



Higgs, Supersymmetry, and CP Violation

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♠ *Contents*

♠ The 1st part: Introduction to

Higgs, Supersymmetry, CP Violation and the LHC

... Please don't be too picky

♠ The 2nd part: My works on manifestations of

CP Violation through the Supersymmetric Higgs sector

at the LHC and other low-energy experiments

... Please don't feel too sleepy



THE 1ST PART

THE 1st PART

♦ Higgs (1/5)

- Why Particles Physics?

... to find answers to the **Eternal Questions** of

"What is the world made of?"

and

"What holds it together?"

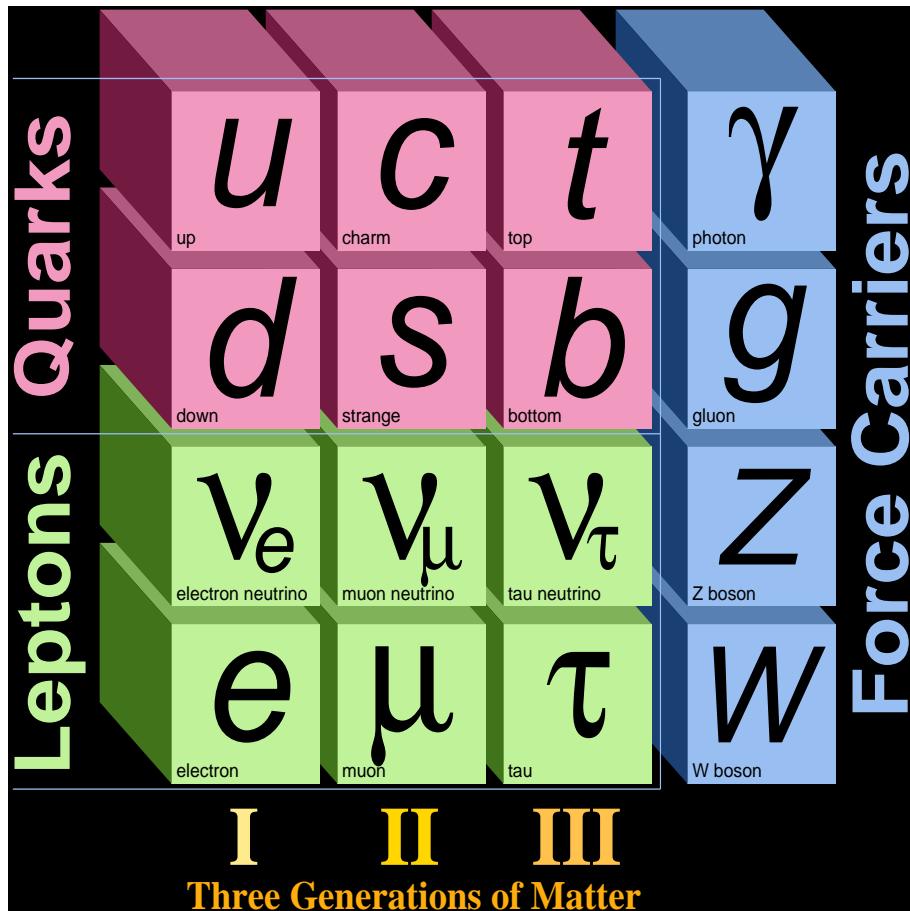
The Particle Adventure

the fundamentals of matter and force

<http://particleadventure.org/particleadventure/>

♦ Higgs (2/5)

- Answers to the Questions in 2011: Standard Model



They are all **Massive** except γ and g

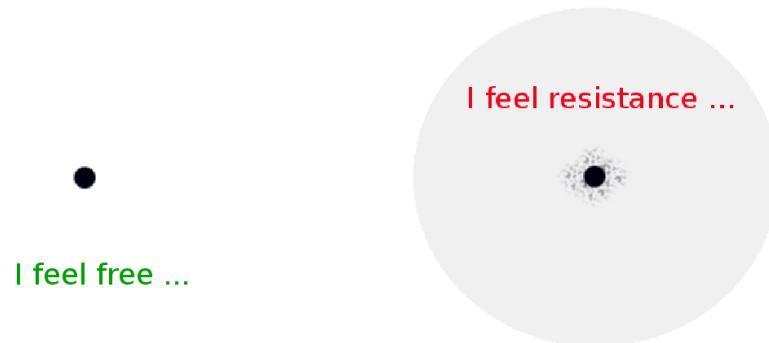
The *BIG* question is :

How do they become massive?

♦ Higgs (3/5)

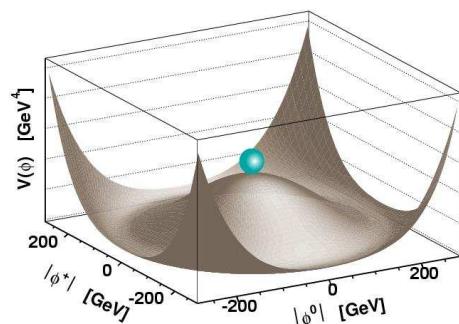
- Spontaneous breaking of Electroweak symmetry Y. Nambu, PRL4(1960)380 Nobel Prize 2008

We are **NOT** living in "True Void" \Rightarrow The "Vacuum" is filled with **Nonvanishing Field Strength** of a scalar field called a **Higgs boson** : $\langle H \rangle_0 \neq 0$



Yukawa interactions $\Rightarrow m_l$ and m_q

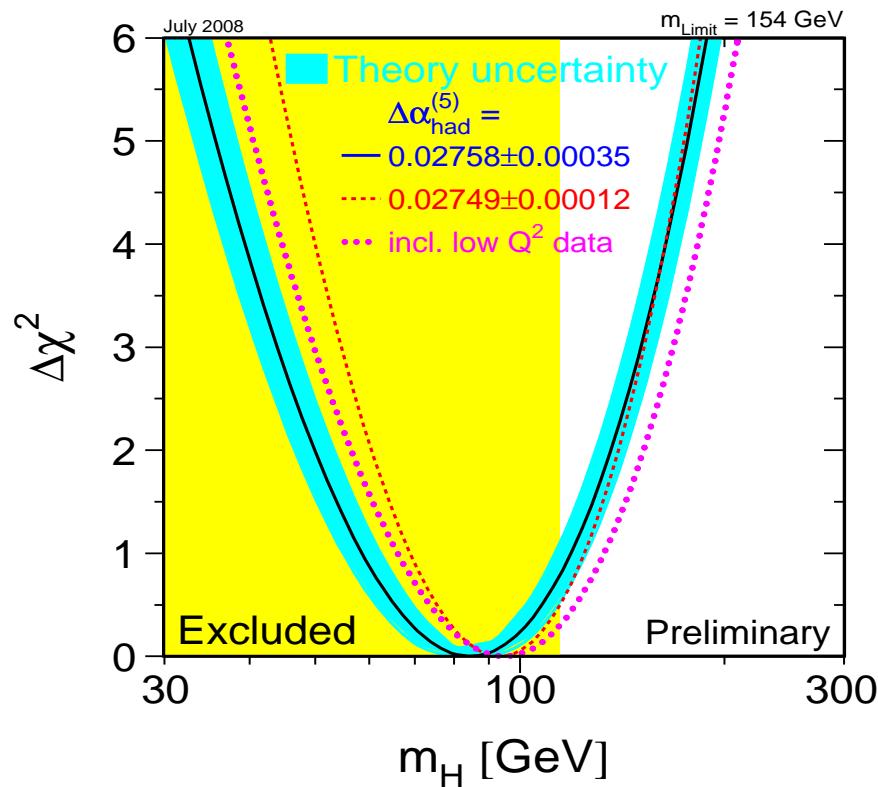
Gauge interactions $\Rightarrow M_W$ and M_Z



* Something else may be needed for m_ν

♠ Higgs (4/5)

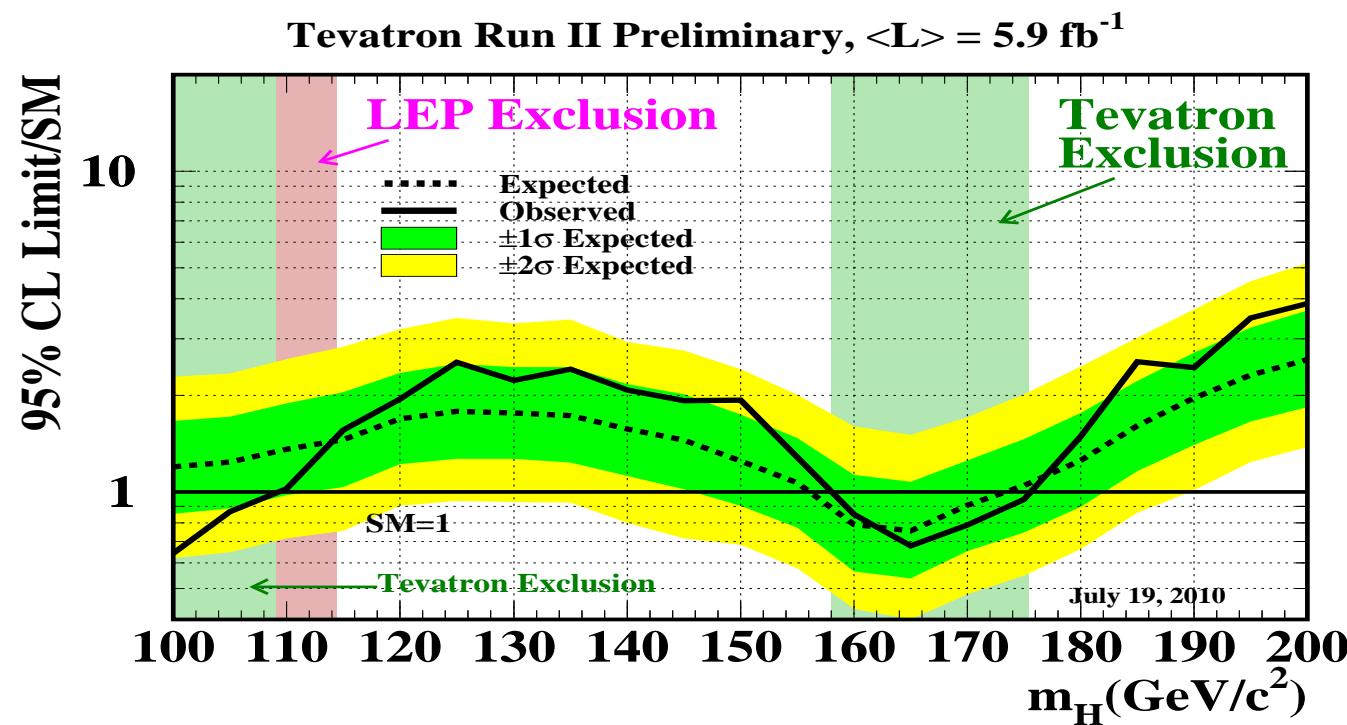
- Status of the SM Higgs:
 - LEP bound: $M_H^{\text{SM}} \geq 114.4 \text{ GeV}$ (95 % C.L.) ADLO, arXiv:hep-ex/0306033
 - Electroweak precision data: $M_H^{\text{SM}} \lesssim 185 \text{ GeV}$ (95 % C.L.) direct-search limit included
ACDDLOS, arXiv:0811.4682[hep-ex]



 Higgs (4'/5)

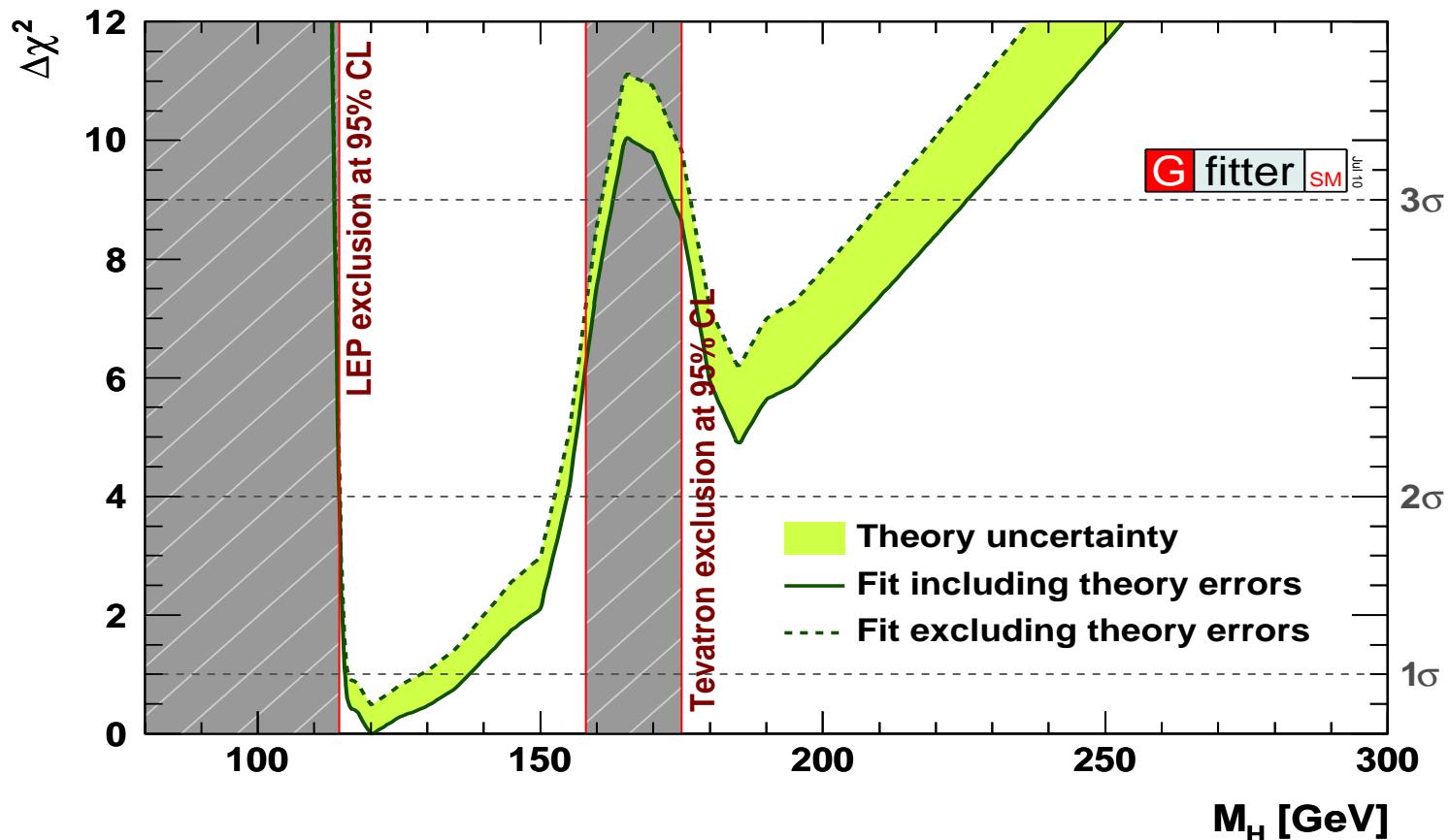
- Status of the SM Higgs: ... *continued*

- Tevatron exclusion: $158 \text{ GeV} \lesssim M_H^{\text{SM}} \lesssim 175 \text{ GeV}$ (95 % C.L.) CDF/D0,
[arXiv:1007.4587\[hep-ex\]](https://arxiv.org/abs/1007.4587)



♠ Higgs: (4''/5)

- Status of the SM Higgs: *combining all...* Gfitter, arXiv:0811.0009



We anticipate the SM Higgs boson lighter than ~ 200 GeV

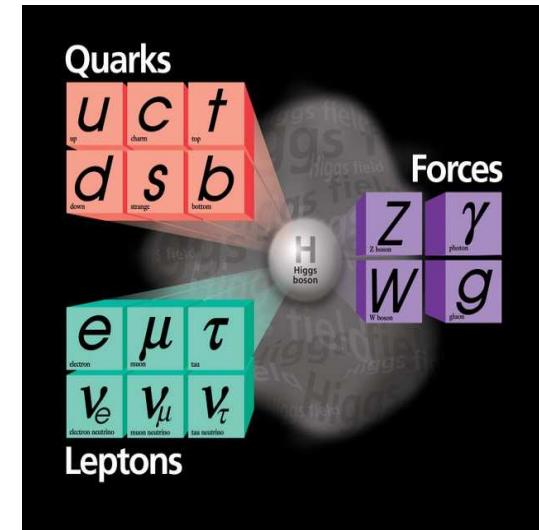
♠ Higgs (5/5)

Higgs = the God particle ?

Answer, What Is the Question?

- elusive ...
- controlling behind indirectly...

and ...

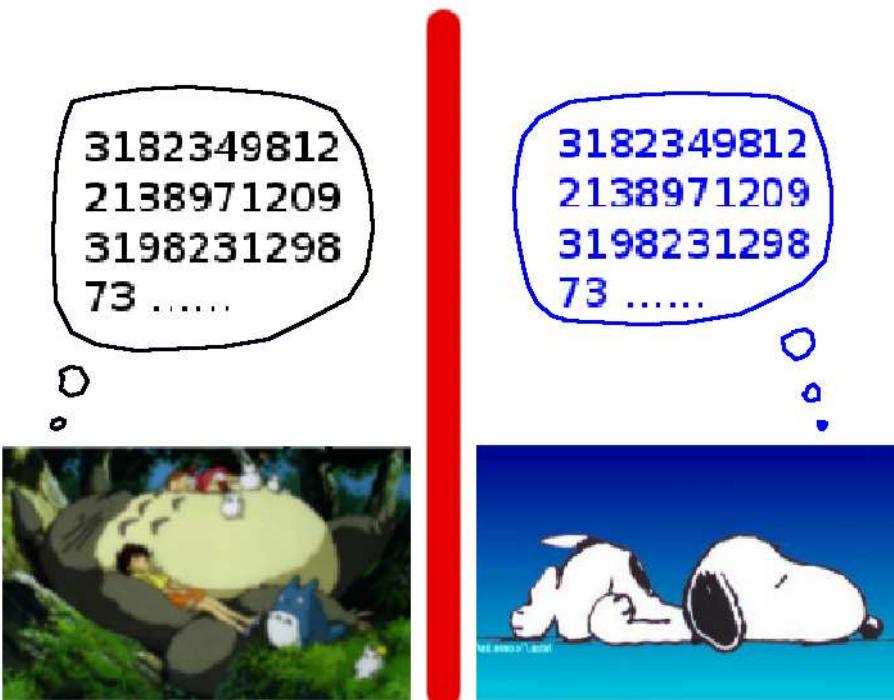


causing conceptual problems ...

♦ *Supersymmetry (1/4)*

- The Naturalness Problem

$$M_H^2 \sim m_0^2 - \frac{\Lambda^2}{16\pi^2} \quad \text{with} \quad \Lambda \sim 10^{19} \text{ GeV} \quad \text{and} \quad M_H \sim 10^2 \text{ GeV}$$



$\mathcal{P} \ll \text{a thunderbolt} \otimes \text{a lottery ticket}$

Isn't it *natural* to
assume
there is *something* ?

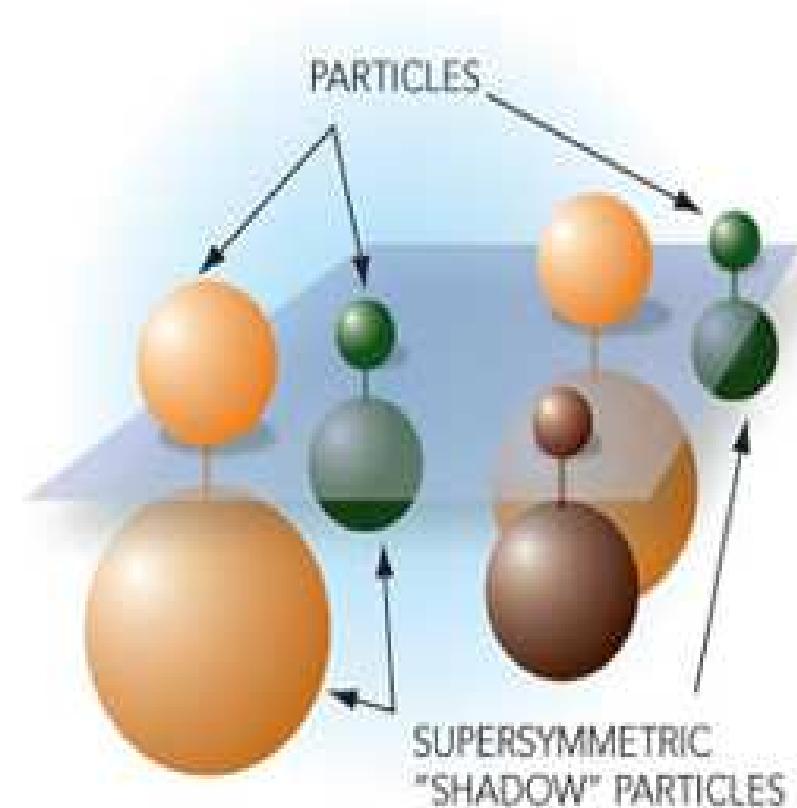
 *Supersymmetry (2/4)*

- Introducing Supersymmetry

$$\delta M_H^2 \sim -\cancel{\Lambda}^2 \text{ (Particles)} + \cancel{\Lambda}^2 \text{ ("S" Particles)} + \underline{M_{\text{SUSY}}^2} \log(\cancel{\Lambda}^2/M_{\text{SUSY}}^2)$$

$$M_{\text{SUSY}} \sim \mathcal{O}(1) \text{ TeV}$$

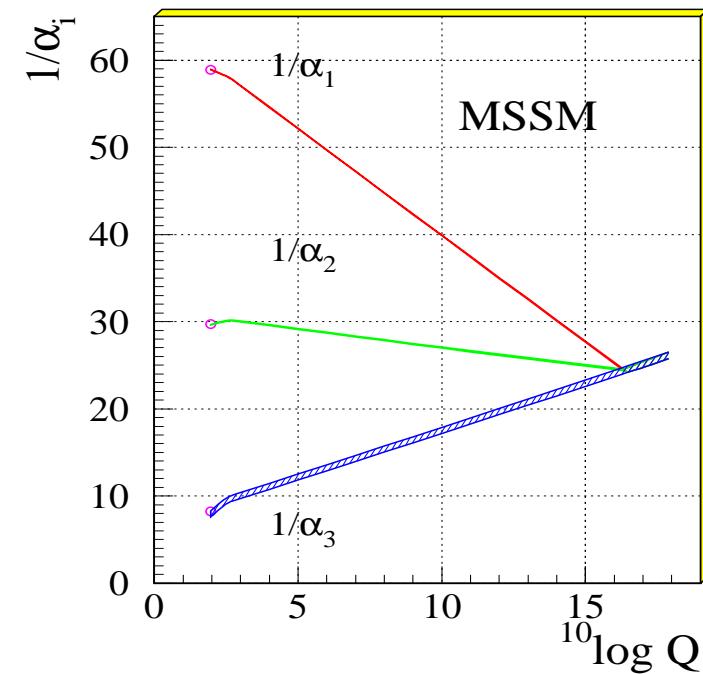
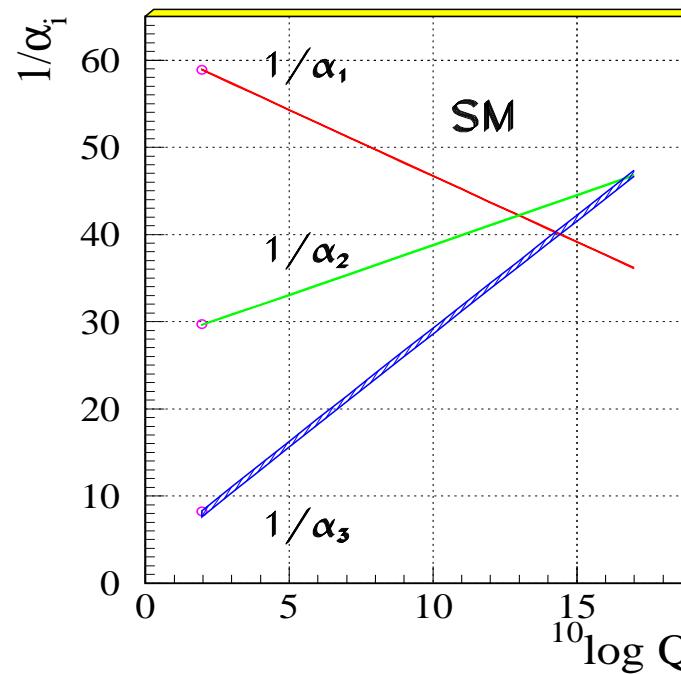
Great Discoveries at the LHC !



