

Quantum transport in nanostructures

奈米結構中的量子輸運

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Outline:

1. Introduction

Why molecular electronics?

Quantum transport theory

2. Comparison with experiments

A self-assembly monolayer (SAM)

A single molecule: High and low conductance

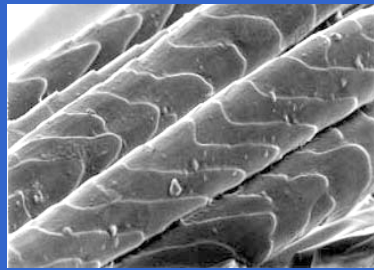
3. Spontaneous oscillation of current

A C₆₀ molecule

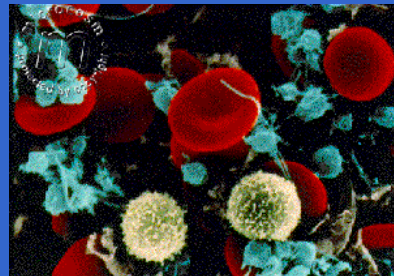
4. Ongoing works

5. Summary

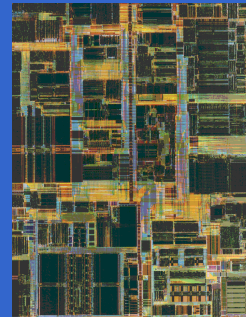
1. Introduction:



Human hair



Cells



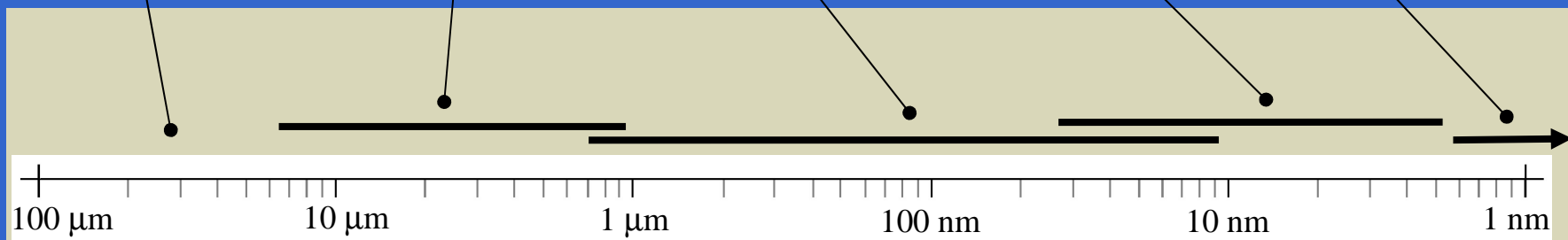
Transistors in
Integrated Circuits



Biological
Macromolecules



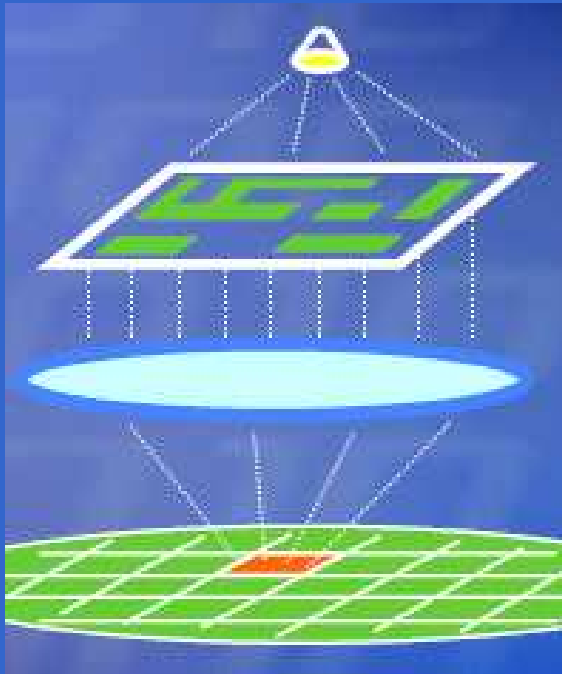
Atoms and
molecules



Nanotechnology: works at the atomic, molecular and supra-molecular levels, at the **0.1 – 100 nm scale**, with **fundamentally new properties**.

What's the problem?

45 nm now



Physical limit:
Diffraction of light.

Economical limitation:
Too expensive.

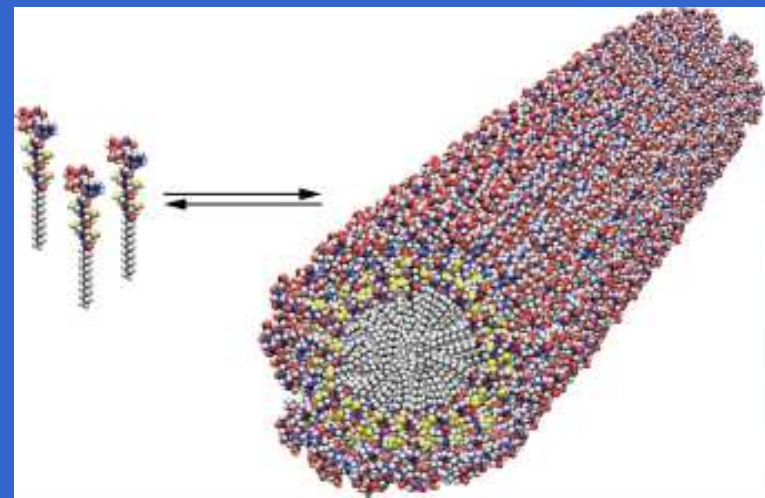
Molecular electronics: A solution

The main idea: use molecules to create analogues of today's IC chips.

Because molecules are small and can form structures by self-assembly.

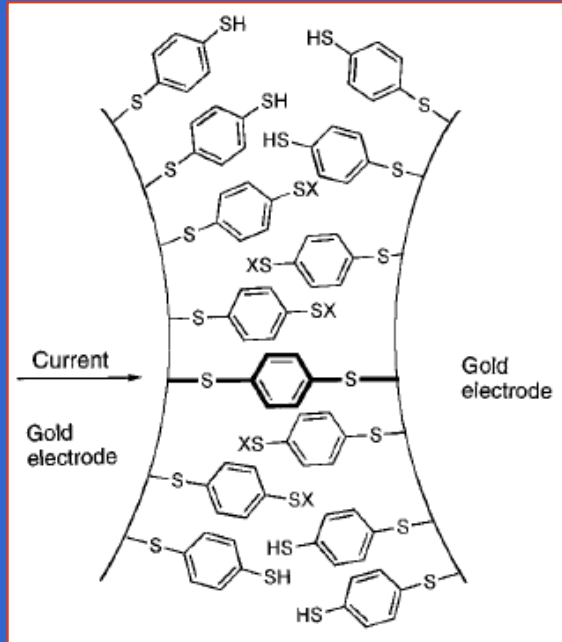
Aviram & Ratner, (1974).

For example ..

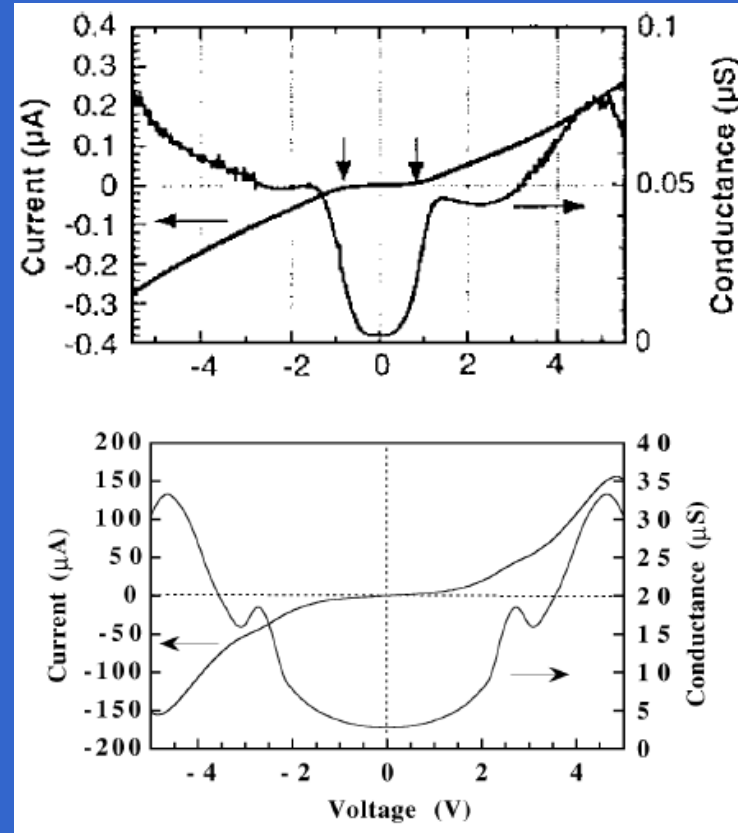


self-assembled
bioactive nanofiber *Science*, **294**, 1684 (2001)

