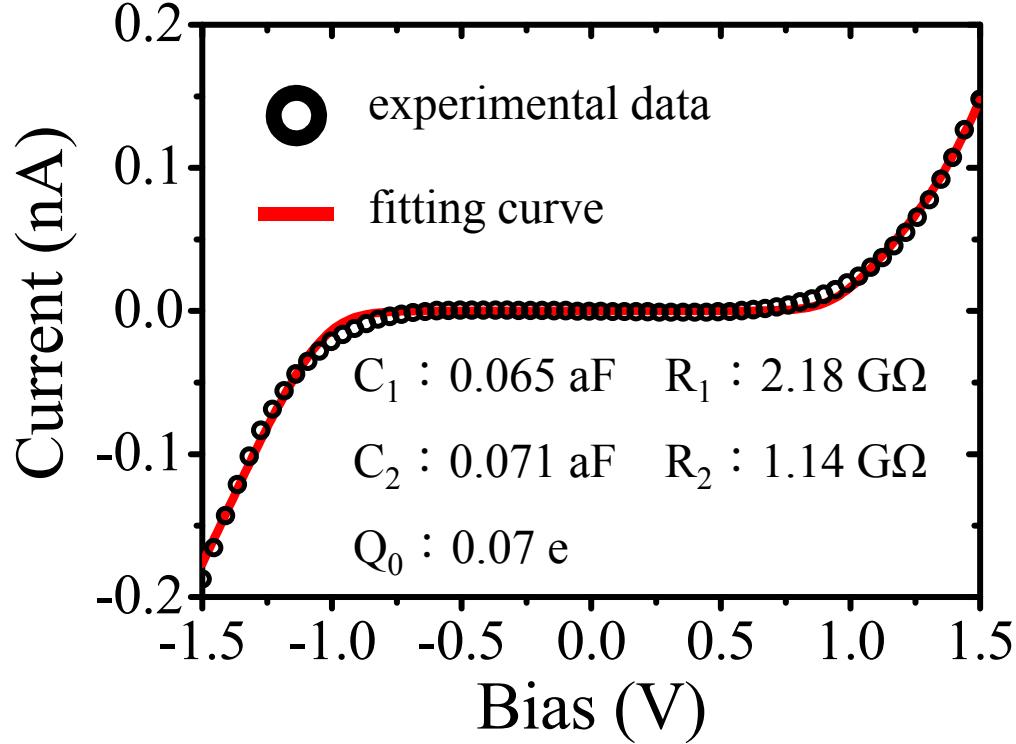
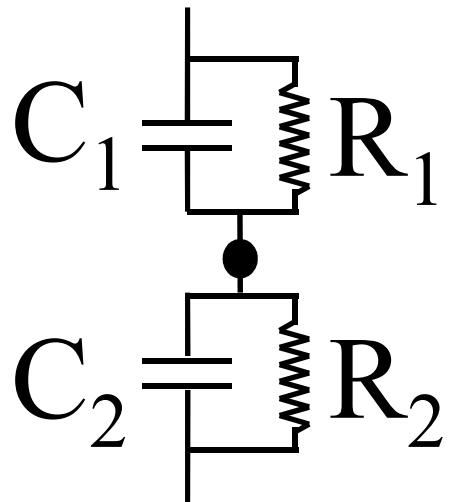
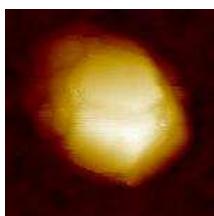
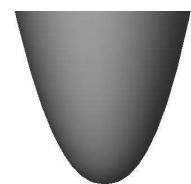


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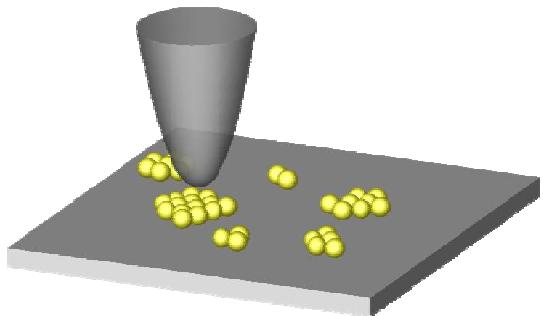
### 3. Results and discussions – single quantum dot

1. An STM tip is schematically drawn above the single QD to illustrate the corresponding tip-to-dot and the dot-to-substrate resistances ( $R_1$  and  $R_2$ ) and capacitances ( $C_1$  and  $C_2$ ) in circuit diagram of the model.
2. The experimental data can be fitted with the orthodox theory at **300 K** to get  $C_1$ ,  $C_2$ ,  $R_1$ ,  $R_2$ , and the polarization charge  $Q_0$ .

