

Probing triple Higgs couplings at colliders
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NTHU-07/05/2009

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Outline

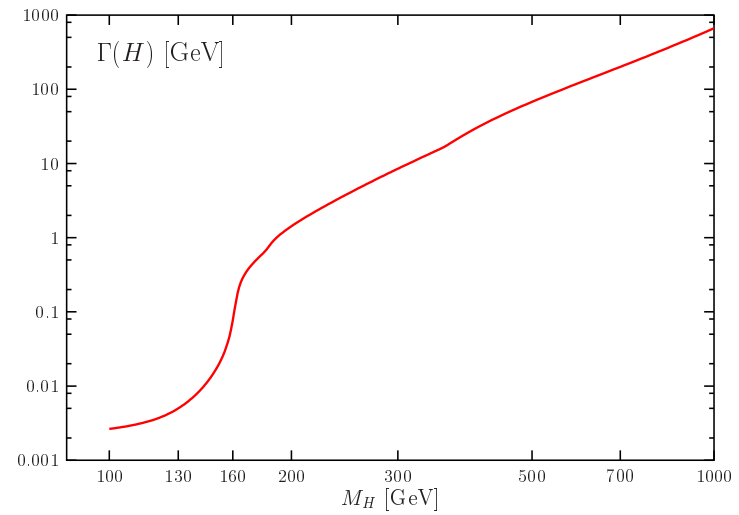
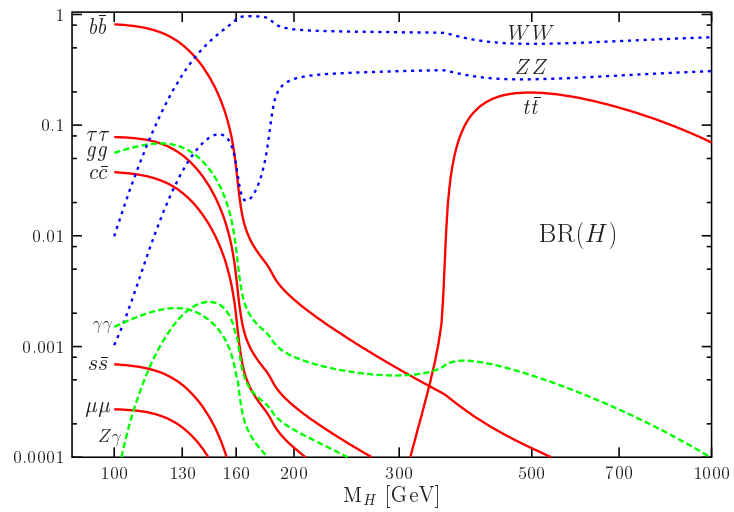
- Introduction: Higgs production and decays
- Two Higgs Doublets Models (2HDM) and its Decoupling regime
- Challenge of the decoupling limit
- Triple Higgs coupling from $h^0 \rightarrow \gamma\gamma$, $h^0 \rightarrow b\bar{b}$
- Triple Higgs couplings at LHC, ILC and $\gamma\gamma$
- Conclusions

	Experiment	SM	Pull
A_{LR}	0.1513 (21)	0.1480	1.6
A_{FB}^l	0.01714 (95)	0.01642	0.8
$A_{e,\tau}$	0.1465 (32)	0.1480	-0.5
A_{FB}^b	0.0992 (16)	0.1037	-2.8
A_{FB}^c	0.0707 (35)	0.0741	-1.0
Q_{FB}	0.23240 (120)	0.23140	-0.8
m_W	80.398 (25)	80.374	0.9
Γ_Z	2495.2 (23)	2495.9	0.3
R_ℓ	20.767 (25)	20.744	0.9
σ_h	41.540 (37)	41.477	1.7
R_b	0.21629 (66)	0.21586	0.7
R_c	0.1721 (30)	0.1722	-0.04
A_b	0.923 (20)	0.935	-0.6
A_c	0.670 (27)	0.668	0.07
m_t	172.6 (1.4)	172.3	0.2
$\Delta\alpha_5(m_Z)$	0.02758 (35)	0.02768	-0.3
$\alpha_S(m_Z)$		0.1186	
m_H		85	
$m_H(95\%)$		148	
χ^2/dof		17.3/12	
$\text{CL}(\chi^2)$		0.14	

M.Chanowitz 0904.3570

- **Best fit analysis:** $M_H = 84_{-26}^{+34}$ GeV which gives $M_H \lesssim 154$ GeV at 95% CL. (LEP Higgs Working Group).
- New analysis with new fitting program gives $M_H = 116.4_{-1.3}^{+18.3}$ GeV [H.Flacher et al, arXiv:0811.0009 \[hep-ph\]](#)
- **LEP II Experiments:** $M_H > 114.4$ GeV
- **Unitarity constraint:** $M_H \lesssim 700$ GeV
- Requiring the SM to be extended up to $\Lambda_{GUT} = 10^{16}$ GeV, one can get $130 \lesssim M_H \lesssim 180$ GeV.
- If the $M_H \gtrsim 200$ GeV, then there should be an additional new ingredient that is relevant at the EWSB scale.

Higgs decays



- At hadron colliders (LHC, Tevatron) the relevant processes are:

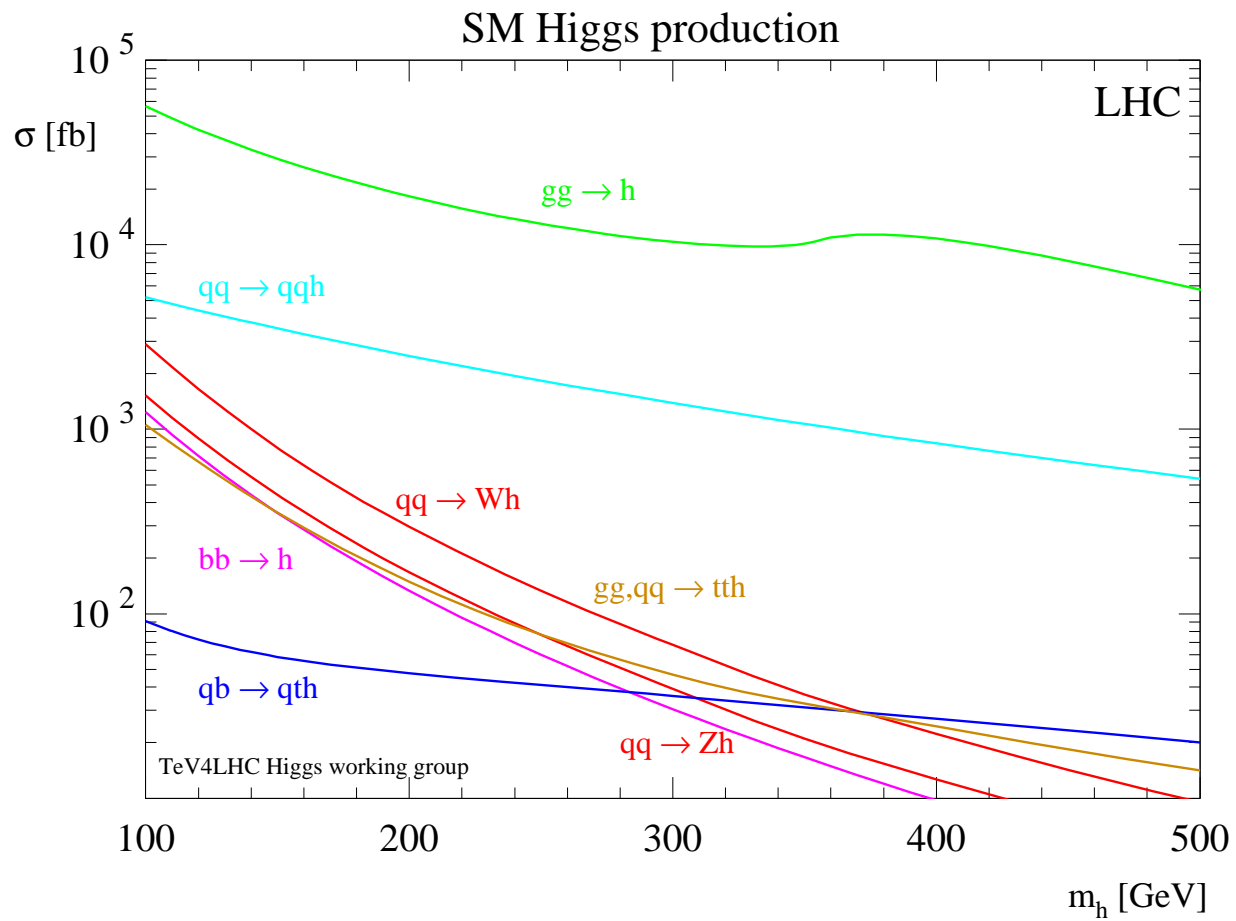
$$gg \rightarrow h_{SM} \rightarrow \gamma\gamma \quad , \quad gg \rightarrow h_{SM} \rightarrow VV^*$$

$$qq \rightarrow qqV^*V^* \rightarrow qqh_{SM} \quad , \quad h_{SM} \rightarrow \gamma\gamma, \tau^+\tau^-, VV^*$$

$$gg, qq \rightarrow t\bar{t}h_{SM} \quad , \quad h_{SM} \rightarrow b\bar{b}, WW^*, WW^*$$

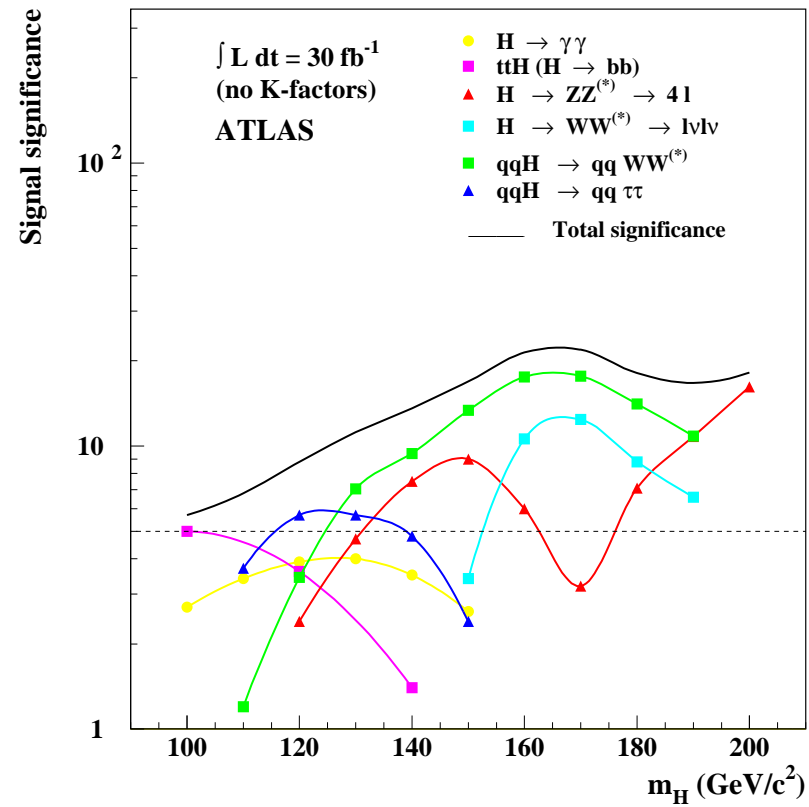
$$qq \rightarrow h_{SM}Z \quad , \quad qq' \rightarrow h_{SM}W \quad , \quad h_{SM} \rightarrow b\bar{b}(\text{Tevatron})$$

