

AN n-TYPE TUNABLE TWO-DIMENSIONAL FERROMAGNETIC SEMICONDUCTOR

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Motivations

- Semiconductor Spintronics: the use of the electron's spin in addition to its charge in semiconductor devices
- This holds promise of combining multiple functionalities (Storage, logic, data processing, communications) in a single chip
- Ultimate goal: quantum computation

Outline

- Ferromagnetism in (III,Mn)As
 - Growth of FM structures
 - Magneto-transport properties: hole-mediate FM
 - Electric Field control of FM
- Theory of FM in DMSs
 - Mean Field Theory and Zener's model
 - Anomalous Hall Effect
- New Structure
- Ohmic contact to $\text{Ga}_{1-x}\text{Mn}_x\text{As}$
- Sample preparation
- Magneto-Transport Measurements
 - Electron-mediated FM with excellent gating capabilities
 - Small Anomalous Hall Effect consistent with an electron-mediated DMS
- Conclusions & Future Directions

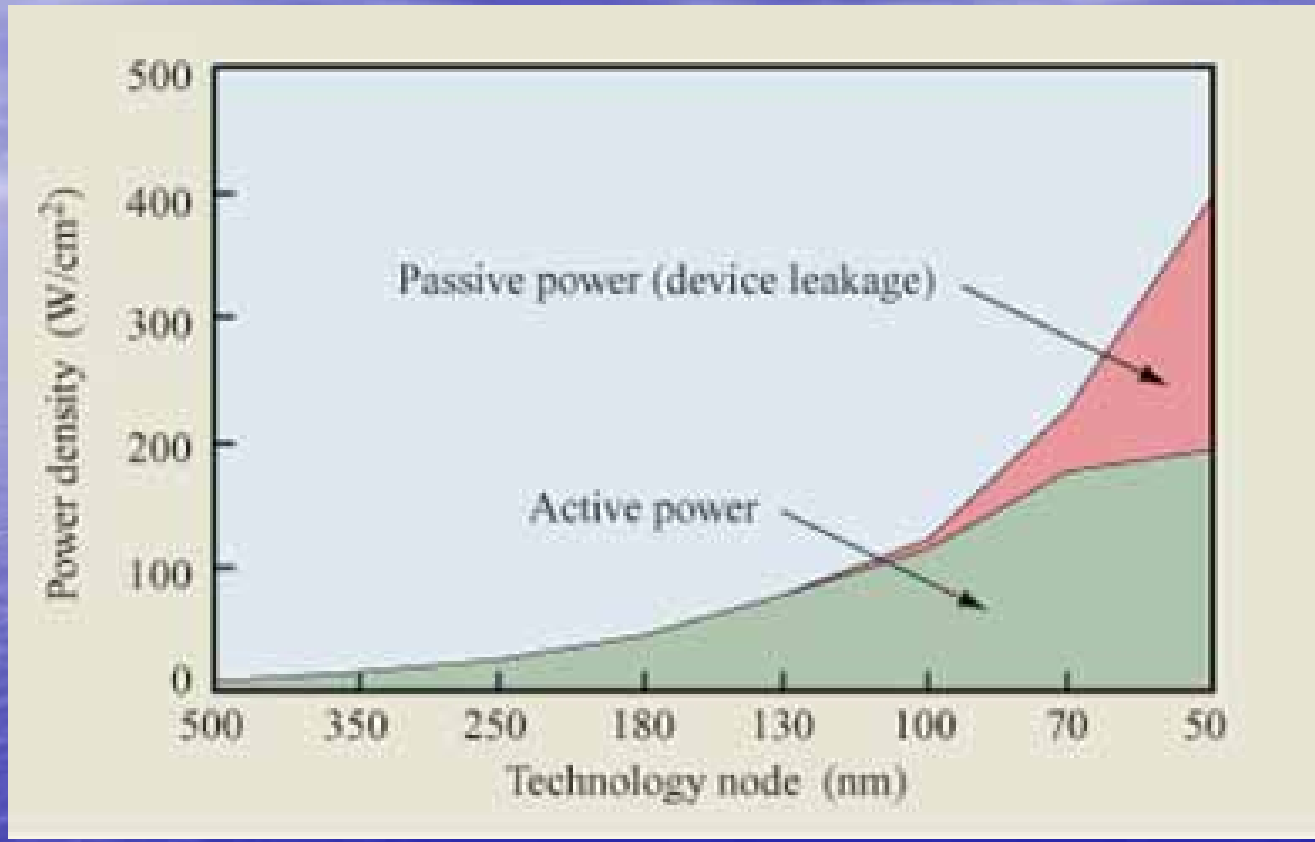
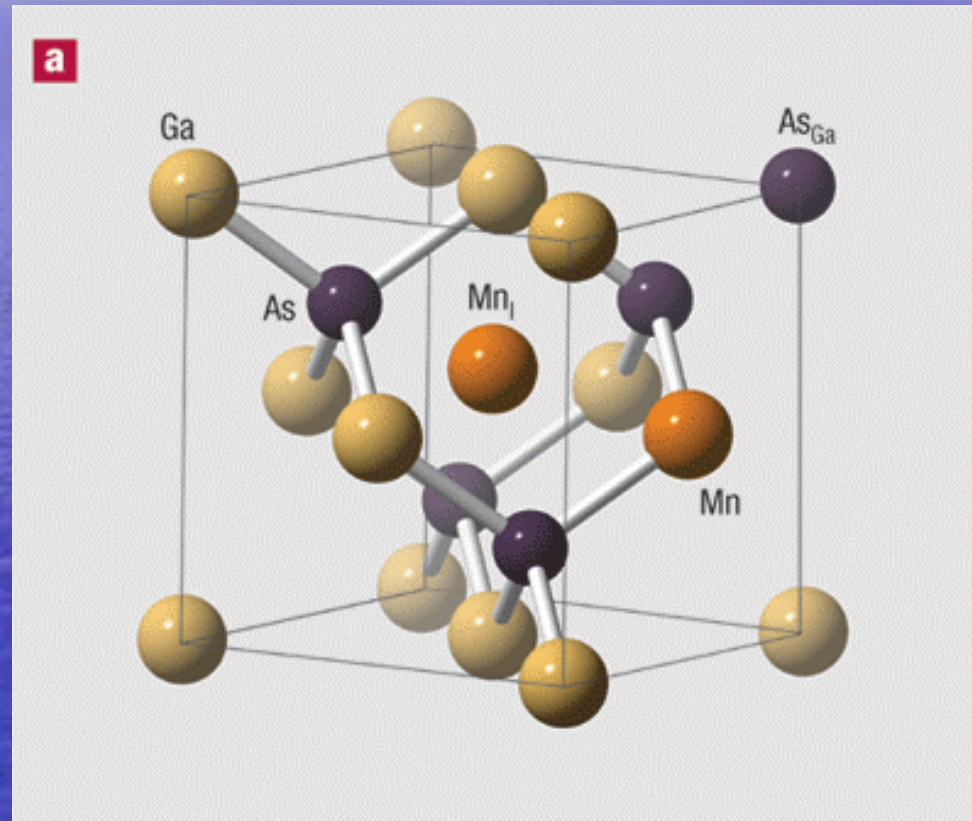
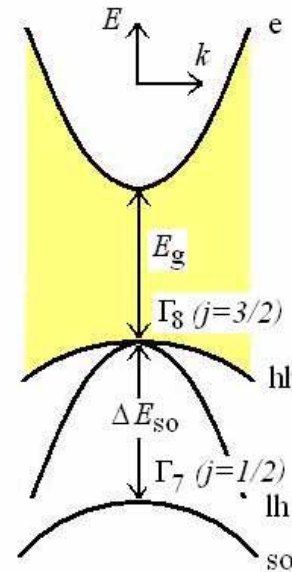
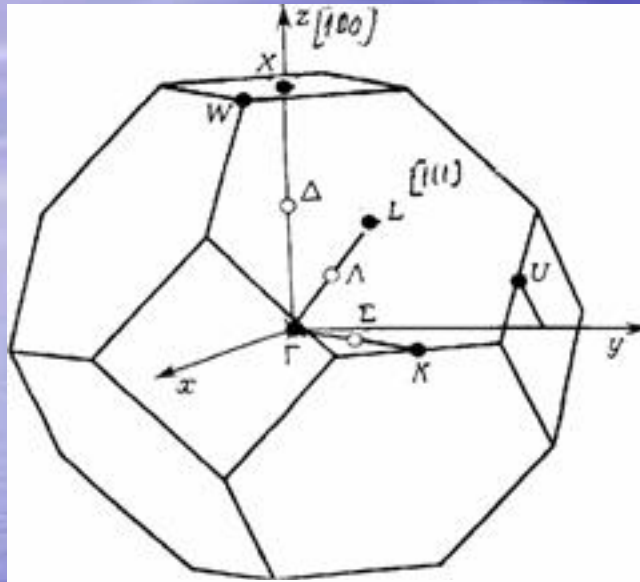


Figure 1

GaAs Crystal Structure with Mn (Zinc-blende structure)



GaAs Band Structure



Schematic electron (e), heavy hole (hh), light hole (lh), and split-off (so) bands near the center of the first Brillouin zone ($k=0$).