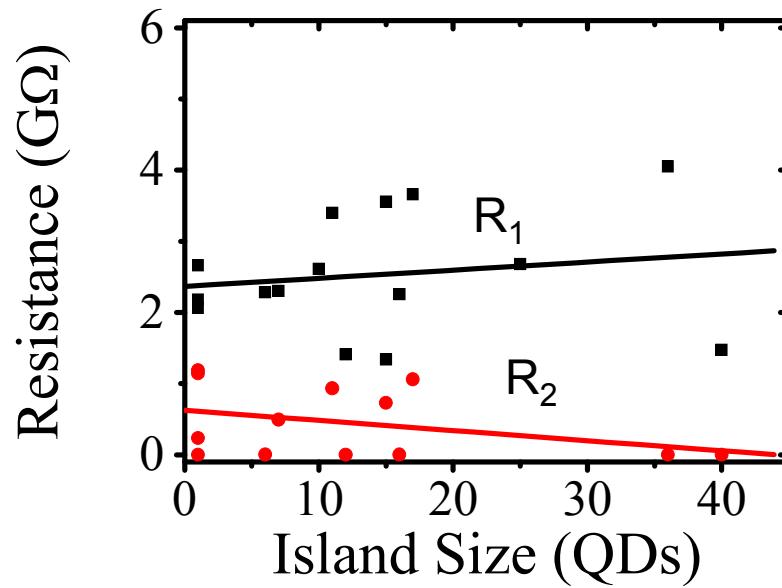
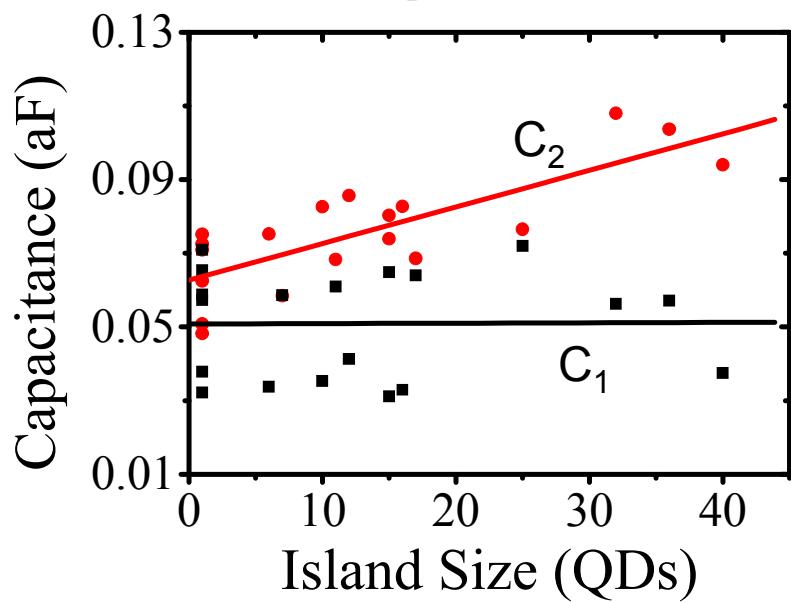
$$E_c = \frac{e^2}{2(C_1 + C_2)} \\ = 0.588 \text{ eV} > 25 \text{ meV}(300k_B)$$