Previous measurement and modeling:



Science 278, 252 (1997)

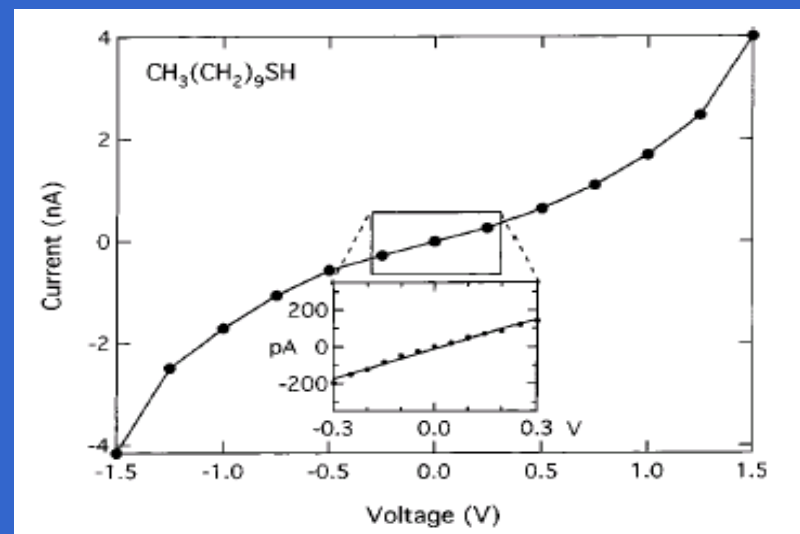
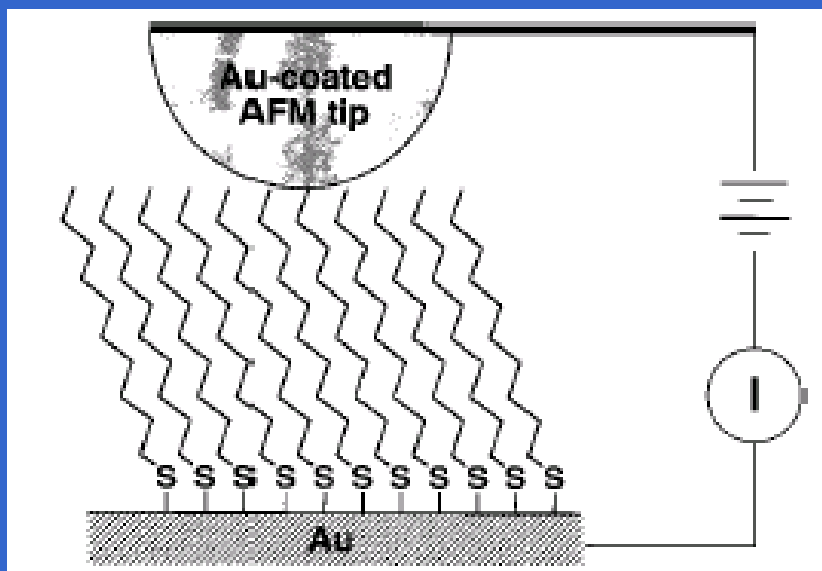


PRL 84, 979 (2000)

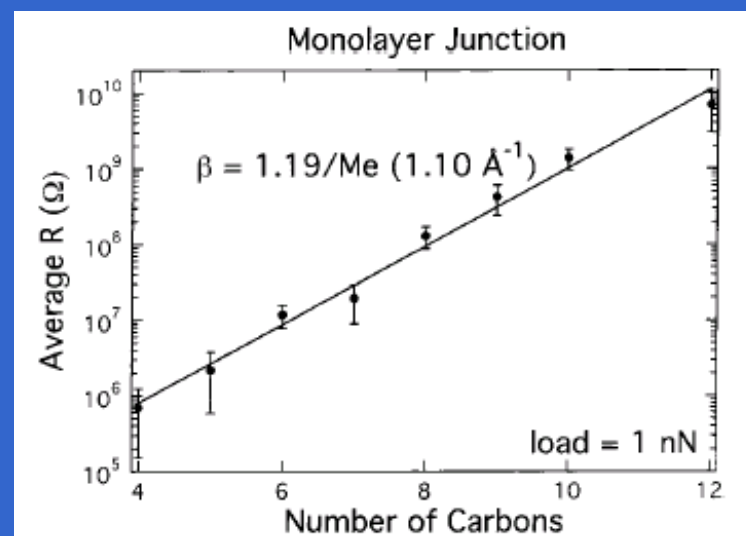
500 times of difference!

A SAM measurement: Alkanethiol molecular wires.

Wold and Frisbie, JACS 123, 5549 (2001)



Rather similar results from other groups: M. Reed et al (2003); Lindsay et al, Nanotechnology, 13, 5 (2002).



Quantum transport theory:

Ohm's law:

$$R = \frac{L}{\sigma A}$$

?

Coherence length:

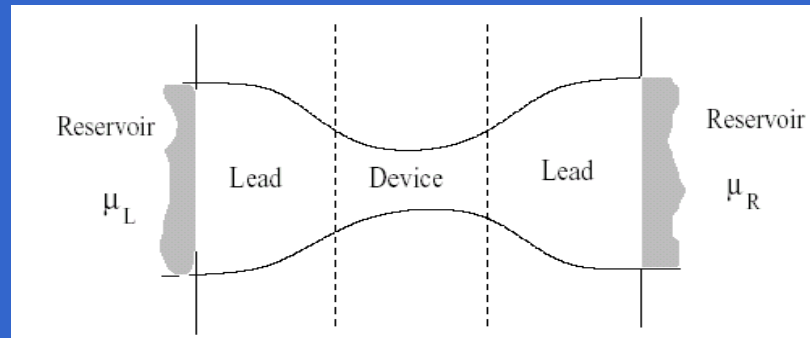
$$l_{\phi}$$

Elastic mean free path:

$$l_m$$

Ballistic regime:

$$L < l_m < l_{\phi}$$



The resistance of a conductor:

$$R = G^{-1} = \frac{h}{2e^2 M} \approx \frac{12.9k\Omega}{M}$$

The origin of resistance : **Contact**

When not ideal, a scattering region appears:

$$R_i = 1 - T_i$$

$$G = \frac{2e^2}{h} \sum_{i=1}^M T_i = \frac{2e^2}{h} MT$$

(Landauer formula)

Our method:

How to calculate current?

Landauer formula:

$$I(V_b) = \frac{2e^2}{h} \int_{-\infty}^{+\infty} T(E, V_b) (f_l - f_r) dE$$

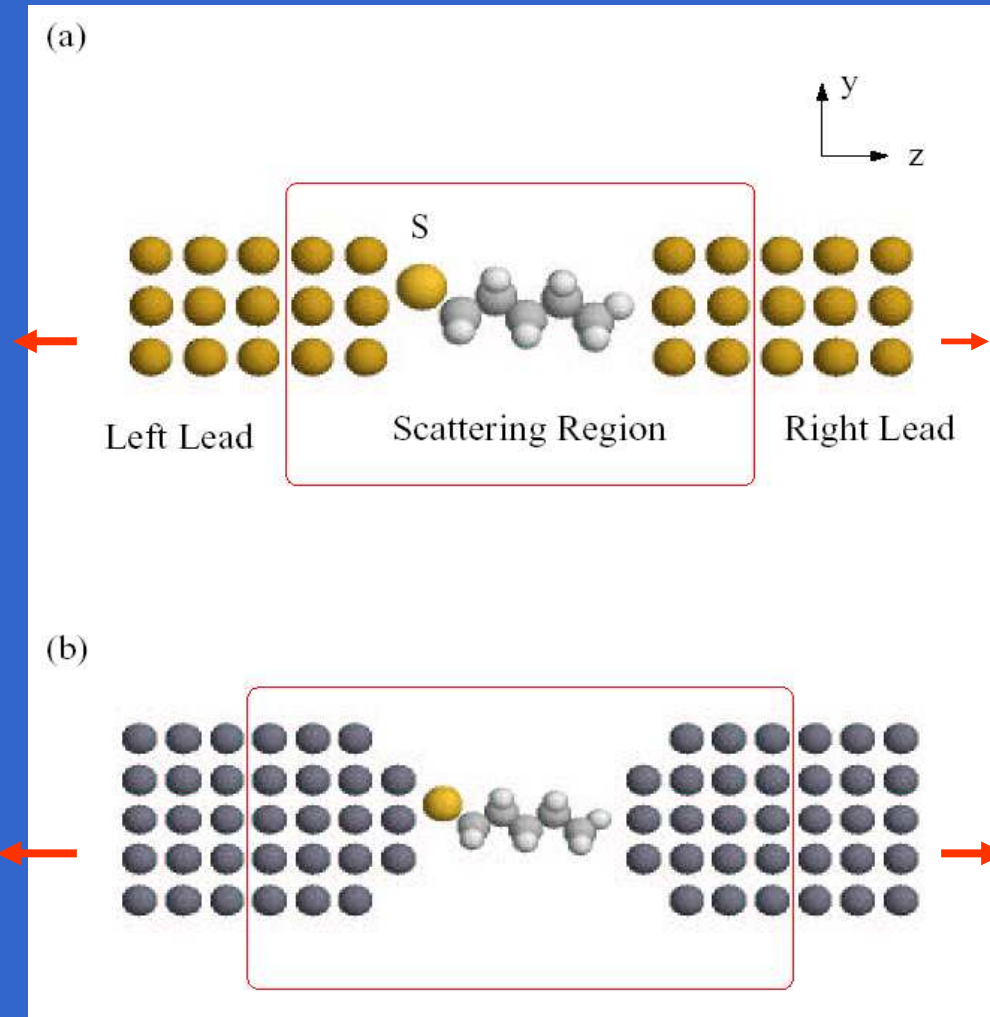
DFT plus non-equilibrium Green's functions:

Taylor, Guo, Wang, PRB 63, 245407(2001)-----McGill-Device-CALculator (McDCAL); Brandbyge, et al, PRB 65, 165401(2002)---Transiesta.