4×4 Luttinger Hamiltonian,

$$H_L = \frac{\hbar^2}{m_0} \left[\left(\gamma_1 + \frac{5}{2} \gamma_2 \right) \frac{k^2}{2} - \gamma_3 (\mathbf{k} \cdot \mathbf{J})^2 + (\gamma_3 - \gamma_2) \sum_i k_i^2 J_i^2 \right]$$

Bloch wave $\psi_{n\mathbf{k}}(\mathbf{r}) = e^{i\mathbf{k} \cdot \mathbf{r}} u_{n\mathbf{k}}(\mathbf{r})$ Periodic

$$H_{\mathbf{k}} u_{n\mathbf{k}}(\mathbf{r}) = \mathcal{E}_{n\mathbf{k}} u_{n\mathbf{k}}(\mathbf{r}) \quad H_{\mathbf{k}} = \frac{P^2}{2m} + \frac{1}{m} \hbar \mathbf{k} \cdot \mathbf{P} + \frac{\hbar^2 k^2}{2m} + V(\mathbf{r})$$

Spin-Orbit in GaAs

$$H_{\text{eff}} = \epsilon_k + V + H_{\text{int}} + H_{\text{ext}},$$

$$H_{\text{int}} = -\frac{1}{2} \mathbf{b}(\mathbf{k}) \cdot \boldsymbol{\sigma},$$

$$H_{\text{ext}} = \lambda \boldsymbol{\sigma} \cdot (\mathbf{k} \times \nabla V),$$

bulk inversion asymmetry

Dresselhaus term

$$H_{\text{D}, 3\text{d}} = \mathcal{B} k_x (k_y^2 - k_z^2) \sigma_x + \text{c.p.}$$

Quantum well (2D)

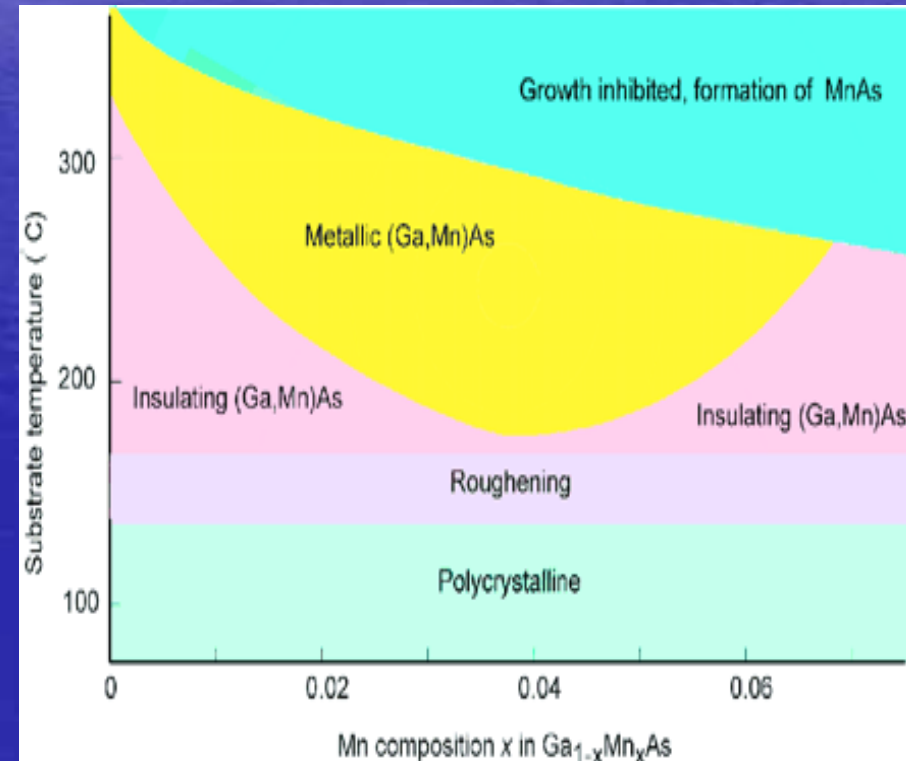
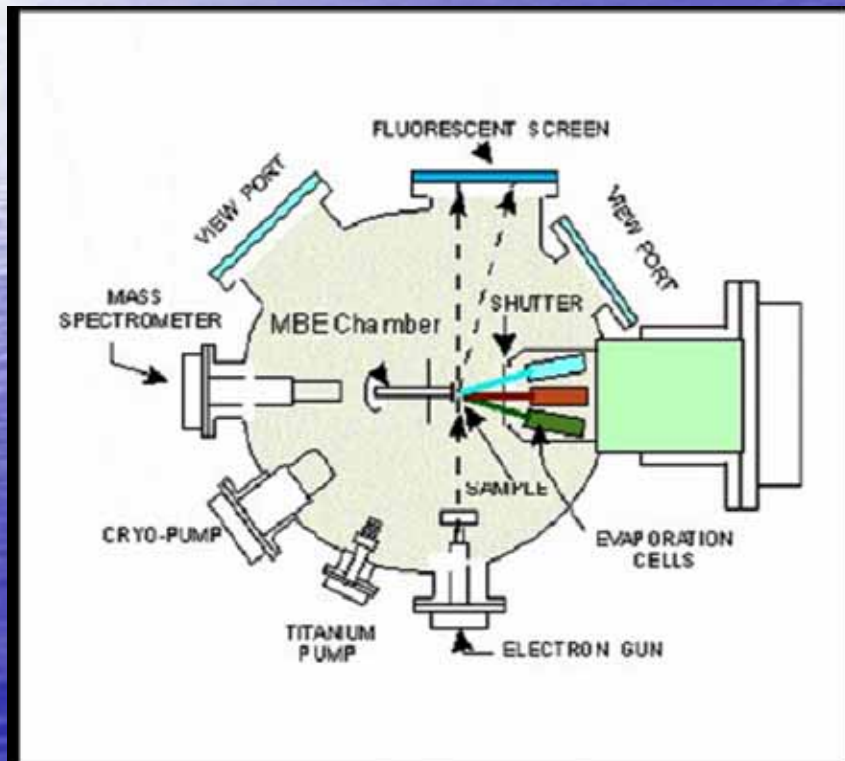
Rashba Hamiltonian

$$H_{\alpha} = \alpha (k_y \sigma_x - k_x \sigma_y) \propto \langle \nabla_z V \rangle$$

$$\mathbf{b}(\mathbf{k}) = 2\alpha \hat{\mathbf{z}} \times \mathbf{k}$$

Ferromagnetism in (III,Mn)As

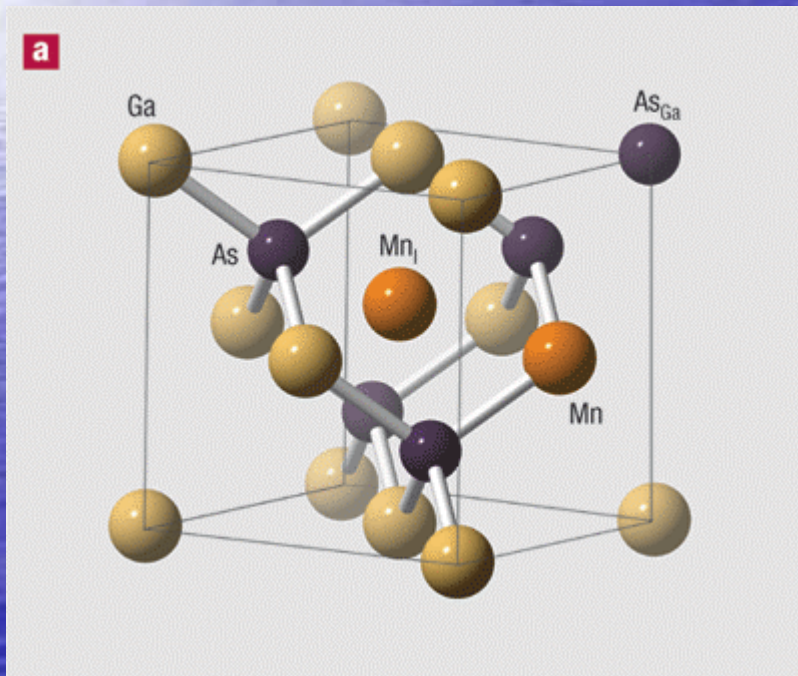
- LT-MBE growth
- Phase diagram: relation between growth parameters and the properties of GaMnAs