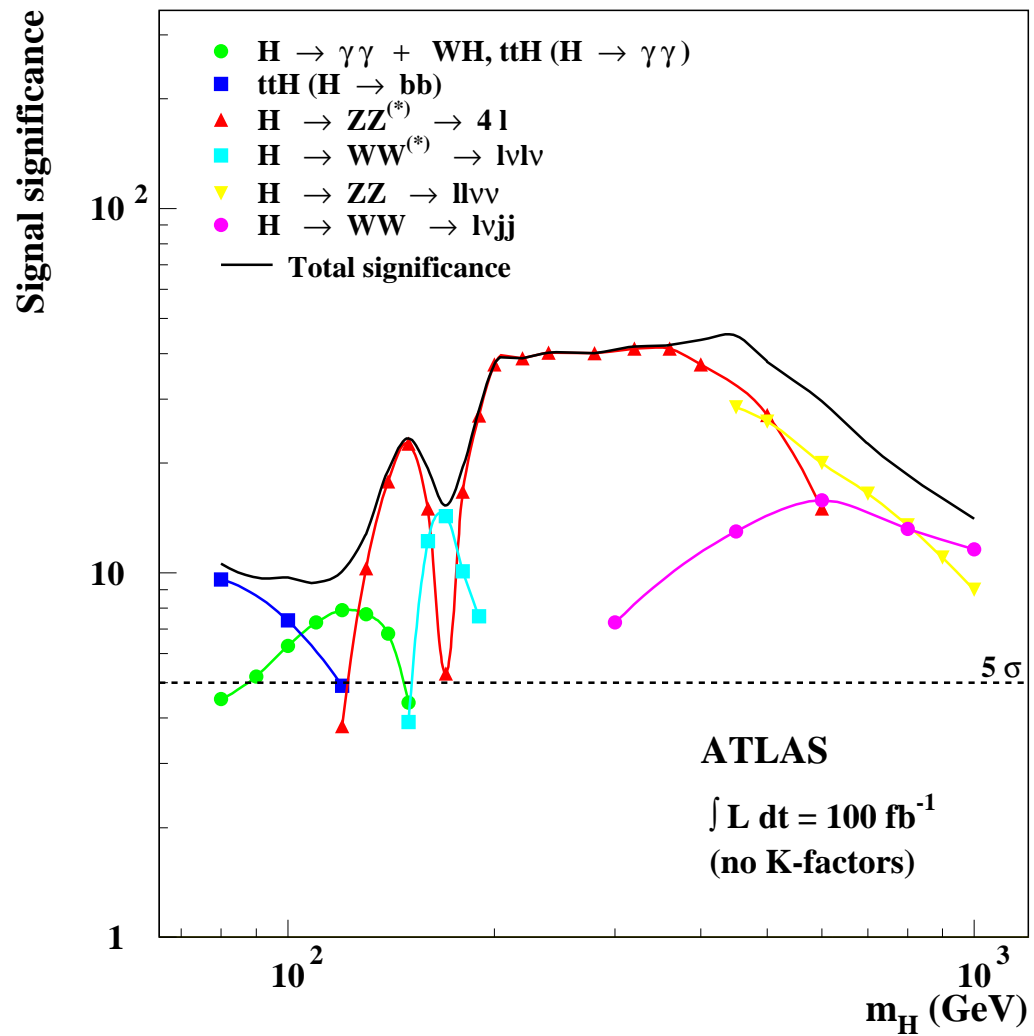
$$gg \rightarrow h_{SM}h_{SM}(\text{double Higgs production})$$



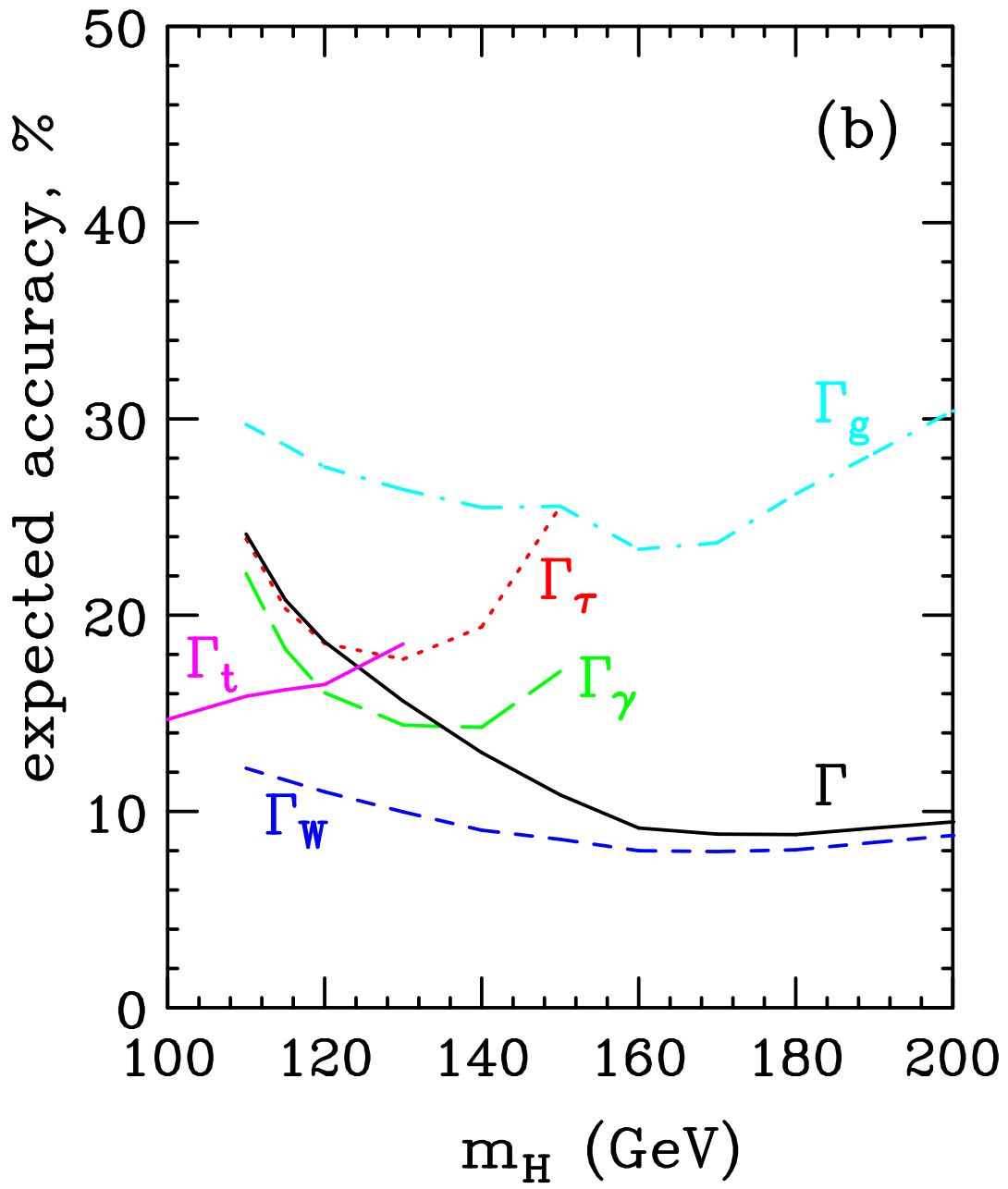
Significance for the experimental detection

Low luminosity

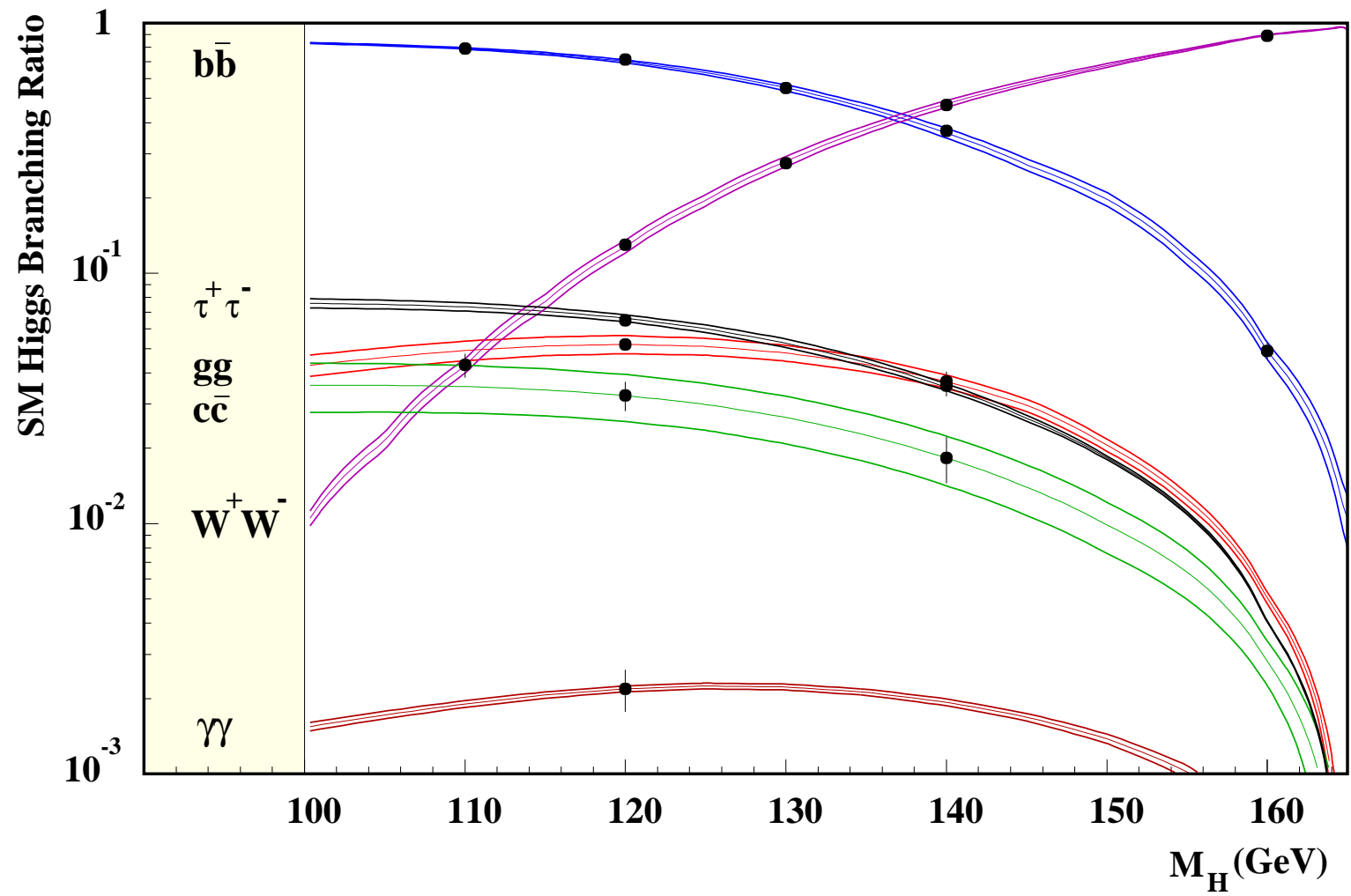




(partial) widths



At linear colliders (LC) Experimental accuracy



Extended Higgs sector

- With **Extended Higgs sector: 2HDM Φ_1 , Φ_2** , CP can be violated either **explicitly** or **spontaneously** in Higgs sector **T.D.Lee'73**
- Some models of **dynamical electroweak symmetry breaking** yields the 2HDM as their low-energy effective theory. [**H. J. He et al, PRD65, (2002) hep-ph/0108041**].
- Models for phase transition require 2 Higgs doublets
- Neutrino masses, Dark Matter, BAU
Zee'80, Ma'06, Aoki, Kanemura, Seto'08

Coupling to fermions

- both Φ_1 and Φ_2 couple to fermions: $M_q = Y^u v_1 + Y^d v_2$:
diagonalisation of M_q does not diagonalise simultaneously $Y^{u,d}$:
FCNC at tree level: 2HDM-III
- 2HDM-I One doublet couple to gauge boson and the other one couple to fermion (like in SM).
- To avoid FCNC at tree level, We impose Z_2 symmetry (Weinberg Theorem): $\Phi_2 \rightarrow -\Phi_2$, $d_{iR} \rightarrow -d_{iR}$: 2HDM-II
- 2HDM-X or lepton-specific 2HDM (or Leptophilic Higgs): one doublet generates the masses of the charged leptons and the second one generates the masses of the quarks
Barnet, Senjanovic, Wolfenstein and Wyler'84

$$\begin{aligned}
V = & \mu_1^2(\Phi_1^+\Phi_1) + \mu_2^2(\Phi_2^+\Phi_2) + \lambda_1(\Phi_1^+\Phi_1)^2 + \\
& \lambda_2(\Phi_1^+\Phi_1)^2 + \lambda_3(\Phi_1^+\Phi_1)(\Phi_2^+\Phi_2) + \lambda_4|\Phi_1^+\Phi_2|^2 \\
& + \{m_{12}^2(\Phi_1^+\Phi_2) + h.c\} + [\lambda_5(\Phi_1^+\Phi_2)^2 + h.c]
\end{aligned}$$

- One can have: **Explicit CP** if $\Im(m_{12}^4\lambda_5^*) \neq 0$;
- One can have **Spontaneous CP** if: $|\frac{m_{12}^2}{\lambda_5 v_1 v_2}| < 1$; $\langle \Phi_1 \rangle = v_1$,
 $\langle \Phi_2 \rangle = v_2 e^{i\theta}$
- Five physical scalars (8 d.o.f=5+3): **a charged Higgs pair H^\pm , two CP-even h^0, H^0 and one CP-odd A^0**
- 10 parameters $(\lambda_i)_{i=1,\dots,5}, \mu_1^2, \mu_2^2, m_{12}^2, v_1, v_2$ with $v_1^2 + v_2^2 = (2\sqrt{2}G_F)^{-1}$ and 2 minimization conditions, **We are left with 7 parameters.**
- **$m_A, m_h, m_H, m_{H^\pm}, \alpha, \tan\beta = v_1/v_2$ and m_{12}^2 free parameters.**

Constraints on 2HDM parameters

Experimentals:

- **Charged Higgs:** $e^+e^- \rightarrow (\gamma^*, Z^*) \rightarrow H^+H^-$ at LEP II followed by $H^+ \rightarrow (\tau\nu_\tau, c\bar{s})$; $M_{H^\pm} > 78.7 \text{ GeV}$.