 *Supersymmetry (3/4)*

- Support for the existence of "S" Particles (I)

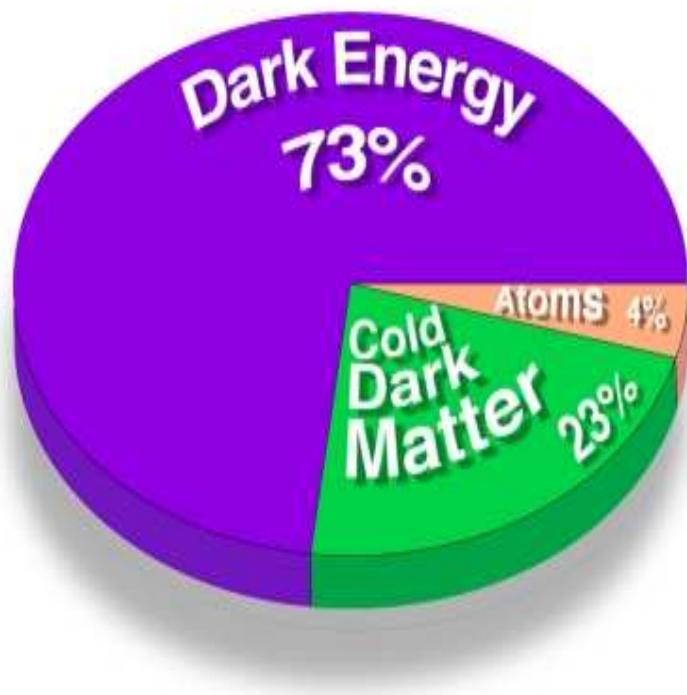
Unification of the Coupling Constants
in the SM and the minimal MSSM



♦ Supersymmetry (4/4)

- Support for the existence of "S" Particles (II)

C. L. Bennett *et al.*, “First Year WMAP Observations: Preliminary Maps and Basic Results,” *Astrophys. J. Suppl.* **148** (2003) 1 [[arXiv:astro-ph/0302207](https://arxiv.org/abs/astro-ph/0302207)]; M. Tegmark *et al.* [SDSS Collaboration], “Cosmological parameters from SDSS and WMAP,” *Phys. Rev. D* **69** (2004) 103501 [[arXiv:astro-ph/0310723](https://arxiv.org/abs/astro-ph/0310723)]; P. Gondolo [[arXiv:hep-ph/0501134](https://arxiv.org/abs/hep-ph/0501134)]



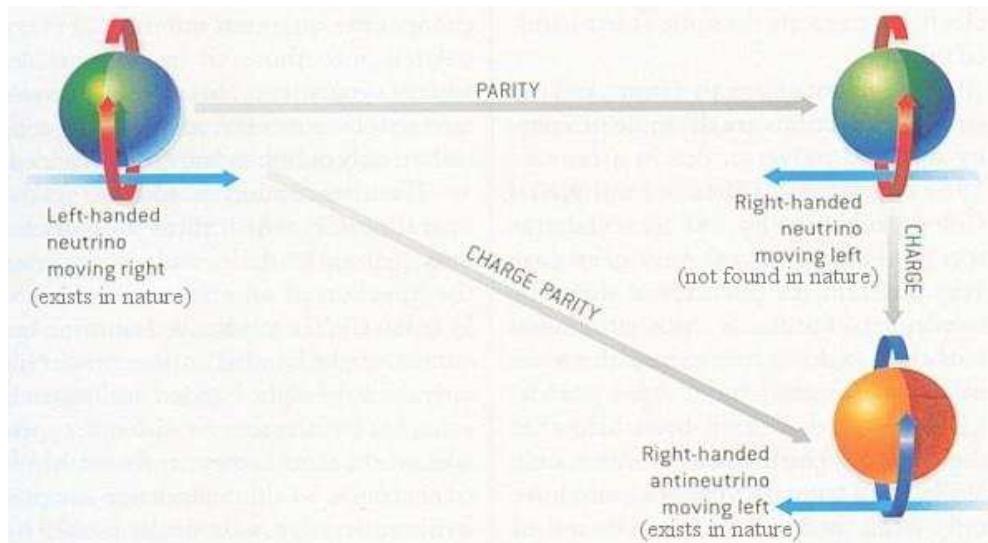
Source: Robert Kirshner
Source: NASA/WMAP Science Team

$$\begin{aligned}\Omega_\Lambda &= 0.72 \pm 0.08 \\ \Omega_m &= 0.27 \pm 0.016 \\ &= \begin{cases} \Omega_b &= 0.0448 \pm 0.0018 \\ \Omega_{\text{CDM}} &= 0.226 \pm 0.0016 \end{cases}\end{aligned}$$

CDM = Lightest Supersymmetric Particle ?

♦ CP violation (1/4)

- What is CP Violation?:



<http://universe-review.ca>

If Nature treated

Left-handed particle moving right and

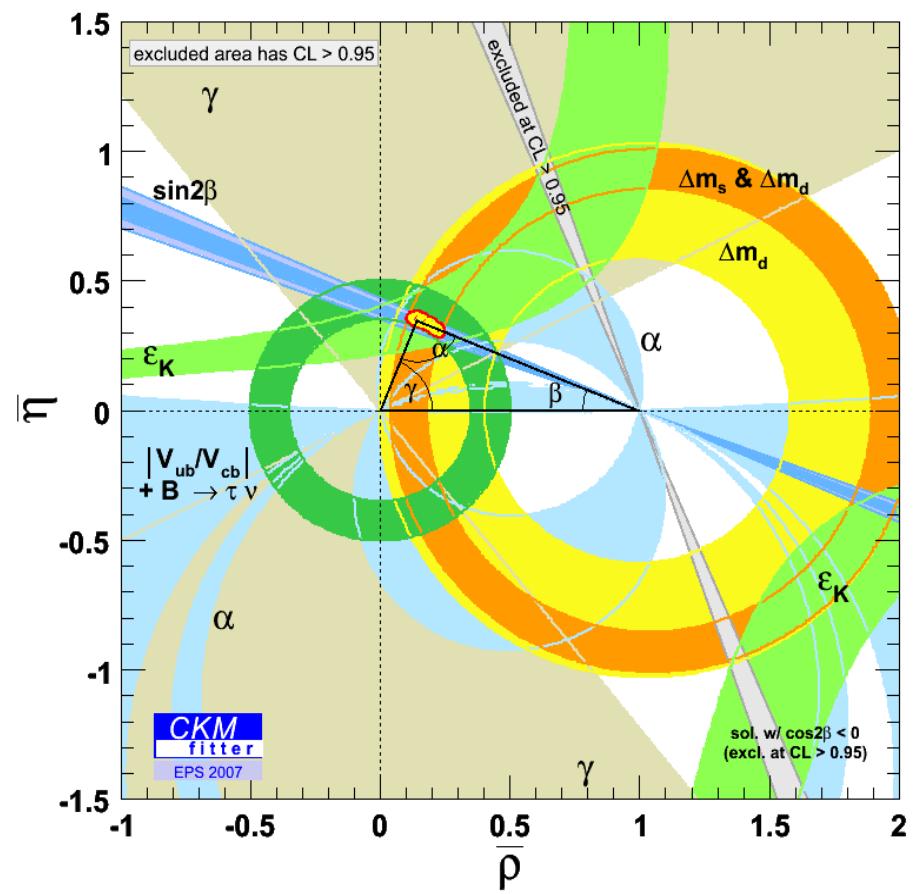
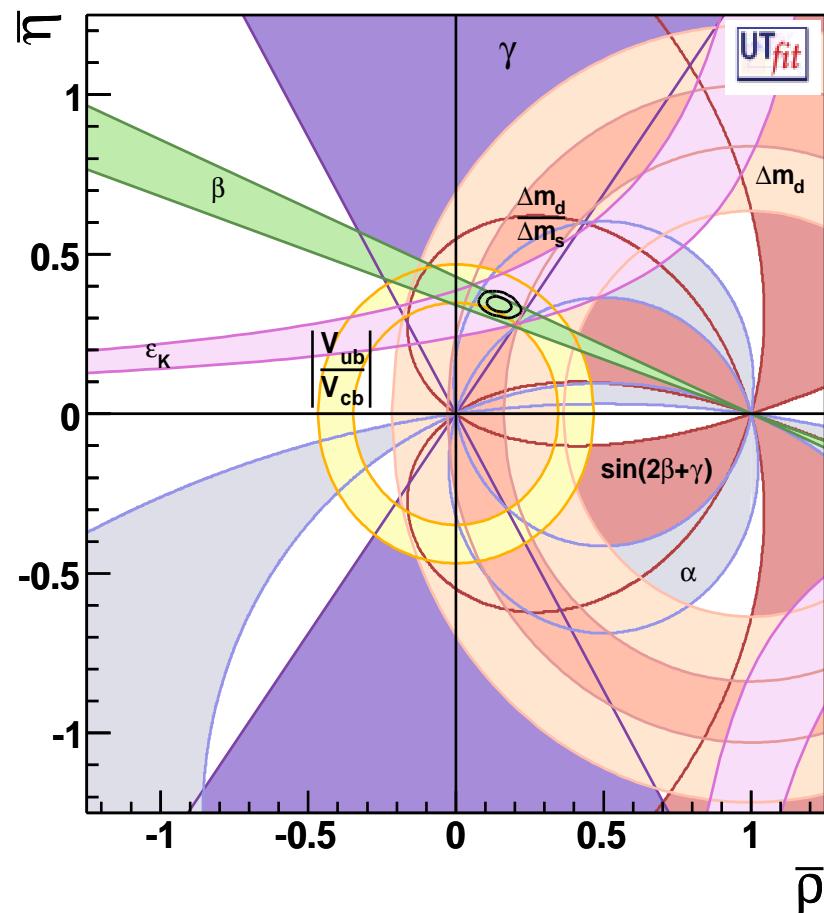
Right-handed antiparticle moving left

differently, we are saying

CP is violated

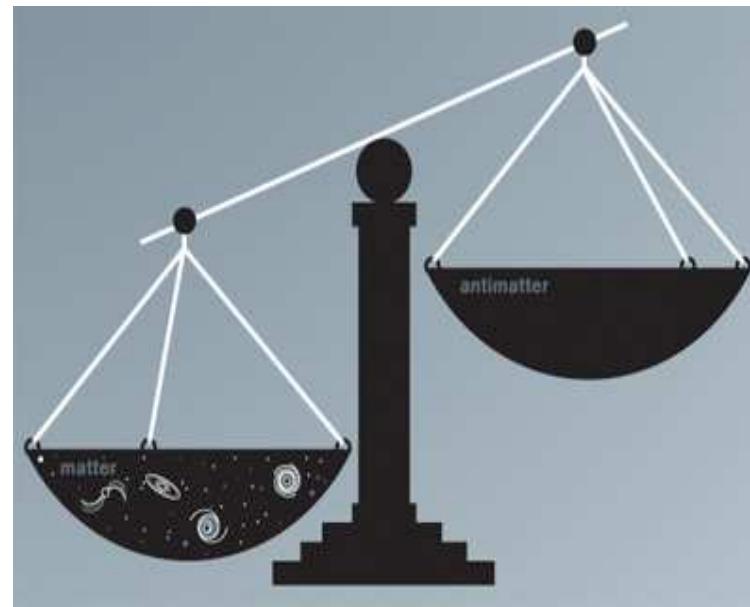
♠ *CP violation (2/4)*

- Why CP Violation?: \Rightarrow There **IS** CP Violation! M. Kobayashi and T. Maskawa, Prog. Theor. Phys. **49** (1973) 652 *Nobel Prize 2008*



♠ *CP violation (3/4)*

- Then, who ordered "more" CP violation beyond the SM CKM phase? [A. D. Sakharov](#),
[JETP Letters 5\(1967\)24](#)



CP violation in the SM is too weak to explain the matter dominance of the Universe [J. Cline](#),
[arXiv:hep-ph/0609145](#)

The matter-dominated Universe did!

♠ *CP violation (4/4)*

- Even the minimal SUSY model contains many possible sources of **CP** violation:

– Gaugino mass terms: $3 \oplus 3 = 6$

$$-\mathcal{L}_{\text{soft}} \supset \frac{1}{2} (\textcolor{red}{M}_3 \widetilde{g}\widetilde{g} + \textcolor{red}{M}_2 \widetilde{W}\widetilde{W} + \textcolor{red}{M}_1 \widetilde{B}\widetilde{B} + \text{h.c.})$$

– Trilinear **a** terms $\mathbf{a}_{\mathbf{f}ij} \equiv \mathbf{h}_{\mathbf{f}ij} \cdot \mathbf{A}_{\mathbf{f}ij}$: $3 \times (3 \oplus 6 \oplus 9) = 54$

$$-\mathcal{L}_{\text{soft}} \supset (\widetilde{u}_R^* \mathbf{a}_{\mathbf{u}} \widetilde{Q} H_2 - \widetilde{d}_R^* \mathbf{a}_{\mathbf{d}} \widetilde{Q} H_1 - \widetilde{e}_R^* \mathbf{a}_{\mathbf{e}} \widetilde{L} H_1 + \text{h.c.})$$

– Sfermion mass terms: $5 \times (3 \oplus 3 \oplus 3) = 45$

$$-\mathcal{L}_{\text{soft}} \supset \widetilde{Q}^\dagger \mathbf{M}_{\widetilde{Q}}^2 \widetilde{Q} + \widetilde{L}^\dagger \mathbf{M}_{\widetilde{L}}^2 \widetilde{L} + \widetilde{u}_R^* \mathbf{M}_{\widetilde{\mathbf{u}}}^2 \widetilde{u}_R + \widetilde{d}_R^* \mathbf{M}_{\widetilde{\mathbf{d}}}^2 \widetilde{d}_R + \widetilde{e}_R^* \mathbf{M}_{\widetilde{\mathbf{e}}}^2 \widetilde{e}_R$$

1 KM phase (SM) \implies 1 + 45 (Minimal SUSY Model)

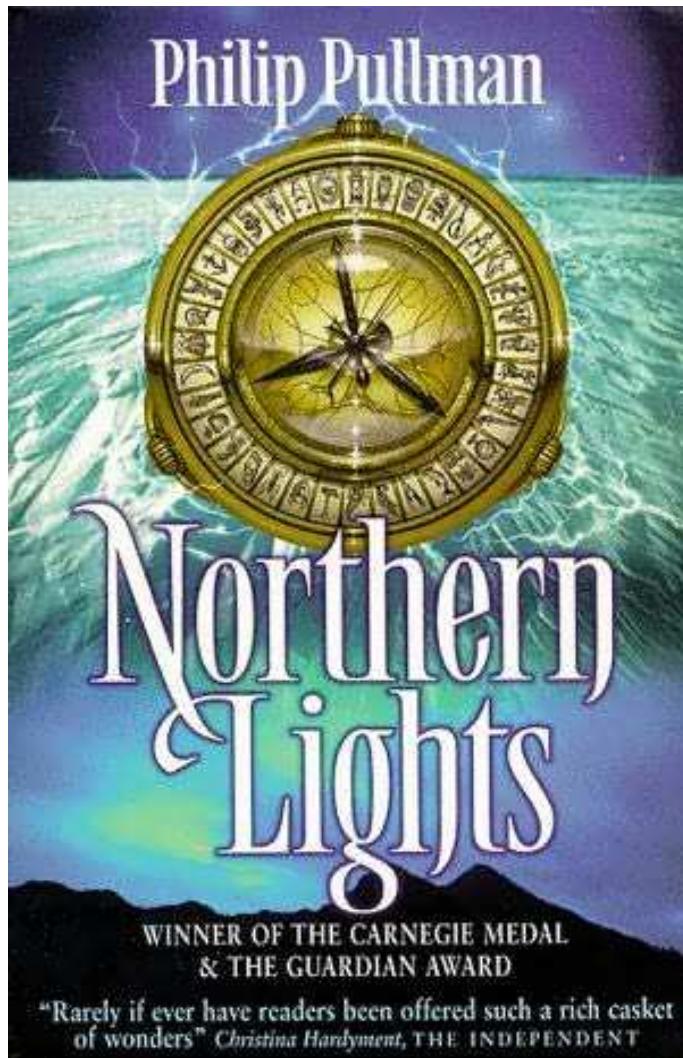
♠ LHC (1/6)

- LHC = the Large Hadron Collider



♦ LHC (1'/6)

- LHC = the Large Hadron Collider



“Human beings can't see anything without wanting to destroy it, Lyra, *That's* original sin. And I'm going to destroy it.”

... Lord Asriel

HIS DARK MATERIALS trilogy #1

♠ LHC (2/6)



- Two protons collide with a kinetic energy of 14 TeV $1 \text{ GeV} \simeq \text{a proton mass}$
- then the two protons are *destroyed* to disappear and we will see something ...

♠ LHC (3/6)

- Past and present ...

1989 : R&D starts

1997 : Construction starts

2003 : Underground installation starts

2008 : Installation completed

11 Sep 2008 : First beam circulated

20 Sep 2008 : Magnet failures ...

23 Nov 2009 : First collisions at $\sqrt{s} = 900$ GeV

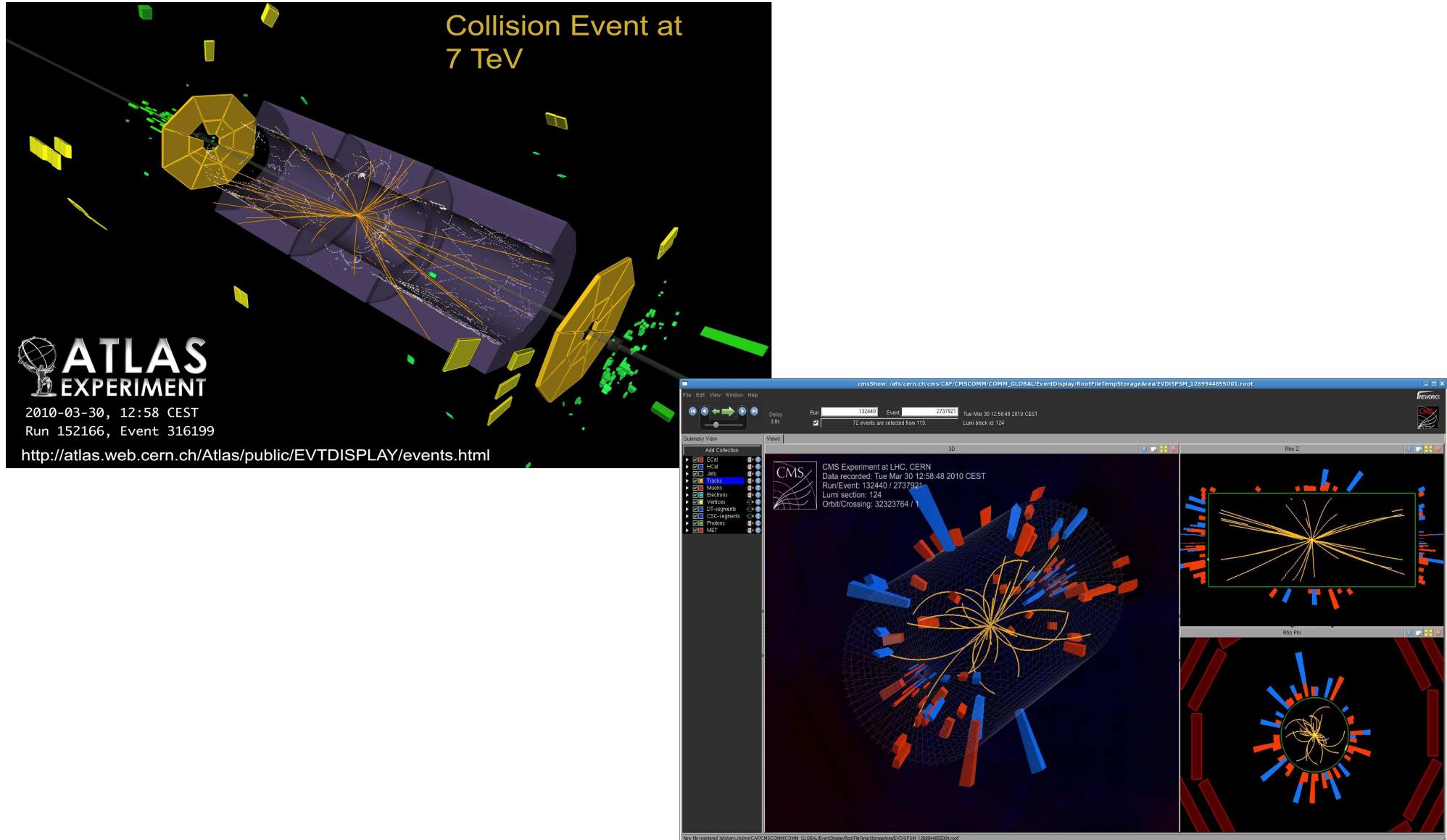
8 Dec 2009 : First collisions at $\sqrt{s} = 2.36$ TeV

30 Mar 2010 : First collisions at $\sqrt{s} = 7$ TeV



From Junichi Kanzaki's talk @ KEKPH2010

♠ LHC (3'/6)



♠ *LHC* (4/6)