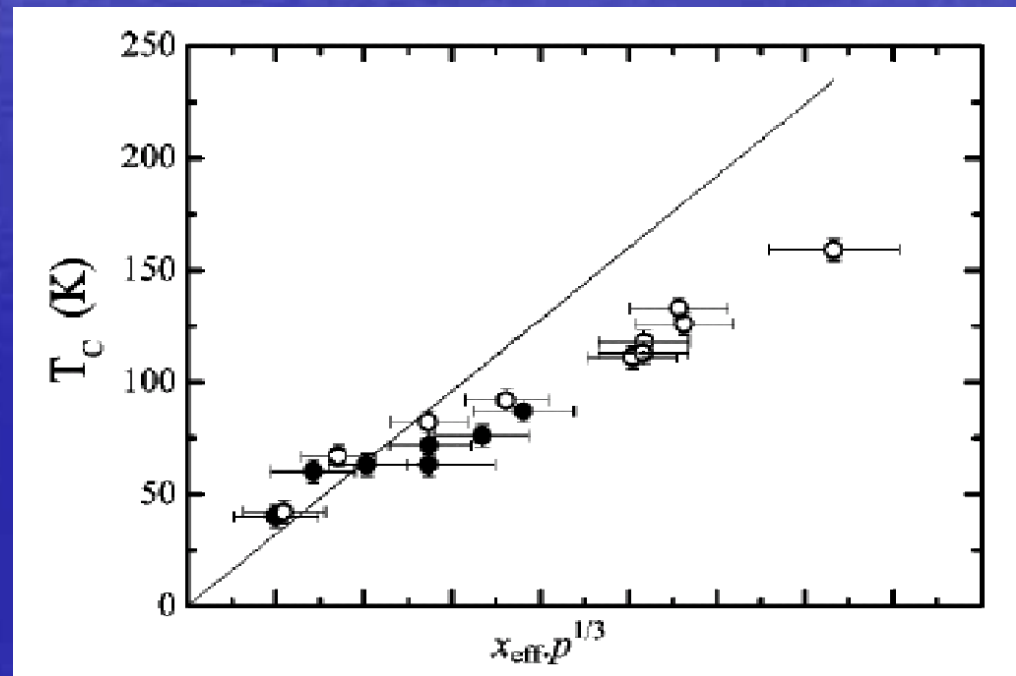
H. Ohno Science 281, 952 (1998)

Ferromagnetism in (III,Mn)As

- Substitutional Mn and growth defects
- Curie temperature increase with post-growth thermal annealing



MacDonald et al. Nature 4, 195 (2005)

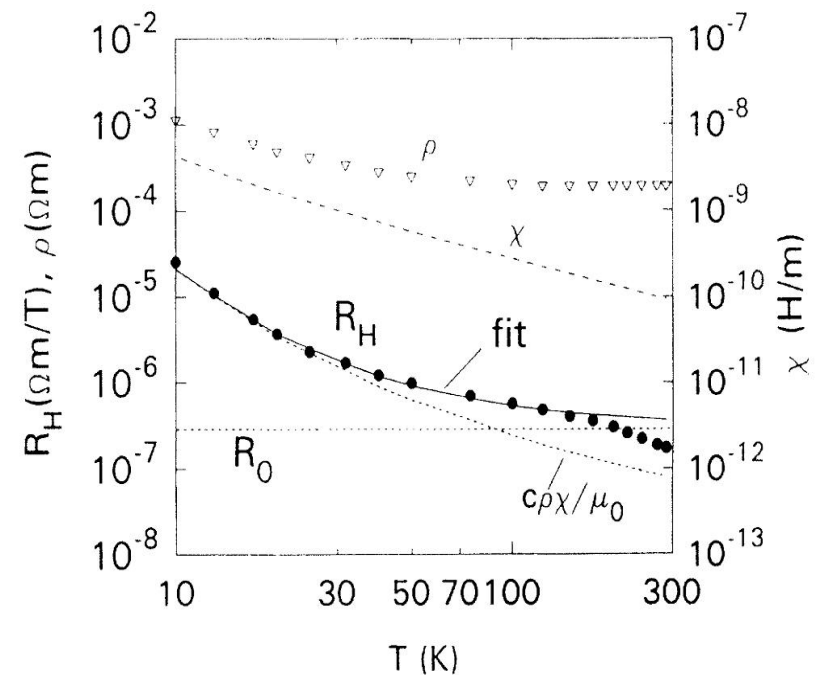
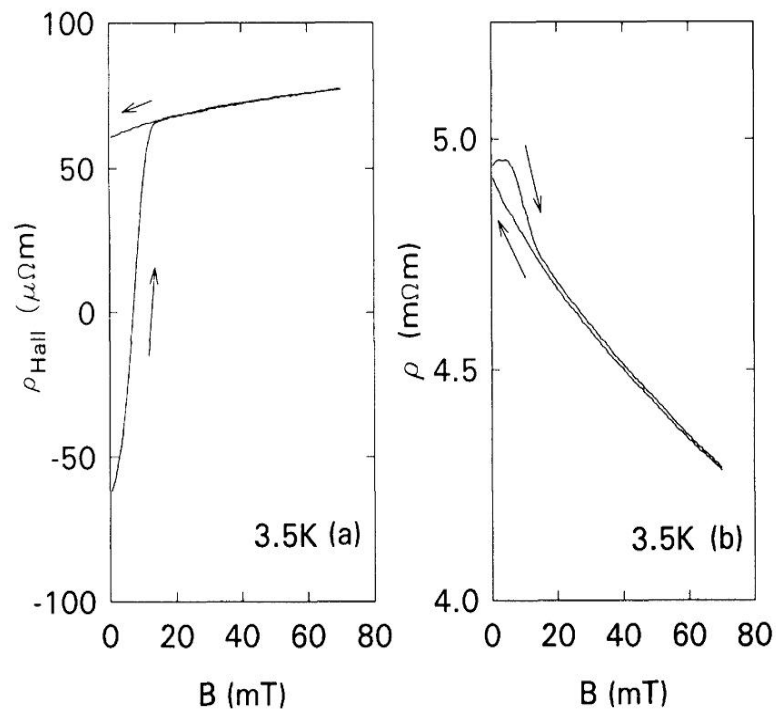


Wang et al. JAP 95, 6512 (2004)

Ferromagnetism in (III,Mn)As

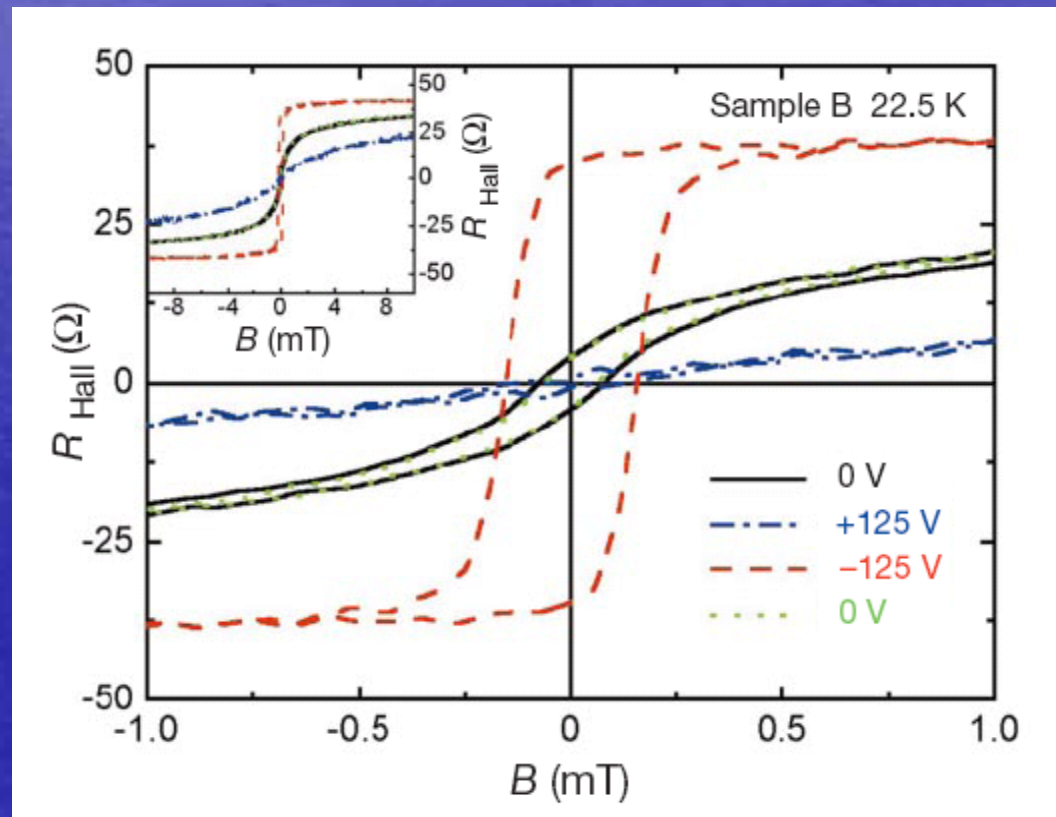
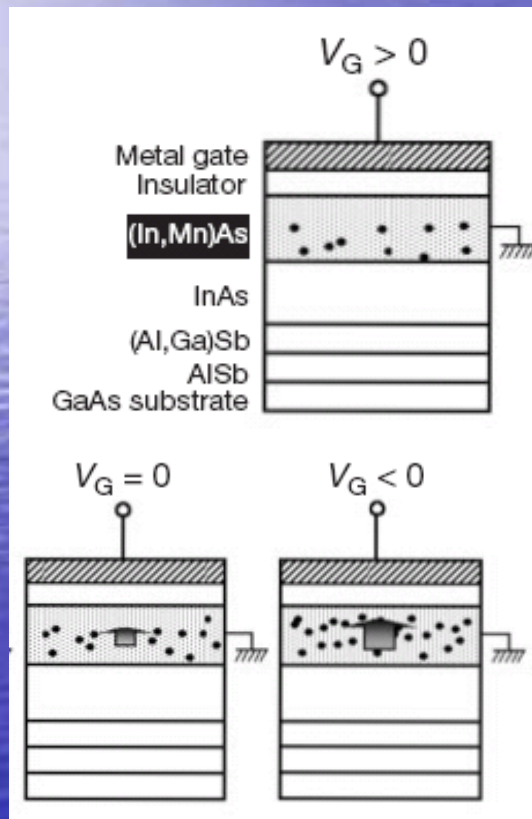
- First DMS InMnAs: $T_C \sim 7.5\text{K}$
- AHE in the Hall coefficient vs. temperature plot