This limit apply to all models in which $\text{BR}(H^\pm \rightarrow \tau\nu_\tau) + \text{BR}(H^\pm \rightarrow cs) = 1$. [L3: hep-ex/0309056, Delphi: hep-ex/0404012.]

- **Neutral Higgs bosons:** From $e^+e^- \rightarrow h^0A^0$ at LEP II, OPAL collaboration has put a limit on h^0 and A^0 masses of the 2HDM assuming 100% decays of h^0 and A^0 into hadrons.

$1 \lesssim M_h \lesssim 55 \text{ GeV}$ and $3 \lesssim M_A \lesssim 63 \text{ GeV}$ is excluded at 95% CL independent of α and $\tan\beta$. [Opal Collab hep-ex/0408097]

Theoretical constraints:

- $b \rightarrow s\gamma$: $m_{H^\pm} > 295 \text{ GeV}$, $\forall \tan \beta$ in 2HDM-II. No such bound in 2HDM-I [P.Gambino et al, '01, F.Borzumati et al '98].
In 2HDM-X, light H^\pm is allowed Aoiki, H.Logan'09
- $\delta\rho \leq 10^{-3}$ [(PDG)]: constrain the splitting M_A and M_{H^\pm}
- Perturbativity on $\tan \beta$: $0.1 \leq \tan \beta \leq 70$ [V.D.Barger '90]
- Perturbativity on λ_i : $|\lambda_i| \leq 8\pi$
- **Potential bounded from below**: $\lambda_{1,2} > 0$, $\sqrt{\lambda_1 \lambda_2} \geq \lambda_3 + \lambda_4 + \lambda_5$
- Unitarity constraints: in 2HDM there is 14 constraints coming from different channel: W^+W^- , ZZ , hh , HH , hH , AA , hA , H^+H^- , hH^+ ... [A.Akeroyd, A.A and E.Naimi PLB'2000, A.A '2000]

The decoupling limit of 2HDM

$$M_{12}^2 \rightarrow \infty, \cos(\alpha - \beta) \rightarrow 0$$

- In this limit, the masses of $\Phi=H, H^\pm, A$:

$$m_\Phi^2 = M_{12}^2 + \sum_i \lambda_i v^2 + \mathcal{O}(v^4/M_{12}^2), \quad , \quad m_h^2 = \sum_i \lambda_i v^2$$

- When $M_{12}^2 \gg \lambda_i v^2$, m_{H,A,H^\pm}^2 are determined by M_{12}^2 , and are independent of λ_i . In this case $\alpha \rightarrow \beta - \pi/2$, The effective theory below M_{12} is described by one Higgs doublet. In this limit:

$$h^0 VV / (h_{SM} VV) = \sin(\beta - \alpha) \rightarrow 1$$

$$h^0 b\bar{b} / h_{SM} b\bar{b} = -\frac{\sin \alpha}{\cos \beta} \rightarrow 1, \quad (h^0 t\bar{t}) / h_{SM} t\bar{t} = \frac{\cos \alpha}{\sin \beta} \rightarrow 1$$

$$H^0 VV \propto \cos(\beta - \alpha) \rightarrow 0, \quad (hhh) / (hhh)_{SM} \rightarrow 1$$

$$h^0 H^+ H^-, h^0 A^0 A^0, h^0 H^0 H^0, H^\pm t\bar{b} \dots \neq 0$$

Challenge of the decoupling limit

In case of extended Higgs sector like MSSM or 2HDM we have 4 physical Higgs: 2 CP even (h^0, H^0), 1 CP odd A^0 and a pair charged Higgs H^\pm :

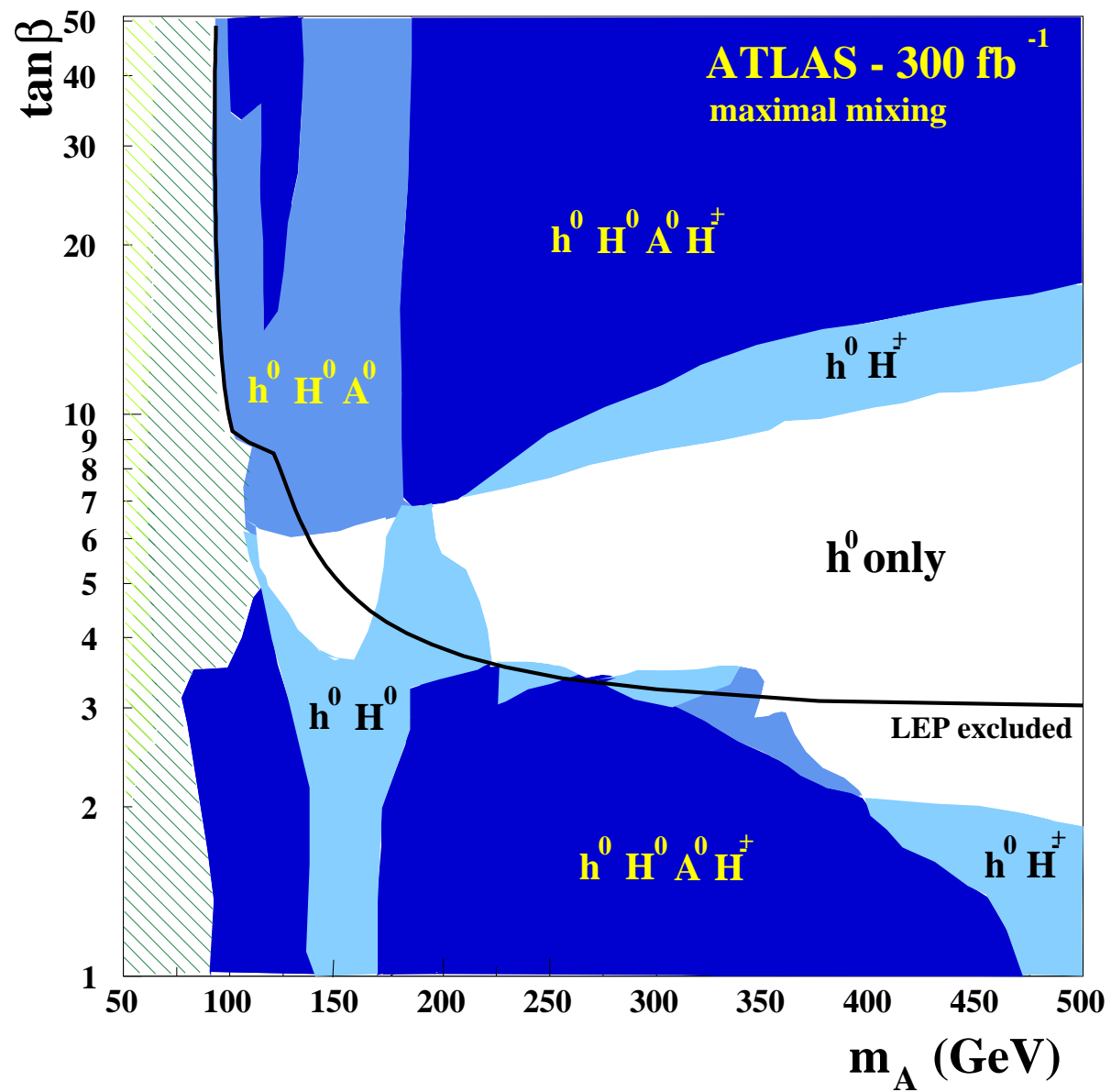
$$\sigma(\{pp, e^+e^-\} \rightarrow Z + h^0/H^0) = \sin^2 / \cos^2(\beta - \alpha) \sigma_{SM}$$

$$\sigma(pp \rightarrow W + h^0/H^0) = \sin^2 / \cos^2(\beta - \alpha) \sigma_{SM}$$

$$\sigma(e^+e^- \rightarrow A^0 + h^0/H^0) = \cos^2 / \sin^2(\beta - \alpha) \lambda \sigma_{SM}$$

$$\sigma(\{pp, e^+e^-\} \rightarrow \nu\bar{\nu} + h^0/H^0) \sin^2 / \cos^2(\beta - \alpha) \sigma_{SM}$$

$$\{gg, \gamma\gamma\} \rightarrow h^0, H^0, A^0$$



A program of precision measurements will begin at LHC and will reach maturity at the ILC :

$$\delta(\Gamma_W)/\Gamma_W \approx 5 - 10\% , \quad \delta(\Gamma_\tau)/\Gamma_\tau = \delta(\Gamma_\gamma)/\Gamma_\gamma \approx 18\% \text{ at LHC}$$

At Linear Collider(ILC), the situation is much better:

Relative accuracies (in %) on M_H and couplings at ILC $\sqrt{s} = 500$ GeV and $\int \mathcal{L} = 500 \text{ fb}^{-1}$ [[hep-ph 0106315](#)]

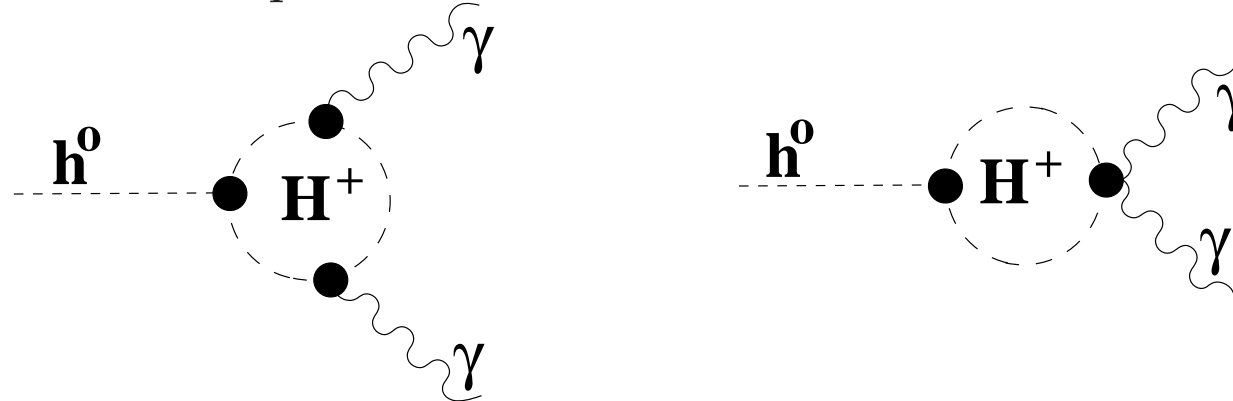
M_H	ΔM_H	g_{HWW}	g_{HZZ}	g_{Htt}	g_{Hbb}	$g_{H\tau\tau}$
120	± 0.033	± 1.2	± 1.2	± 3.0	± 2.2	± 3.3

In $\gamma\gamma$ option of ILC: $\delta\Gamma(H \rightarrow \gamma\gamma)/\Gamma(H \rightarrow \gamma\gamma) \approx 2\%$ can be achieved (from $\gamma\gamma \rightarrow H \rightarrow b\bar{b}$).