2. Comparison with experiments: Alkanethiol molecules

Our model:

Au electrodes

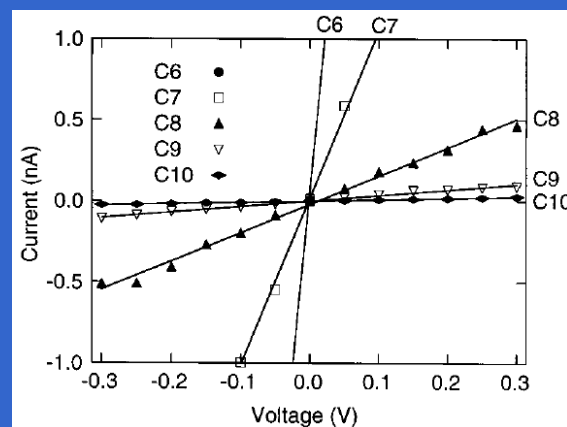
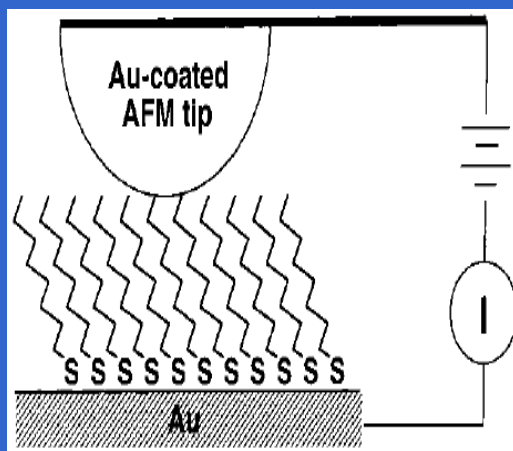


Al electrodes

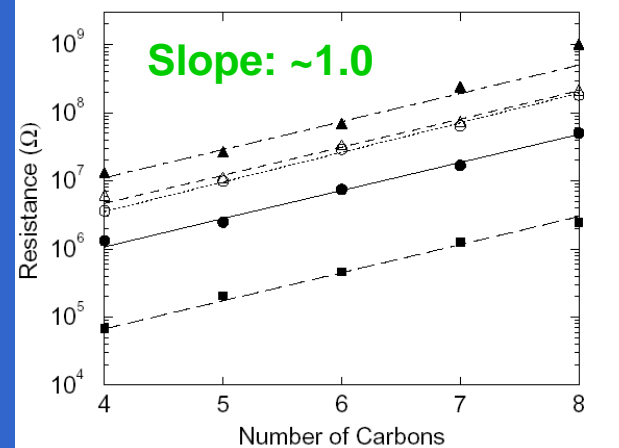
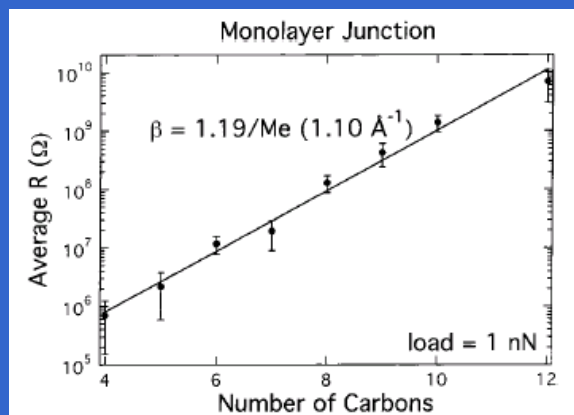
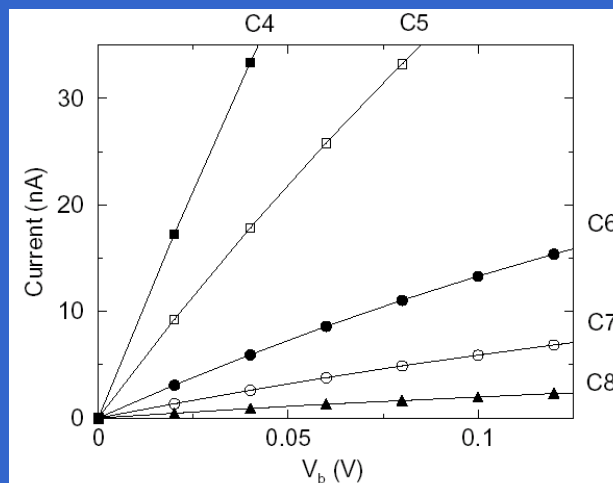
Kaun & Guo, Nano Lett. 3, 1521 (2003)

Comparison with experiments

Experiment



Our modeling

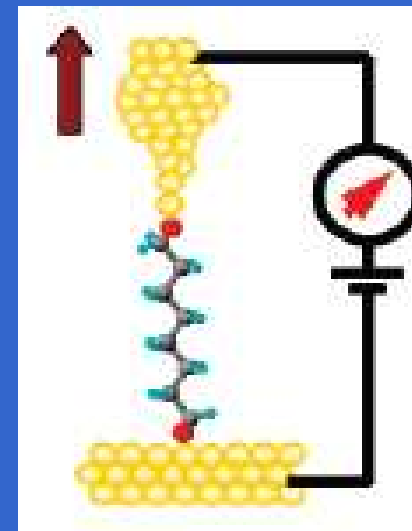
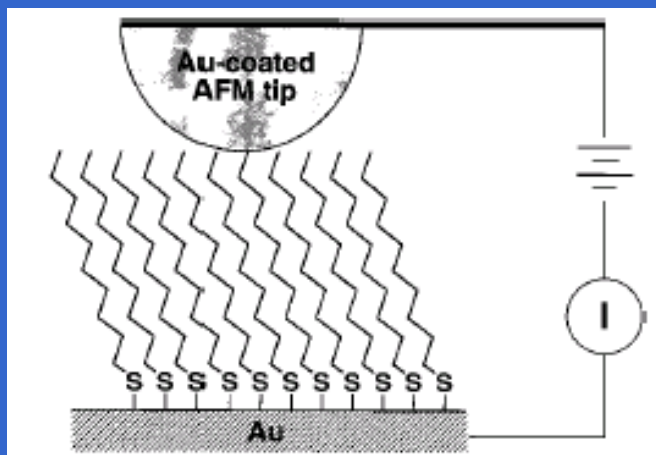


$$R_n = R_o \exp(\beta n)$$

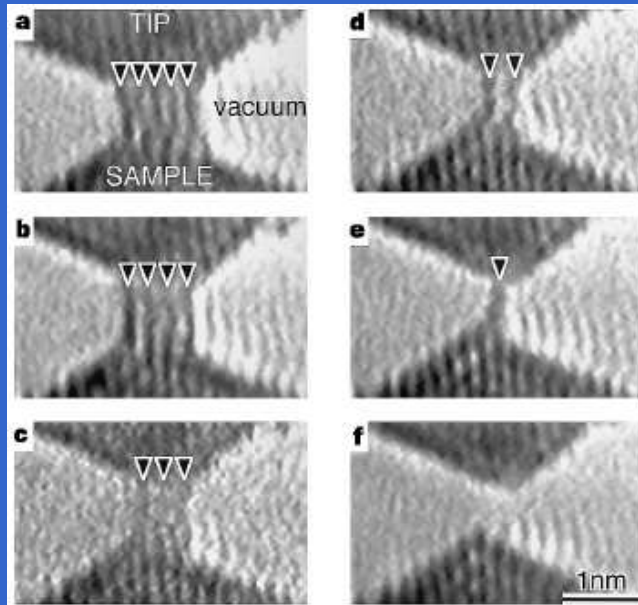
JACS 123, 5549 (2001)

Nano Lett. 3, 1521 (2003)