### 3. Results and discussions – the array is regarded as an island.

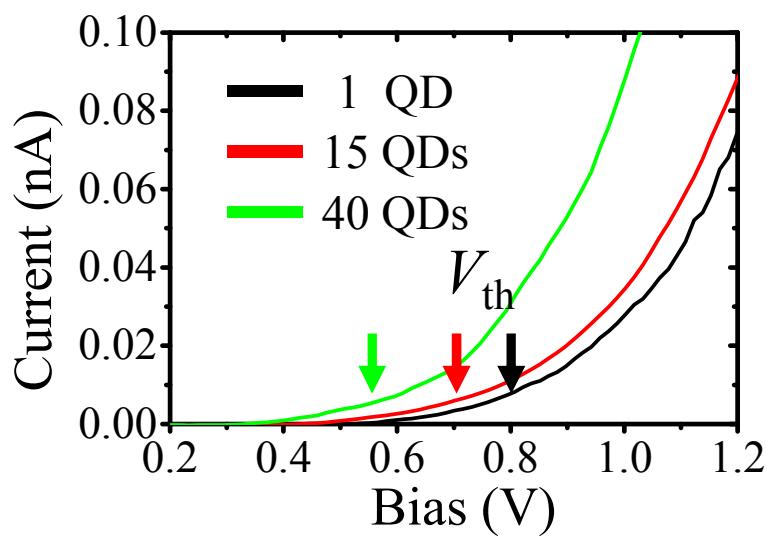
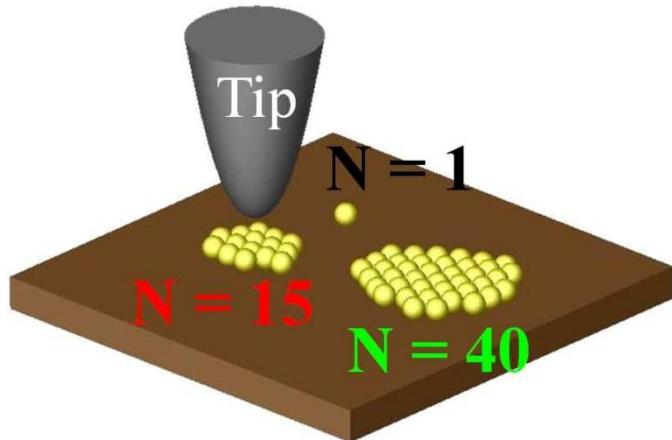


1. Hundreds of CITS image points are averaged to get a single characteristic  $I$ - $V$  curve for analysis to obtain  $C_1$ ,  $C_2$ ,  $R_1$ , and  $R_2$  for a specified QD array.
2. The area of the array expands about 40 times but  $C_2$  only duplicates its values.
3. The small increase in  $C_2$  implies that the QD array cannot be simply regarded as an island.