Non decoupling effects in Higgs decays

A.A, W.Hollik and S.Penaranda PLB'04

- $h^0 \rightarrow \gamma\gamma$ is loop-mediated processes since the photon does not couple to neutral particles

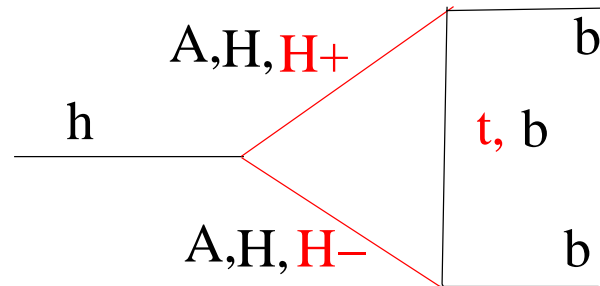


- The only pure **2HDM** contribution comes from charged Higgs loops (if $\alpha = \beta - \pi/2$): $h^0 t\bar{t} \approx \frac{c_\alpha}{s_\beta} \approx 1\dots$

$$g[h^0 H^+ H^-] \approx -\frac{g}{2M_W} \{M_{h^0}^2 + 2(M_{H^\pm}^2 - M_{12}^2)\}$$

The decoupling is achieved when $M_{12} \rightarrow \infty$

- $h_0 \rightarrow b\bar{b}$, already exists at the tree level because of the Higgs- b Yukawa interaction
- Pure **2HDM** one-loop contributions not present in the **SM** case:



$\alpha \rightarrow \beta - \pi/2 \Rightarrow$ only $h^0 H^+ H^-$, $h^0 H^0 H^0$ and $h^0 A^0 A^0$ don't vanish or reduce to their **SM** values

$$g[h^0 H^+ H^-] \approx -\frac{g}{2M_W} \{M_{h^0}^2 + 2(M_{H^\pm}^2 - M_{12}^2)\}$$

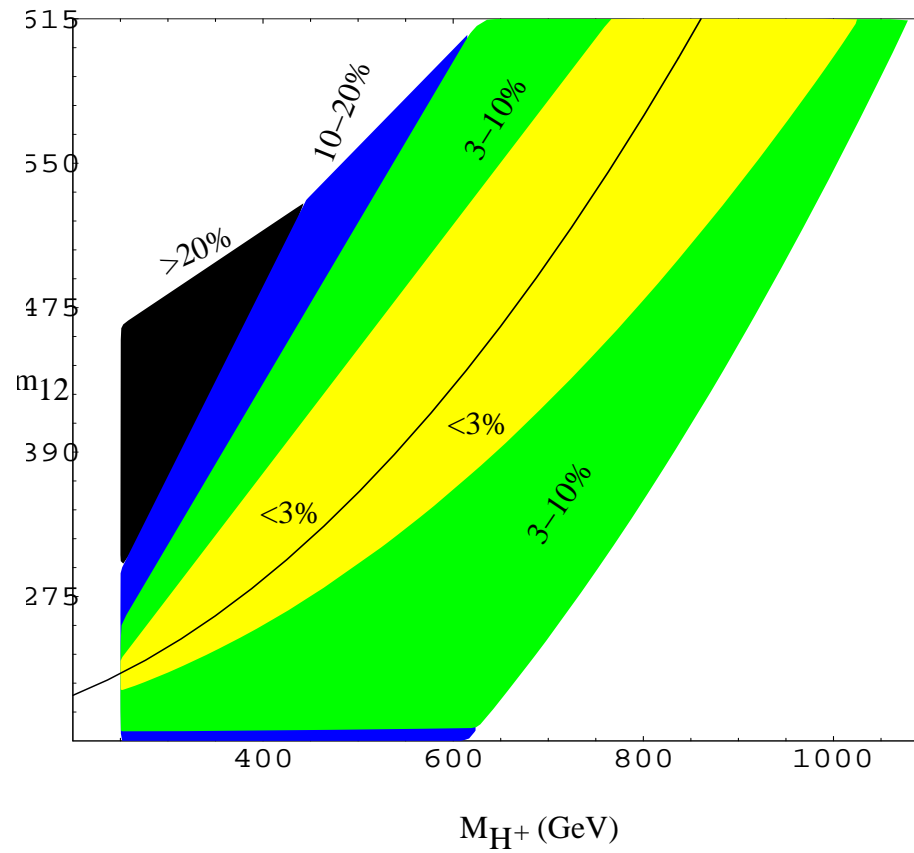
$$g[h^0 H^0 H^0] \approx -\frac{g}{2M_W} \{M_{h^0}^2 + 2(M_{H^0}^2 - M_{12}^2)\}$$

$$g[h^0 A^0 A^0] \approx -\frac{g}{2M_W} \{M_{h^0}^2 + 2(M_{A^0}^2 - M_{12}^2)\}$$

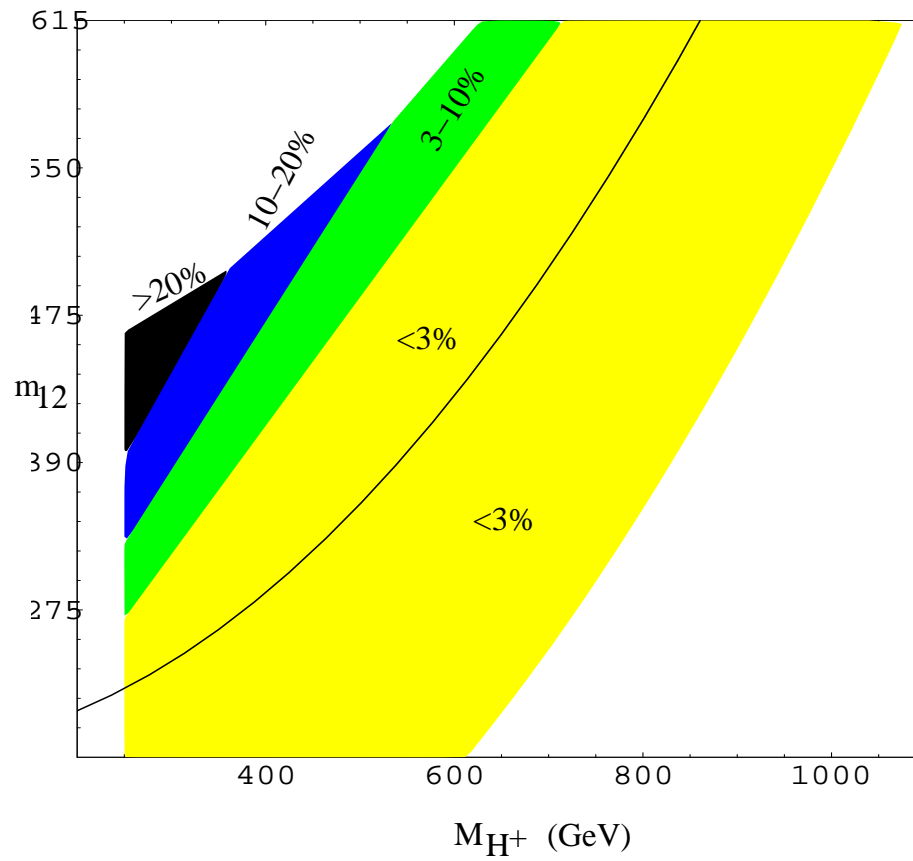
- $\Gamma_{\gamma\gamma}$ can be measured with **16% accuracy at ILC** and Γ_{bb} with 2.2%.
- We want to distinguish **2HDM** from **SM** in the decoupling regime: $(m_{A^0}, m_H, m_{H^\pm} \gg m_Z)$
- In the numerical evaluation we have parameterized the Higgs sector with:

$$M_{h^0} = 120 \text{ GeV} , \quad M_{H^0} = M_{A^0} = M_{H^\pm} , \quad \alpha \approx \beta - \pi/2 , \quad M_{12}$$

$$h^0 \rightarrow \gamma\gamma: \Delta_{\gamma\gamma} = \left| \frac{\Gamma(h \rightarrow \gamma\gamma)^{2HDM} - \Gamma(h \rightarrow \gamma\gamma)^{SM}}{\Gamma(h \rightarrow \gamma\gamma)^{SM}} \right|$$



$$h \rightarrow b\bar{b}: \Delta_{bb} = \left| \frac{\Gamma(h \rightarrow b\bar{b})^{2HDM} - \Gamma(h \rightarrow b\bar{b})^{SM}}{\Gamma(h \rightarrow b\bar{b})^{SM}} \right|$$

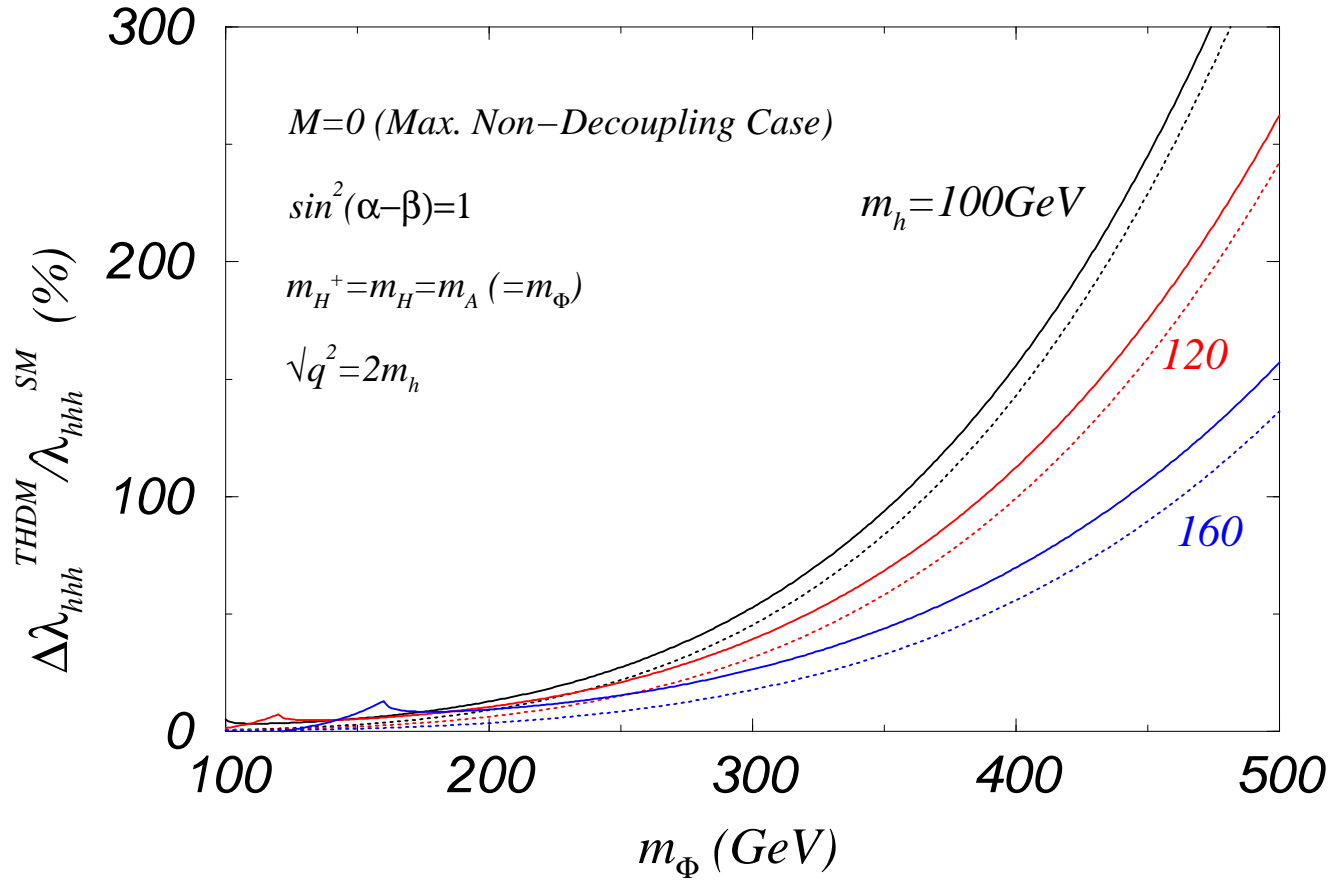


hhh^{eff} from S.Kanemura, E.Senaha, Y.Okada, C.P.Yuan PLB'02,

In the decoupling limit hhh^{eff} takes the following form

$$hhh_{eff} = \frac{3M_h^2}{v} \left\{ 1 + \frac{m_\Phi^4}{3\pi^2 m_h^2 v^2} \left(1 - \frac{m_{12}^2}{\sin^2 \beta \cos^2 \beta m_\Phi^2} \right)^3 - \frac{N_{ct} m_t^4}{3\pi^2 m_h^2 v^2} \right\},$$

with $m_\Phi = m_H = m_A = m_{H\pm}$.



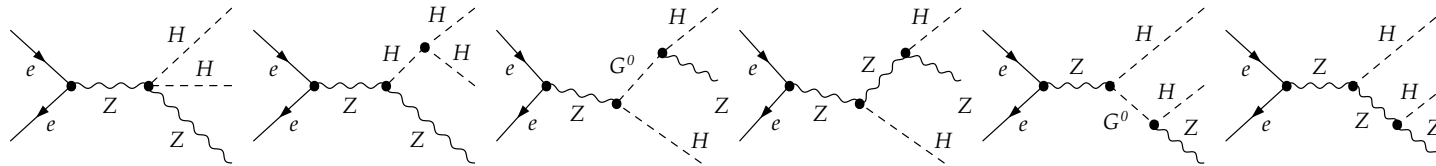
$\Delta\lambda_{hhh}^{THDM} \equiv \lambda_{hhh}^{eff}(THDM) - \lambda_{hhh}^{eff}(SM)$. The results of the full one-loop calculation are shown as solid curves.