- ... and near/far future of the LHC

2010 ~ 2011 : 7 TeV (3.5+3.5 TeV) runs until 1 fb^{-1} *LHC 1/2*

⇒ For SUSY searches with 35 pb^{-1} , see next page

2012 ~ 2012 : Shutdown for repairing to achieve 7 (6.5) TeV/beam collisions

2013 ~ 2014 : Go to 7 (6.5) + 7 (6.5) TeV runs to get $\sim 10 \text{ fb}^{-1}$ *LHC*

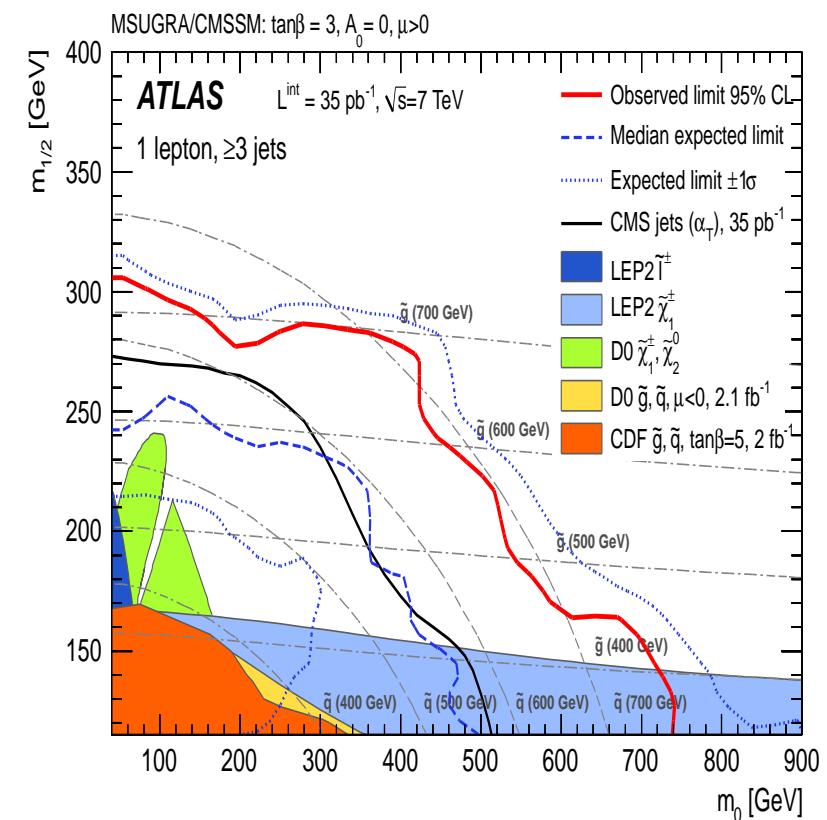
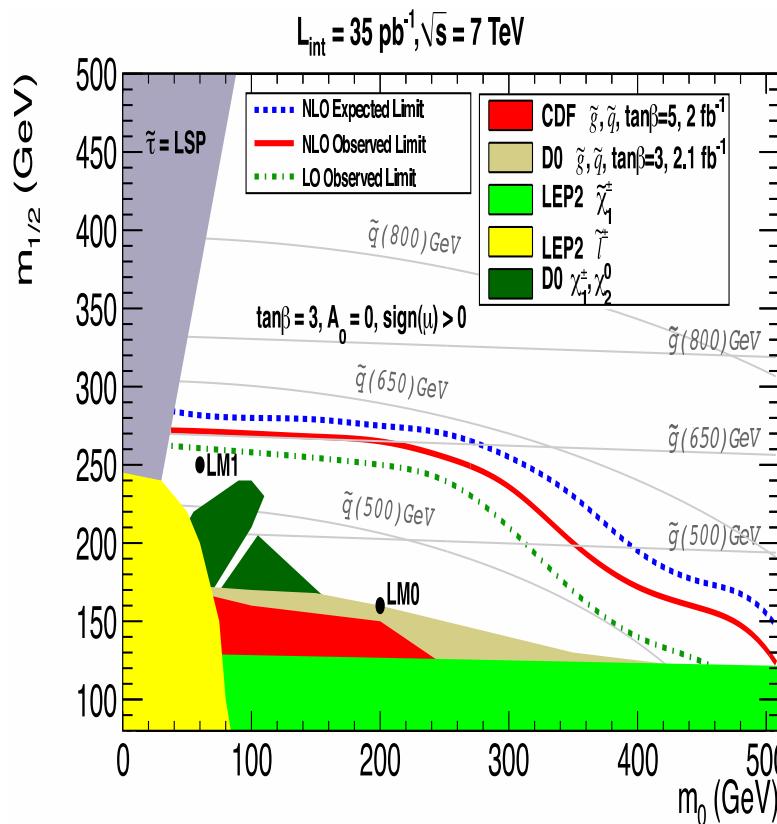
2015 ~ 202? : accumulate 3000 fb^{-1} with $250 \sim 300 \text{ fb}^{-1}$ per year

again, from Junichi Kanzaki's talk @ KEKPH2010, or
LHC Performance Workshop - Chamonix 2010 (Jan)

♠ *Initial SUSY searches with 35 pb^{-1} at the LHC*

- CMS (jets + missing E_T ; left) and ATLAS (lepton + jets + missing E_T ; right)

CMS, PLB698(2011)196,2011, arXiv:1101.1628 [hep-ex] and ATLAS, arXiv:1102.2357 [hep-ex]



ATLAS, more stringent ...

♦ *LHC (4'/6)*

- ... and near/far future of the LHC

2010 ~ 2011 : 7 TeV (3.5+3.5 TeV) runs until 1 fb^{-1} *LHC 1/2*

2012 ~ 2012 : Shutdown for repairing to achieve 7 (6.5) TeV/beam collisions

2013 ~ 2014 : Go to 7 (6.5) + 7 (6.5) TeV runs to get $\sim 10 \text{ fb}^{-1}$ *LHC*

2015 ~ 202? : accumulate 3000 fb^{-1} with $250 \sim 300 \text{ fb}^{-1}$ per year

again, from Junichi Kanzaki's talk @ KEKPH2010, or
LHC Performance Workshop - Chamonix 2010 (Jan)

♦ LHC (5/6)

- ... and near/far future of the LHC: ... *continued*

$3000 \text{ fb}^{-1} \approx 2,400,000,000 \text{ } t\bar{t}$ pairs : Top factory

$\approx 100,000,000$ 130 GeV SM Higgs bosons

$\approx 3,000,000$ $\mathcal{O}(1)$ TeV gluinos + squarks

$\approx 300,000$ $\mathcal{O}(1)$ TeV charginos + neutralinos

♠ LHC (6/6)

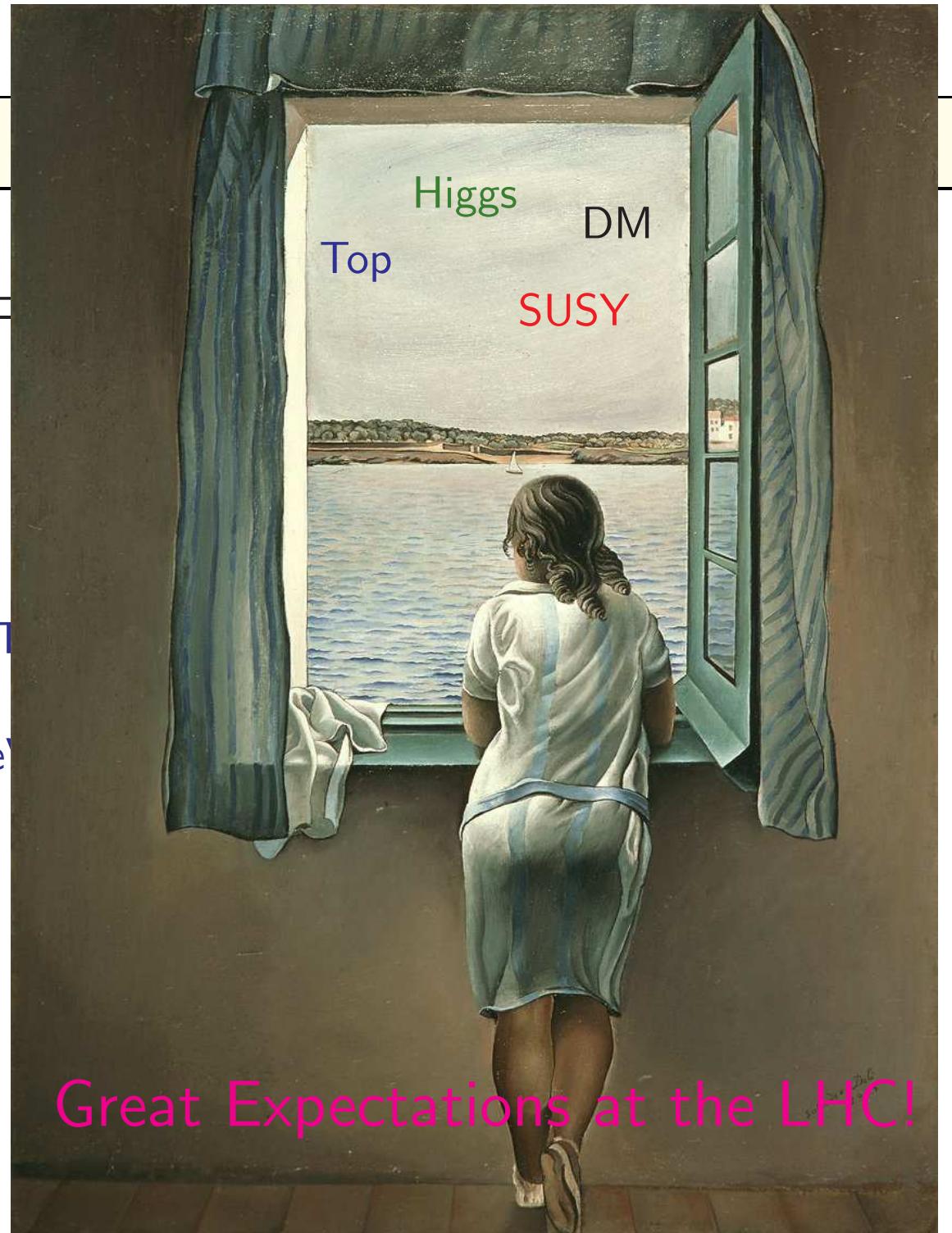
- ... and near/far future of the LHC

$3000 \text{ fb}^{-1} \approx 2,400,000,000 \text{ } t\bar{t}$

$\approx 100,000,000 \text{ } 130$

$\approx 3,000,000 \mathcal{O}(1) \text{ TeV}$

$\approx 300,000 \mathcal{O}(1) \text{ TeV}$





THE 2ND PART

THE 2nd PART

♠ Preliminary (1/4)

- The Nobel Prize in Physics 2008: "*Passion for symmetry*" (*broken?*)



The Nobel Prize in Physics 2008

"for the discovery of the mechanism of spontaneous broken symmetry in subatomic physics"

"for the discovery of the origin of the broken symmetry which predicts the existence of at least three families of quarks in nature"



Photo: University of Chicago

Yoichiro Nambu



Photo: KOK

Makoto Kobayashi

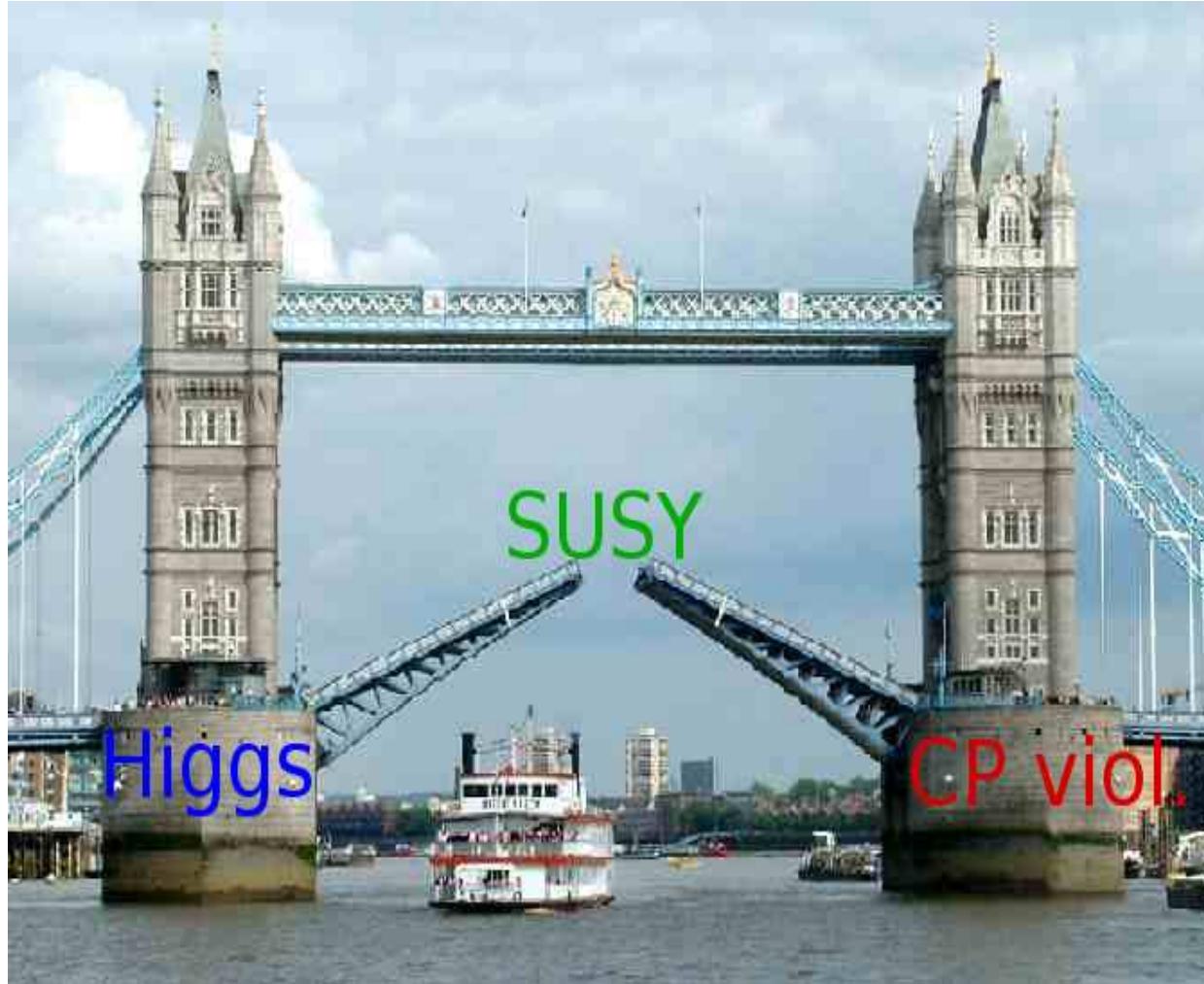


Photo: Kyoto University

Toshihide Maskawa

♠ Preliminary (2/4)

- My works aim at ...:



♠ Preliminary (3/4)

- Introducing SUSY \implies Introducing lots of additional CP phases ! :

1 KM phase (SM) \implies 1 + 45 (Minimal SUSY Model)

My Question:

How does the SUSY CP violation manifest itself through the Higgs sector ?

more specifically,

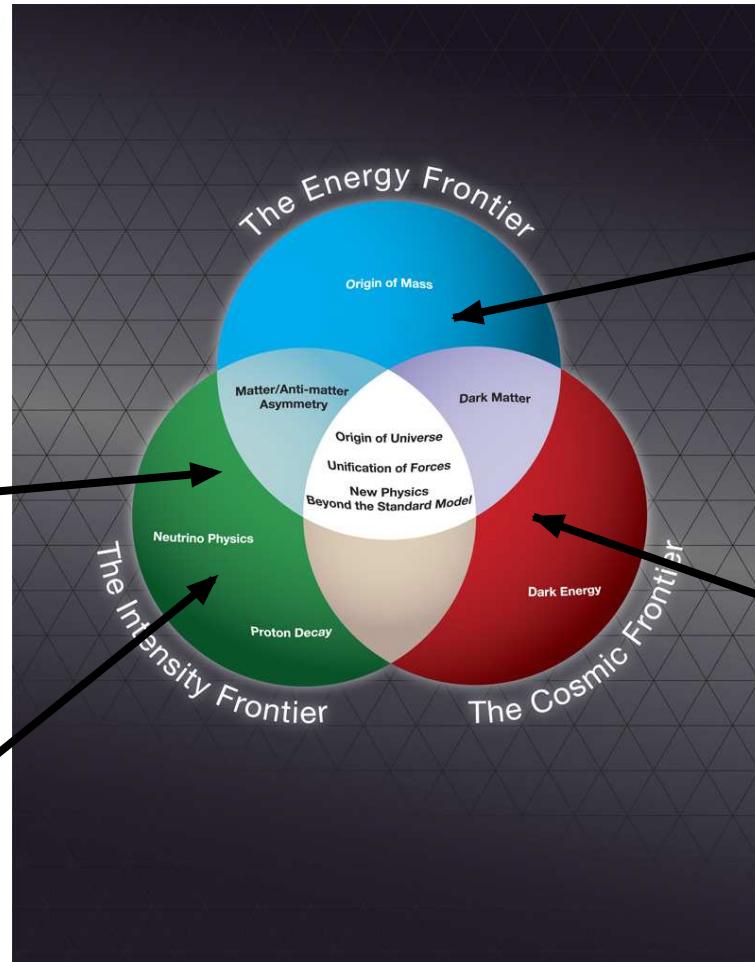
Where to find it?

and

Why through Higgs sector?

♠ Preliminary (4/4)

- Where to find it?



Colliders : LHC

{
SM Higgs
MSSM Higgs
CPV Signatures

Dark Matter

{
 $\chi\chi \rightarrow \gamma, \bar{p}, etc$

B-meson Observables

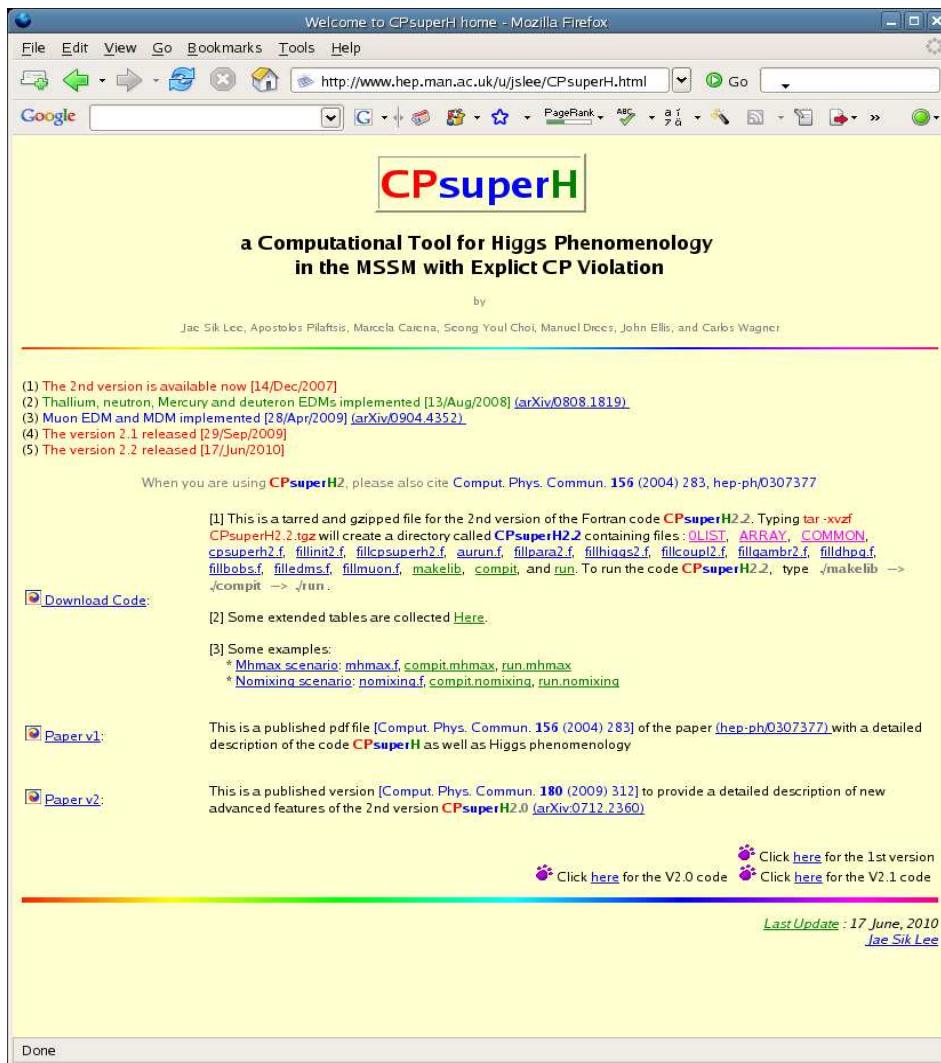
{
 $\Delta M_{B_{d,s}}, B_s \rightarrow \mu^+ \mu^- ,$
 $B \rightarrow \tau\nu, B \rightarrow X_s \gamma ,$
 \dots

Electric Dipole Moments

- Why through Higgs sector?
 - Experimental Side: LHC
 - * Higgs boson will be searched most intensively
 - * Higgs boson will be studied most extensively
 - Theoretical Side: Quantum sensitivity
 - * Large quantum correction
 - * Resonant enhancement

♠ CPsuperH

- Tool: CPsuperH : △ RG-improved effective potential approach



- For *experimentalists* as well as phenomenologists who are exploring the MSSM Higgs sector both in *CP-conserving* and *CP-violating* cases V. M. Abazov *et al.* [D0 Collaboration], “Search for neutral supersymmetric Higgs bosons in multijet events at $s^{**}(1/2) = 1.96\text{-TeV}$,” Phys. Rev. Lett. **95** (2005) 151801 [[arXiv:hep-ex/0504018](#)]; A. Abulencia *et al.* [CDF Collaboration], “Search for charged Higgs bosons from top quark decays in $p\bar{p}$ collisions at $\sqrt{s} = 1.96\text{-TeV}$,” Phys. Rev. Lett. **96** (2006) 042003 [[arXiv:hep-ex/0510065](#)].
- *Consistent computational tool for both Energy- and Intensity-Frontier experiments including several B observables and EDMs*

♠ Where to find it ?