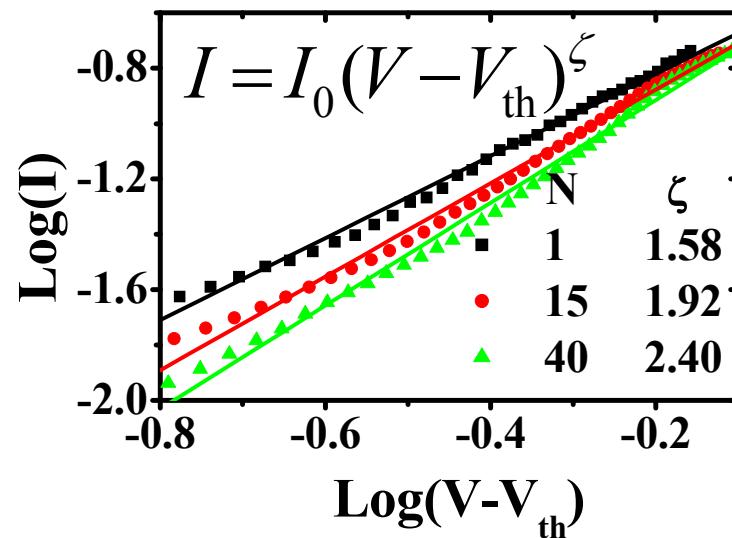


### 3. Results and discussions – the array is regarded as coupled quantum dots

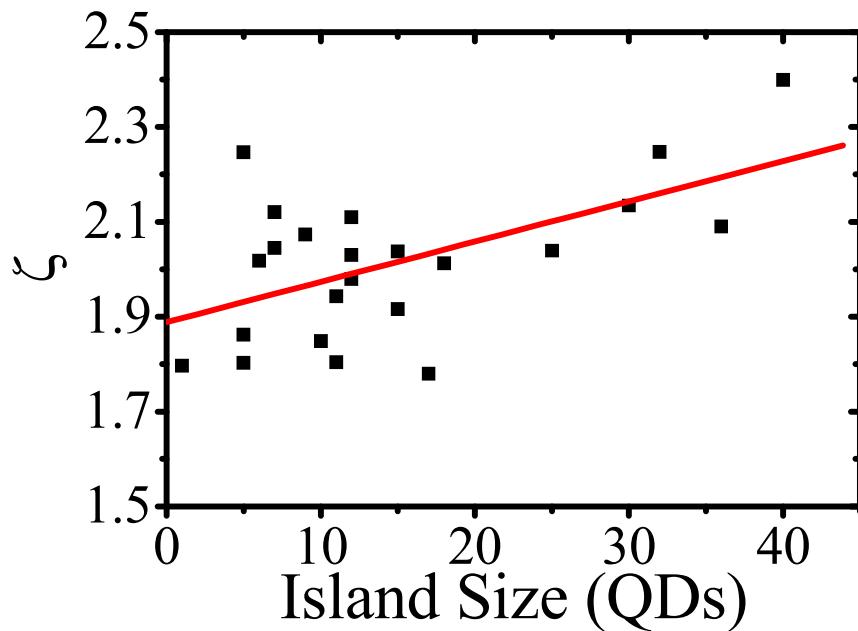
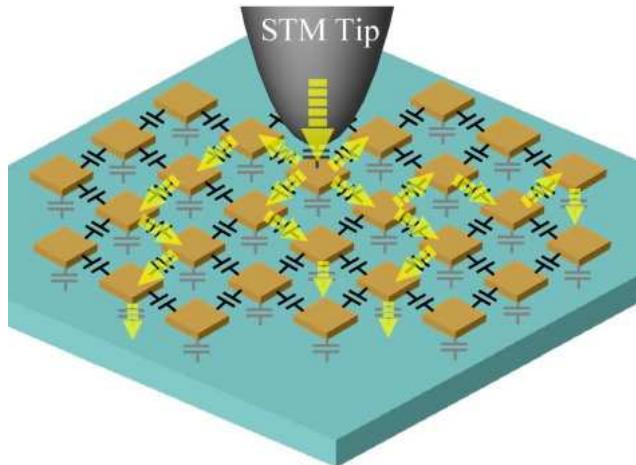
Use collective transport & MW model to analyze IV data.



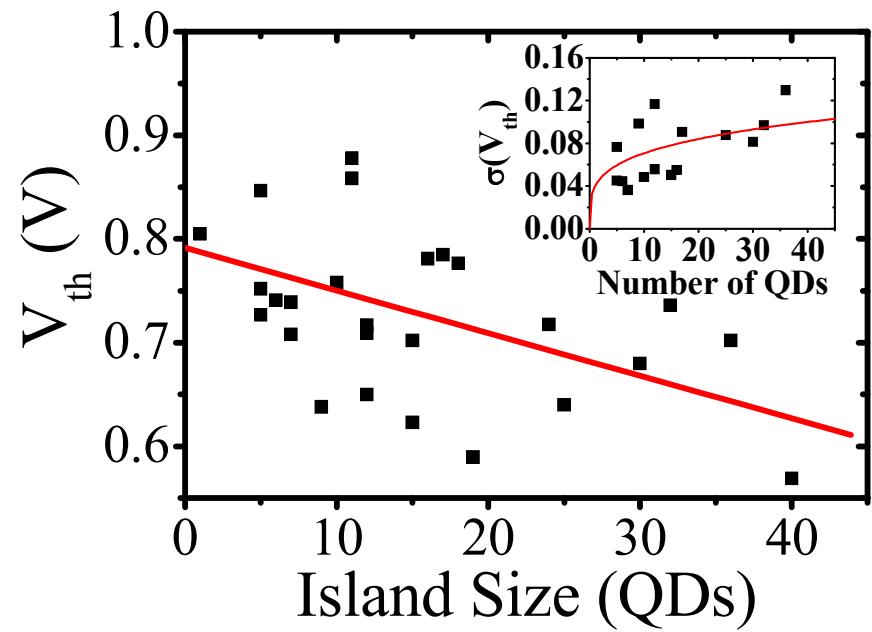
1. The averaged threshold current of ~5.5 pA of the single QD is used to evaluate the  $V_{th}$ 's of all the other QD arrays.
2. The IV curve show power law behavior  $I(V-V_{th})^\zeta$  exhibiting linear dependence in a logarithmic scale.