Ohno et al. PRL 68, 2664 (1992)



Ferromagnetism in (III,Mn)As

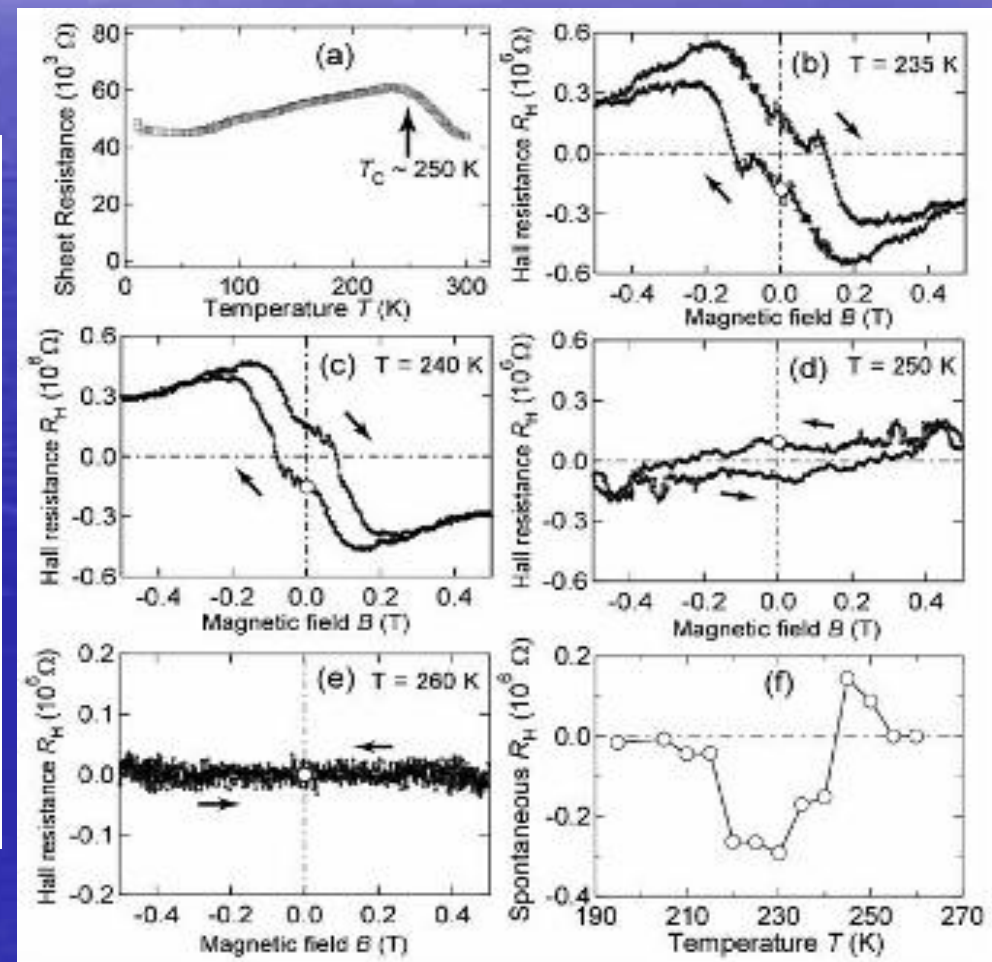
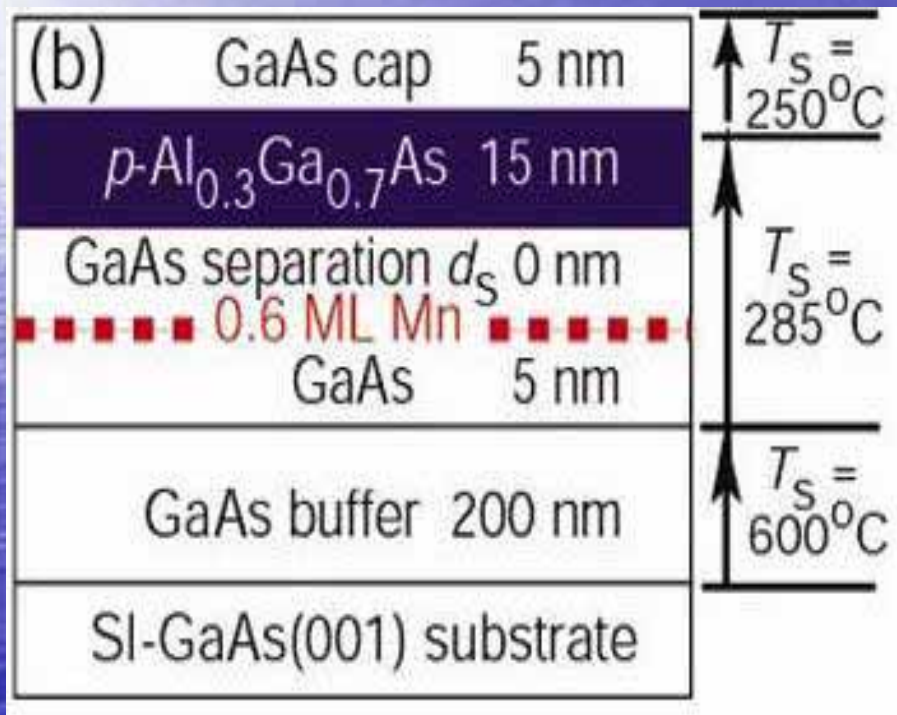
- Electric field control of FM



Ohno et al., Nature 408, 944 (2000)

Ferromagnetism in (III,Mn)As

- High T_C Heterostructures: $T_C \sim 250\text{K}$



Nazmul et al. PRL 95, 017201 (2005)

Theory of FM in DMSs

- Mean Field Theory & Zener's model

Mn Spin Free energy: $F_S = \frac{1}{2} \alpha S^2$
(antiferromagnetic Mn-Mn int.)

Carrier's Free energy: $F_C = \frac{1}{2} \gamma s^2$ (kinetic energy)

Mn-Carrier Interaction: $F_{\text{int}} = -\beta s S$

Minimize $F = F_S + F_C + F_{\text{int}} \rightarrow s = (\beta/\gamma)S$

$$F = \frac{1}{2} (\alpha - \beta^2/\gamma) S^2$$

[Ferromagnetic when $(\alpha - \beta^2/\gamma) < 0$.]

$$H = H_{KL} + \vec{S} \cdot \vec{h}_{MF} \quad \xrightarrow{\text{Diagonalization}} \quad \text{Carrier's Free energy } F_C$$

$$M_S = g\mu_B N_0 x_{eff} S \left[\frac{g\mu_B |H_{MF}|}{k_B (T + T_{AF})} \right] \quad \rightarrow \quad \text{Spin's Free energy } F_S$$

$$F = F_C [M] + F_S [M]$$

$$B_J(x) = \frac{2J+1}{2J} \coth\left(\frac{2J+1}{2J}x\right) - \frac{1}{2J} \coth\left(\frac{1}{2J}x\right)$$

$$L(x) = \coth(x) - \frac{1}{x}$$

$$x = \frac{g\mu_B J B}{k_B T}$$

Theory of FM in DMSs

- Mean Field Theory & Zener's model

$$F = F_C[M] + F_S[M]$$

Minimization with respect to M

$$M = g\mu_B N_0 x_{eff} S B_S \left[\frac{g\mu_B (-\partial F_C[M] / \partial M + H)}{k_B (T + T_{AF})} \right]$$

when $k_B T \gg g\mu_B H$

Brillouin function Taylor expansion

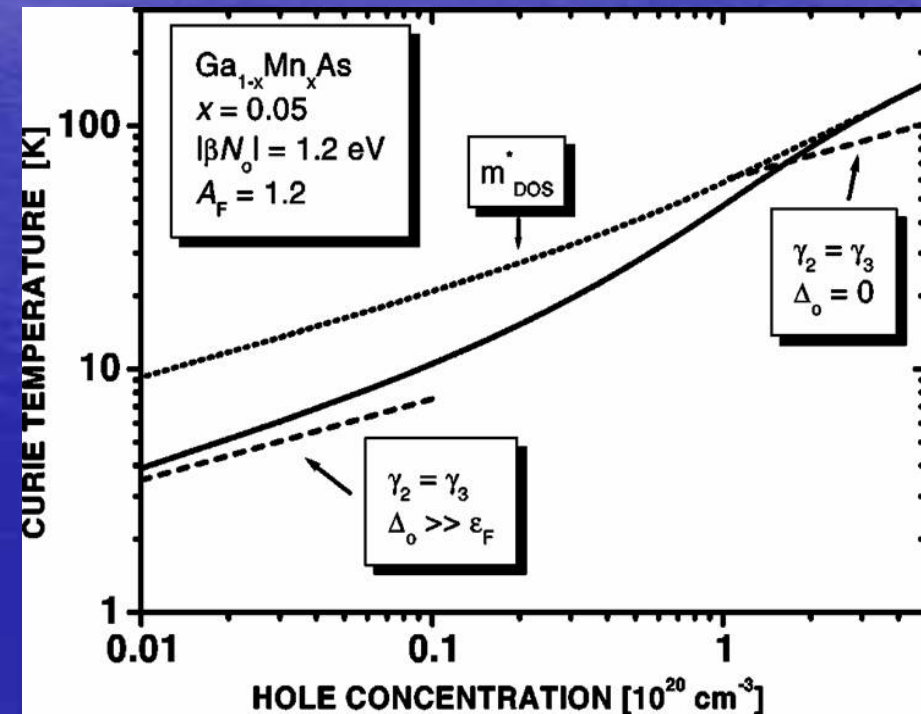
$$T_C = N_0 x_{eff} \frac{S(S+1)}{12k_B} J_{pd}^2 \rho_s(T_C) A_F - T_{AF}$$