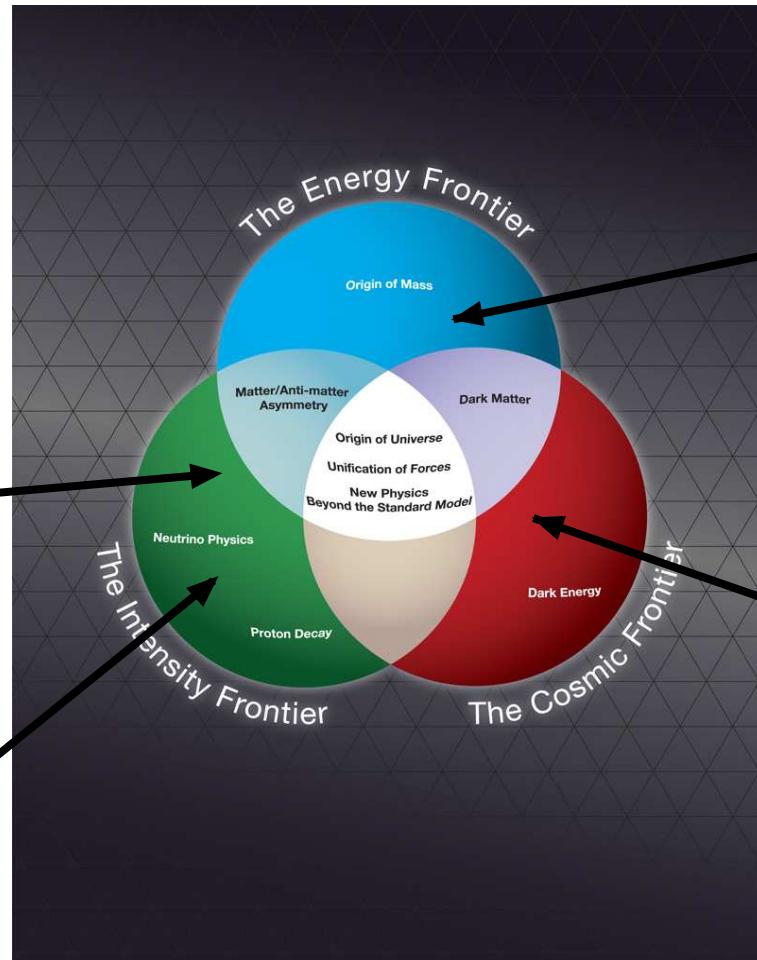
II-A

Colliders

B-meson Observables

$\left\{ \Delta M_{B_{d,s}}, B_s \rightarrow \mu^+ \mu^- , B \rightarrow \tau \nu, B \rightarrow X_s \gamma, \dots \right.$

Electric Dipole Moments



Colliders : LHC

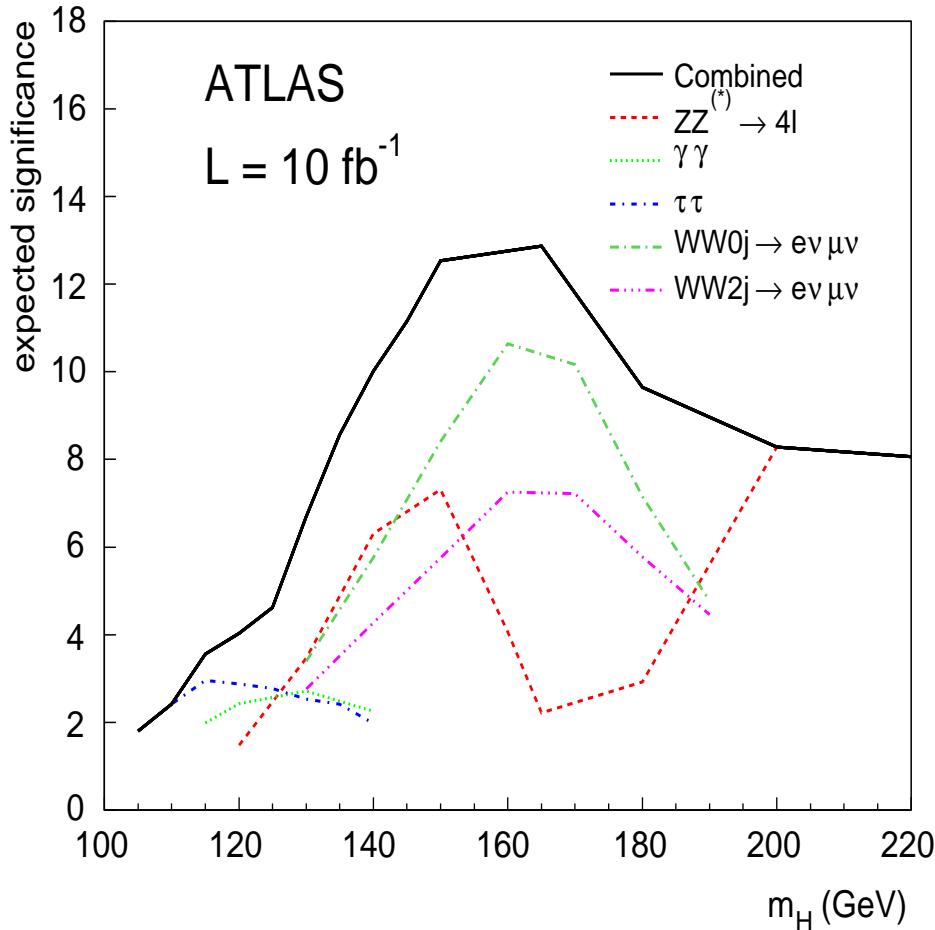
{ SM Higgs
MSSM Higgs
CPV Signatures

Dark Matter

{ $\chi \chi \rightarrow \gamma, \bar{p}, \text{etc}$

♠ SM Higgs (1/2)

- LHC Discovery Significance of the SM Higgs [ATLAS TDR, arXiv:0901.0512\[hep-ex\]](#)

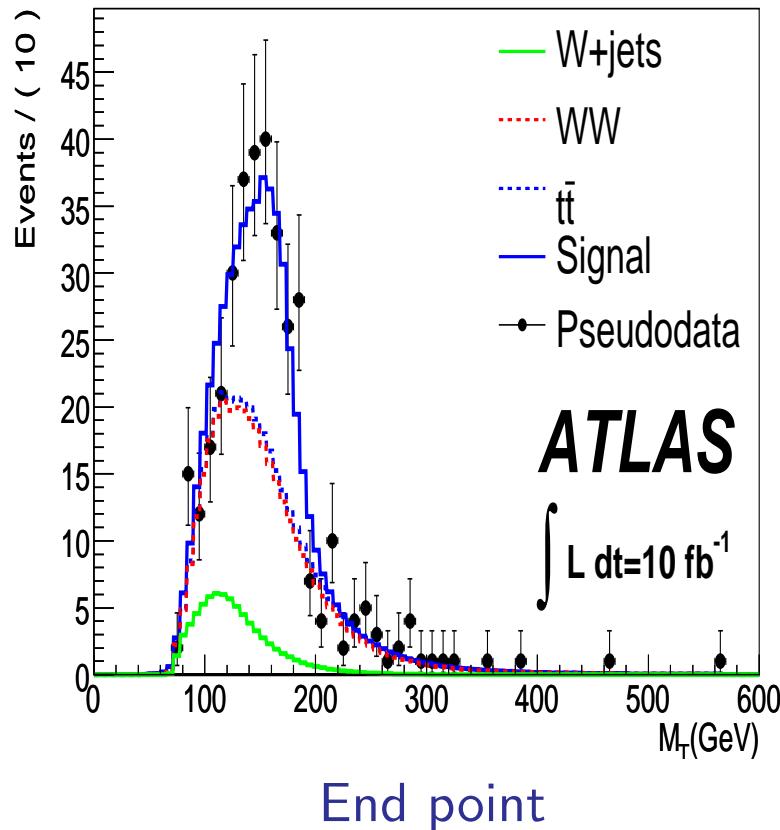


- $H \rightarrow \tau\tau$
- $H \rightarrow \gamma\gamma$
- ▷ $H \rightarrow WW^* \rightarrow l\nu l\nu$ (GF)
- ▷ $H \rightarrow WW^* \rightarrow l\nu l\nu$ (VBF)
- $H \rightarrow ZZ^{(*)} \rightarrow 4l$

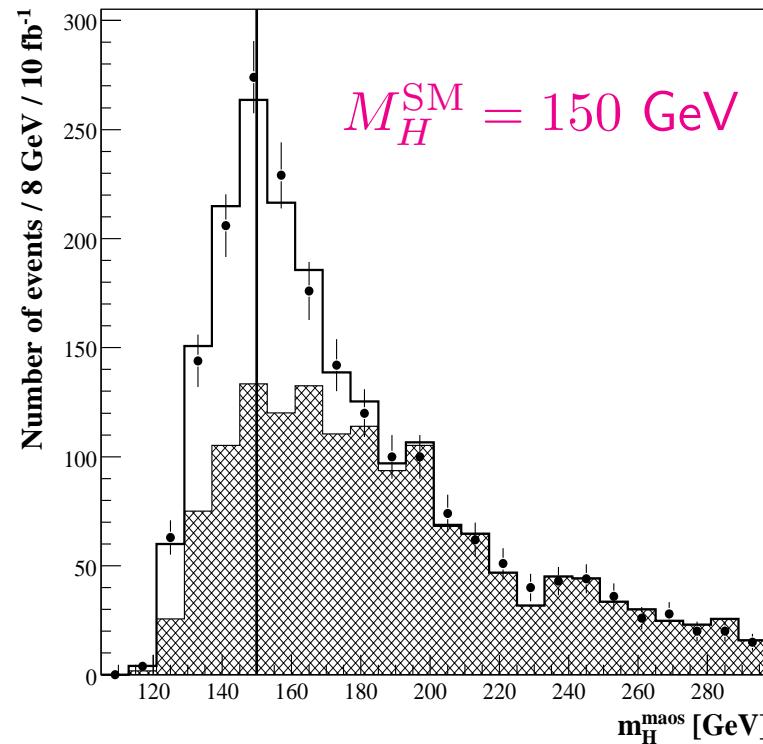
The WW channel plays a dominant role for $130 \text{ GeV} \lesssim M_H \lesssim 190 \text{ GeV}$!

♦ *SM Higgs (2/2)*

- The 2 missing neutrinos: Transverse mass vs. MAOS Higgs mass



End point



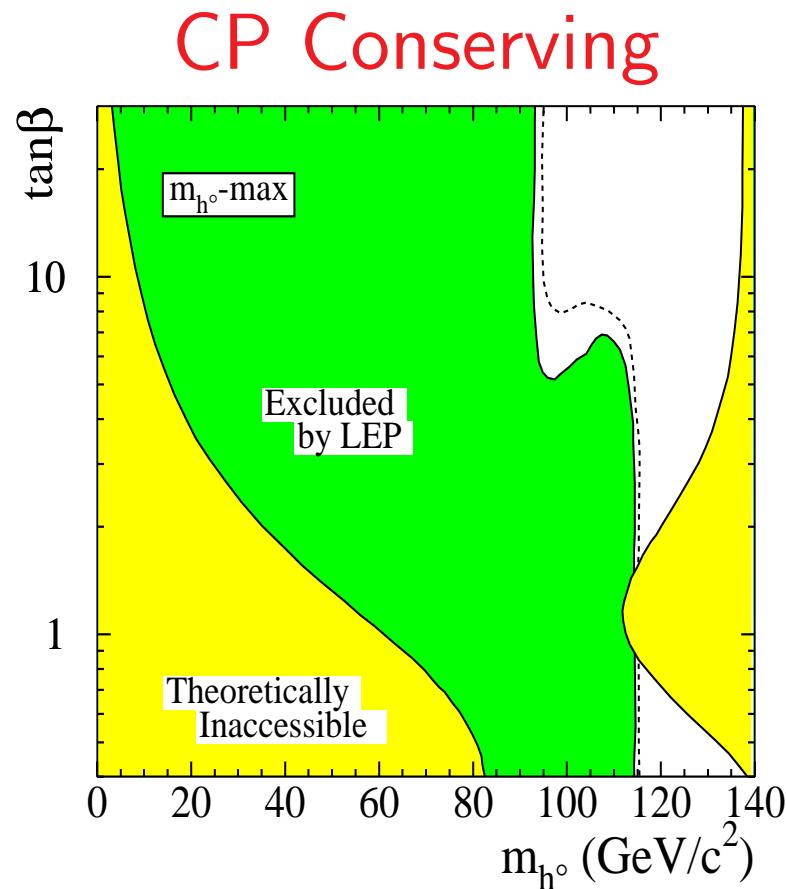
Mass peak

K. Choi, S. Choi, JSL, C.B. Park, PRD**80** (2009) 073010;

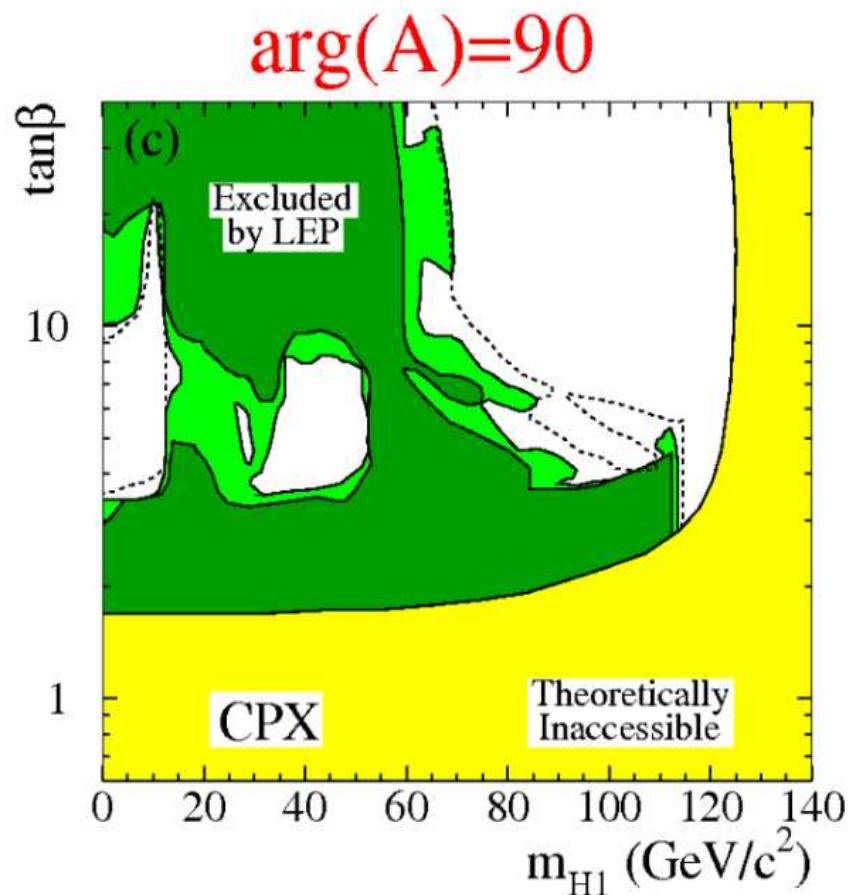
K. Choi, JSL, C.B. Park, arXiv:1008.2690 [hep-ph], to appear in PRD

♠ MSSM Higgs (1/2)

- LEP Limits on the MSSM Higgs: A. Djouadi, hep-ph/0503173 and references there in: P. Bechtle, CPNSH Report, CERN-2006-009, hep-ph/0608079; ADLO, hep-ex/0602042, Combined results with FeynHiggs



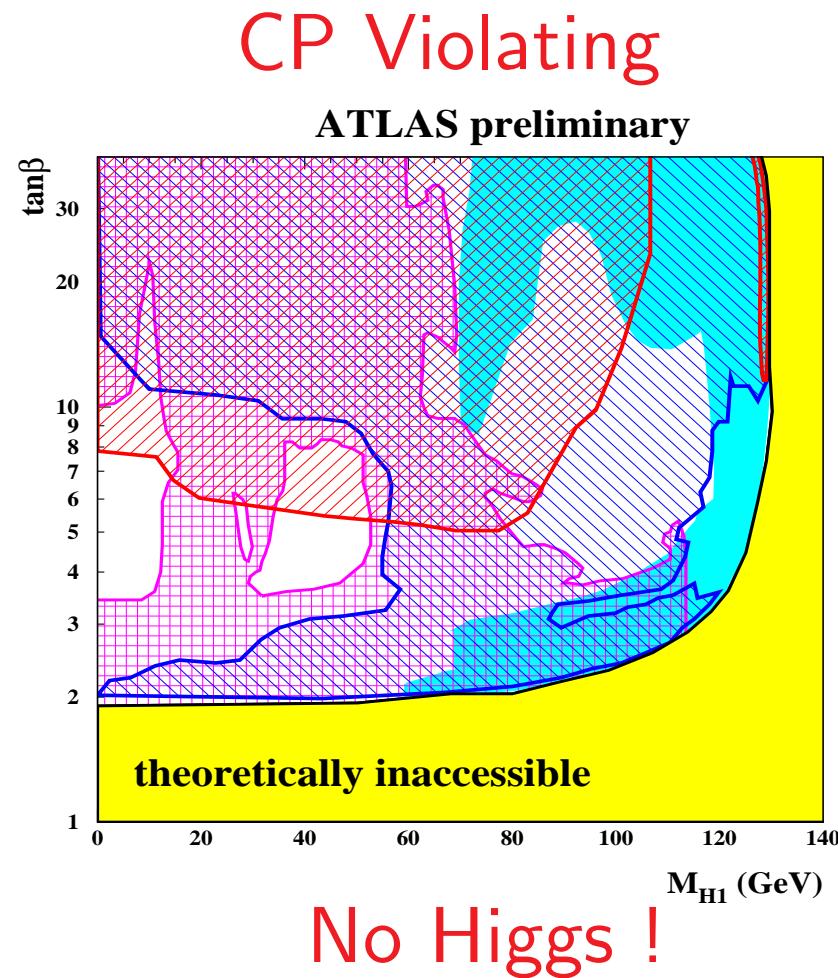
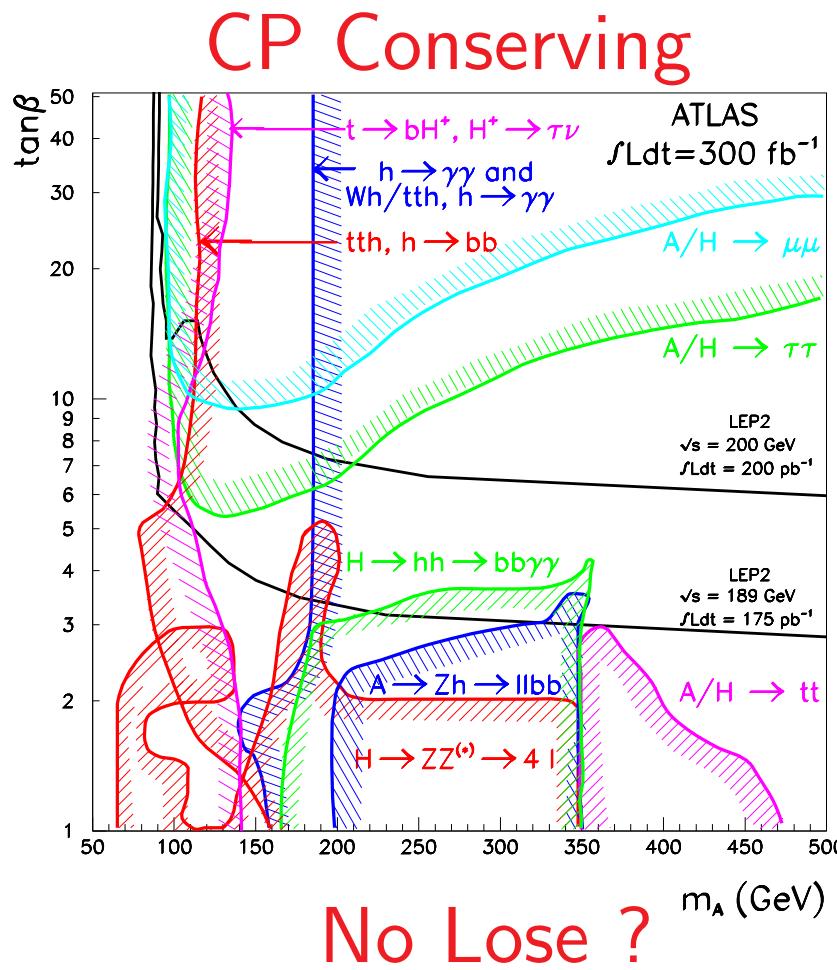
$M_{H_1} \gtrsim 90 \text{ GeV} ?$



$M_{H_1} \lesssim 10 \text{ GeV} !$

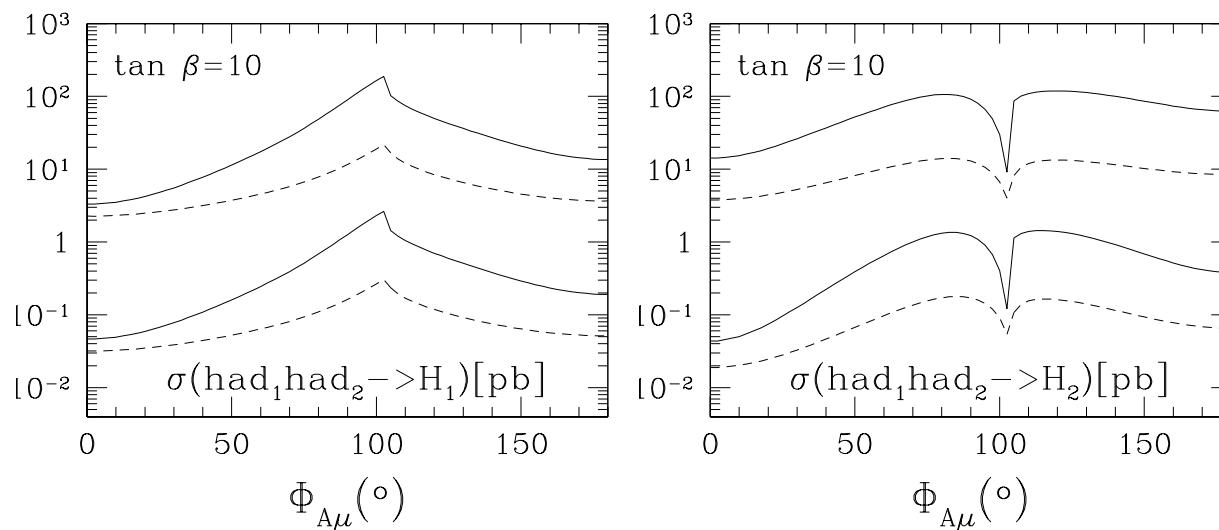
♠ MSSM Higgs (2/2)

- LHC Discovery of the MSSM Higgs: ATLAS TDR(1999); M. Schumacher, CPNSH Report, CERN-2006-009, hep-ph/0608079



♦ *b-quark Fusion (1/2)*

- Strong dependence of Higgs-boson production via *b*-quark fusion on CP phases: [CPX](#)
 Scenario with $\Phi_3 = 0^\circ$ or $\Phi_3 = 180^\circ$ and $M_{H_1} = 115$ GeV. F. Borzumati and JSL, [PLB595\(2004\)347](#) and [PLB641\(2006\)486](#)



- * Solid: $\Phi_3 = 180^\circ$ and Dashed: $\Phi_3 = 0^\circ$
- * Around $\Phi_{A\mu} = 100^\circ$, $M_{H_2} - M_{H_1} \simeq 3$ GeV \implies Distinguishable ?