### 3. Results and discussions

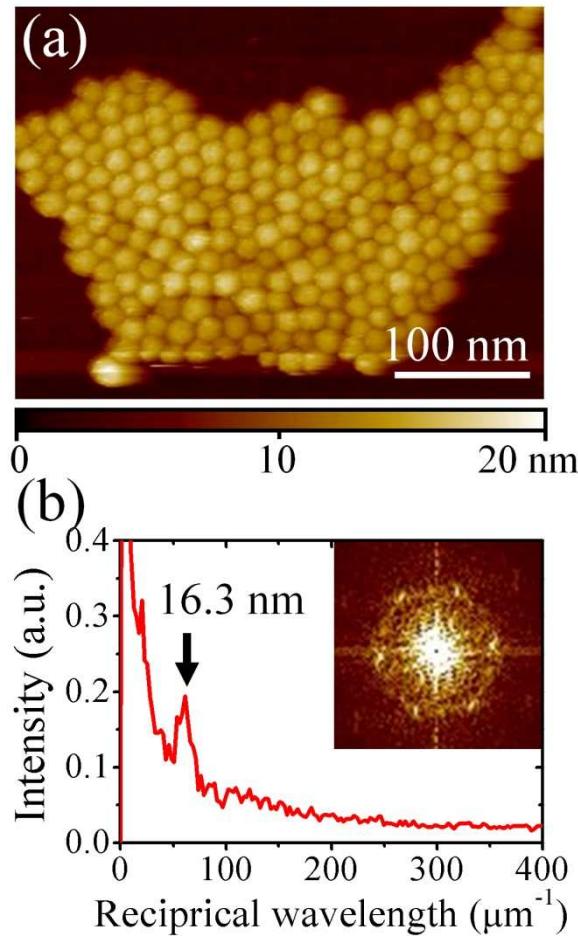
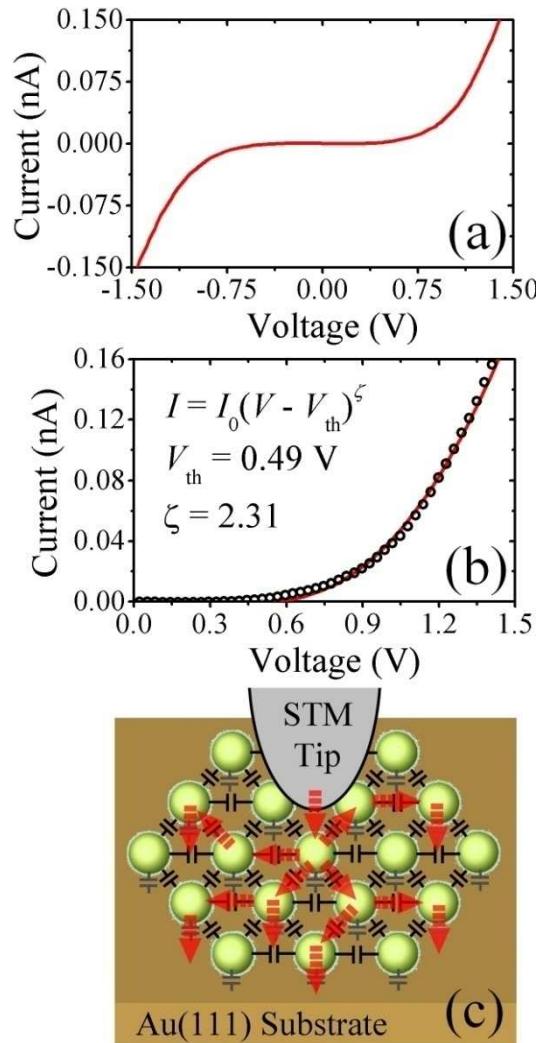


1. The scaling exponent  $\zeta$  gradually increases with an enlarging size of the PbSe QD array.
2. The threshold voltage  $V_{\text{th}}$  gradually diminishes from 0.8 to 0.6 V as the number of QDs increases from 1 to 40.
3. The standard deviation  $\sigma(V_{\text{th}})$  of the fluctuation in  $V_{\text{th}}$  increases as  $N^{1/4}$ , where  $N$  is the number of QDs in the array.