Theory of FM in DMSs

- For a strongly degenerate carrier liquid

$$\rho_s = \frac{m_{DOS}^* k_F}{\pi^2 \hbar^2} \text{ and } T_{AF} \sim 0$$

$$T_C \sim m^* x_{eff} n^{1/3}$$



Ohno et al., PRB 63, 195205 (2001)

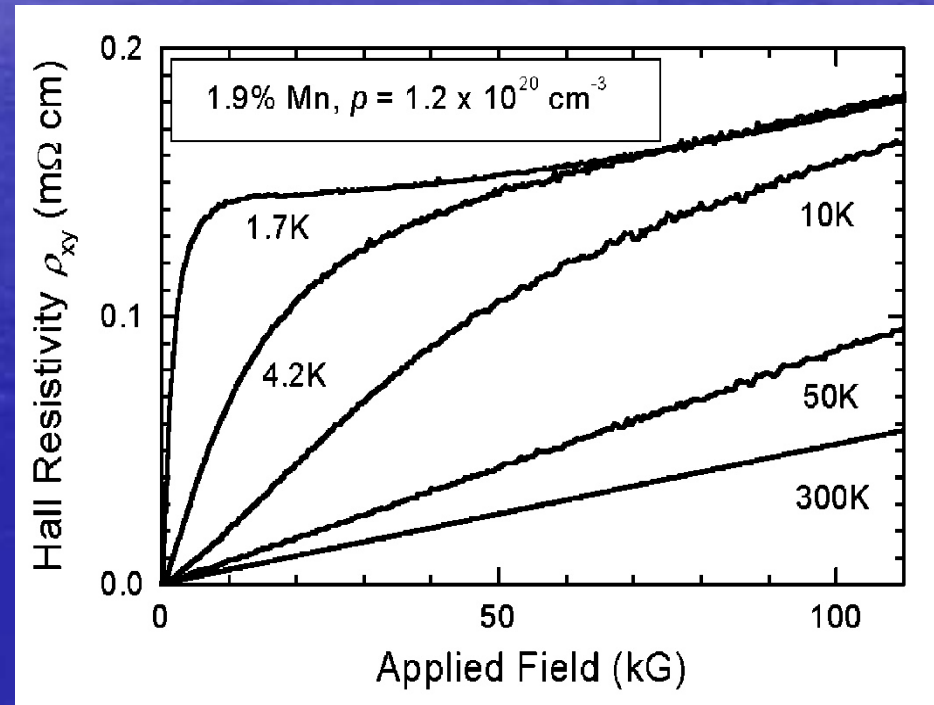
- Anomalous Hall Effect

$$\rho_{Hall} = R_0 B + R_s M$$

$$\text{when } T \geq T_C \quad M = \frac{\chi B}{\mu_0}$$

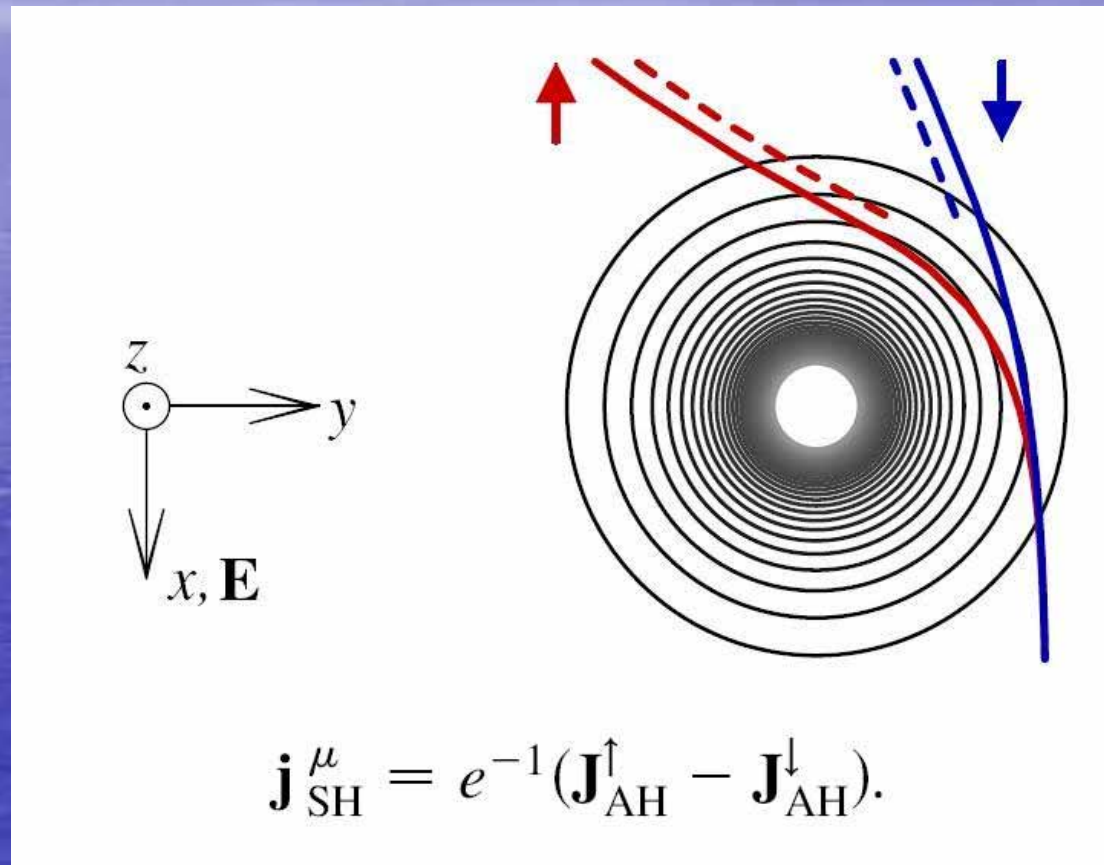
$$\chi = \frac{C}{T - T_C}$$

$$\text{where } C = \frac{4g^2 S_{Mn} (S_{Mn} + 1) \mu_B^2 x}{3a_0^3 k_B}$$



Ferrand et al., PRB 63, 085201 (2001)

Spin-Orbit Scattering— Skew S. and Side-jump S.



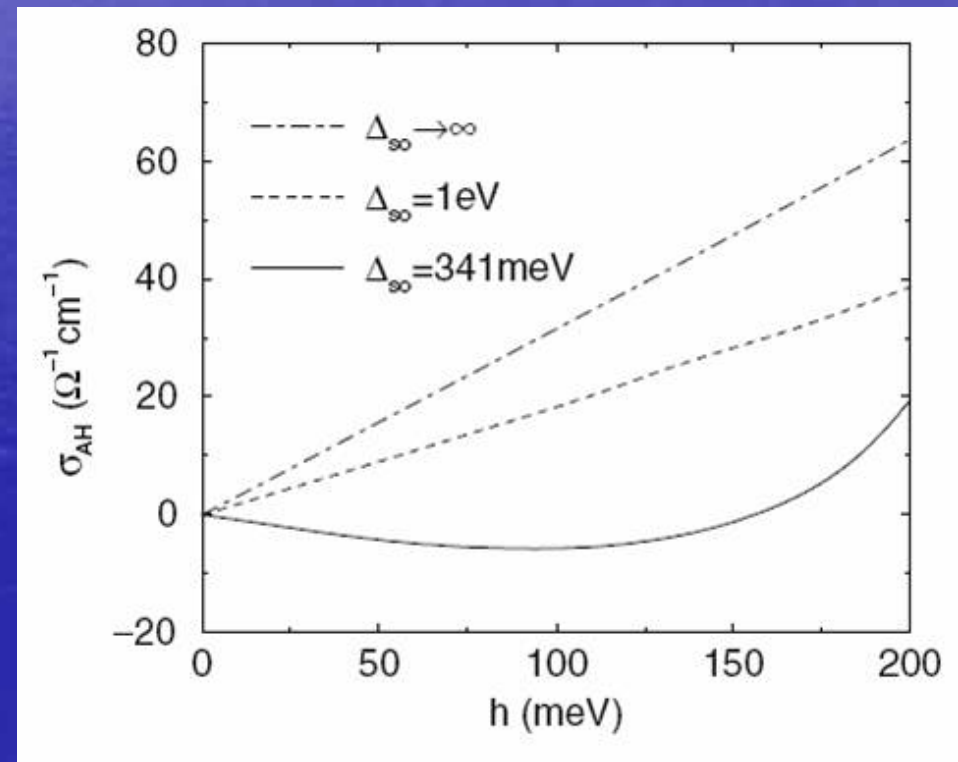
- Intrinsic AHE (Karplus & Luttinger)

$$R_s \propto \rho_{xx}^2$$

- Skew Scattering (Smit)

$$R_s \propto \rho_{xx}$$

- Intrinsic AHE + Berry phase (Jungwirth et al.)