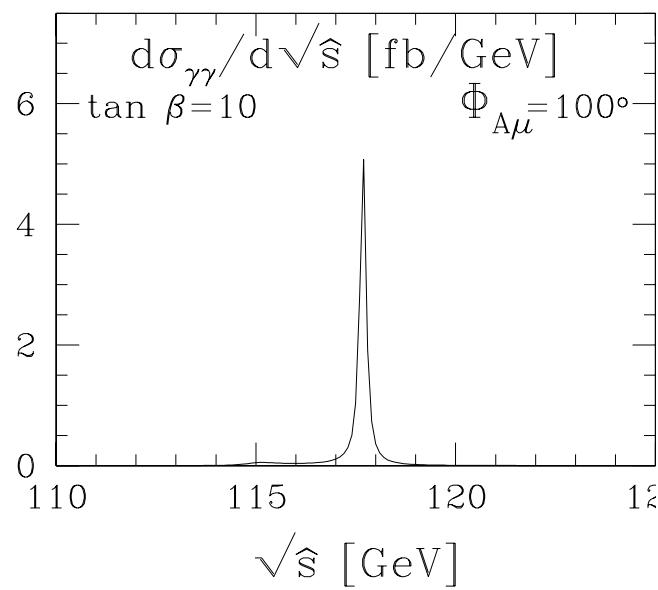
♦ *b-quark Fusion (2/2)*

- Invariant mass distribution when Higgs bosons decay into two γ 's and/or $\mu^+\mu^-$

At the LHC, the experimental resolution $\delta M_{\gamma\gamma} \sim 1$ GeV and $\delta M_{\mu\mu} \sim 3$ GeV

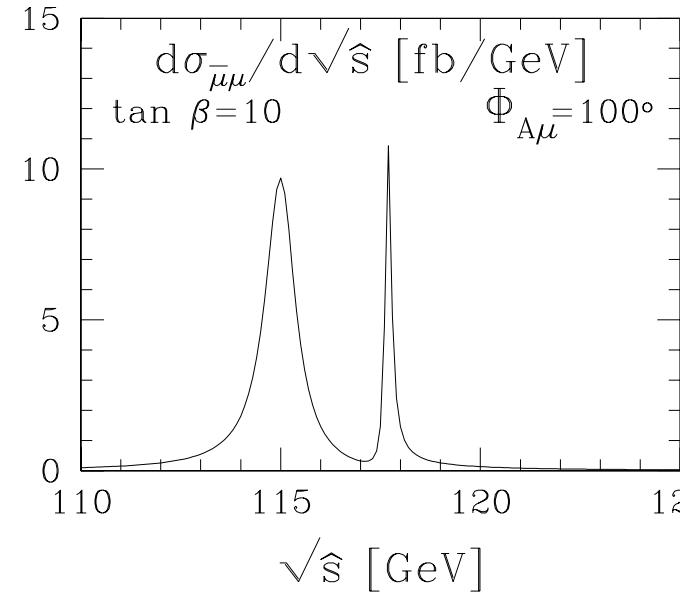
ATLAS TDR, Vol 2, CERN-LHCC-99-15, ATLAS-TDR-15 (1999); CMS Physics TDR, Volume II, CERN-LHCC-2006-021, 25 June 2006

$$H_{1,2} \rightarrow \gamma\gamma$$



One peak

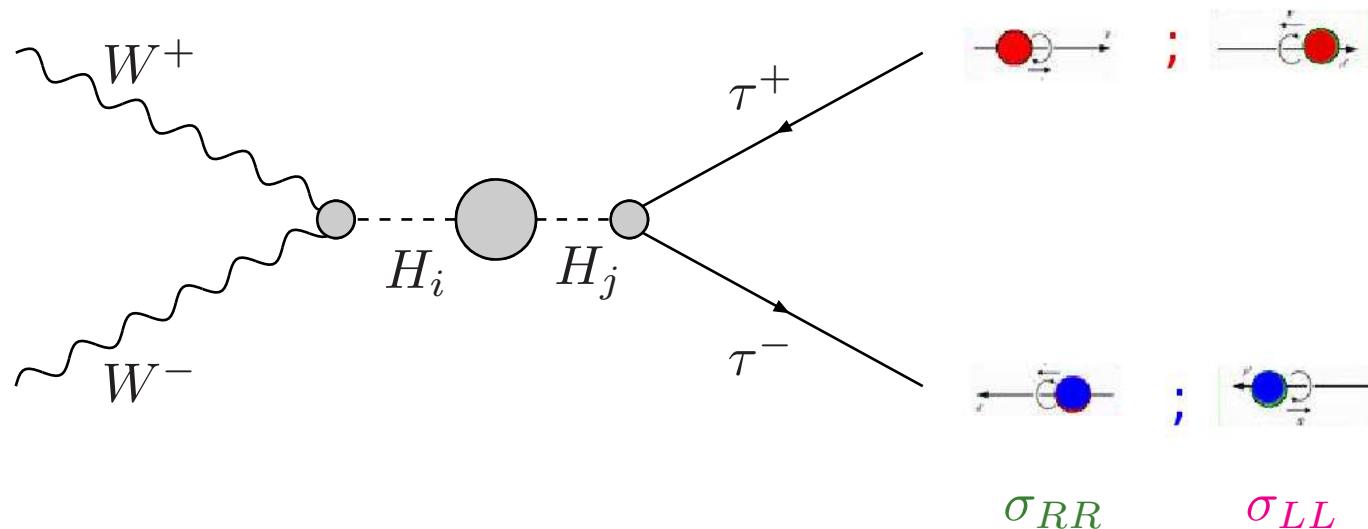
$$H_{1,2} \rightarrow \mu^+\mu^-$$



Two peaks

♦ *CP Asymmetries (1/3)*

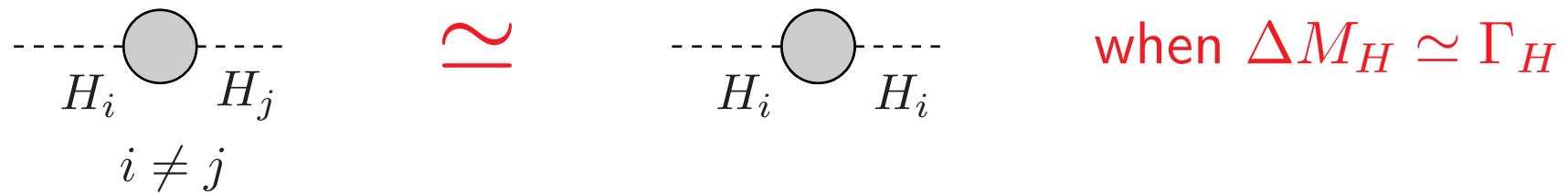
- CP asymmetry in Higgs decays in the tau leptons : J. Ellis, JSL and A. Pilaftsis, D71(2005)075007



$$\mathcal{A}_{\text{CP}} = \frac{\sigma_{RR} - \sigma_{LL}}{\sigma_{RR} + \sigma_{LL}} \quad \text{with} \quad \begin{cases} \sigma_{RR} \equiv \sigma(pp \rightarrow H \rightarrow \tau_R^+ \tau_R^- X) \\ \sigma_{LL} \equiv \sigma(pp \rightarrow H \rightarrow \tau_L^+ \tau_L^- X) \end{cases}$$

♠ *CP Asymmetries (2/3)*

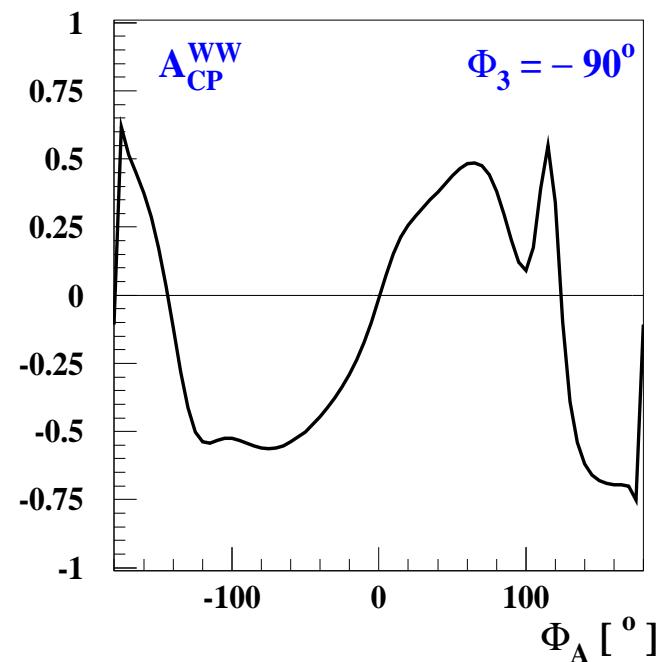
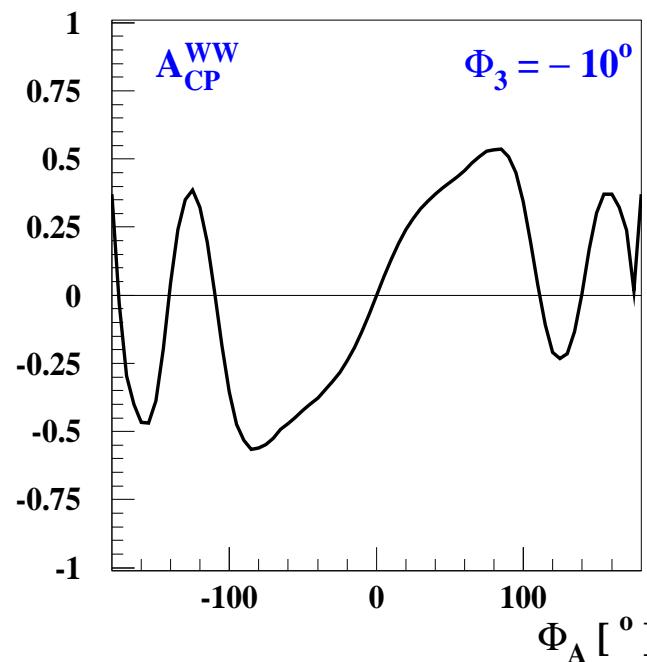
- Resonant transitions between Higgs bosons enhance the asymmetry!:



The neutral Higgs bosons should not be treated separately !

♦ *CP Asymmetries (3/3)*

- Integrated CP asymmetry $\mathcal{A}_{\text{CP}}^{WW}$ with $\sigma_{\text{tot}}^{WW} > 0.2 \text{ pb}$:

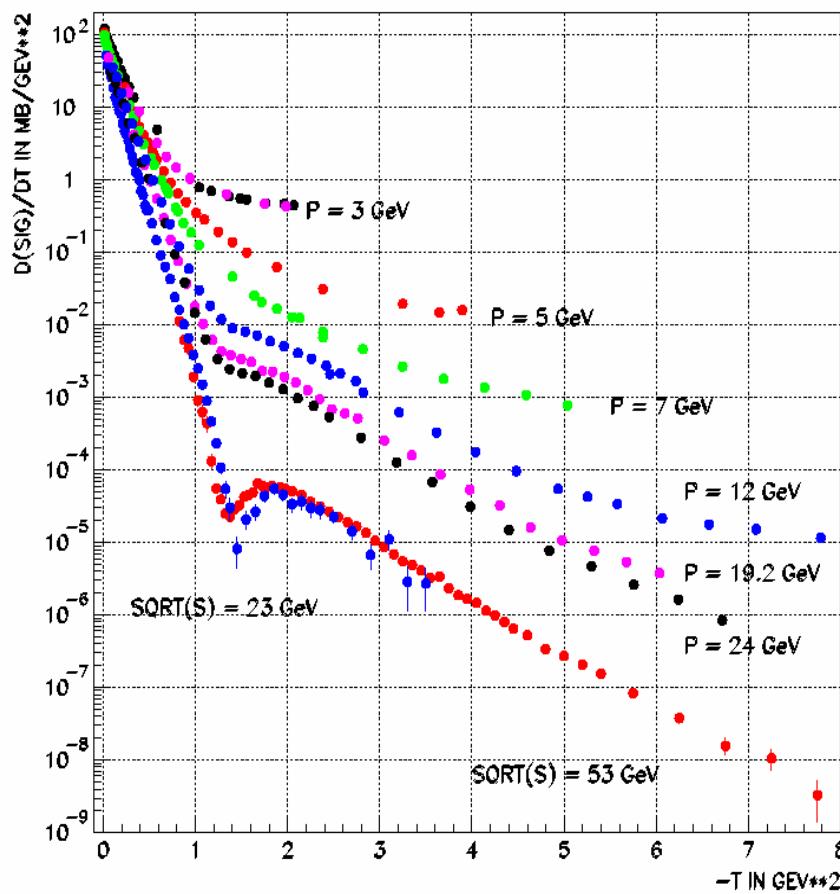


CP asymmetry is large over the whole ranges of CP phases !

♠ Diffraction (1/3)

- Diffraction is a process with a *t*-channel exchange leading to a Large Rapidity Gap

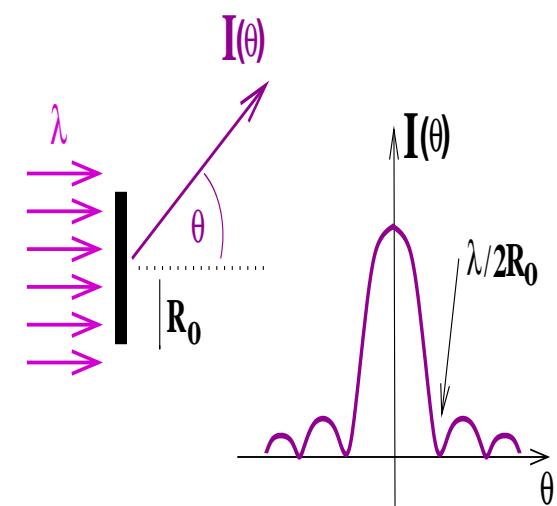
M. Arneodo, M. Diehl, hep-ph/0511047



The differential cross section

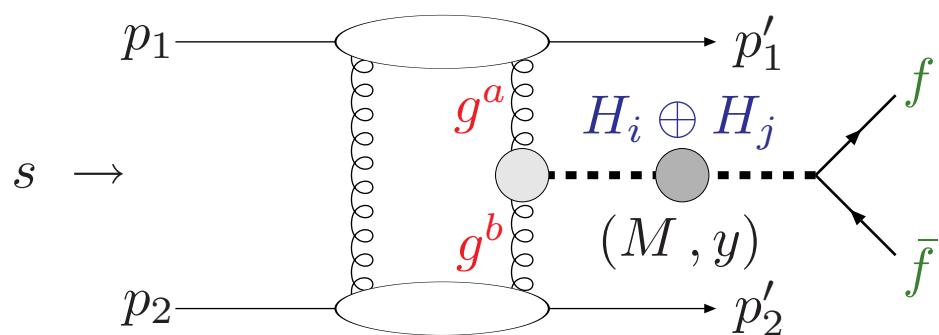
$$\frac{d\sigma(pp \rightarrow pp)}{dt} \Big|_{\text{elastic}}$$

has a resemblance to the diffraction pattern in optics:



♦ Diffraction (2/3)

- Exclusive double diffractive process



Outgoing protons remain intact & scatter through small angles with $p_\perp \ll 1$ GeV

J. Ellis, JSL and A. Pilaftsis, D71(2005)075007

* Need TOTEM/ATLASFP detectors

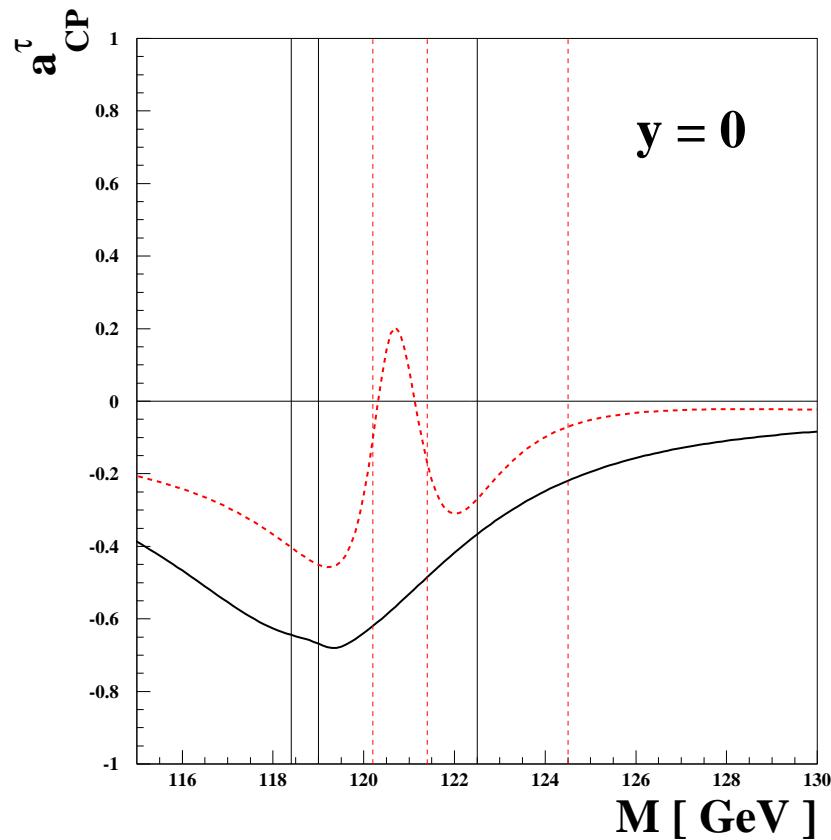
$$\dagger M^2 = s - 2\sqrt{s}(E'_1 + E'_2) + (p'_1 + p'_2)^2 \\ \Rightarrow \delta M \sim 1 \text{ GeV} !$$

\dagger Clean environment due to the large rapidity gap

A. De Roeck, *et al.*, EPJC25 (2002) 391; M. Boonekamp, *et al.*, PLB598 (2004) 243; K. A. Assamagan *et al.* hep-ph/0406152; B. E. Cox, hep-ph/0409144, hep-ph/0501064; B.E. Cox*, J.R. Forshaw, JSL, J.W. Monk* and A. Pilaftsis, PRD68 (2003) 075004; V.A. Khoze, A.D. Martin and M.G. Ryskin, EPJC34 (2004) 327

♠ Diffraction (3/3)

- $pp \rightarrow p H_i p ; H_i \rightarrow \tau^+ \tau^-$ $(\Phi_A, \Phi_3) = (90^\circ, -90^\circ)$ $(\Phi_A, \Phi_3) = (90^\circ, -10^\circ)$

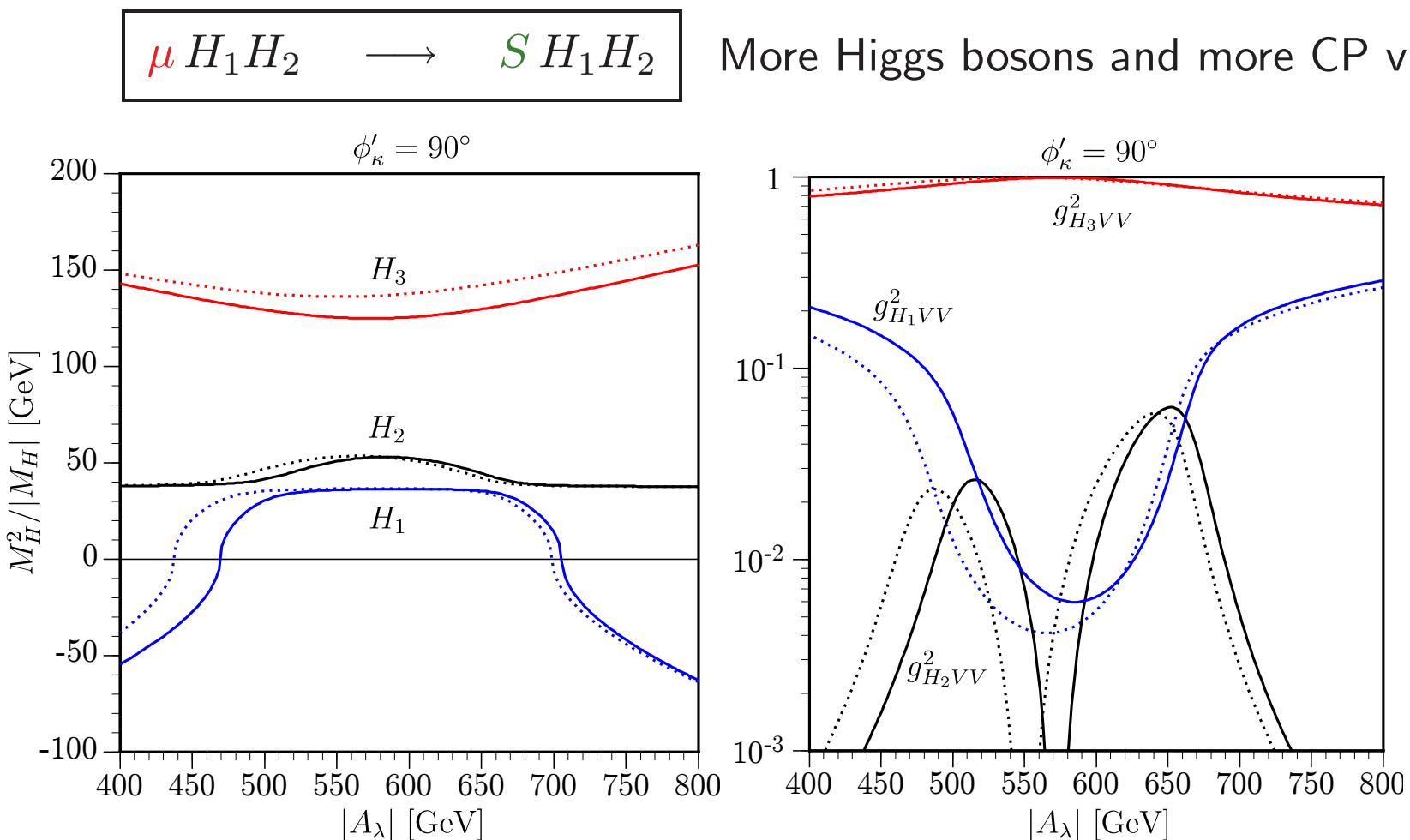


Invariant mass distribution can be studied !



Beyond the Minimal SUSY Model (1/2)

- The μ problem J. E. Kim and H. P. Nilles, Phys. Lett. B **138**, 150 (1984)





Beyond the Minimal SUSY Model (2/2)

- We are working on ...
 - Constraints from EDMs on the new CP violation
 - ElectroWeak Phase Transitions
 - New CP-phase driven baryogenesis
 - B - and K -meson observables
 - Collider signatures of the light Higgs bosons
 - Higgs Inflation(?)
 - etc

 *Summary (LHC)*

- Phases of the LHC :

I (2013 ~ 2014) : *LHC with $\mathcal{L} \sim 10 \text{ fb}^{-1}$*

SM Higgs Discovery,

Non-SM-like Higgs decays and productions, Multiple Higgs peaks

II (2015 ~ 2016) : *LHC with $\mathcal{L} \sim 300 \text{ fb}^{-1}$*

I \oplus Strongly-coupled Higgs, CP asymmetries, Final-state spin-spin correlations

III (2017 ~ 202?) : *LHC with $\mathcal{L} \gg 300 \text{ fb}^{-1}$*

I \oplus II \oplus Exotic Higgs productions

♠ *Conclusions and Future Prospects*

- Spontaneous breaking of the electroweak symmetry *may* be responsible for the masses of SM particles
- Supersymmetry *may* stabilize the Higgs-boson masses against the Quantum corrections
- The additional CP phases in the models extended by Supersymmetry *may* explain the matter dominance of the Universe
- The Supersymmetric CP phases *may* manifest themselves through the Higgs sector in Energy-, Intensity-, and Cosmic-Frontier experiments
- The LHC is to give definite answers to these *may*'s

♠ Where to find it ?