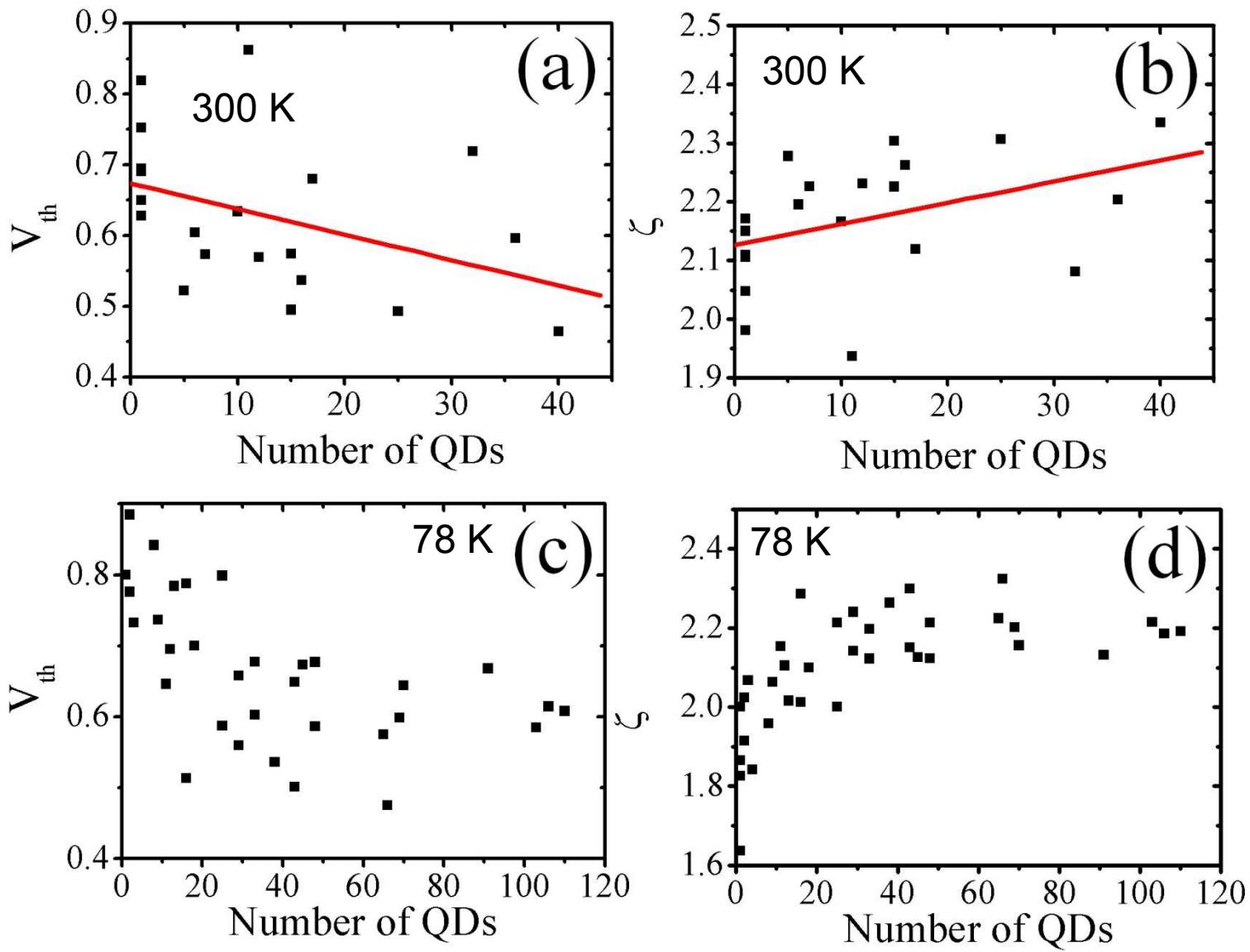
### 3. Results and discussions

Analyzed by another method, nonlinear least square fitting.