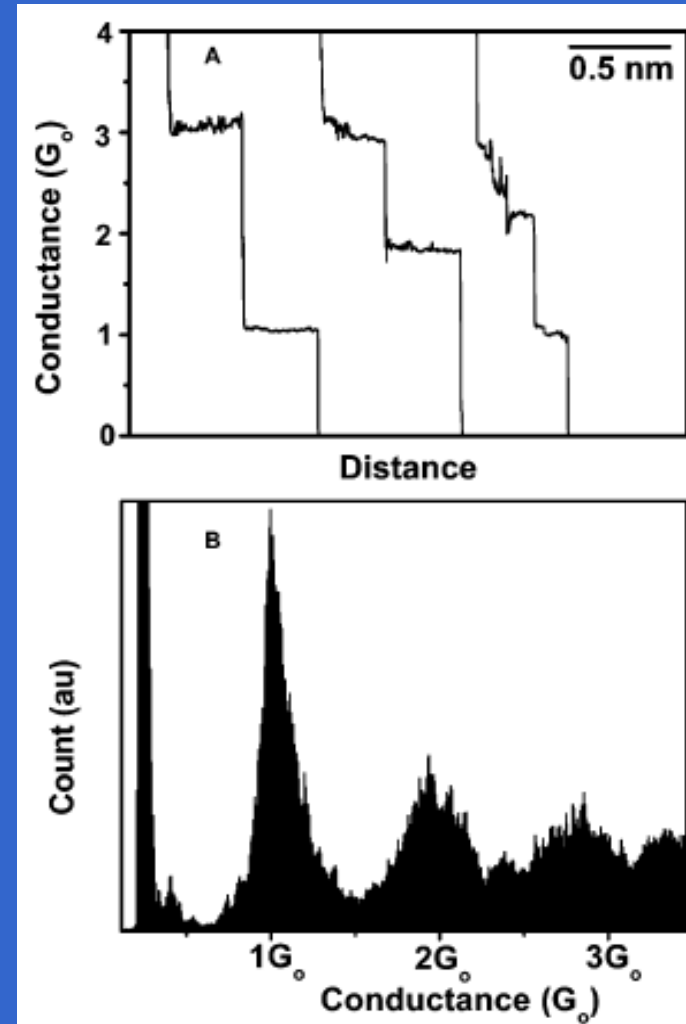
What is the single-molecule conductance?



Conductance of a Au nanowire:

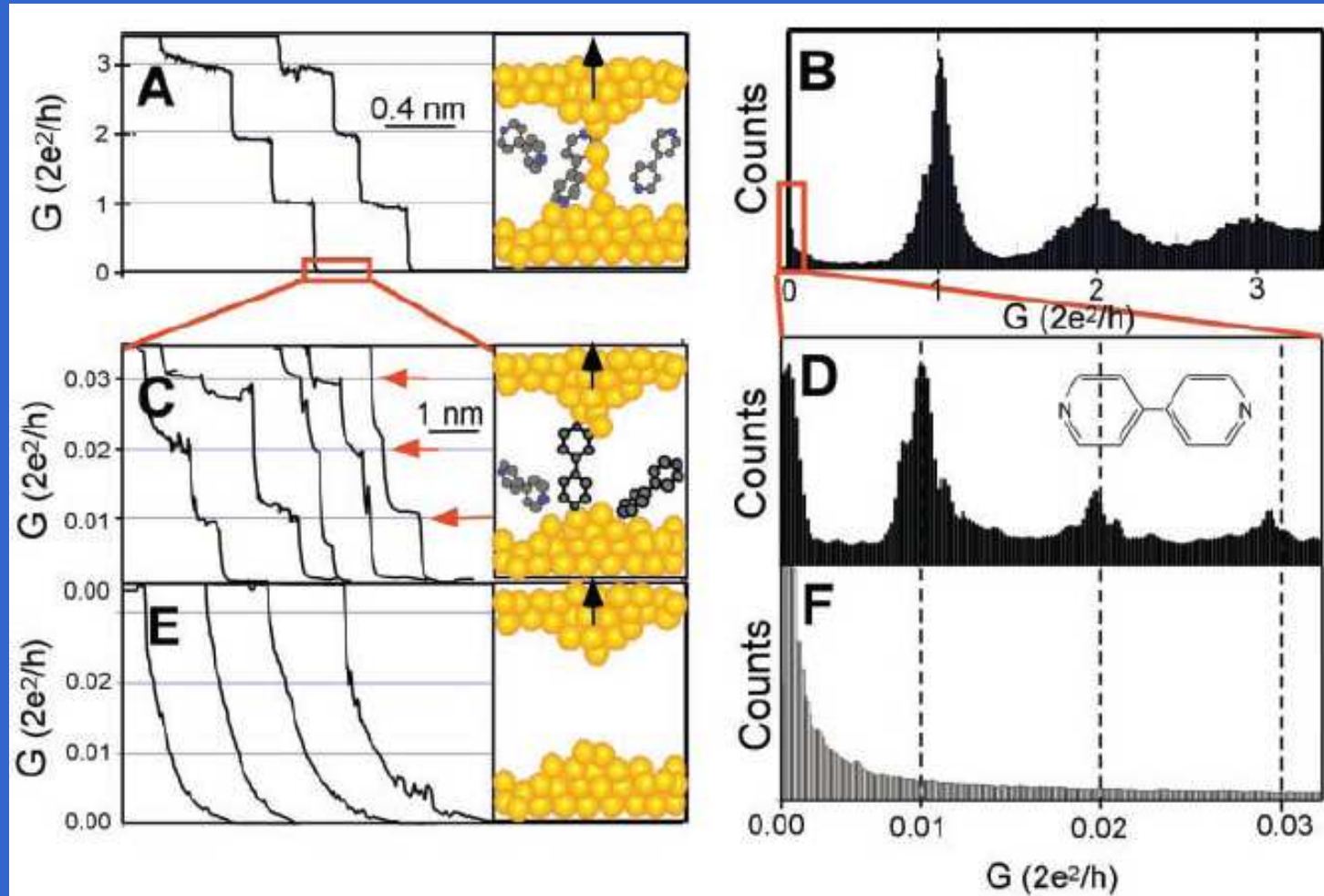


Nature 395, 780 (1998)



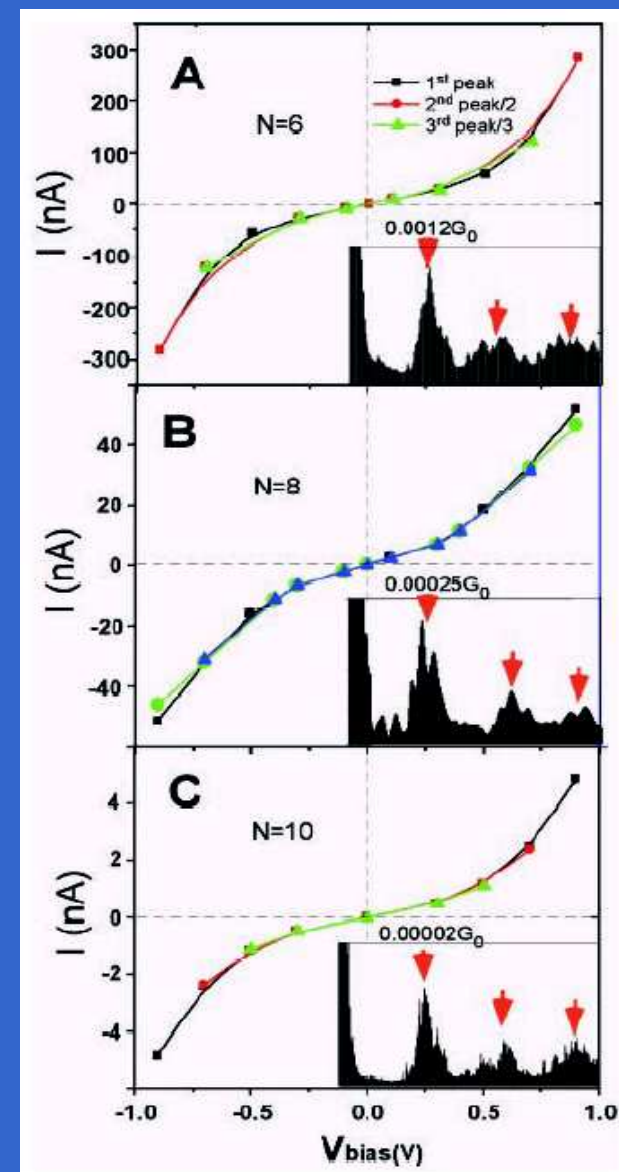
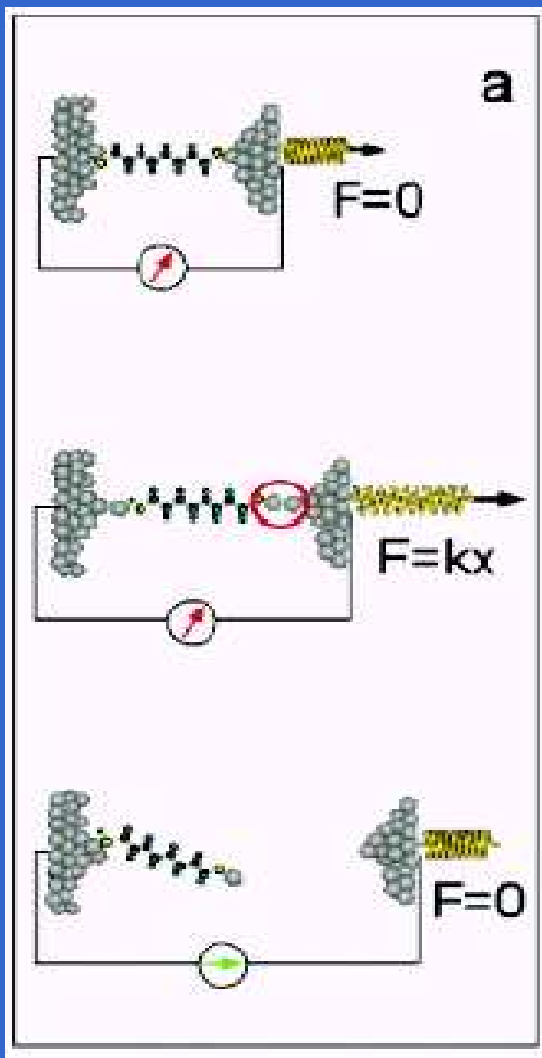
Nano Lett. 6, 2362 (2006)