Jungwirth et al., PRL 88, 207208 (2002)

New Structure

- Fabrication of two-dimensional devices with low carrier concentration and high mobility with the ultimate objective of making the first ferromagnetic quantum dot
- Development of a scheme for the fabrication of Ohmic contact, by thermal annealing, to buried 2D hole/electron gas

New Structure

- 2DHG Triangular QW

$$p = 2.3 \times 10^{13} \text{ cm}^{-2}$$

$$\mu = 1937 \text{ cm}^2 / \text{Vs}$$

➤ Good control of the growth process

➤ Clean chamber

GaAs (001) Substrate

SI-GaAs 275 nm

SI-AlGaAs 57 nm

GaAlAs:Be 3.3 nm

SI-AlGaAs 11 nm

SI-GaAs 23 nm

New Structure

- Square QW

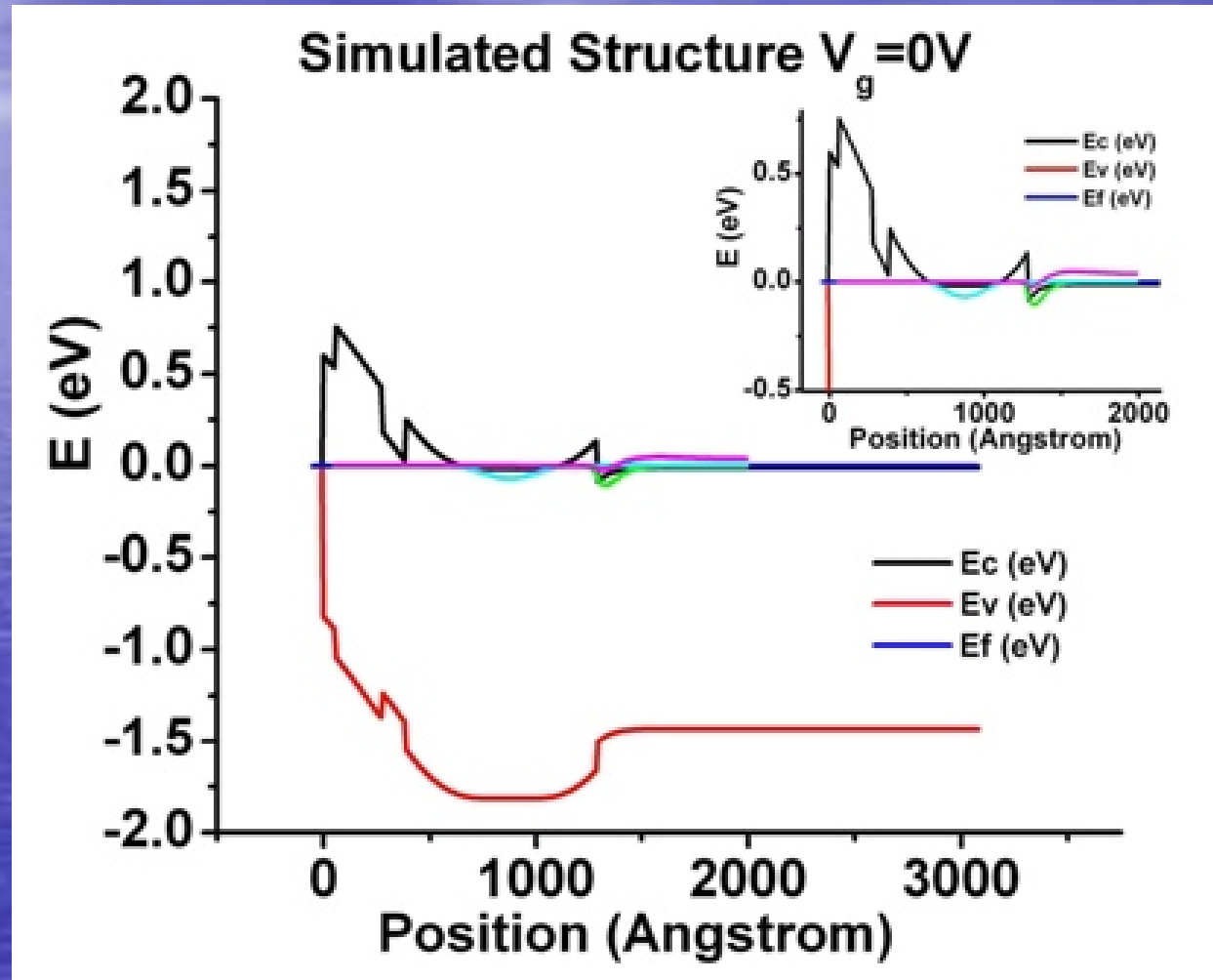
- Easier to grow

- Less impurity for scattering

- Reduced presence of Mn_i

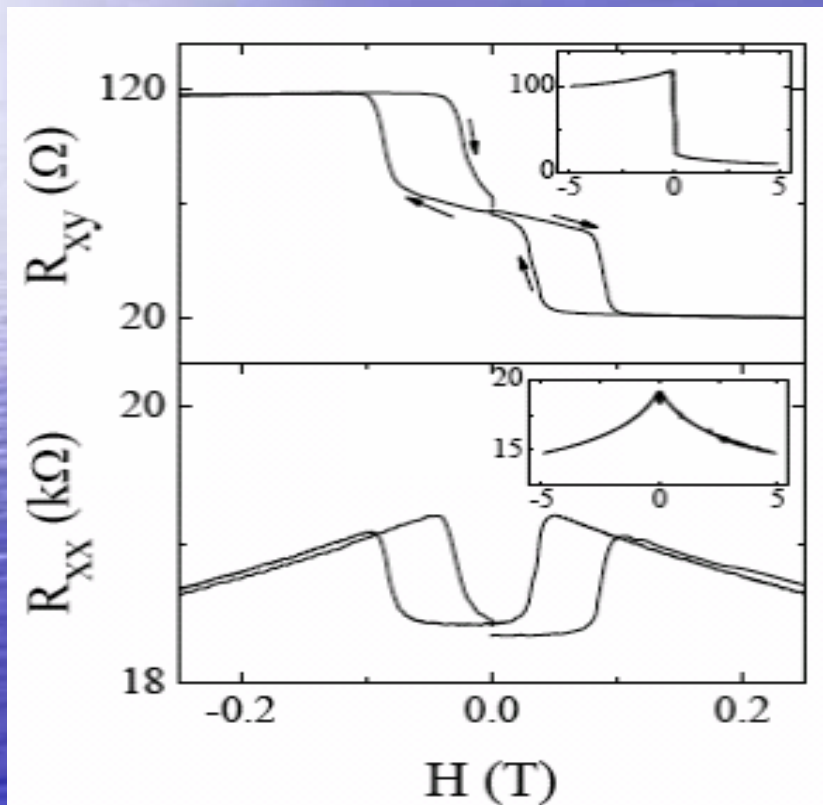
GaAs (001)	Substrate
GaAs:Si	100 nm
AlGaAs:Be	200 nm
SI-GaAs	10 nm
LT-Mn	2/3 ML
LT-AlGaAs:Be	10 nm
LT-AlGaAs	15 nm
LT-GaAs	5 nm