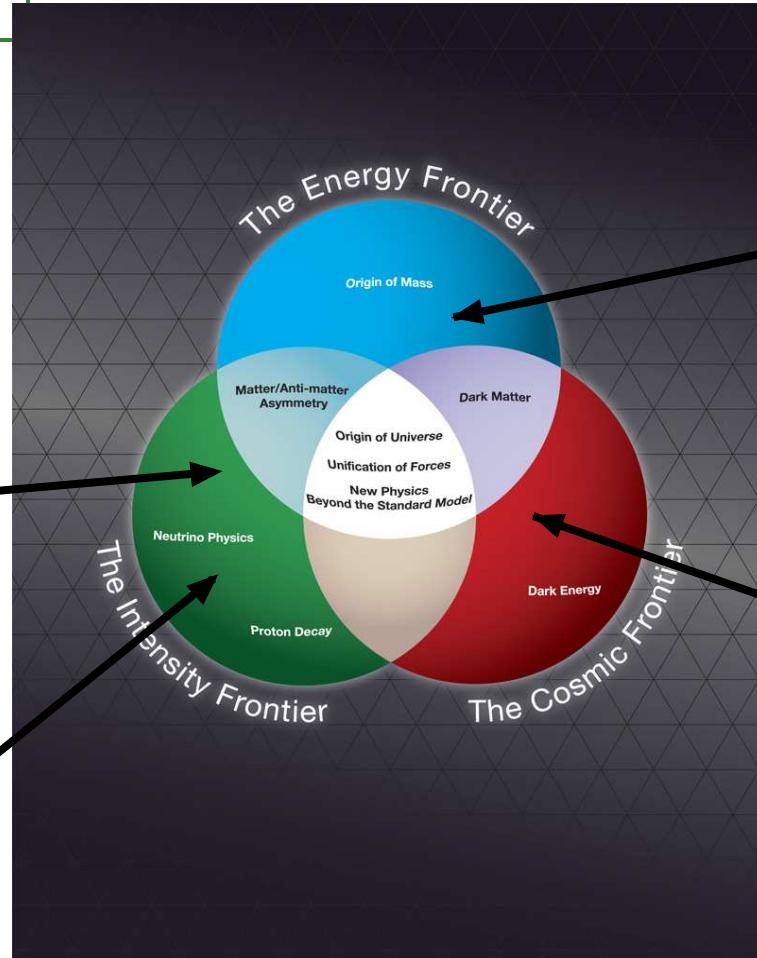
II-B

B-meson Observables

B-meson Observables

{ $\Delta M_{B_d, s}$, $D_s \rightarrow \mu^+ \mu^-$,
 $B \rightarrow \tau \nu$, $B \rightarrow X_s \gamma$,
...

Electric Dipole Moments



Colliders

{ LEP Holes
LHC Signatures

Dark Matter

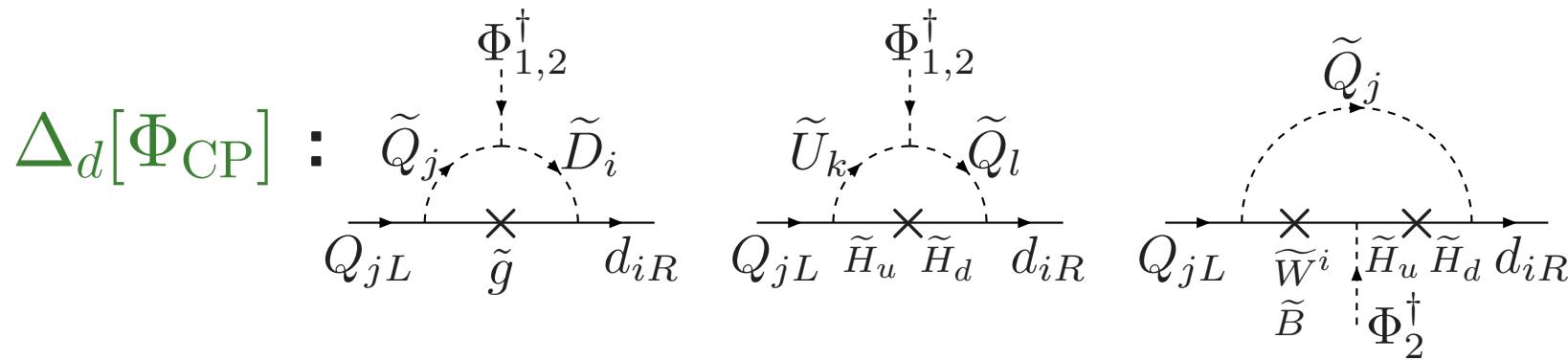
{ $\chi \chi \rightarrow \gamma, \bar{p}, \text{etc}$

♦ *B Observables (1/4)*

- Higgs-mediated B-meson mixing and rare decays: LHCb and SuperB J. Ellis, JSJ and A. Pilaftsis, PRD76(2007)115011

$$(-\mathcal{L}_{\text{eff}}^d)^H = \frac{g}{2M_W} \bar{d} \widehat{M}_d \mathbf{g}_{H_i \bar{d} d}^L P_L d H_i + \text{h.c.}$$

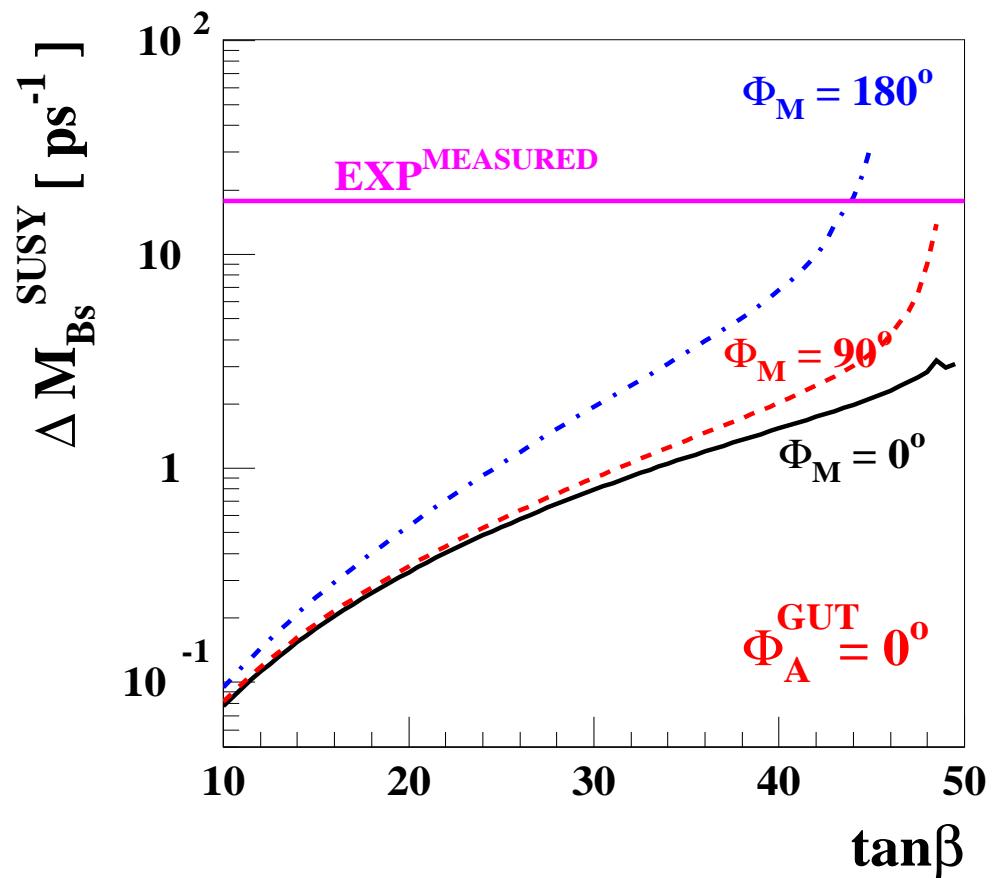
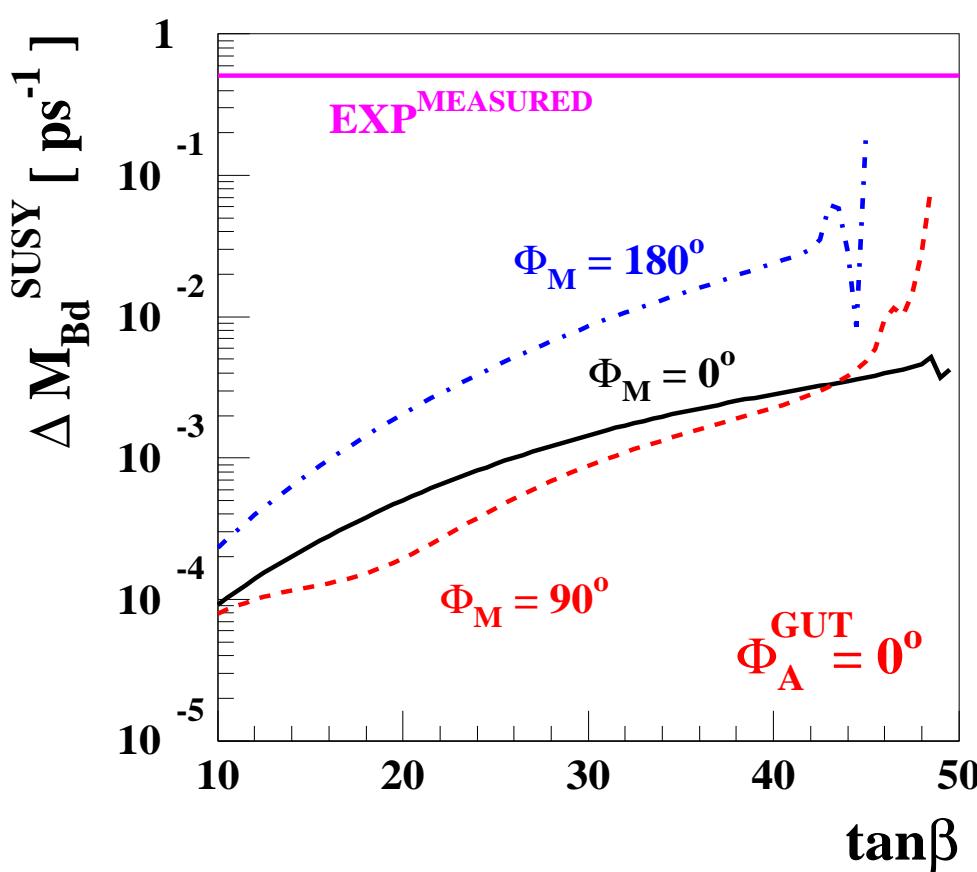
$$\mathbf{g}_{H_i \bar{d} d}^L \propto V_{\text{CKM}}^\dagger [1 + \tan \beta \Delta_d]^{-1} V_{\text{CKM}}$$



Non-universal Quantum interactions inducing the mixing and rare decays !

♦ *B Observables (2/4)*

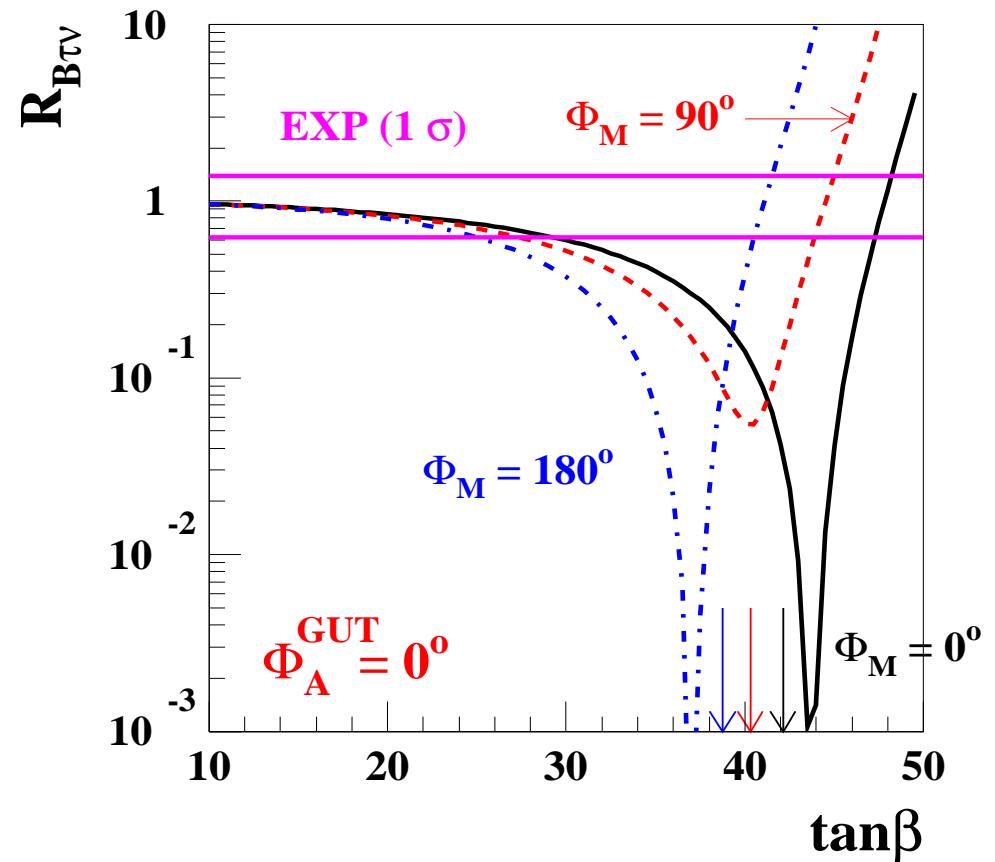
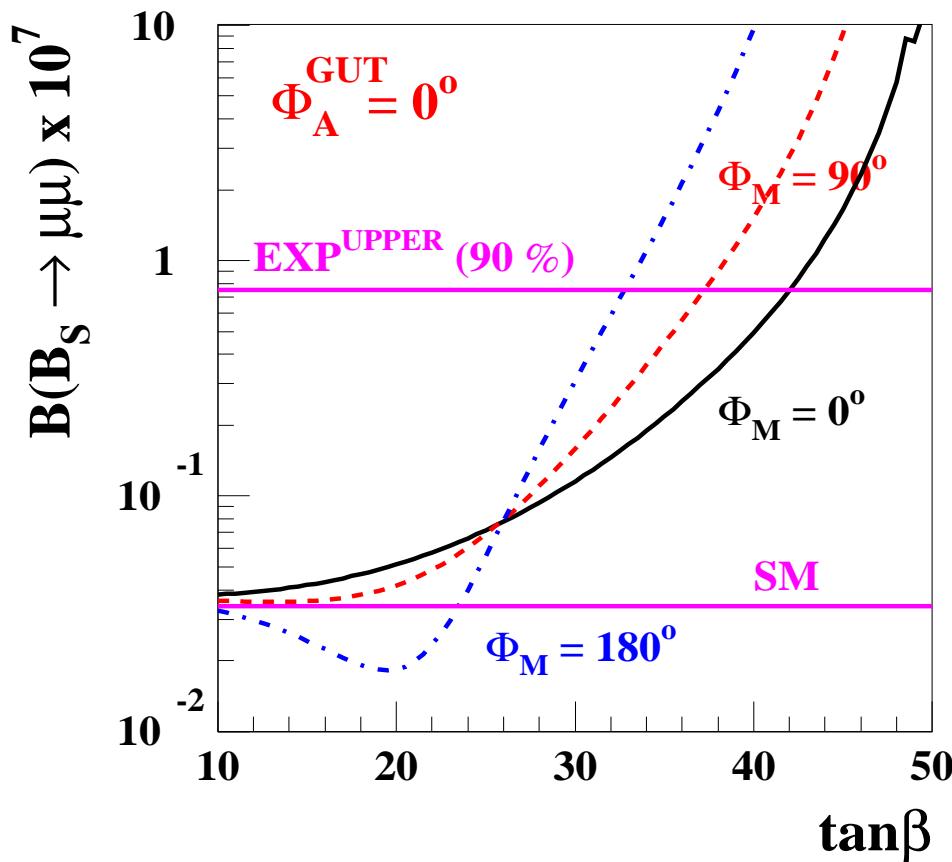
- $\Delta M_{B_d}^{\text{SUSY}}$ and $\Delta M_{B_s}^{\text{SUSY}}$ as functions of $\tan\beta(M_{\text{SUSY}})$ for three values of $\Phi_M \equiv \Phi_1 = \Phi_2 = \Phi_3$ SPS1a-like scenario $\tilde{M}_{L,E} = 200$ GeV and $\Phi_A^{\text{GUT}} = 0^\circ$



Strong CP phase dependence

♠ *B Observables (3/4)*

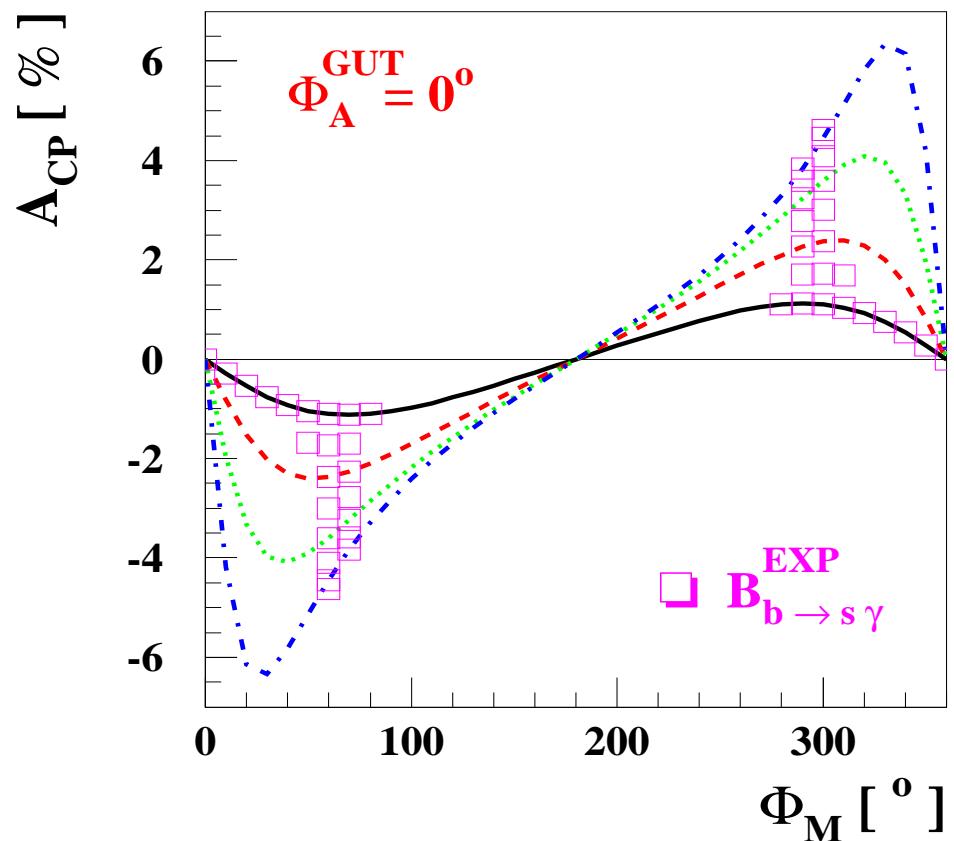
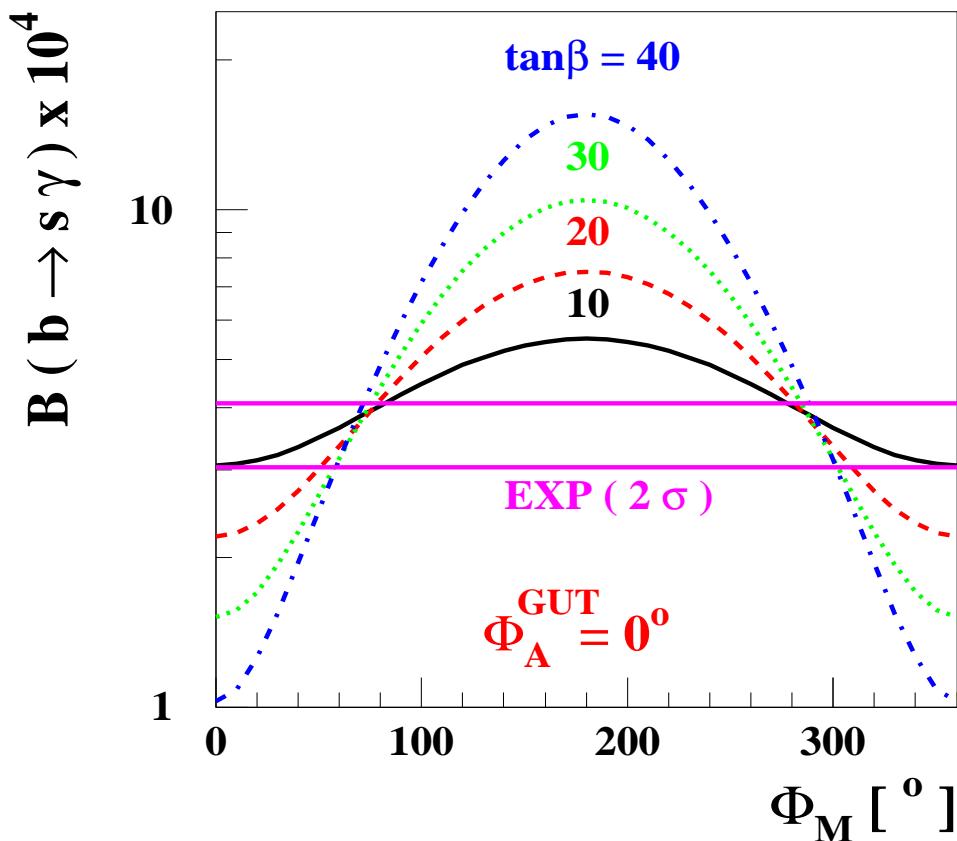
- $B(\bar{B}_s^0 \rightarrow \mu^+ \mu^-)$ and the ratio $R_{B\tau\nu}$ as functions of $\tan \beta(M_{\text{SUSY}})$ for three values of $\Phi_M \equiv \Phi_1 = \Phi_2 = \Phi_3$ SPS1a-like scenario $\widetilde{M}_{L,E} = 200$ GeV and $\Phi_A^{\text{GUT}} = 0^\circ$



Strong CP phase dependence

♦ *B Observables (4/4)*

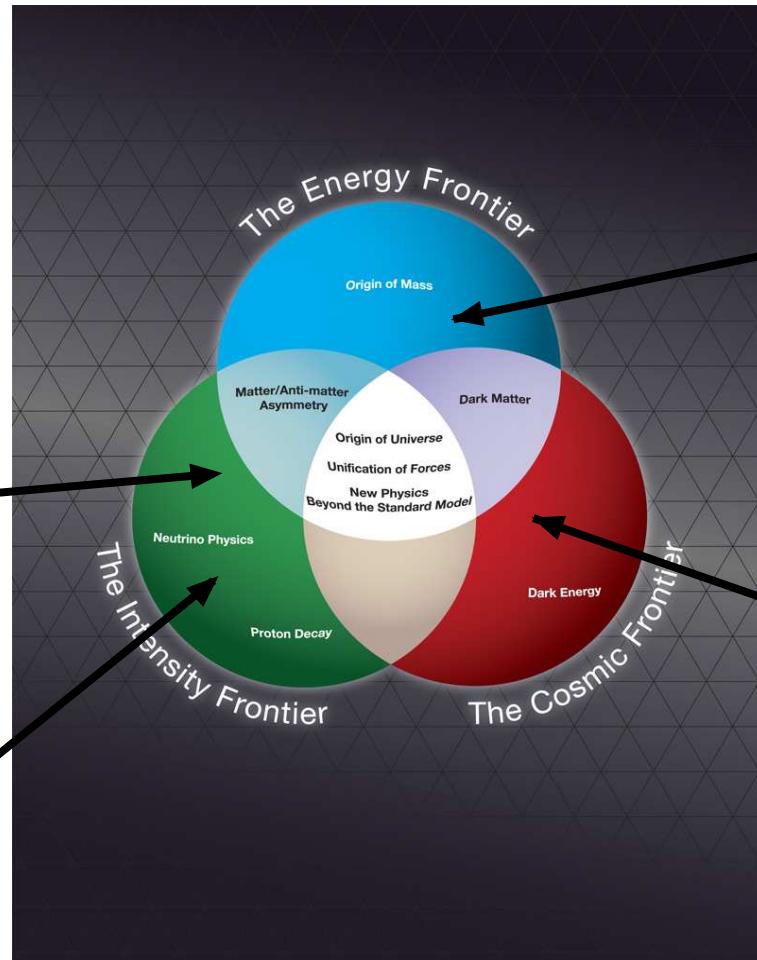
- $B(B \rightarrow X_s \gamma)$ and $\mathcal{A}_{\text{CP}}^{\text{dir}}(B \rightarrow X_s \gamma)$ as functions of Φ_M for four values of $\tan \beta(M_{\text{SUSY}}) = 10, 20, 30, 40$ SPS1a-like scenario $\tilde{M}_{L,E} = 200 \text{ GeV}$ and $\Phi_A^{\text{GUT}} = 0^\circ$



Strong CP phase dependence

♠ Where to find it ?