Conductance of a single molecule



J. Tao et al, Science (2003)

New measurement on single alkanedithiol molecule



J. Tao et al, JACS (2003); Science (2003)

Previous modeling:

PRL 95, 156803 (2005)

PHYSICAL REVIEW LETTERS

week ending
7 OCTOBER 2005

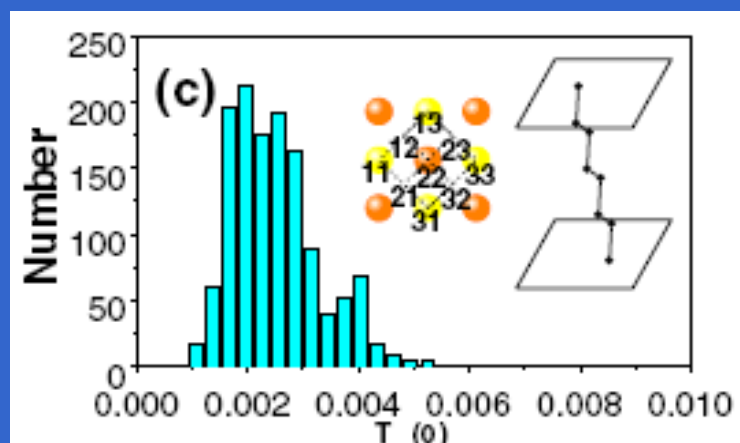
Conductance of an Ensemble of Molecular Wires: A Statistical Analysis

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(Received 21 April 2005; published 3 October 2005)



Calculation

Experiment

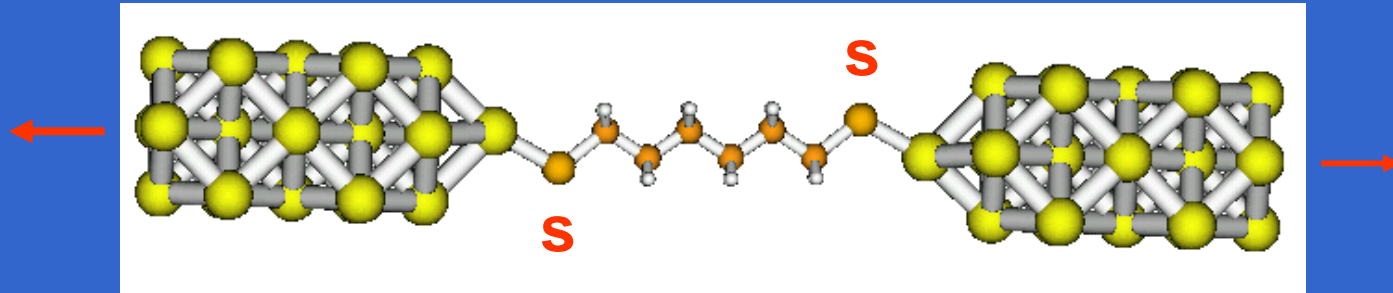
$N = 6$

$G = 0.0025$

0.0012

Unit: G_0

Our model:



Calculation

Experiment

$$N = 6$$

$$G = 0.0010$$

$$0.0012$$

$$N = 8$$

$$G = 0.00013$$

$$0.00025$$

$$N = 10$$

$$G = 0.00002$$

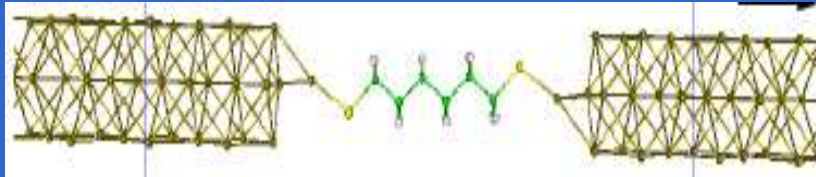
$$0.00002$$

Unit: G_0

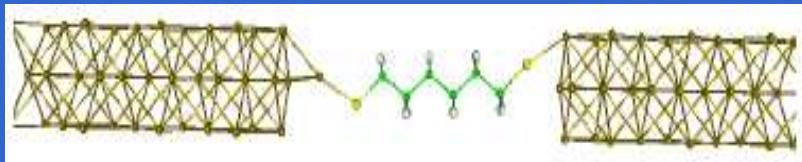
Kaun & Seideman, Phys. Rev. B 77, 033414 (2008)

Contact effect (N=6):

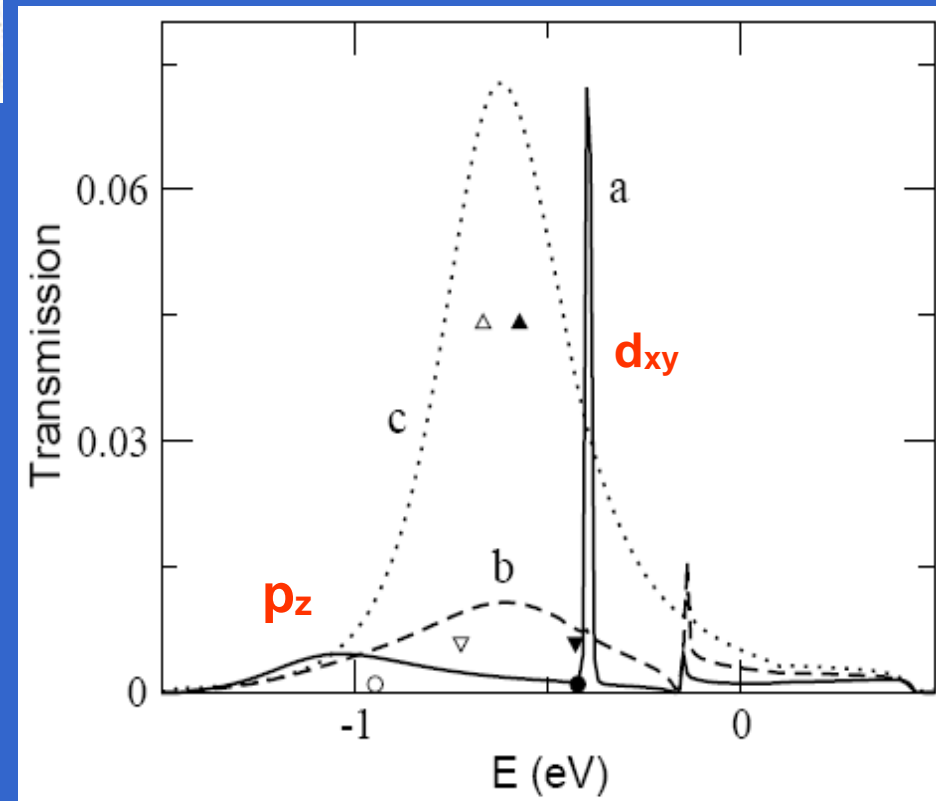
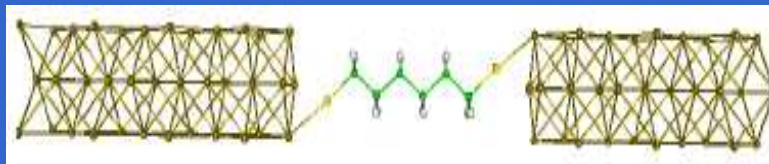
a