1. Probing triple Higgs couplings in the 2HDM at e^+e^- collider

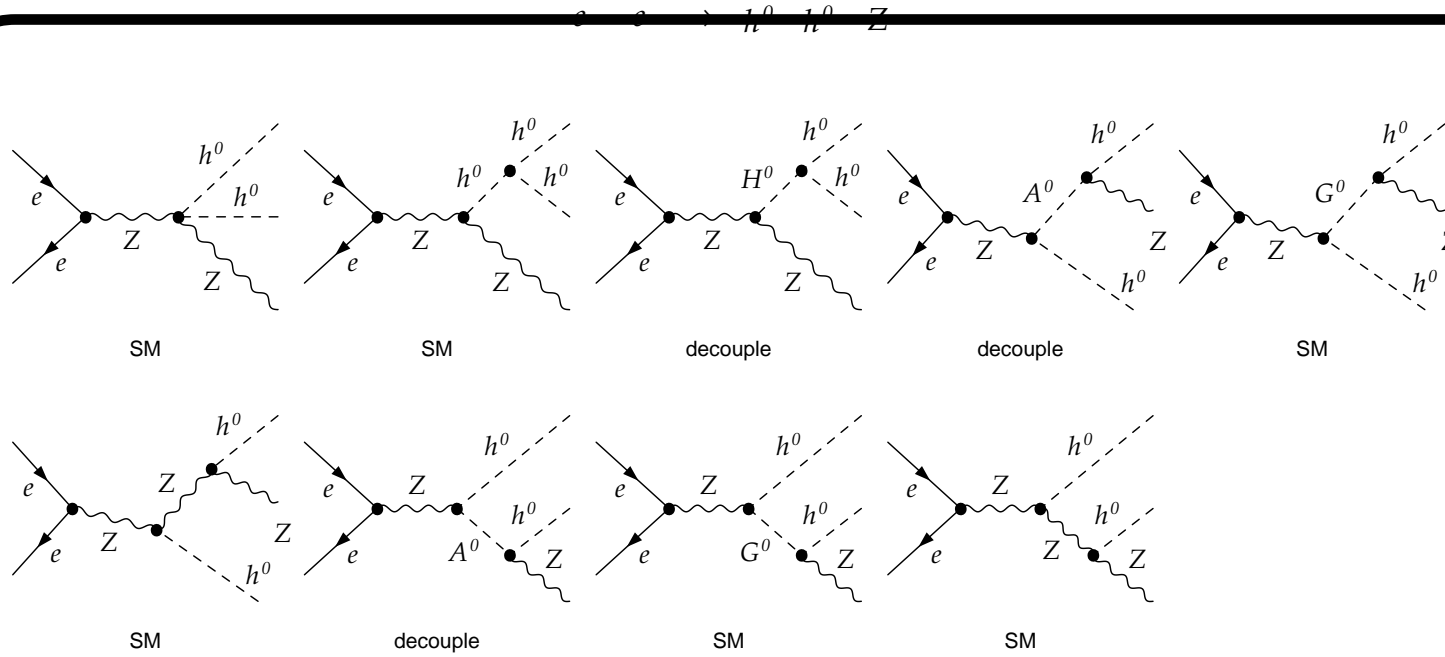
A.A, R.Benbrik and C.W. Chiang'08

- If the Higgs exist, it will be produced either at Tevatron-II or LHC.
- In order to establish the Higgs mechanism, we need to measure the Higgs couplings to fermions, to gauge boson as well as the self-interaction of Higgs bosons.
- Complementarity of LHC/ILC [G. Weiglein et al, “Physics interplay of the LHC and the ILC,” Phys. Rept'06, hep-ph/0410364]
- SM scalar potential can be reconstructed by measuring the triple coupling λ_{hhh} and quartic coupling λ_{hhhh} .
- One can access to λ_{hhh} at ILC from $e^+e^- \rightarrow Zhh$

$e^+e^- \rightarrow Zhh$ in SM



- In SM, $\sigma(e^+e^- \rightarrow Zhh)$ is rather small, for $\sqrt{s}, m_H = 500, 120$ GeV, $\sigma(e^+e^- \rightarrow Zhh) = 0.2$ fb
- possible to extract a signal from EW and QCD background $e^+e^- \rightarrow Zbb\bar{b}\bar{b}$ by simple kinematics cuts: e.g, invariant masses...
Much more events are possible if: [[D.Miller et al hep-ph/9906395](#)]
 - Very high luminosity
 - Excellent b tagging
 - Beam polarization.



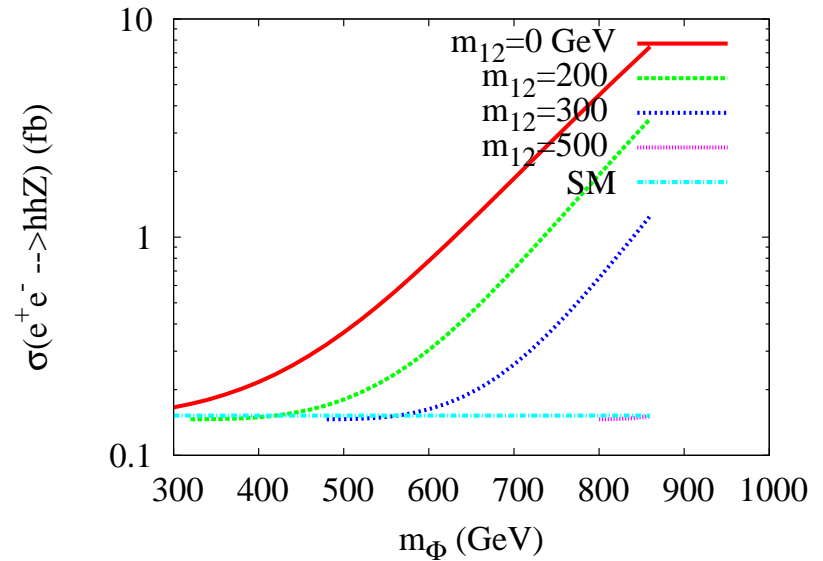
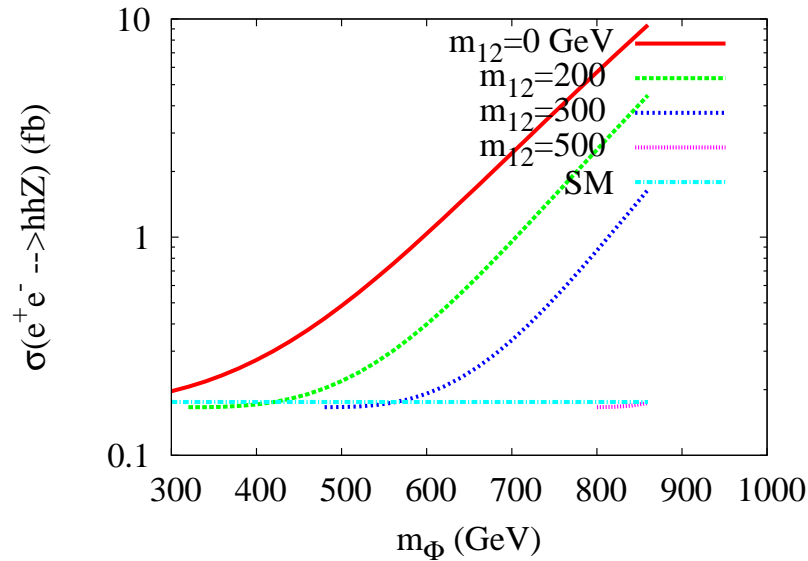
In 2HDM we are sensitive to:

$$hhh = \frac{-3e}{m_W s_W s_{2\beta}^2} \left[(c_\beta c_\alpha^3 - s_\beta s_\alpha^3) s_{2\beta} m_{h^0}^2 - c_{\beta-\alpha}^2 c_{\beta+\alpha} m_{12}^2 \right]$$

$$Hhh = -\frac{1}{2} \frac{e c_{\beta-\alpha}}{m_W s_W s_{2\beta}^2} \left[(2m_{h^0}^2 + m_{H^0}^2) s_{2\alpha} s_{2\beta} - (3s_{2\alpha} - s_{2\beta}) m_{12}^2 \right]$$

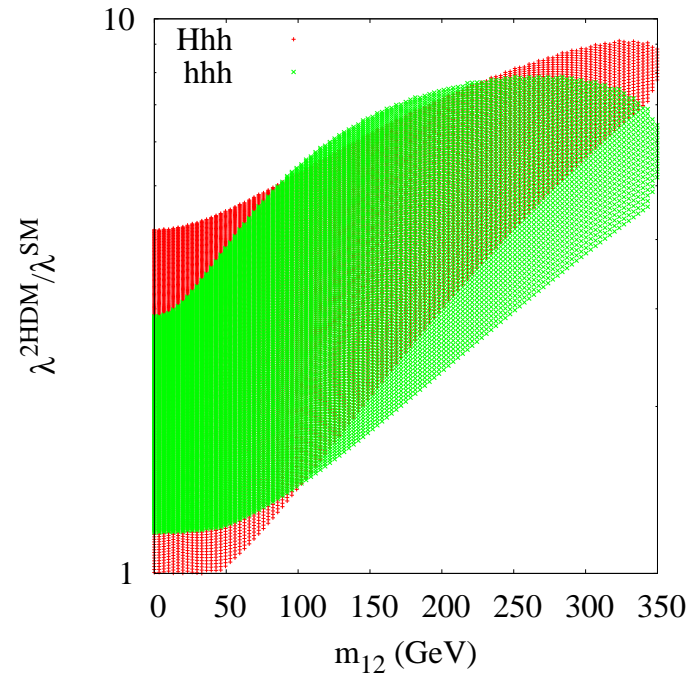
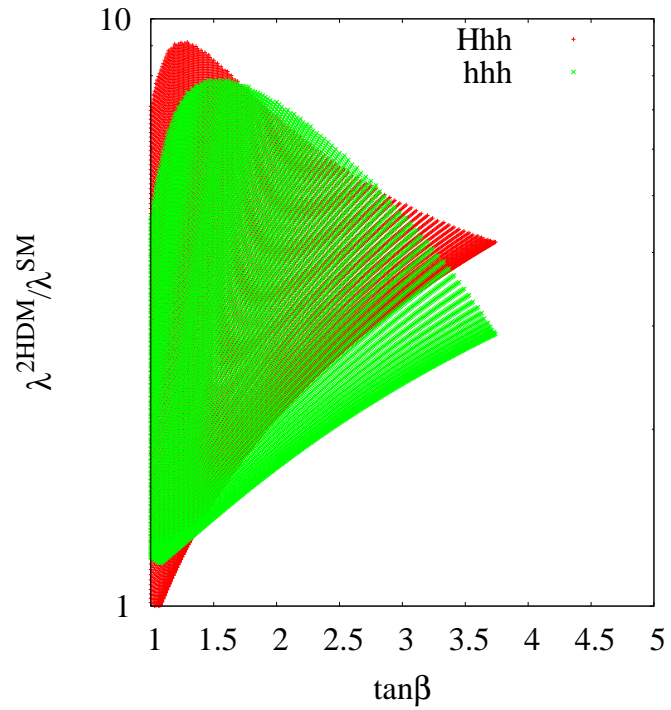
$e^+e^- \rightarrow Zhh$ in the decoupling limit: $m_\Phi = m_H = m_A = m_{H^\pm}$

$$hhh_{eff} = \frac{3M_h^2}{v} \left\{ 1 + \frac{m_\Phi^4}{3\pi^2 m_h^2 v^2} \left(1 - \frac{m_{12}^2}{\sin^2 \beta \cos^2 \beta m_\Phi^2} \right)^3 - \frac{N_{ct} m_t^4}{3\pi^2 m_h^2 v^2} \right\},$$



$m_h = 120$ GeV, $\sqrt{s} = 500$ GeV (left) and $\sqrt{s} = 800$ GeV (right).

Away from decoupling limit one can reach 100 fb for $Z\Phi_i\Phi_j$.