II-C EDMs



B-meson Observables

{ $\Delta M_{B_{d,s}}$, $B_s \rightarrow \mu^+ \mu^-$,
 $B \rightarrow \tau \nu$, $B \rightarrow X_s \gamma$,
...

Electric Dipole Moments

Colliders

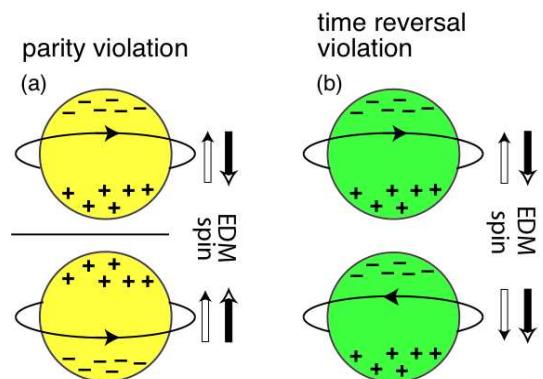
{ *LEP Holes*
LHC Signatures

Dark Matter

{ $\chi \chi \rightarrow \gamma, \bar{p}$, etc

♠ EDMs (1/4)

- Electric Dipole Moments (EDMs): T violation \Rightarrow CP violation (under CPT)



$$\mathcal{H}^{\text{EDM}} = -d \mathbf{E} \cdot \hat{\mathbf{S}}$$

$$|d_{\text{Tl}}| < 9 \times 10^{-25} \text{ e cm}, \quad |d_{\text{Hg}}| < 3.1 \times 10^{-29} \text{ e cm}, \quad |d_{\text{n}}| < 3 \times 10^{-26} \text{ e cm}$$

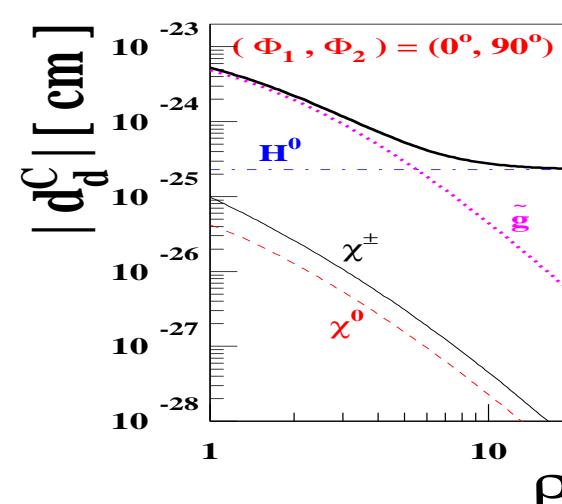
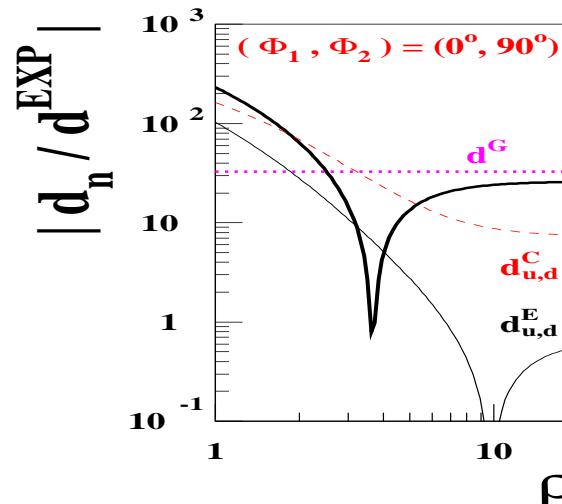
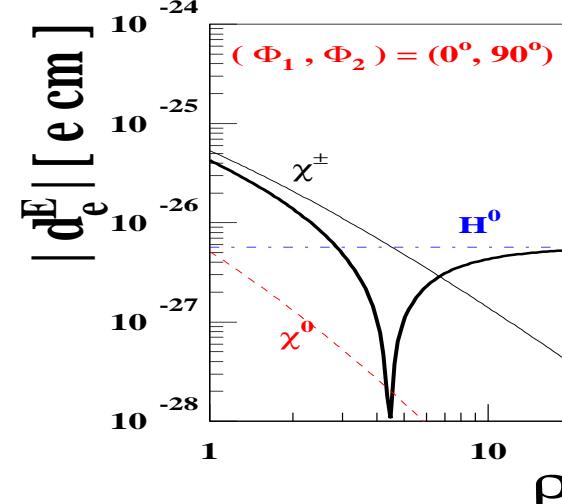
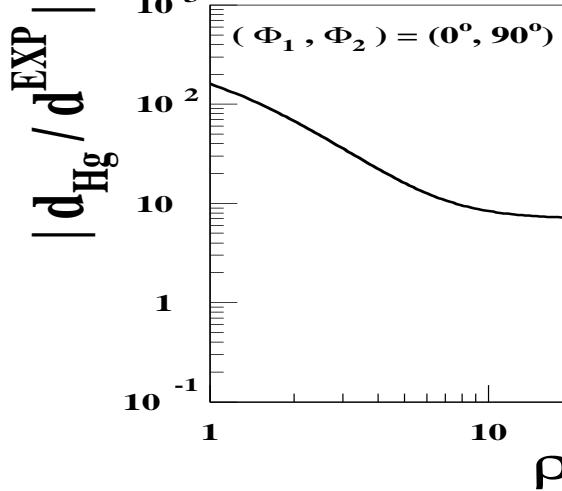
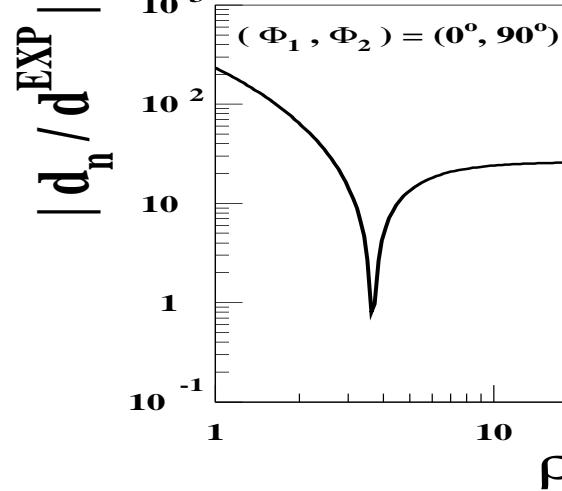
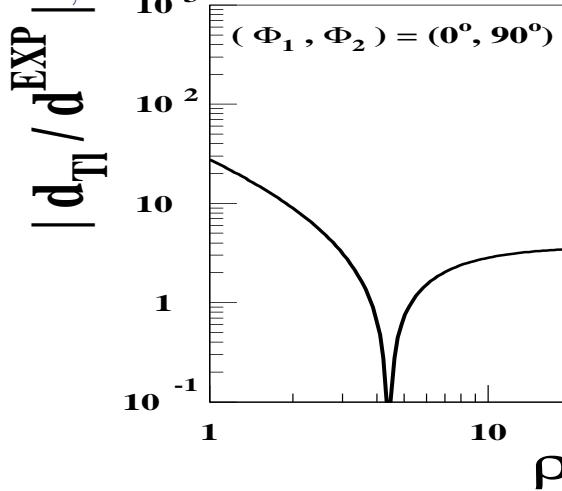
B. C. Regan, E. D. Commins, C. J. Schmidt and D. DeMille, PRL**88** (2002) 071805; W. C. Griffith, M. D. Swallows, T. H. Loftus, M. V. Romalis, B. R. Heckel and E. N. Fortson, PRL**102** (2009) 101601; C. A. Baker *et al.*, PRL**97** (2006) 131801

- No large CP phases? -No! But, one needs to introduce **some hierarchy** between first two and third generations and/or some **moderate tuning** among parameters

♦ EDMs (2/4)

- EDM constraints and cancellation: CPX Scenario with $\Phi_{A_{t,b}} = \Phi_3 = 90^\circ$, $\Phi_{A_{u,d,c,s}} = 0^\circ$ $\tan\beta = 5$, $M_{H^\pm} = 300$ GeV, $|M_2| = 2|M_1| = 100$ GeV, and $M_{\text{SUSY}} = 0.5$ TeV The hierarchy factor ρ :

$M_{\tilde{X}_{1,2}} = \rho M_{\tilde{X}_3}$ with $X = Q = U = D = L = E$ J. Ellis, JSJ and A. Pilaftsis, JHEP08(2008)049



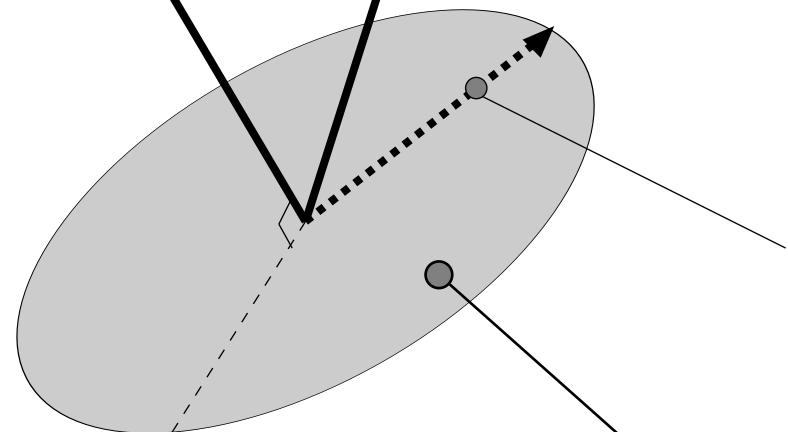
♦ EDMs (3/4)

- Analytic determination of the cancellation regions: EDM-free directions and
Optimal direction J. Ellis, JSL and A. Pilaftsis, JHEP10(2010)049

EDM vector

An Observable vector

$$\Phi = E \times (O \times E)$$



An Optimal direction

Subspace of EDM-free directions

CP-phase space

♦ *EDMs* (4/4)

- Optimal direction : the higher-dimensional generalization with N CP phases and n EDM constraints

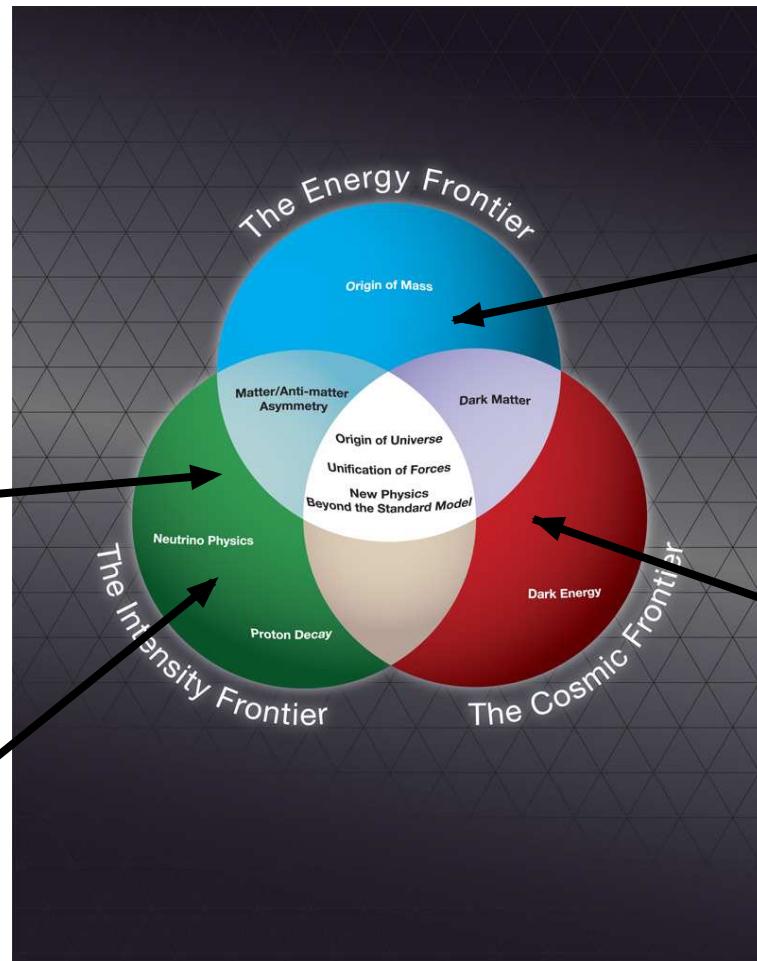
$$\Phi_\alpha = \epsilon_{\alpha\beta_1\dots\beta_n\gamma_1\dots\gamma_{N-n-1}} E_{\beta_1}^{(1)} \dots E_{\beta_n}^{(n)} B_{\gamma_1\dots\gamma_{N-n-1}}$$

where $(N-n-1)$ -dimensional B form is

$$B_{\gamma_1\dots\gamma_{N-n-1}} = \epsilon_{\gamma_1\dots\gamma_{N-n-1}\sigma\beta_1\dots\beta_n} O_\sigma E_{\beta_1}^{(1)} \dots E_{\beta_n}^{(n)}$$

♠ Where to find it ?

II-D Dark Matter



Colliders

{ LEP Holes
LHC Signatures

B-meson Observables

{ $\Delta M_{B_{d,s}}$, $B_s \rightarrow \mu^+ \mu^-$,
 $B \rightarrow \tau \nu$, $B \rightarrow X_s \gamma$,
...

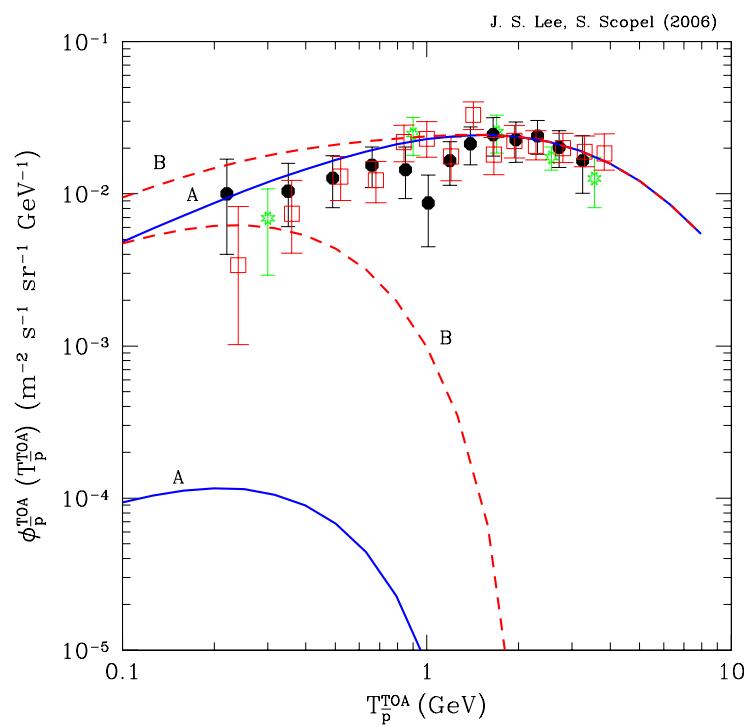
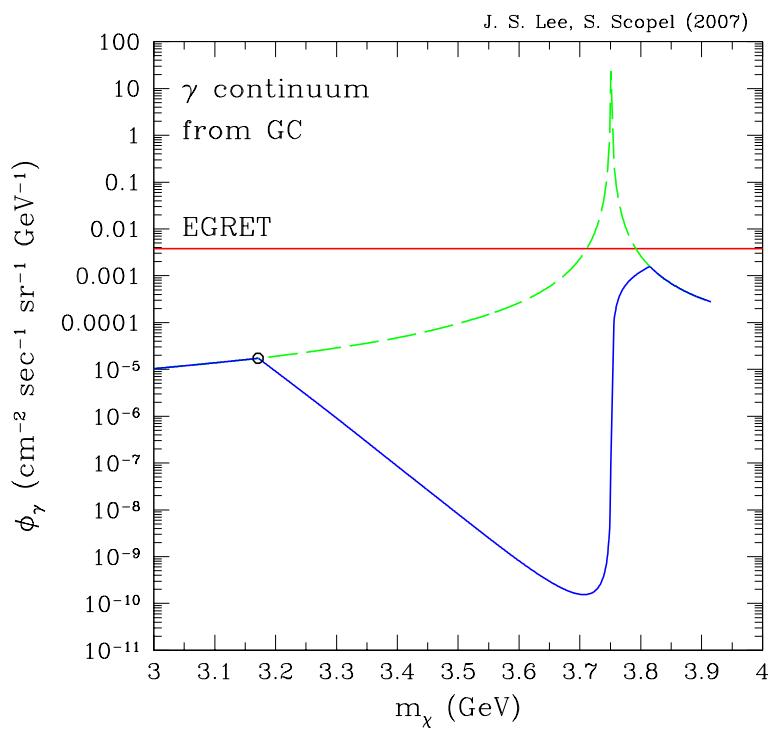
Electric Dipole Moments

Dark Matter

{ $\chi \chi \rightarrow \gamma, p$, etc

♦ Dark Matter (1/1)

- LEP Holes \Rightarrow Very light 7.5 GeV Higgs signals through the inclusive process $\chi\chi \rightarrow H \rightarrow \gamma, \bar{p}$ JSL and S. Scopel, Phys. Rev. D **75** (2007) 075001 [arXiv:hep-ph/0701221]



♠ MAOS momenta of the missing neutrinos (1/2)

- MAOS = M_{T2} -Assisted On-shell Scheme:

$$H \rightarrow W(\mathbf{p} + \mathbf{k}) W(\mathbf{q} + \mathbf{l}) \rightarrow l(p) \nu(k) l'(q) \nu'(l)$$

$$(M_H^2)^{\text{MAOS}} = (\mathbf{p} + \mathbf{k}^{\text{MAOS}} + \mathbf{q} + \mathbf{l}^{\text{MAOS}})^2$$

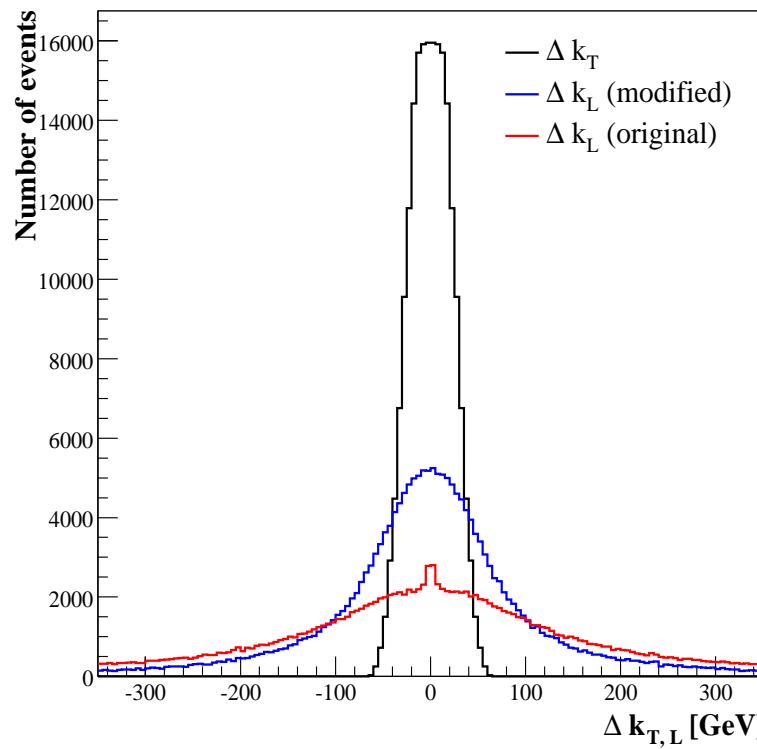
$$\mathbf{k}_T^{\text{MAOS}} = -\mathbf{q}_T \quad \text{and} \quad \mathbf{l}_T^{\text{MAOS}} = -\mathbf{p}_T$$

$$k_L^{\text{MAOS}} = \frac{|\mathbf{k}_T^{\text{MAOS}}|}{|\mathbf{p}_T|} p_L, \quad l_L^{\text{MAOS}} = \frac{|\mathbf{l}_T^{\text{MAOS}}|}{|\mathbf{q}_T|} q_L$$