b

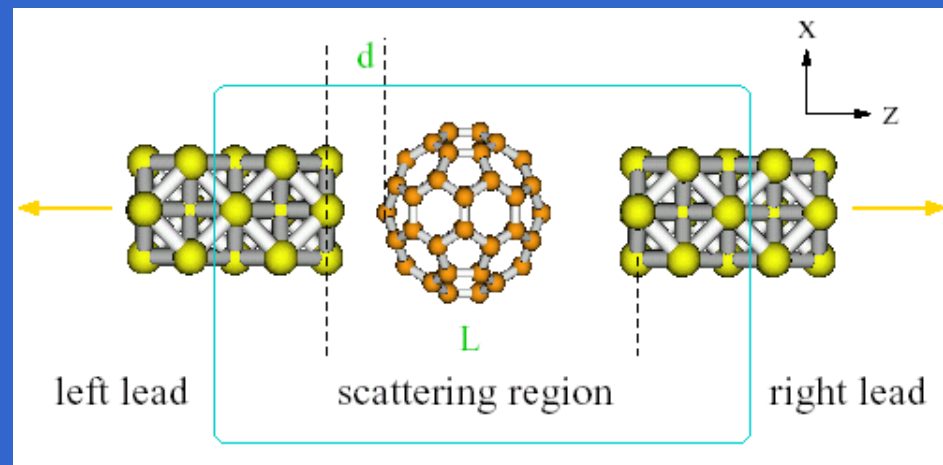


c

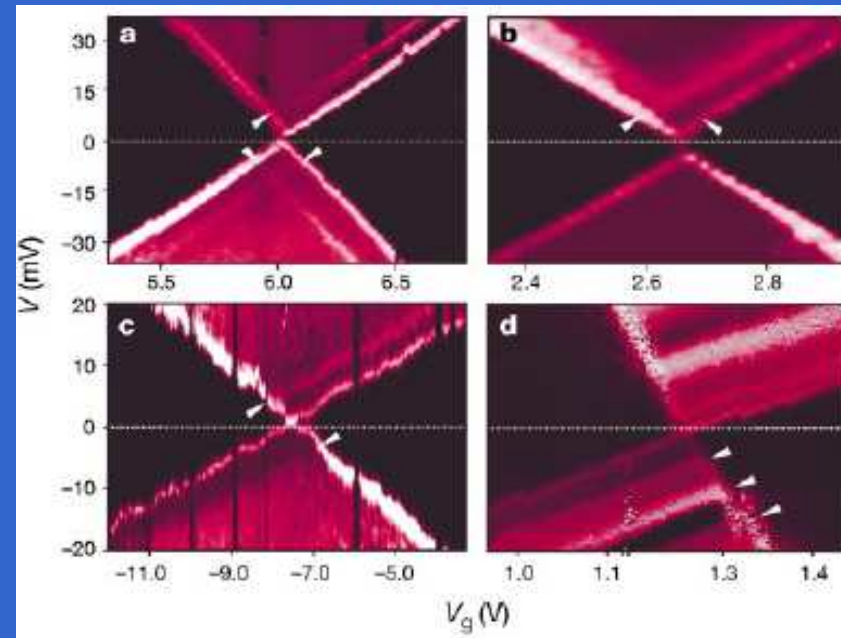
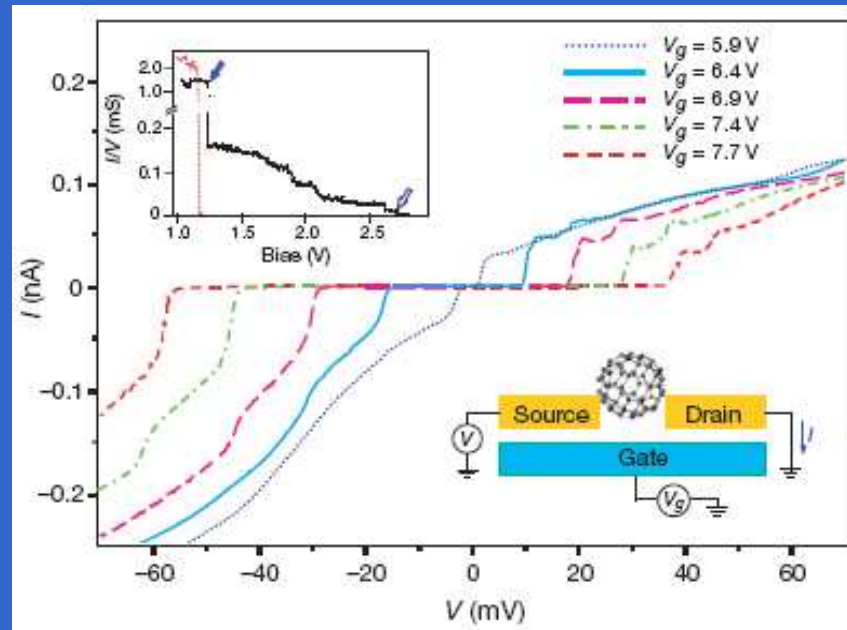


Kaun & Seideman, Phys. Rev. B 77, 033414 (2008)

4. Spontaneous oscillation of current

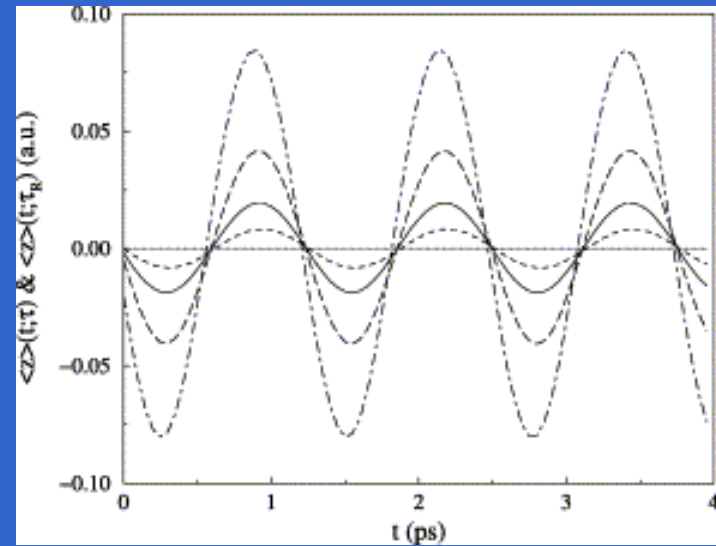
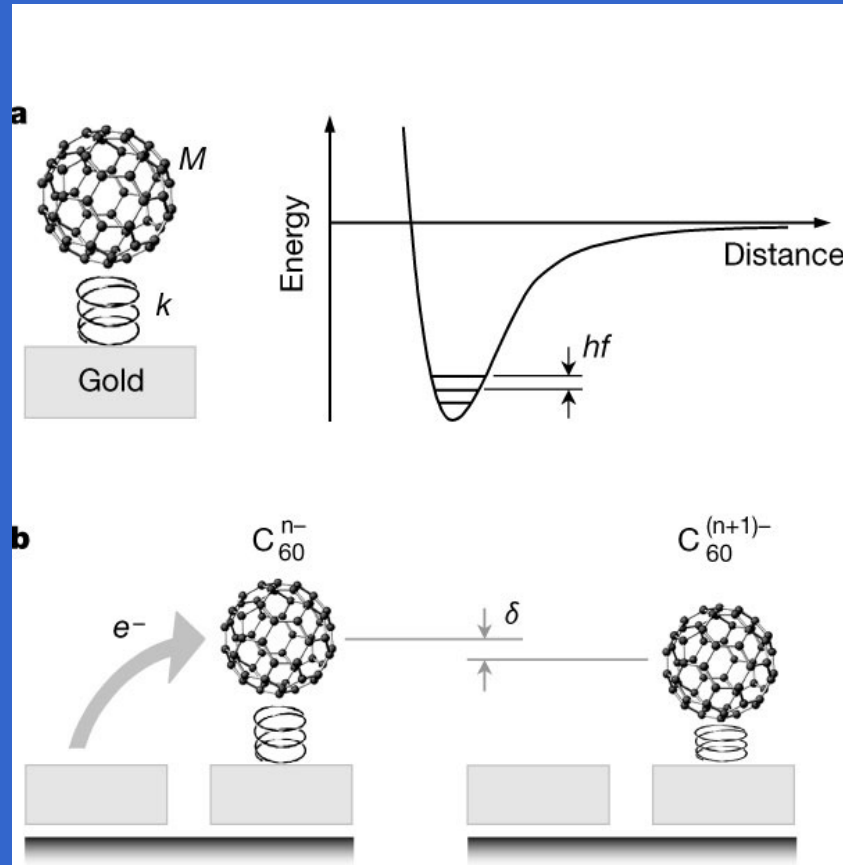


Nanomechanical oscillations in a single-C₆₀ transistor



H. Park, et al, Nature (2000)

Current-driven oscillations:



Predictions from calculations

T. Seideman, et al, Chem. Phys. (2002)

$\langle Z \rangle$ ← the lifetime of resonance

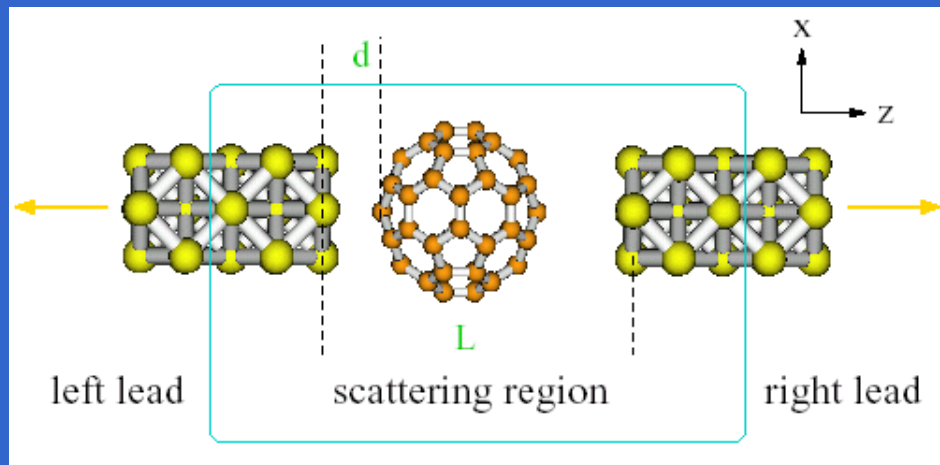
f ← the C₆₀ mass

The bouncing Bucky ball

H. Park, et al, Nature (2000)

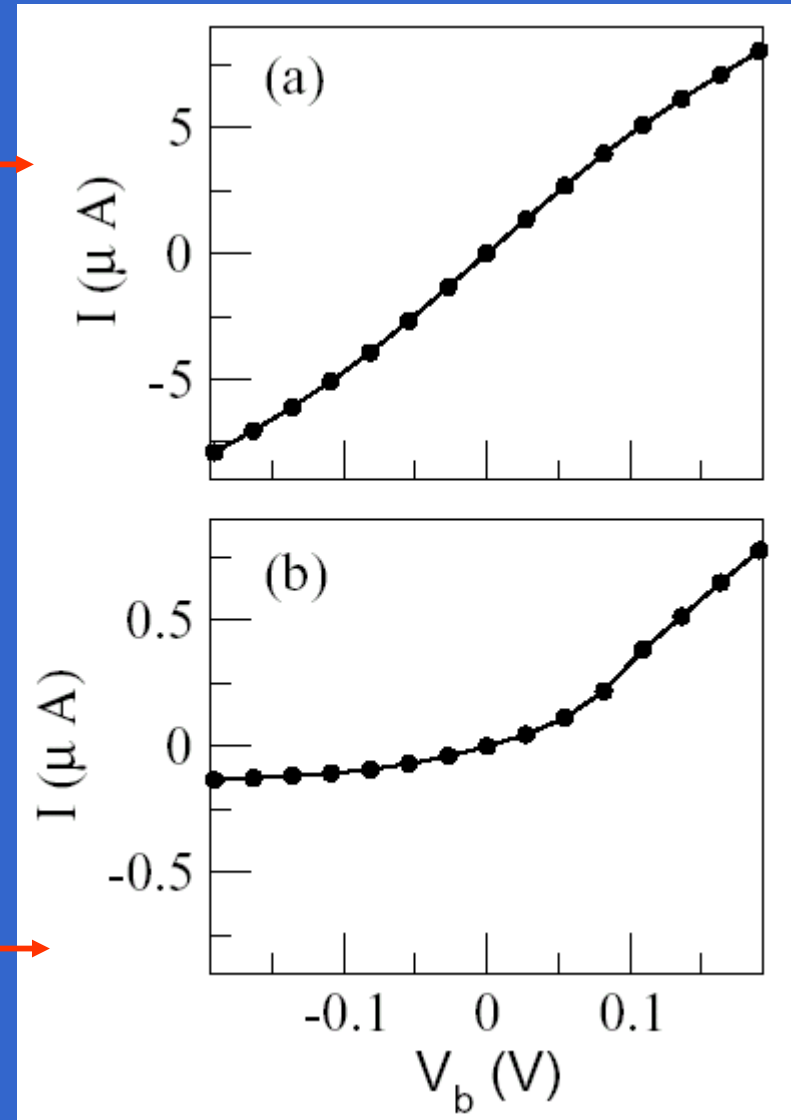
Our model:

Symmetric coupling

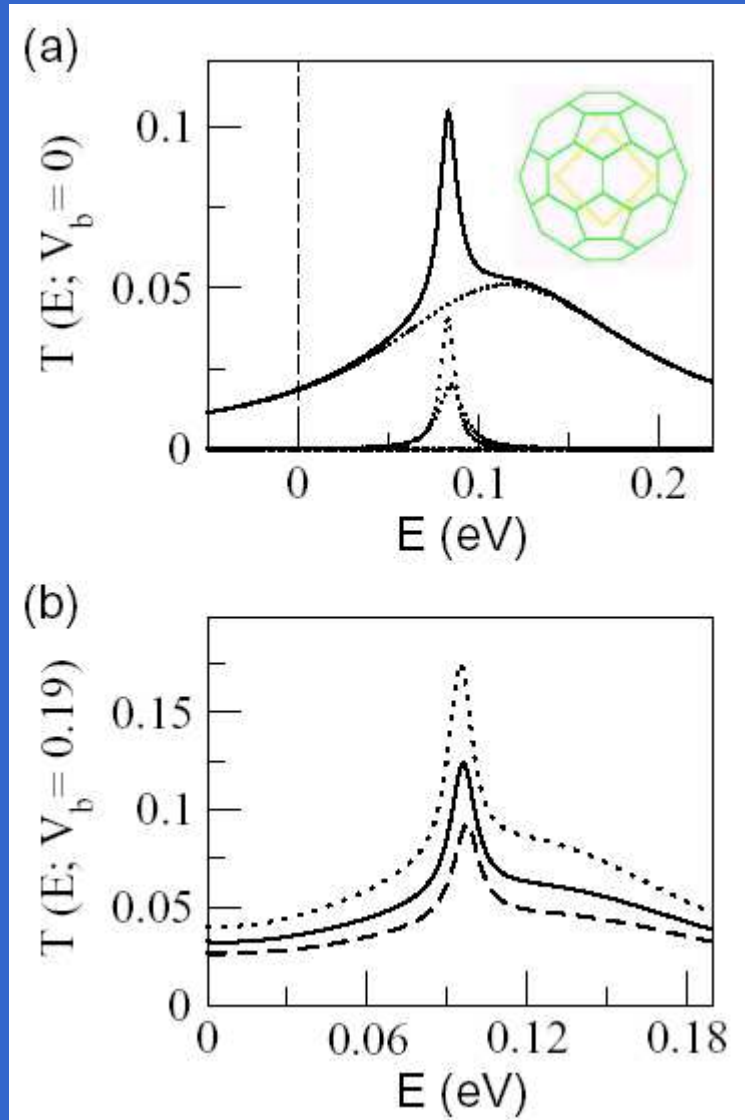


Asymmetric coupling

($L = 26.42$ a.u.)



Transmission spectra:

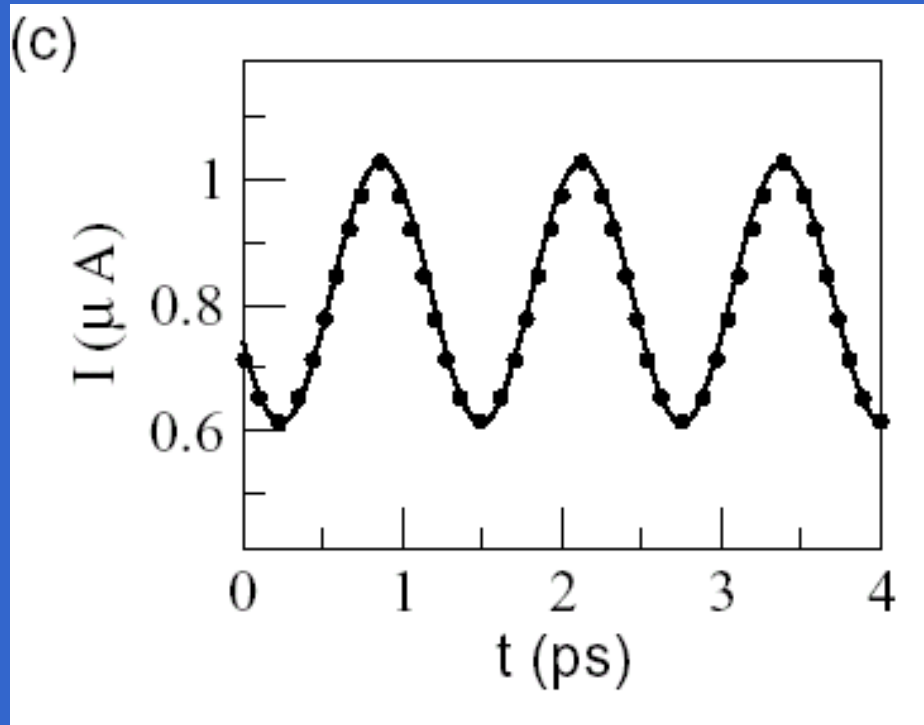


← **Three channels**

One induces the motion;
the other probes it.