$m_h, M_H, M_A, M_{H\pm} = 120, 300, 350, 300$ GeV, $\sin\alpha = -0.9$,
 $1 \lesssim \tan\beta \lesssim 10$, $m_{12} \in [0, 600]$ GeV

$$e^+e^- \rightarrow Z\Phi_i\Phi_j$$

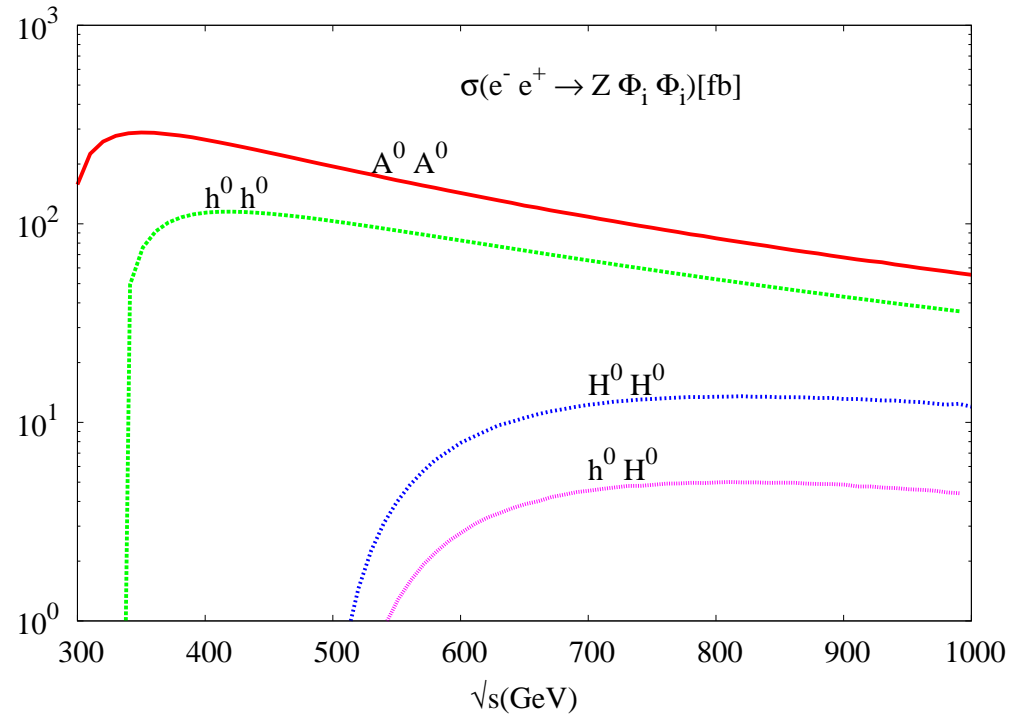
$$m_{12} = 0, m_{H\pm} = 250 \text{ GeV}, \tan\beta = 10$$

$$\text{Zhh}, m_{h,H,A} = 120, 240, 150 \text{ GeV}, \sin\alpha = 0.8$$

$$\text{ZAA}, m_{h,H,A} = 120, 200, 100 \text{ GeV}, \sin\alpha = 0.6$$

$$\text{ZHH}, m_{h,H,A} = 120, 140, 360 \text{ GeV}, \sin\alpha = -0.1$$

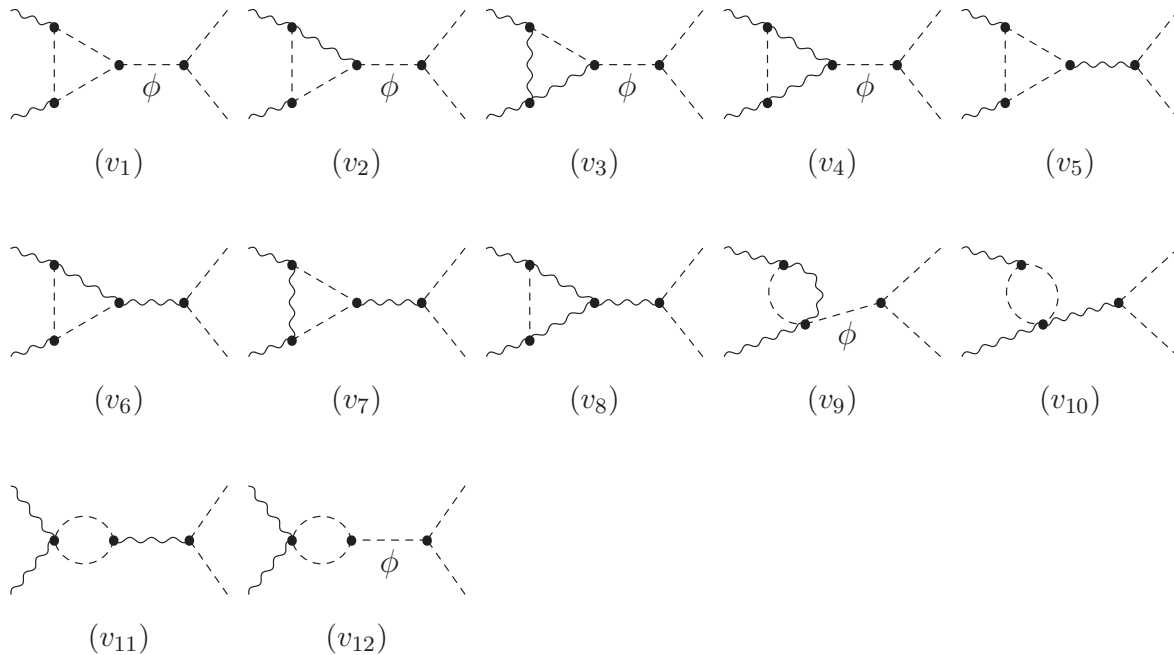
$$\text{ZhH}, m_{h,H,A} = 120, 200, 300 \text{ GeV}, \sin\alpha = -0.7$$



Probing triple Higgs couplings in the 2HDM at $\gamma\gamma$ collider

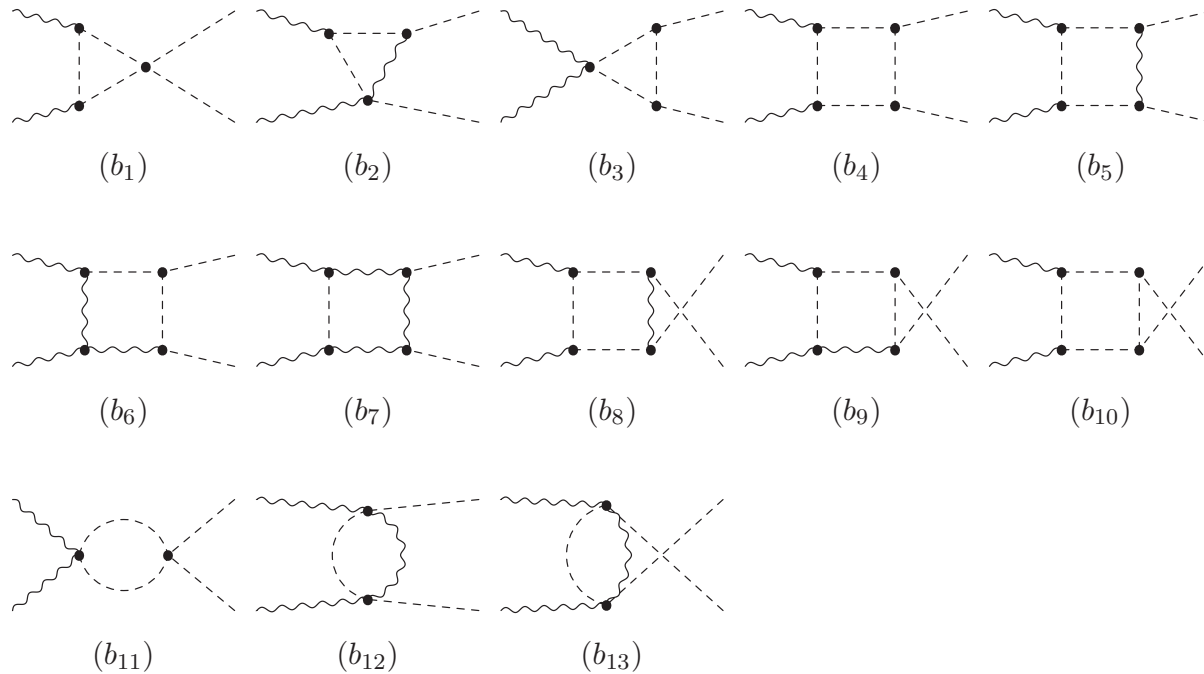
A.A, R.Benbrik and C.H.Chen and R.Santos'09

- $\gamma\gamma \rightarrow hh$ is loop mediated, then very sensitive to new physics.
- $\gamma\gamma \rightarrow hh$ has more phase space than $e^+e^- \rightarrow Zhh$



Just charged Higgs contribution are shown

In 2HDM, scalar loops dominate

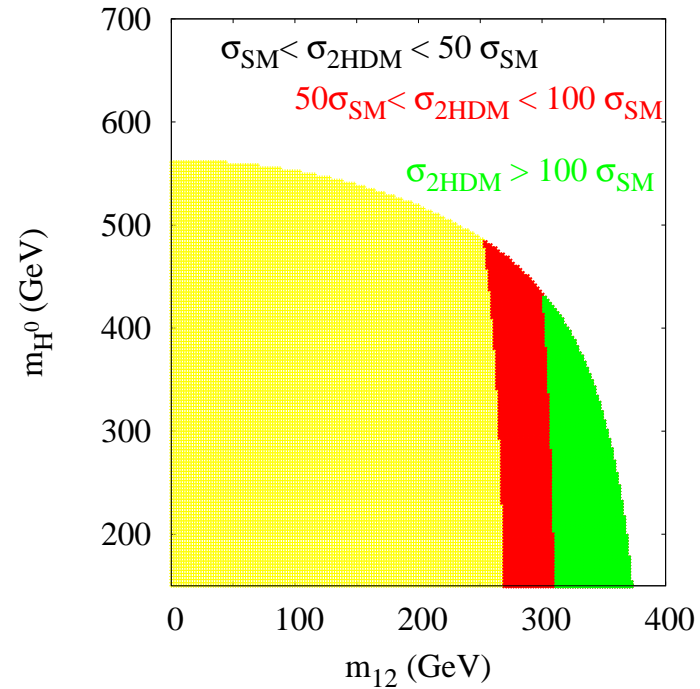
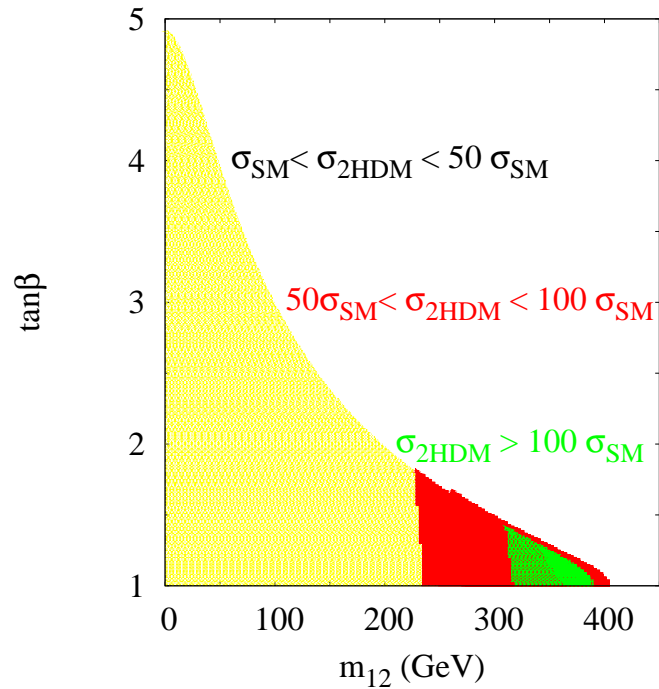


www.FeynArts.de , FormCalc , LoopTools, (T.Hahn)

$\gamma\gamma \rightarrow HH$ in SM

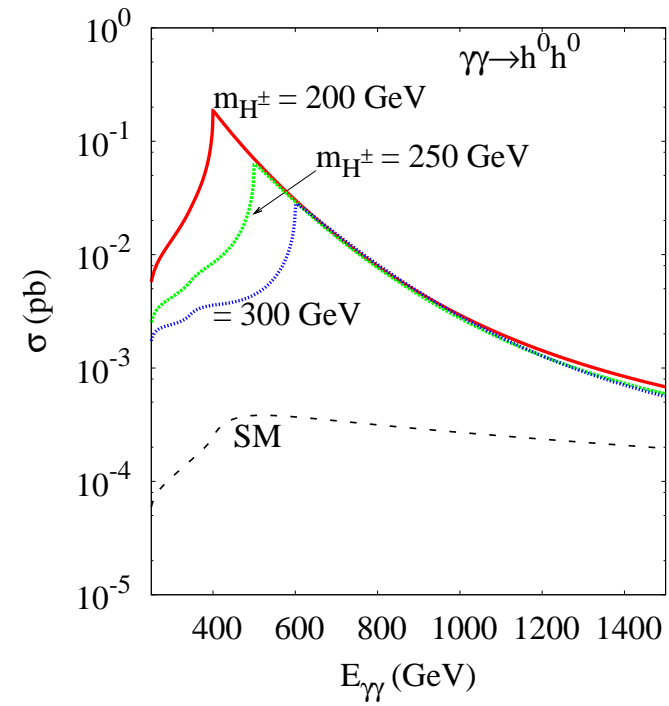
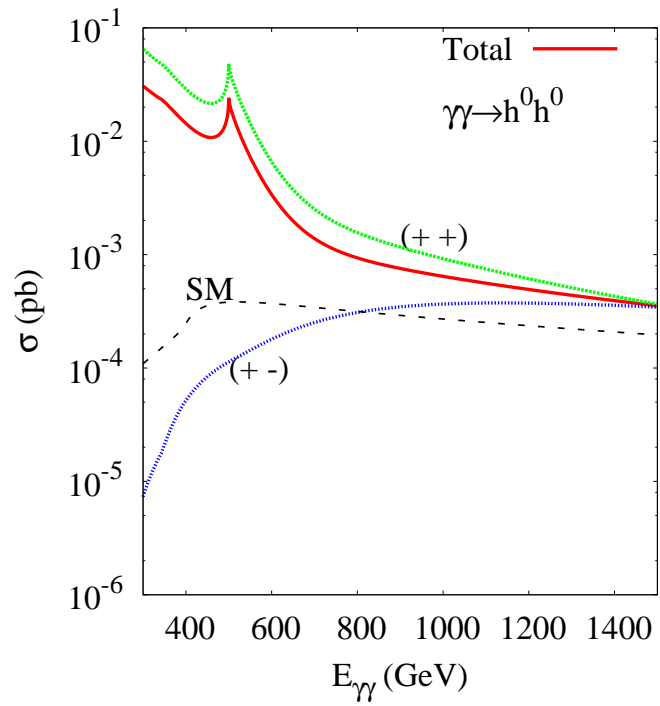
Jikia'92, Belusevic'04 and Takahashi'08

- look for $\gamma\gamma \rightarrow HH \rightarrow 4b$
- Main background from W^+W^- and from non-resonant four jet final state.
- Select 2 jet and reconstruct Higgs mass, $M(q\bar{q} - MH) < 5$ GeV
- **Conclusion:** For a center of mass energy of 350 GeV and $m_H = 120$ GeV an integrated luminosity of 450 fb^{-1} would be needed to exclude a zero Higgs boson self-coupling at the 5σ level.