Simulated Band Structure

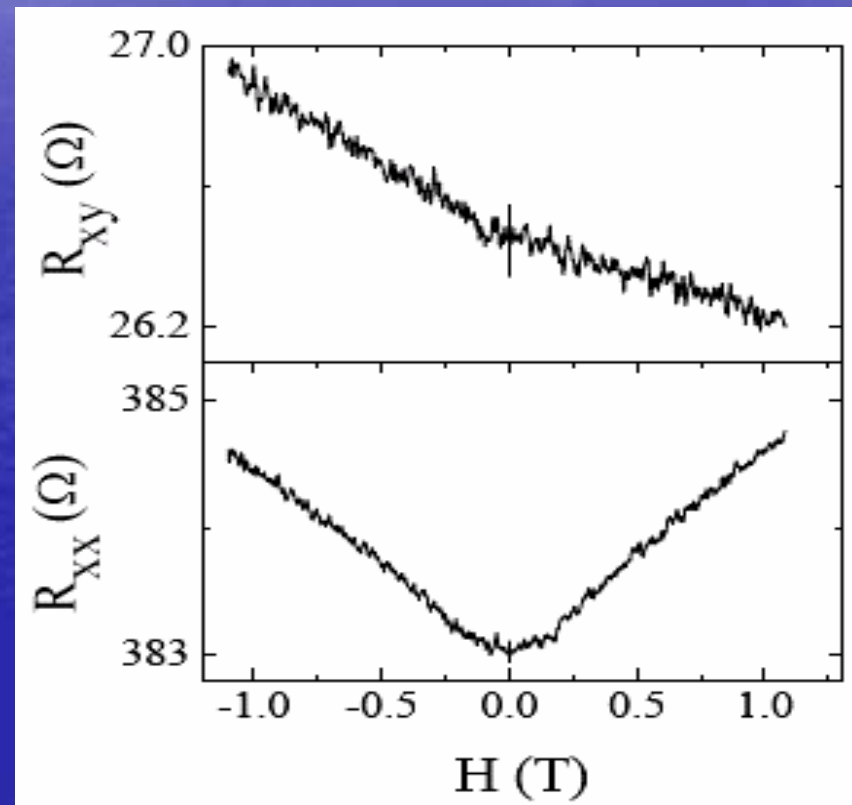


Ohmic contact to $\text{Ga}_{1-x}\text{Mn}_x\text{As}$

- Ferromagnetism in perpendicular field



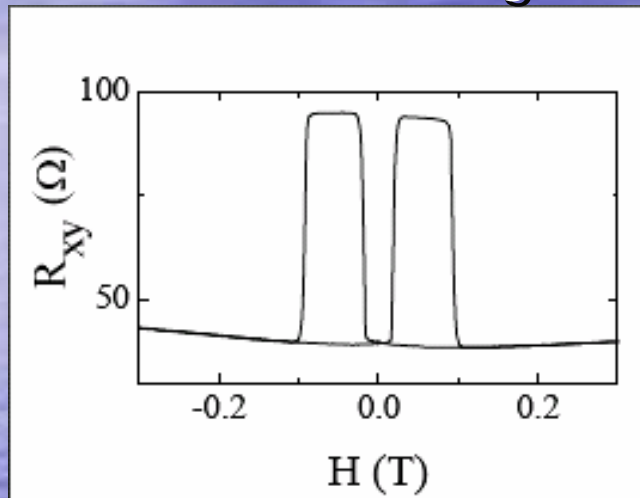
No Annealing



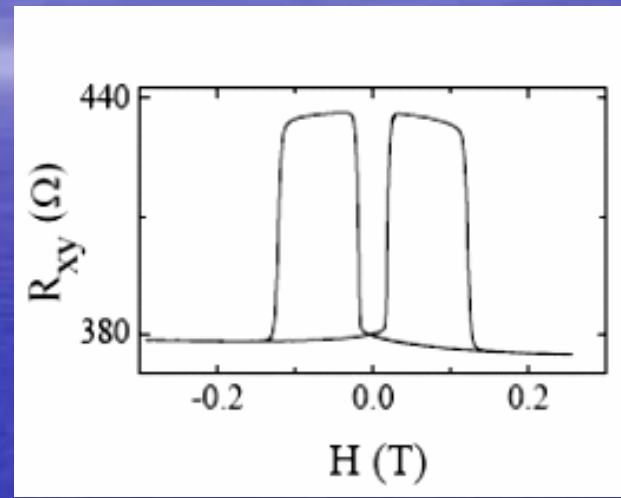
470 °C for 30 s

Ohmic contact to $\text{Ga}_{1-x}\text{Mn}_x\text{As}$

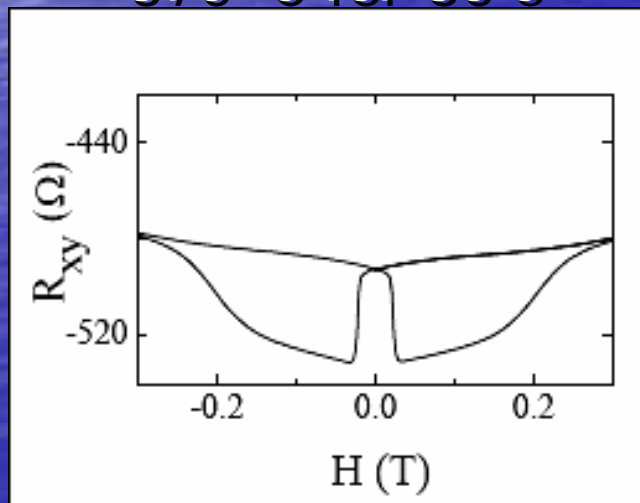
No Annealing



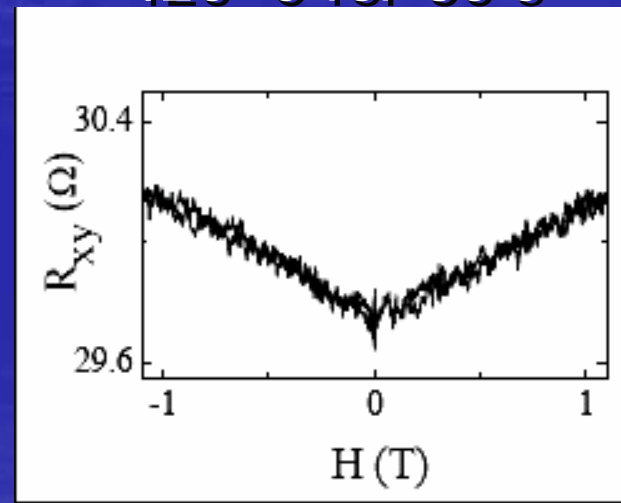
320 °C for 30 s