← **Different locations**

Current oscillates as the molecule vibrates



The ac/dc ratio, the power output efficiency, is 0.26 ($L = 26.42$ a.u.)

When $L = 25.42$ a.u., the ratio is 0.07

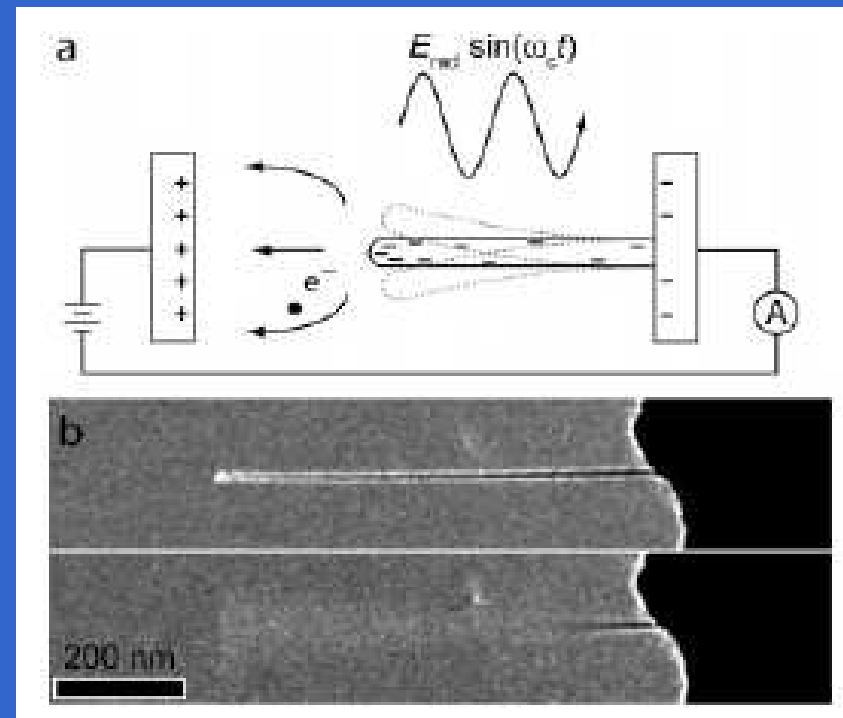
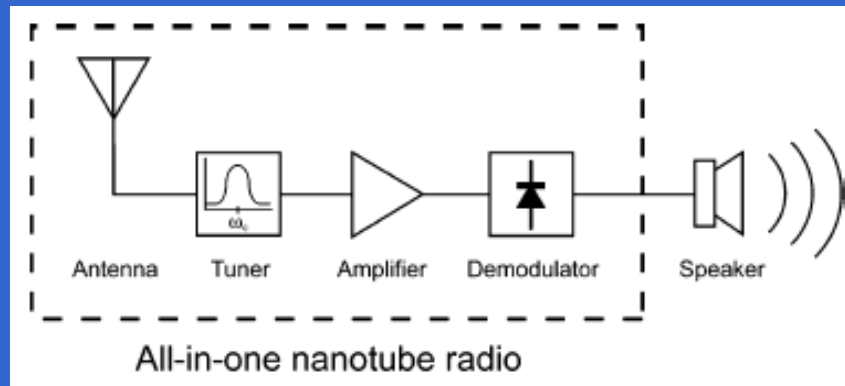
Only a range of L permits both a large ratio and high average conductance

Kaun and Seideman, PRL 94, 226801 (2005)

Applications:

- **A nanoscale generator of a radiation field, thus a THz optoelectronic device.**
- **A miniature mass spectrometry.**
- **The direct, time-domain probing of the current-driven dynamics in nanojunctions.**

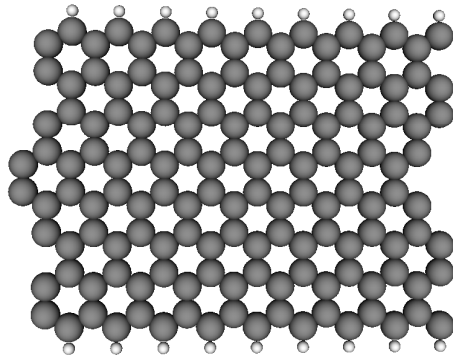
Experimentally Nanotube radio



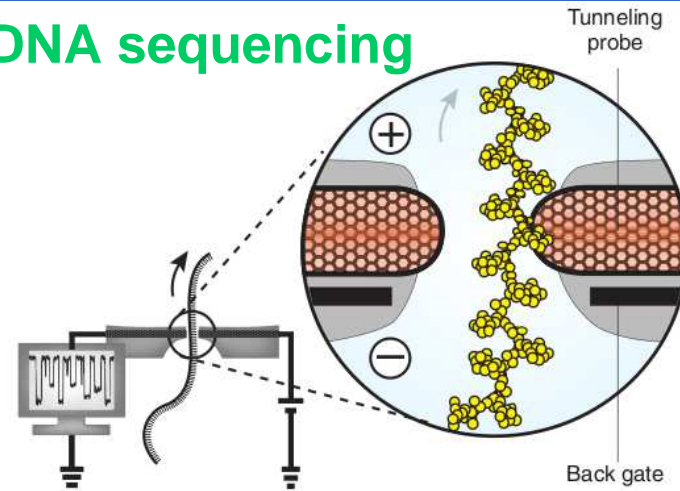
A. Zettl et al, Nano Lett. 7, 3508 (2007)

Ongoing works:

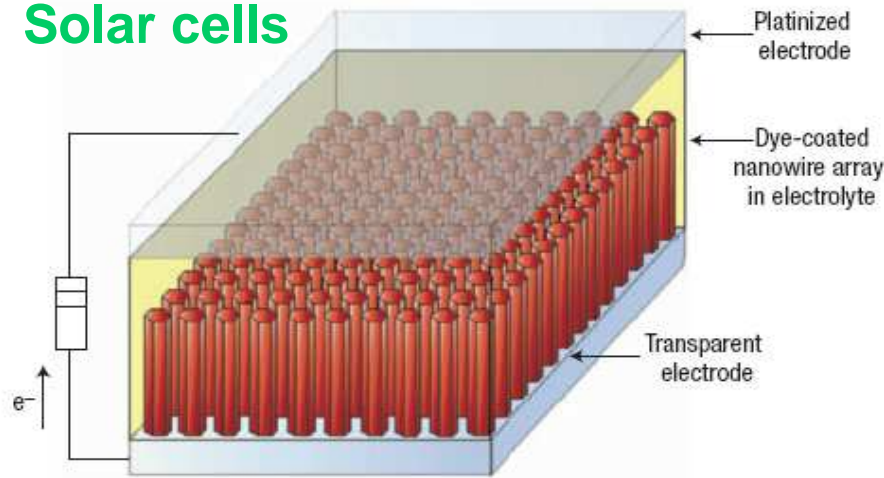
Graphene nanoribbons



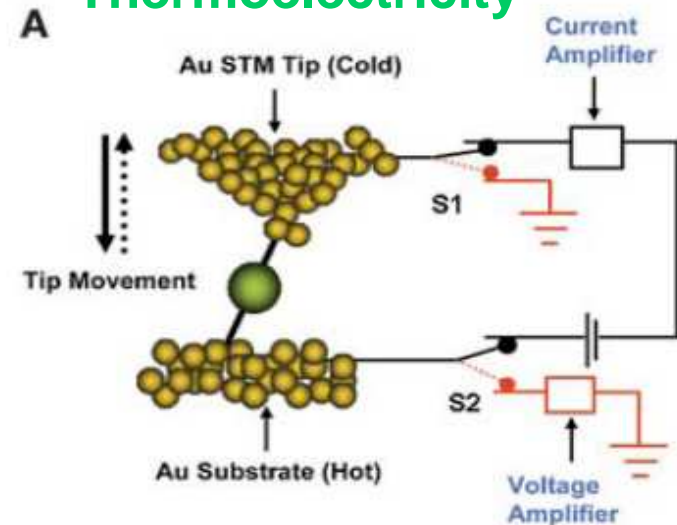
DNA sequencing



Solar cells



Thermoelectricity



Summary:

- **Conductance are quantitative consistent to experimental data**
- **The structure of electrodes plays an important role.**
- **Current-driven dynamics can be used to produce oscillating current in molecular junctions**
- **There are plenty of rooms in the Ballistic regime.**

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- **Prof. H. Guo McGill Univ., Canada**