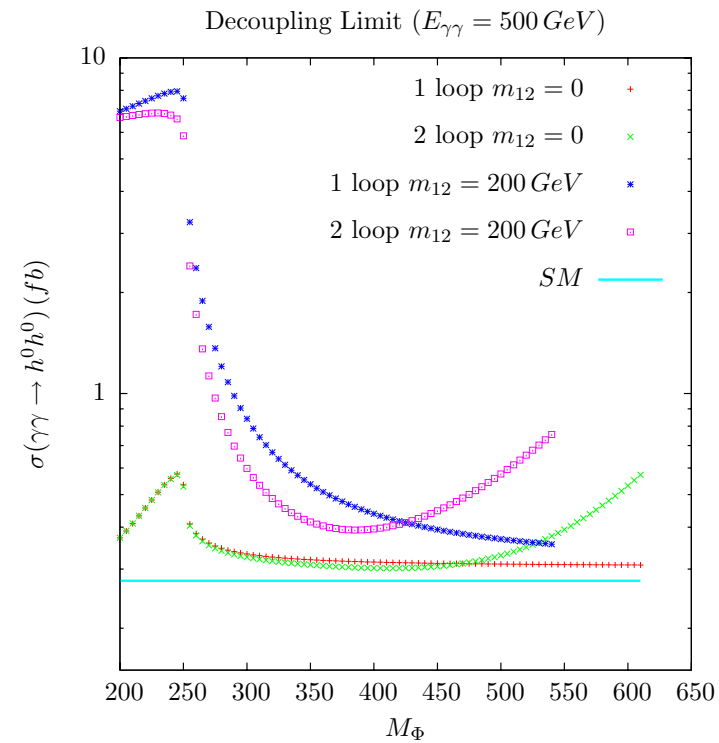
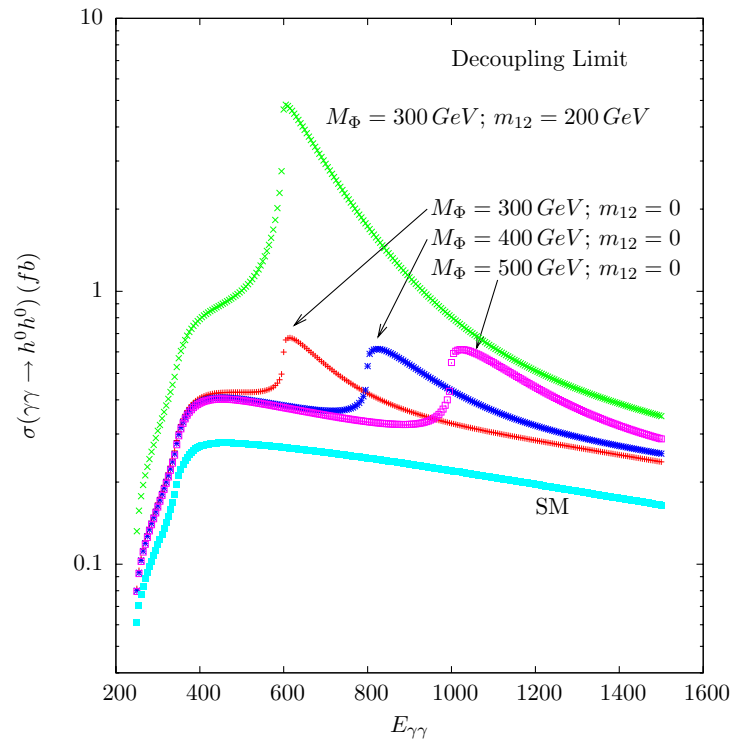


$m_{h^0} = 115 \text{ GeV}$, $m_{A^0} = 270 \text{ GeV}$, $m_{H^\pm} = 350 \text{ GeV}$.

Left $m_{H^0} = 2m_{h^0}$, $E_{\gamma\gamma} = 500 \text{ GeV}$, $-1 \leq \sin \alpha \leq 1$, $1 \lesssim \tan \beta \lesssim 10$
 and right $\tan \beta = 1$, $\sin \alpha = -0.9$, $E_{\gamma\gamma} = 800 \text{ GeV}$



Decoupling limit, $m_h = 120$ GeV

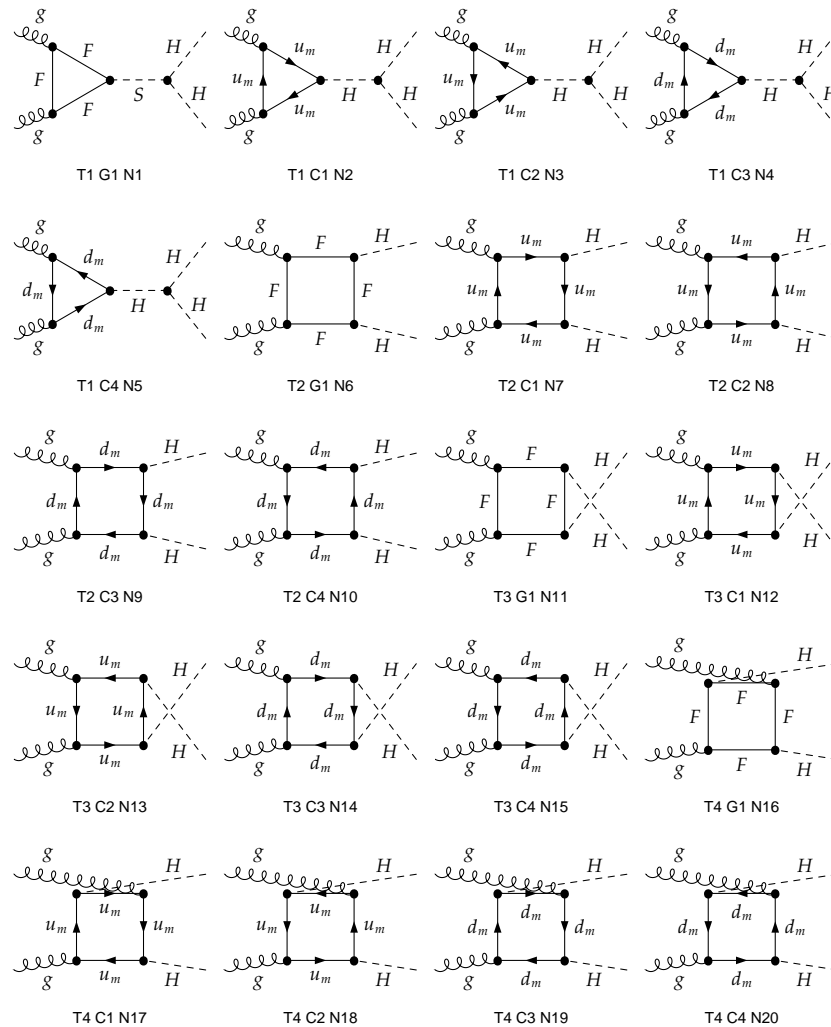


(Left) $\gamma\gamma \rightarrow hh$ at LO,

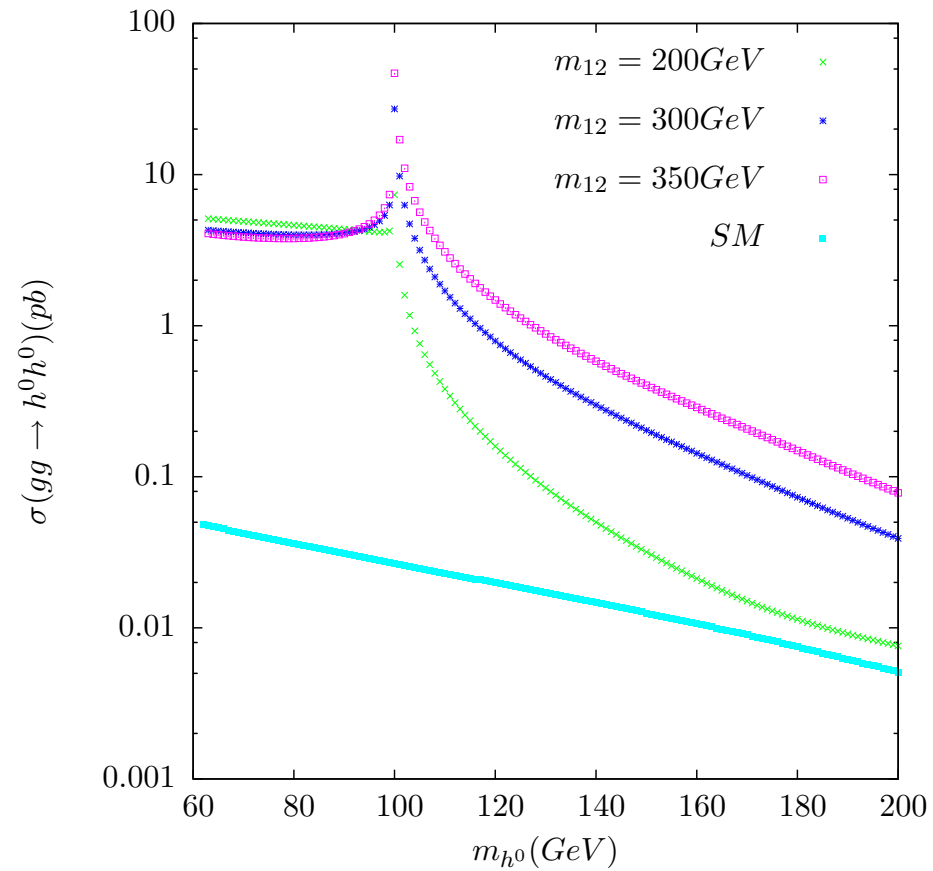
(Right) $\gamma\gamma \rightarrow hh$ at LO and LO + High order corrections to hhh

3. Probing triple Higgs couplings in the 2HDM at LHC

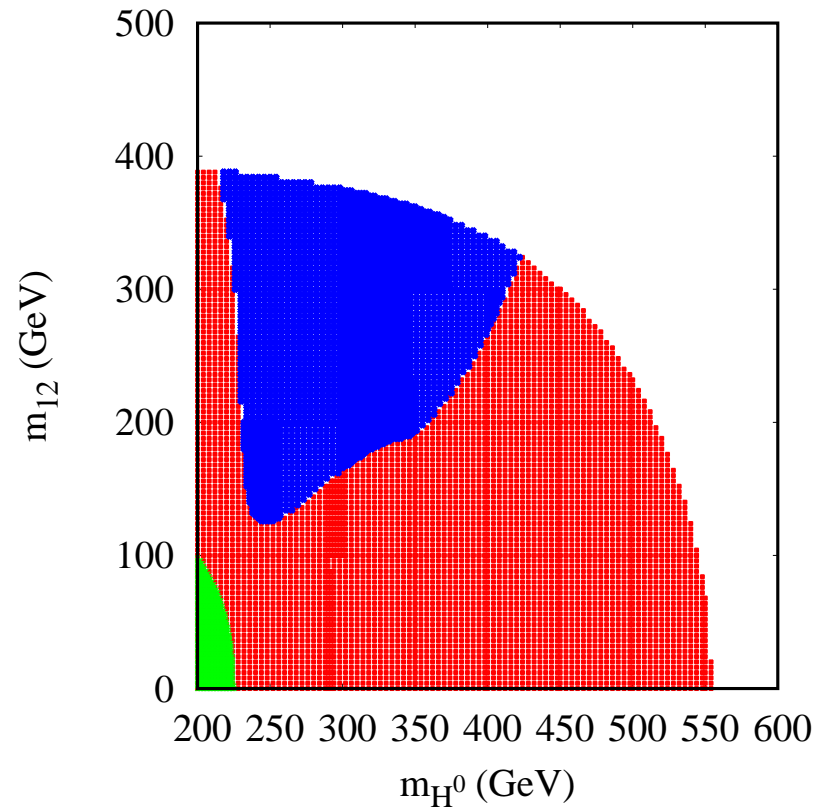
(A.A, R.Benbrik, C.H. Chen, R. Guedes and R.Santos'09)