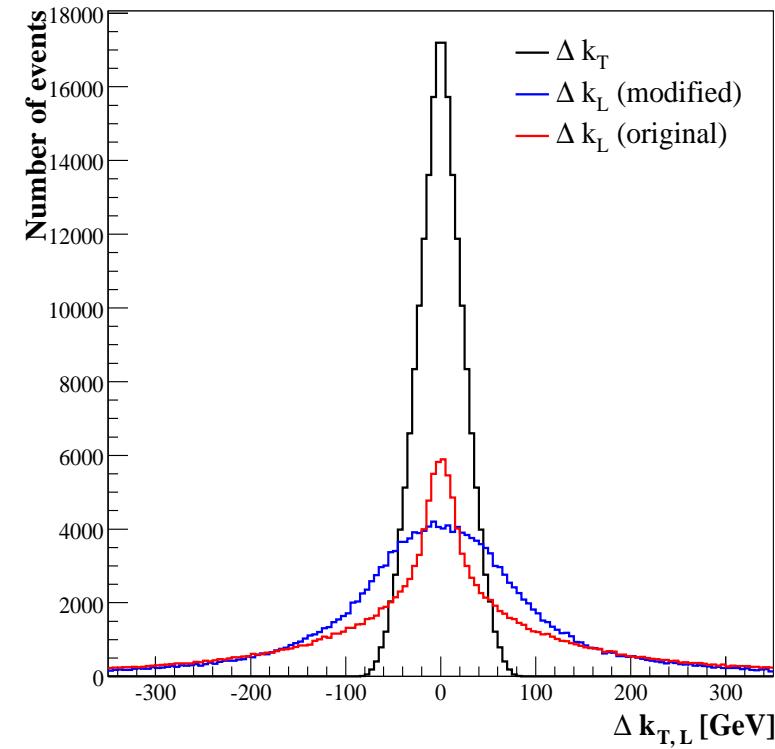
♠ MAOS momenta of the missing neutrinos (2/2)

- Is the modified MAOS scheme working well?:

$M_H = 140 \text{ GeV}$

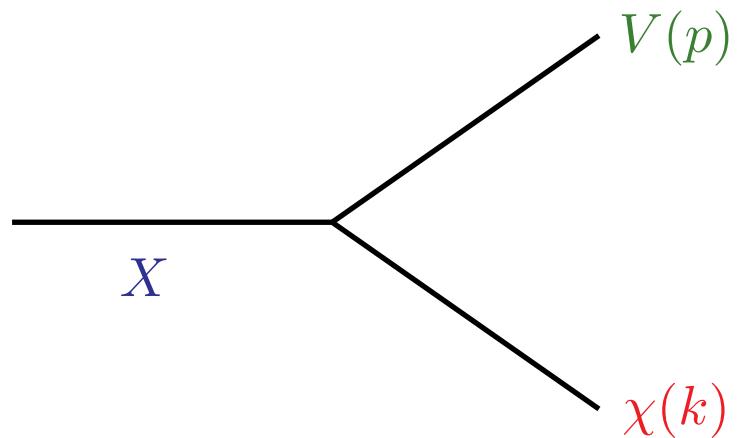


$M_H = 180 \text{ GeV}$



♦ M_{T2} : 1/2

- Transverse Mass M_T :



$$p^\mu = (\sqrt{m_V^2 + |\mathbf{p}_T|^2 + p_L^2}, \mathbf{p}_T, p_L)$$

$$k^\mu = (\sqrt{m_\chi^2 + |\mathbf{k}_T|^2 + k_L^2}, \mathbf{k}_T, k_L)$$

$$\mathbf{k}_T = \mathbf{p}_T \text{ (*fully determined*)}$$

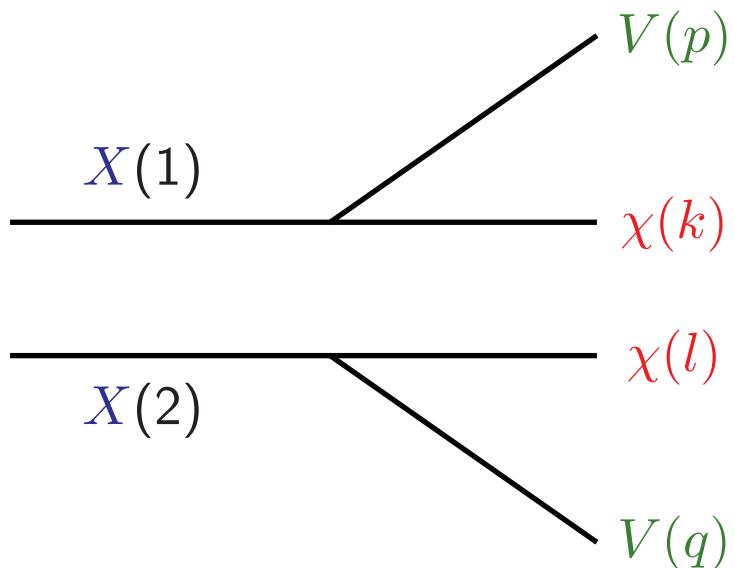
$$M_X^2 = m_V^2 + m_\chi^2 + 2 \left(\sqrt{m_V^2 + |\mathbf{p}_T|^2 + p_L^2} \sqrt{m_\chi^2 + |\mathbf{k}_T|^2 + k_L^2} - \mathbf{p}_T \cdot \mathbf{k}_T - p_L k_L \right)$$

$$M_T^2 = m_V^2 + m_\chi^2 + 2 \left(\sqrt{m_V^2 + |\mathbf{p}_T|^2} - \sqrt{m_\chi^2 + |\mathbf{k}_T|^2} - \mathbf{p}_T \cdot \mathbf{k}_T \right)$$

$$M_T \leq M_X$$

♠ M_{T2} : 2/2

- ... then M_{T2} ?: Generalization of M_T when there are 2 missing particles



$$\mathbf{k}_T + \mathbf{l}_T = \mathbf{p}'_T$$

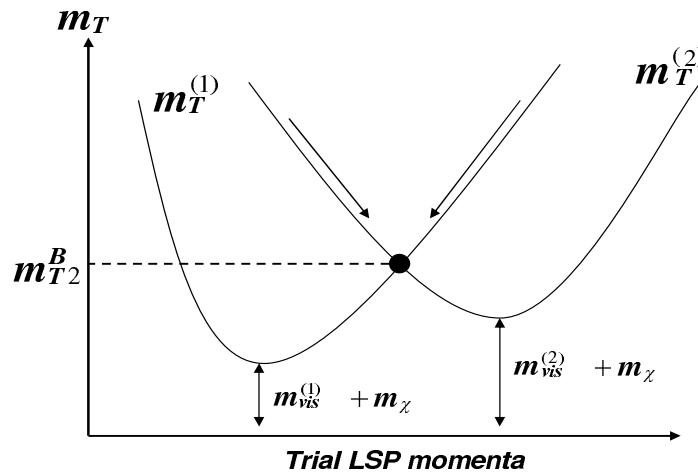
Only determined are ...
the 2 among the 4 unknown degrees of freedom !

... but we know:

$$\max\{M_T^{(1)}, M_T^{(2)}\}(\mathbf{k}_T^{\text{true}}, \mathbf{l}_T^{\text{true}}) \leq M_X$$

♦ M_{T2} : $2'/2$

- ... then M_{T2} ?: Generalization of M_T when there are 2 missing particles



$$\mathbf{k}_T + \mathbf{l}_T = \mathbf{p}'_T$$

Only determined are ...
the 2 among the 4 unknown degrees of freedom !

... but we know:

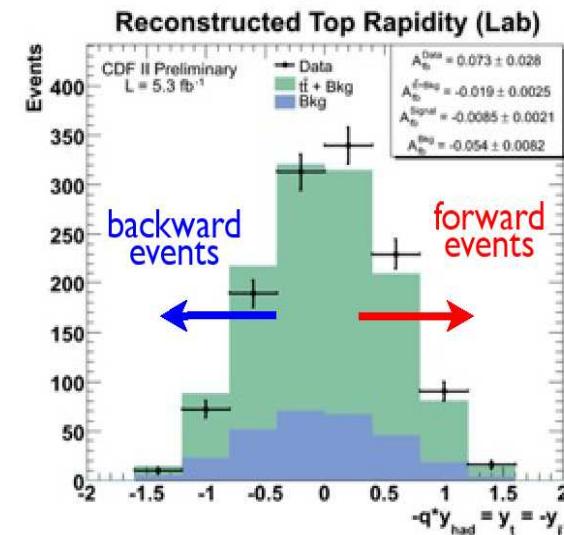
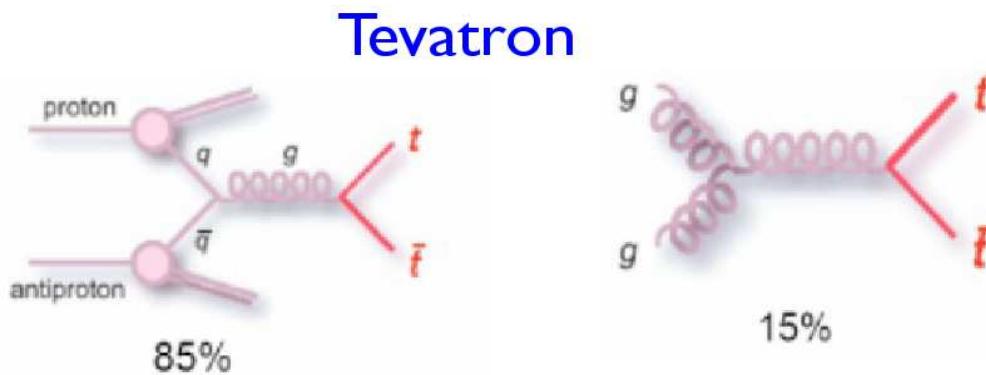
$$\max\{M_T^{(1)}, M_T^{(2)}\}(\mathbf{k}_T^{\text{true}}, \mathbf{l}_T^{\text{true}}) \leq M_X$$

$$\max\{M_T^{(1)}, M_T^{(2)}\}(\mathbf{k}_T^{\min}, \mathbf{l}_T^{\min}) \leq \max\{M_T^{(1)}, M_T^{(2)}\}(\mathbf{k}_T^{\text{true}}, \mathbf{l}_T^{\text{true}}) \leq M_X$$

$$M_{T2} \equiv \min_{\mathbf{k}_T + \mathbf{l}_T = \mathbf{p}'_T} \left[\max \left\{ M_T^{(1)}, M_T^{(2)} \right\} \right] \leq M_X$$

♦ A_{FB} at the Tevatron: 1/2

- $q\bar{q} \rightarrow t\bar{t}$ and A_{FB} at the Tevatron [Shabamina\(Blois2010\)](#)



$$A_{fb} (\text{raw}) = 0.073 \pm 0.028$$

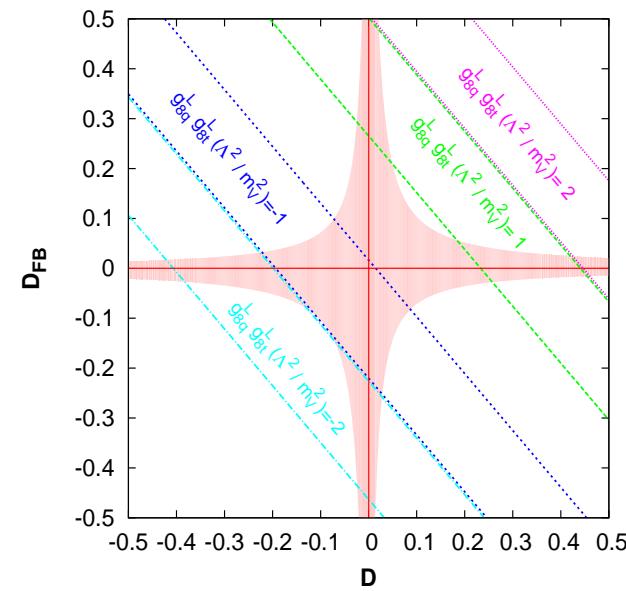
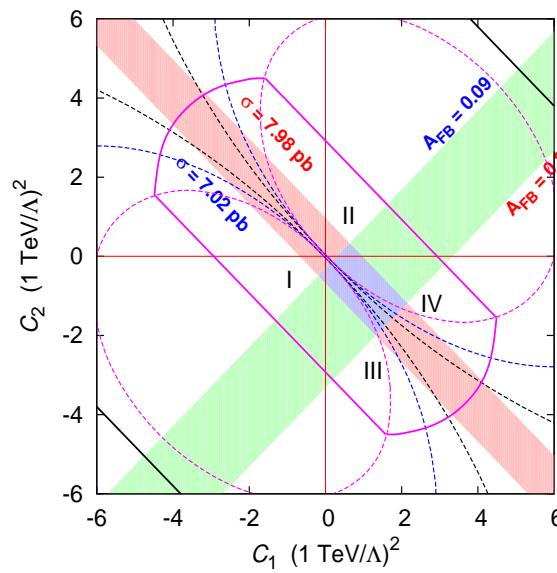
$$A_{FB} \equiv \frac{N_t(\cos \theta \geq 0) - N_{\bar{t}}(\cos \theta \geq 0)}{N_t(\cos \theta \geq 0) + N_{\bar{t}}(\cos \theta \geq 0)} = (0.15 \pm 0.05 \pm 0.024)$$

Pertinent $\sim 2\sigma$ deviation !

♦ A_{FB} at the Tevatron: 2/2

- Effective Lagrangian approach to explain the anomaly [D.-W. Jung, P. Ko, JSL, S.-h. Nam, PLB691\(2010\)238; D.-W. Jung, P. Ko, JSL, arXiv:1012.0102 \[hep-ph\]](#)

$$\mathcal{L}_6 = \frac{g_s^2}{\Lambda^2} C_{8q}^{AB} (\bar{q}_A T^a \gamma_\mu q_A)(\bar{t}_B T^a \gamma^\mu t_B)$$



$$C_1 \equiv C_{8q}^{RR} + C_{8q}^{LL}, \quad C_2 \equiv C_{8q}^{LR} + C_{8q}^{RL}, \quad D, D_{\text{FB}} \propto (C_{8q}^{RR} - C_{8q}^{LL}) \pm (C_{8q}^{LR} - C_{8q}^{RL})$$

♠ Backup

- CPX Scenario:

Recall CPV mixing $\propto \Im m(A_f\mu)/M_{\text{SUSY}}^2$

$$M_{\tilde{Q}_3} = M_{\tilde{U}_3} = M_{\tilde{D}_3} = M_{\tilde{L}_3} = M_{\tilde{E}_3} = M_{\text{SUSY}}$$

$$|\mu| = 4 M_{\text{SUSY}}, \quad |A_{t,b,\tau}| = 2 M_{\text{SUSY}}$$

$$|M_3| = 1 \text{ TeV}$$

Varying parameters are :

$$\tan \beta, \quad M_{H^\pm}^{\text{pole}}, \quad M_{\text{SUSY}}$$

$$(\Phi_\mu), \quad \Phi_{A_t}, \quad \Phi_{A_b}, \quad \Phi_{A_\tau}, \quad \Phi_3$$

* M_1 and M_2

* For simplicity, common Φ_A

♠ Backup

- Large $\tan \beta$ and $M_{H^\pm}^{\text{pole}} \sim 150$ GeV \Rightarrow Trimixing scenario J. Ellis, JSL and A. Pilaftsis, PRD70(2004)075010, PRD71(2005)075007, PRD72(2005)095006, and NPB718(2005)247

$$\tan \beta = 50, \quad M_{H^\pm}^{\text{pole}} = 155 \text{ GeV},$$

$$M_{\tilde{Q}_3} = M_{\tilde{U}_3} = M_{\tilde{D}_3} = M_{\tilde{L}_3} = M_{\tilde{E}_3} = 0.5 \text{ TeV},$$

$$|\mu| = 0.5 \text{ TeV}, \quad |A_{t,b,\tau}| = 1 \text{ TeV}, \quad |M_{1,2}| = 0.3 \text{ TeV}, \quad |M_3| = 1 \text{ TeV},$$

$$\Phi_\mu = 0^\circ, \quad \Phi_{1,2} = 0^\circ.$$

For $\Phi_{A_t, A_b, A_\tau} = 90^\circ$ and $\Phi_3 = -90^\circ$, we have (in GeV)

$$M_{H_1} = 117.6, \quad M_{H_2} = 118.7, \quad M_{H_3} = 122.6,$$

$$\Gamma_{H_1} = 1.48, \quad \Gamma_{H_2} = 8.12, \quad \Gamma_{H_3} = 8.21.$$

All Higgs bosons are nearly degenerate with $\Gamma_i \gtrsim \Delta M_H$!

♠ Backup

- SPS1a-like scenario

- At M_Z : Three gauge couplings $\alpha_1(M_Z)$, $\alpha_2(M_Z)$, and $\alpha_3(M_Z)$
- At m_t^{pole} : Quark and Lepton masses $m_{q,l}(m_t^{\text{pole}})$ and $V_{\text{CKM}}(m_t^{\text{pole}})$
- At M_{SUSY} : $\tan \beta(M_{\text{SUSY}})$
- At $M_{\text{MFV}} = M_{\text{GUT}}$: 19 MCPMFV Parameters

$$|M_{1,2,3}| e^{i \Phi_{1,2,3}}, \quad |A_{u,d,e}| e^{i \Phi_{A_{u,d,e}}}, \quad \widetilde{M}_{Q,U,D,L,E}^2, \quad M_{H_{u,d}}^2$$

Specifically, we have taken the parameter set:

$$|M_{1,2,3}| = 250 \text{ GeV}$$

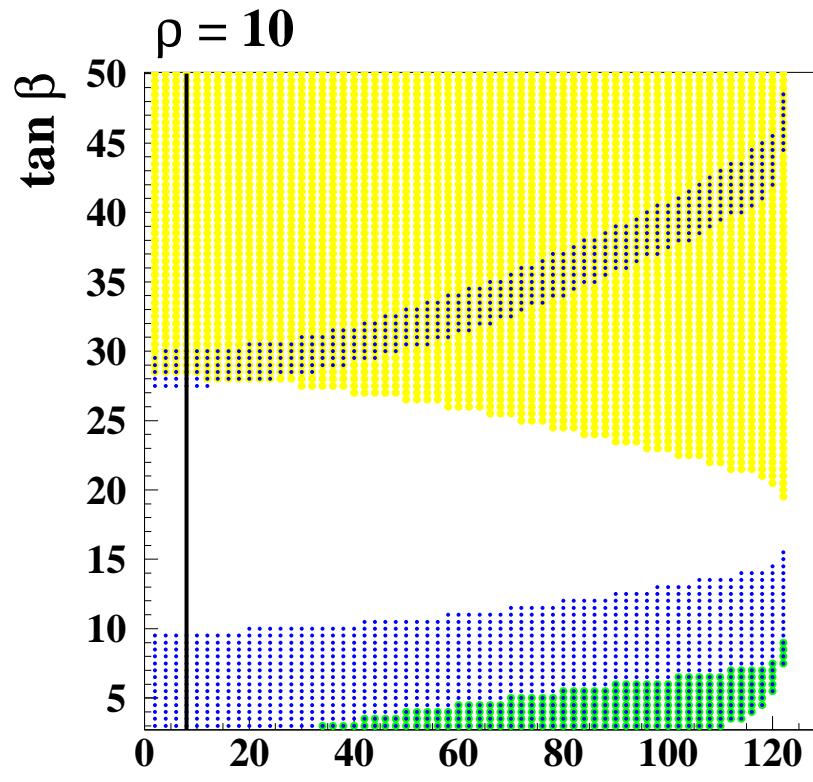
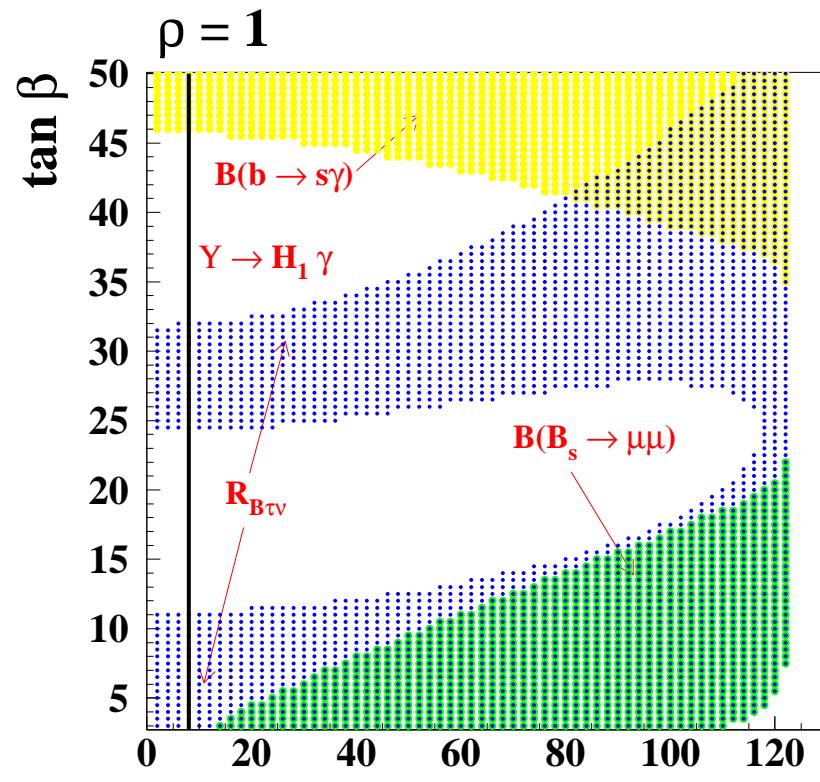
$$M_{H_u}^2 = M_{H_d}^2 = \widetilde{M}_Q^2 = \widetilde{M}_U^2 = \widetilde{M}_D^2 = \widetilde{M}_L^2 = \widetilde{M}_E^2 = (100 \text{ GeV})^2$$

$$|A_u| = |A_d| = |A_e| = 100 \text{ GeV}$$

This parameter set is equivalent to SPS1a when $\Phi_{A_{u,d,e}} = 180^\circ$ and $\Phi_{1,2,3} = 0^\circ$ if $M_{\text{SUSY}} = m_t^{\text{pole}}$ and $\tan \beta = 10$

♠ Backup

- The B -meson observables strike against CPX!: $B(B_s \rightarrow \mu^+ \mu^-)$ (95 %), $B(B \rightarrow X_s \gamma)$ (2 σ), $R_{B\tau\nu}$ (1 σ), $\Upsilon(1S) \rightarrow H_1 \gamma$ CPX scenario with $\Phi_A = \Phi_3 = 90^\circ$ and $M_{\text{SUSY}} = 0.5$ TeV JSL, M. Carena, J. Ellis, A. Pilaftsis, C.E.M. Wagner, arXiv:0712.2360; JSL and S. Scopel, PRD75(2007)075001



The CPX scenario excluded ? ... flavour-mixing terms