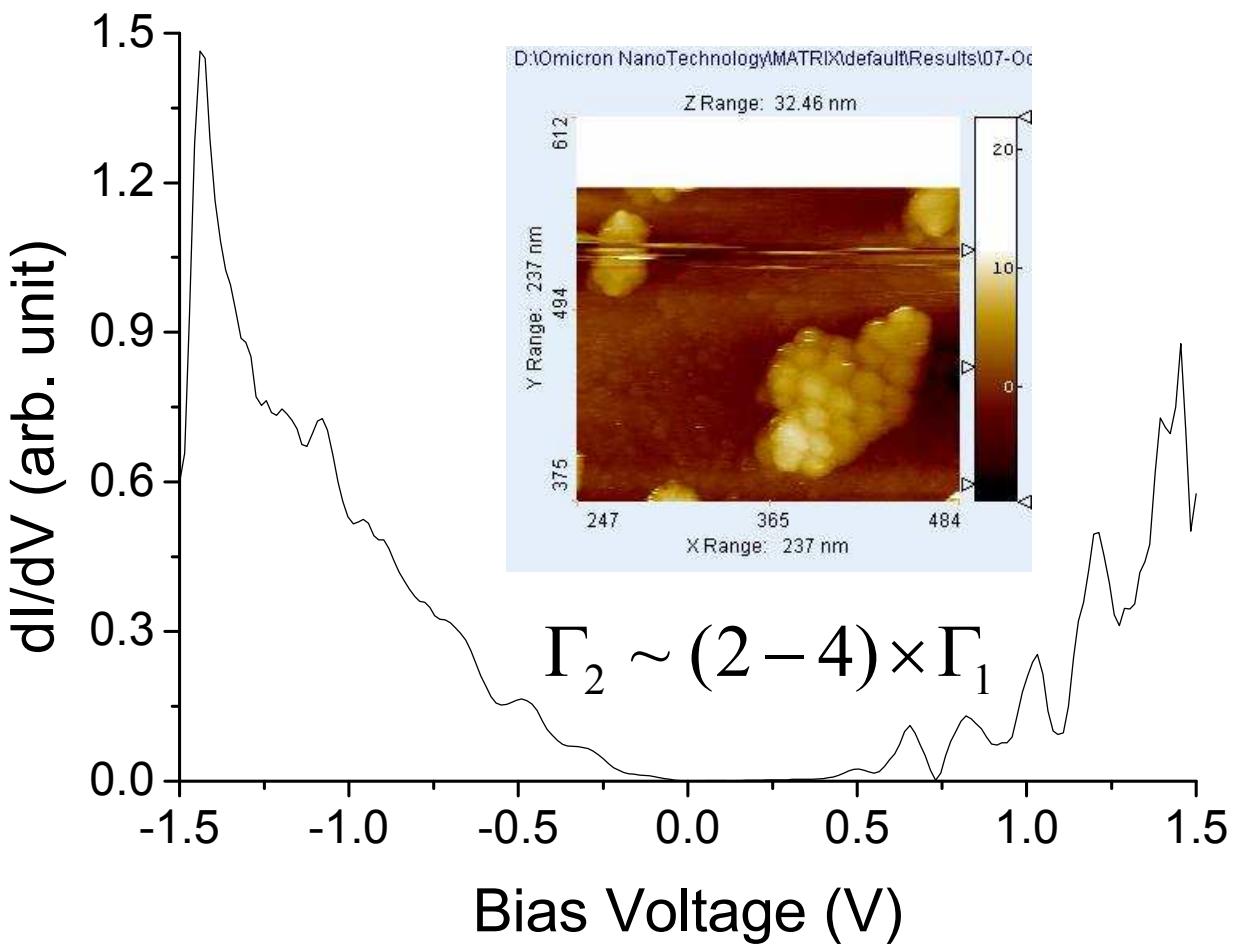
The average diameter of PbSe QDs is 14.6 nm, so the separation distance between two PbSe QDs is evaluated to be 1.7 nm. Using a parallel plate capacitor model with the interdot spacing 1.7 nm and taking the QDs as cubic with one side 14.6 nm, we can judge the interdot capacitance to be 2.26 aF. The interdot capacitance gives a Coulomb charging energy of 35.4 meV.

### 3. Results and discussions



### 3. Results and discussions

The tunneling spectra show artificial-atom states at ~5 K.





## 4. Conclusions

1. We have deposited PbSe QD arrays with different numbers of QDs on the flat Au(111) surfaces and have obtained tunneling spectra on individual QD arrays.
2. The characteristic IV behaviors of the QD arrays have been obtained and analyzed in accordance with the orthodox theory to extract the shunt capacitances and resistances.
3. The array-to-substrate capacitance increase steadily but not rise as fast as the area of the array.
4. The QD arrays can neither be simply treated as an island nor be regarded as independent QDs.
5. We find that, after translation on the voltage scale with the threshold voltage  $V_{th}$ , the  $I/(V-V_{th})$  curves of the QD arrays follow a scaling law with a scaling exponent  $\zeta$ .
6. The scaling exponent  $\zeta$ , the threshold voltage  $V_{th}$ , and the fluctuation in threshold voltages  $\sigma(V_{th})$  strongly depends on the number (size) of the PbSe QD arrays.



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# Thank You for Your Attention