- In SM, the cross section is small $1 \lesssim \sigma(gg \rightarrow HH) \lesssim 3$ fb for $120 \lesssim M_H \lesssim 190$ GeV.
- $150 \lesssim M_H \lesssim 200$ GeV, from $gg \rightarrow HH \rightarrow W^+W^-W^+W^- \rightarrow 2l4j$ or $3l2j$, the non vanishing of the triple Higgs coupling of the SM can be established at 95% CL (with 300 fb^{-1}).
- One need VLHC to measure the triple Higgs coupling of the SM with an accuracy of 8-25% at 95% CL. [U. Baur et al '03](#)
- $M_H \lesssim 140$ GeV, $gg \rightarrow HH \rightarrow b\bar{b}\gamma\gamma$, look promissing. With 600 fb^{-1} or more, we could make a rough first measurement for $M_H = 120$ GeV (with 6 signal events). [U. Baur et al '04](#)

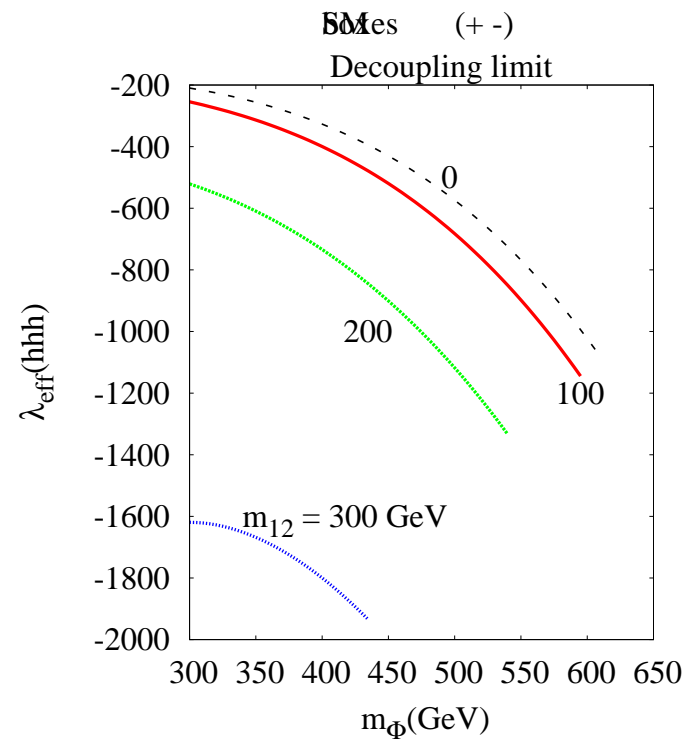
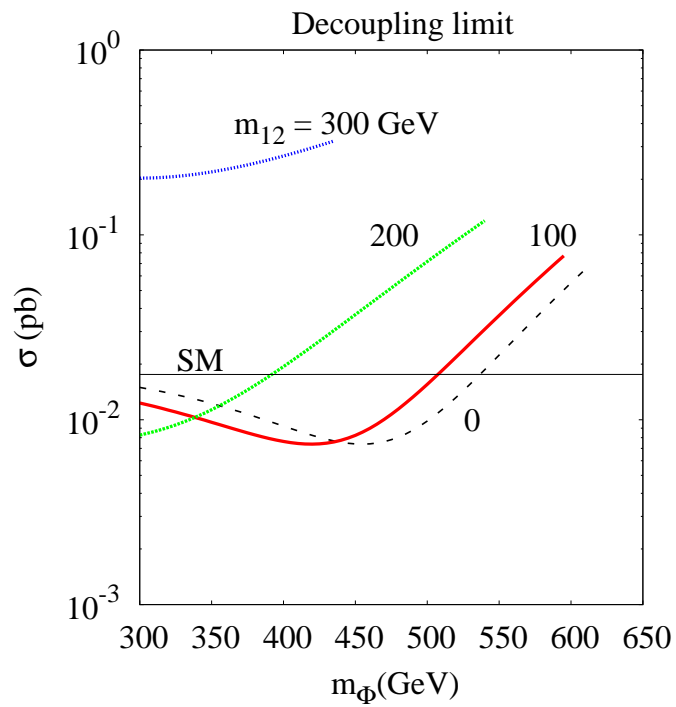


$m_{H^0} = 200\text{GeV}$, $m_A = 200\text{GeV}$, $m_{H^\pm} = 300\text{GeV}$, $\sin \alpha = 0.631$ and $\tan \beta = 1$. ($\sin(\beta - \alpha) = 0.1$)



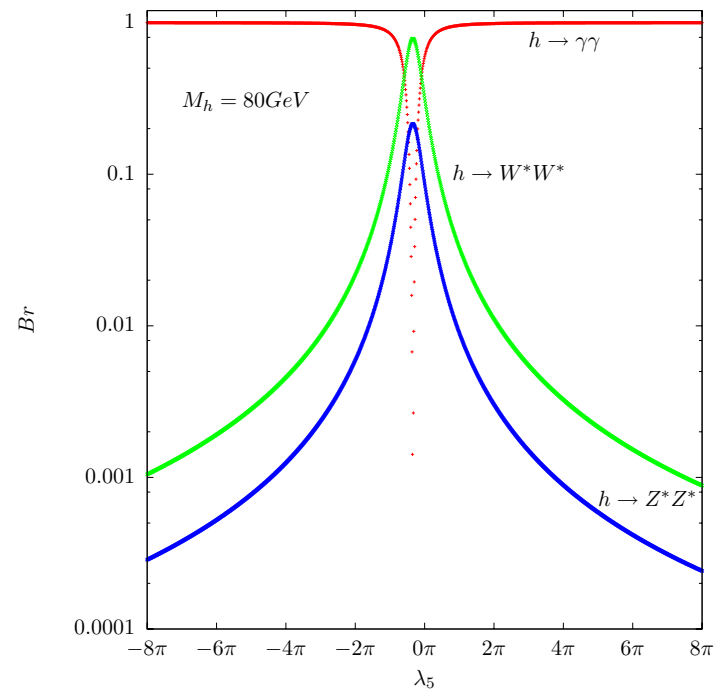
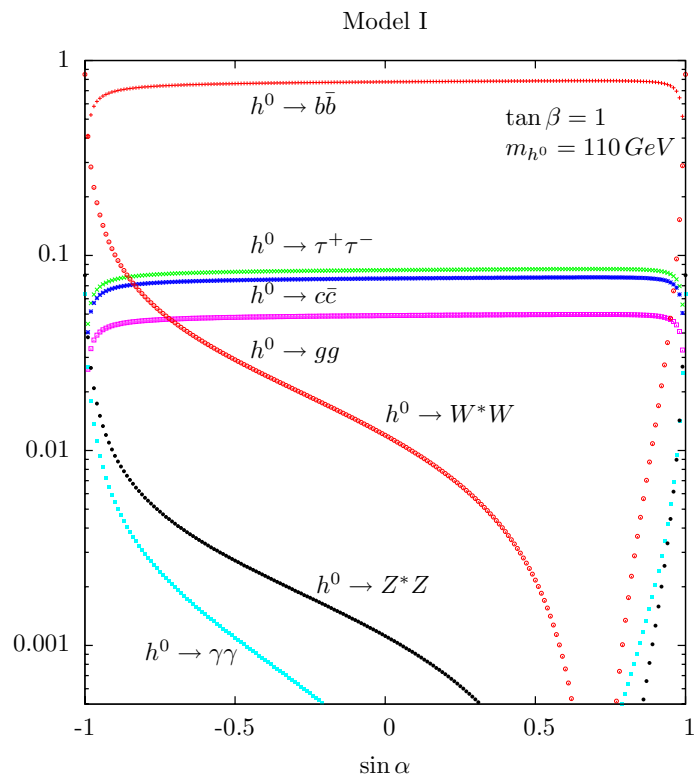
$m_h = 115$, $m_{H^\pm} = 300$, $m_A = 100$ GeV $\sin \alpha = -0.9$, $\tan \beta = 1$,
 $200 \lesssim m_H \lesssim 600$ GeV, $0 \lesssim m_{12} \lesssim 400$ GeV.

$\sigma_{2HDM} < \sigma_{SM}$, $\sigma_{2HDM} > 100\sigma_{SM}$, $\sigma_{SM} \lesssim \sigma_{2HDM} < 100\sigma_{SM}$,

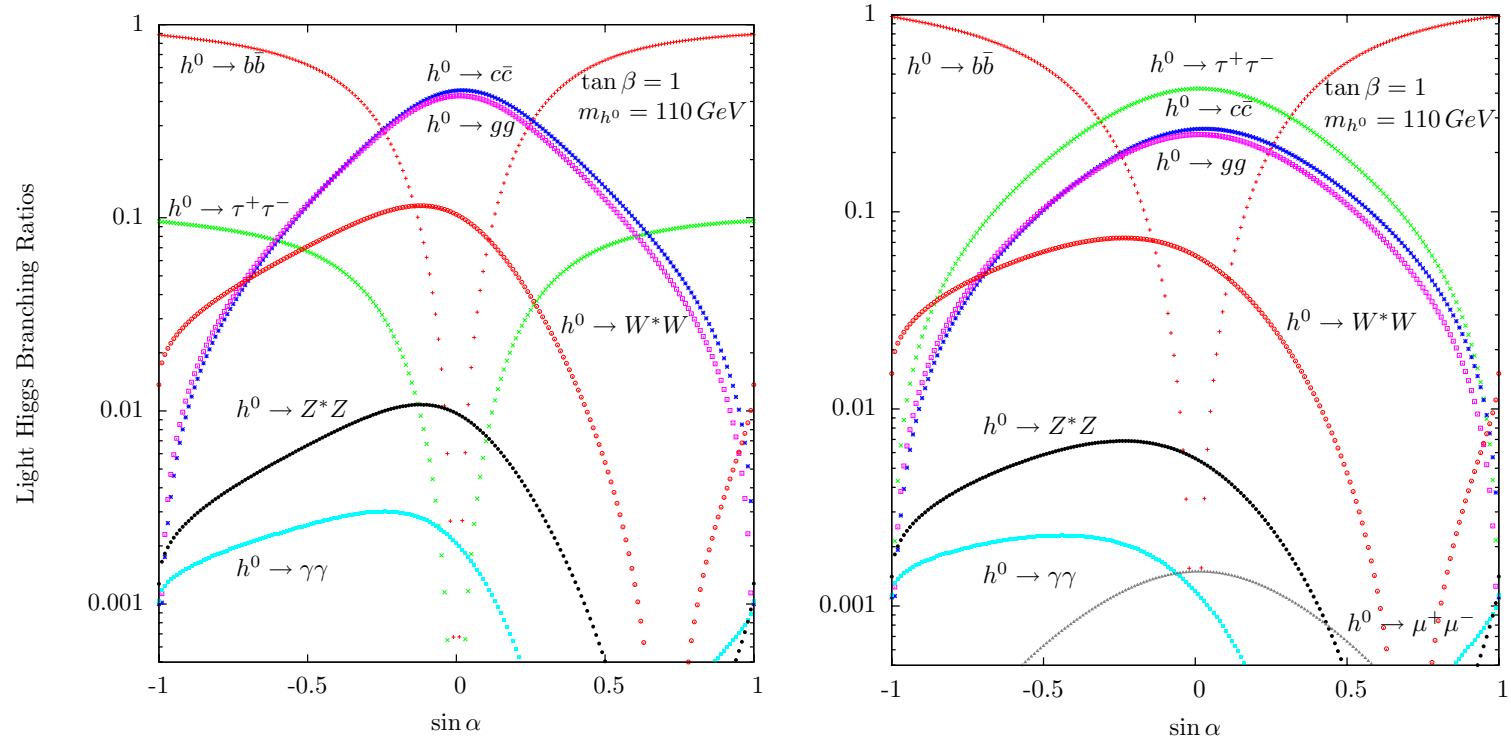


(+ +)

Higgs signatures



Higgs signatures



Left: 2HDM-II , Right 2HDM-X (leptophilic Higgs)

Conclusions

- LHC will be capable to discover the Higgs bosons and measure its coupling to top quark, τ lepton, W and Z with 10–30% accuracy ($\mathcal{L} = 300 fb^{-1}$).
- At LC, the precision of the measurement is about 1–2%, such precision is needed to **distinguish** between models.
- In 2HDM, non decoupling effects could be large to be measured both at LHC and ILC and its $\gamma\gamma$ option.
- If 2HDM Higgs masses are not too heavy, their triple self couplings can be accessible at LHC and ILC