370 °C for 30 s

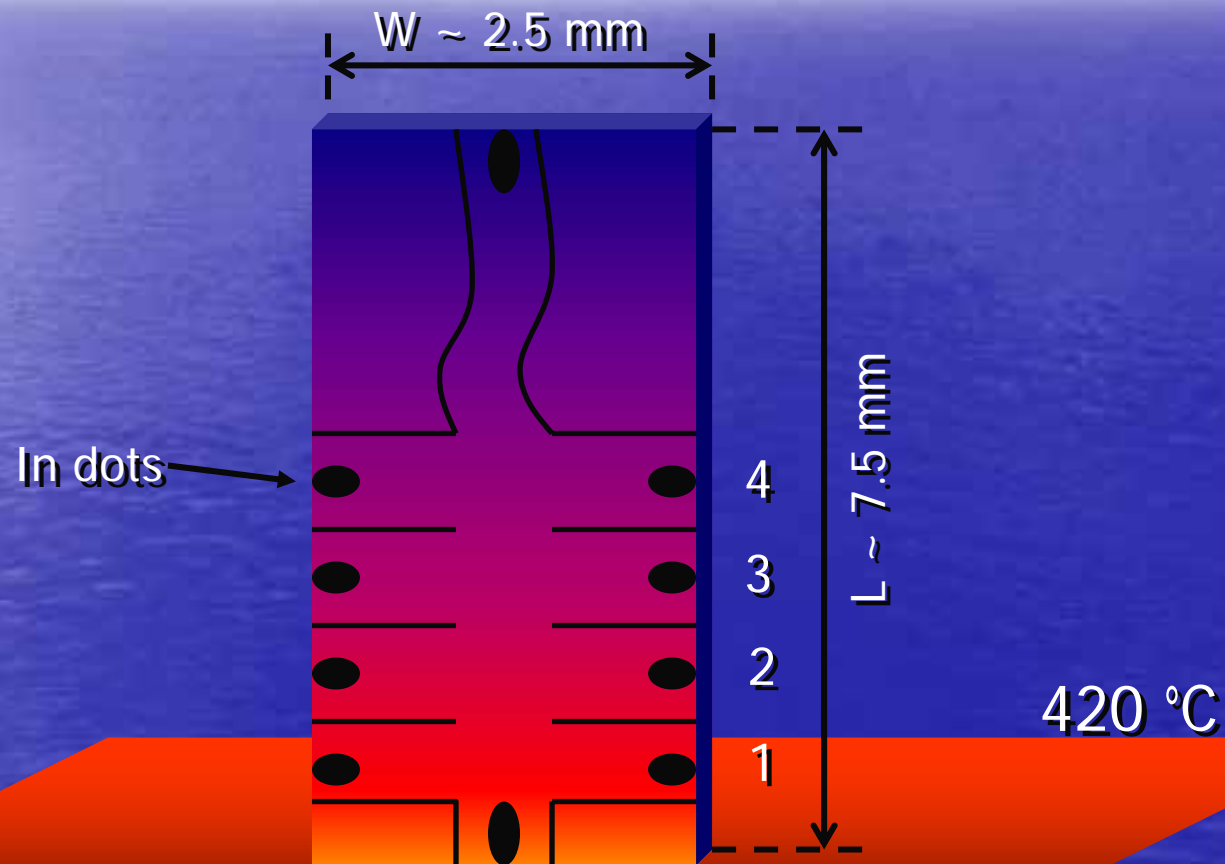


420 °C for 30 s

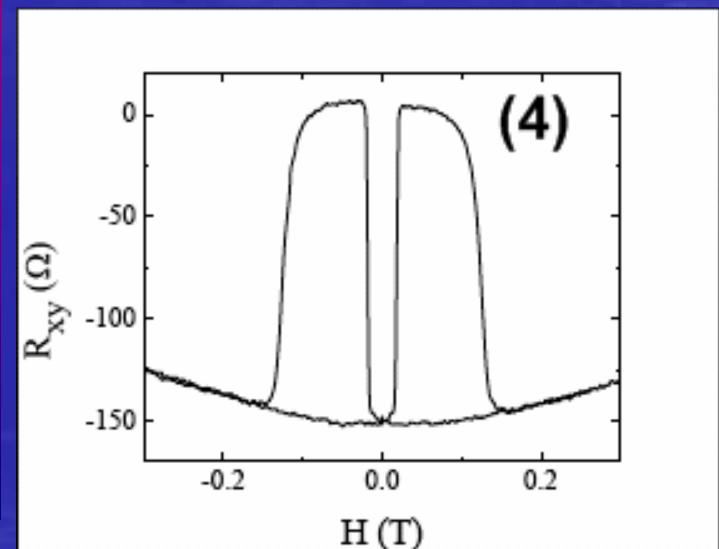
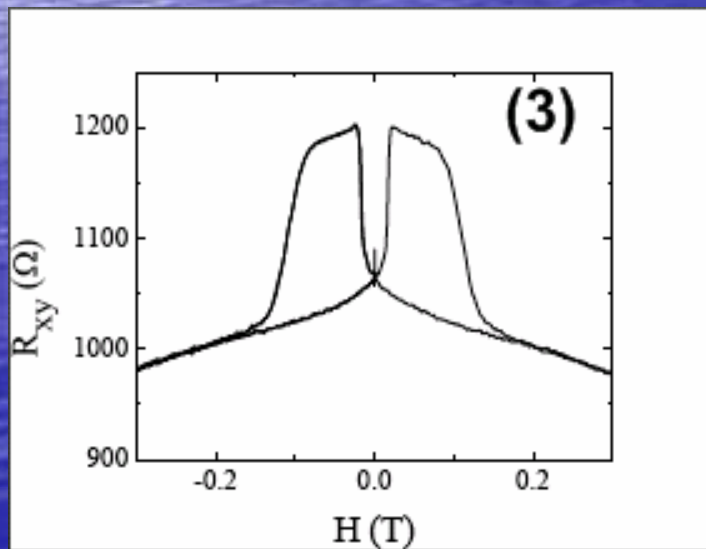
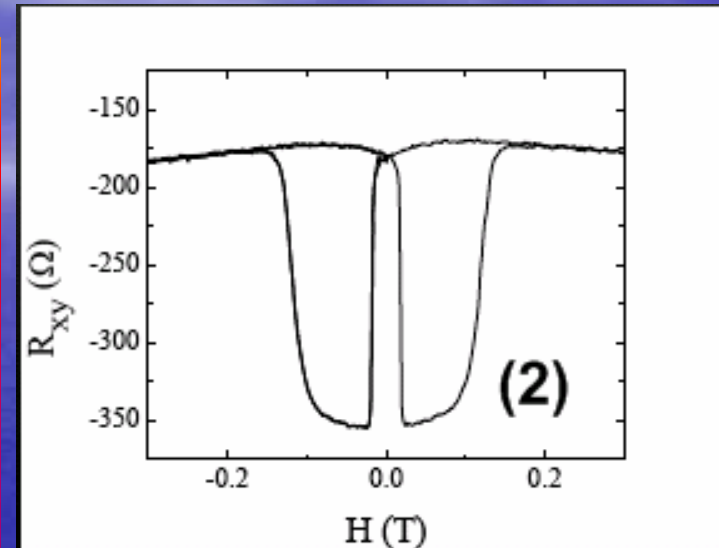
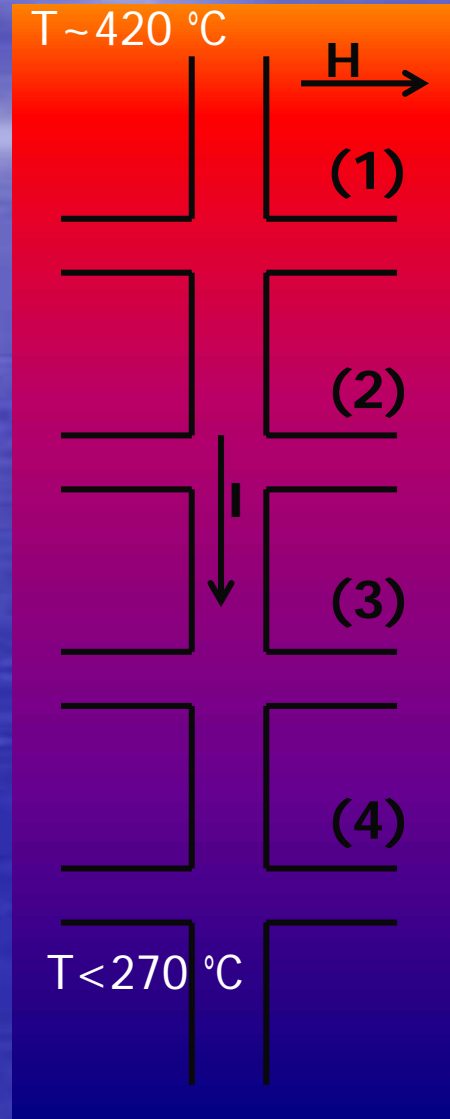
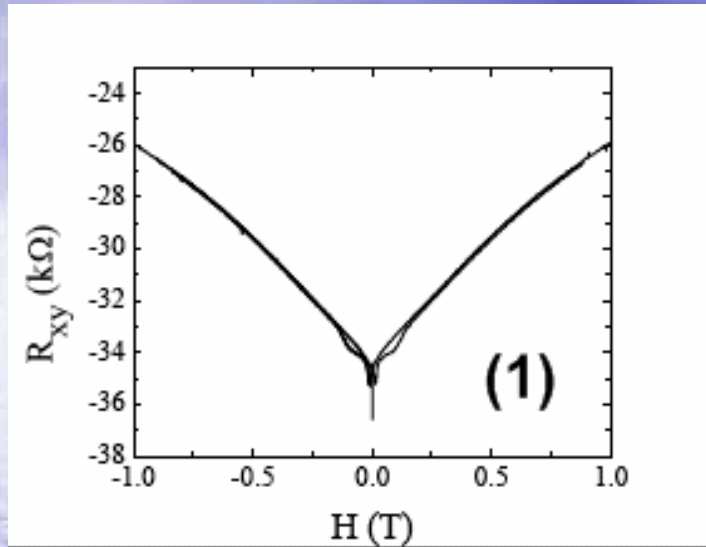


Ohmic contact to $\text{Ga}_{1-x}\text{Mn}_x\text{As}$

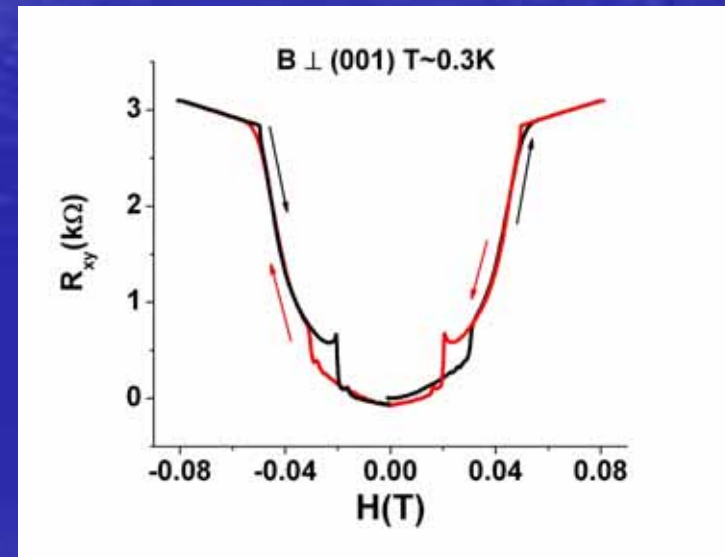
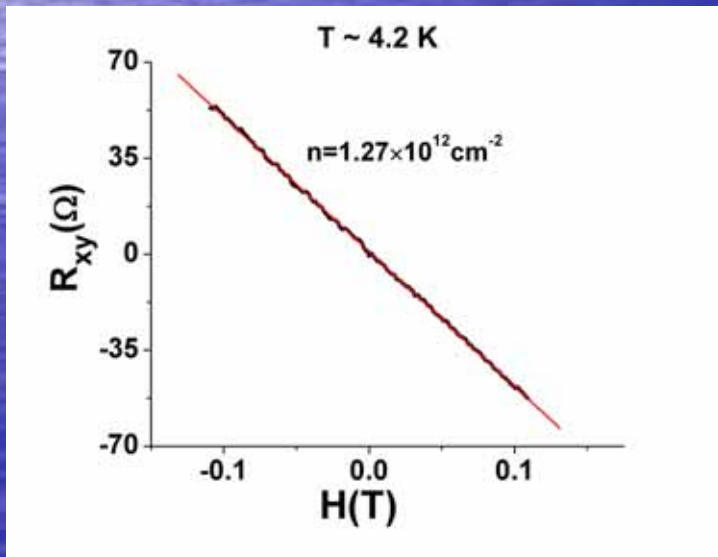
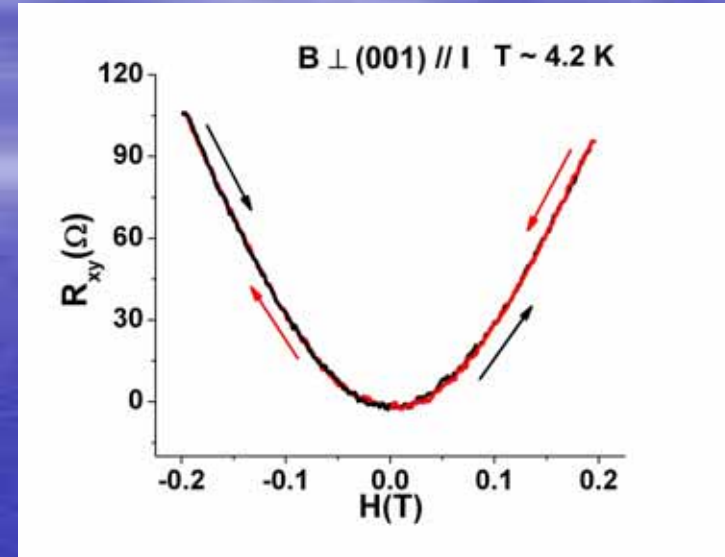
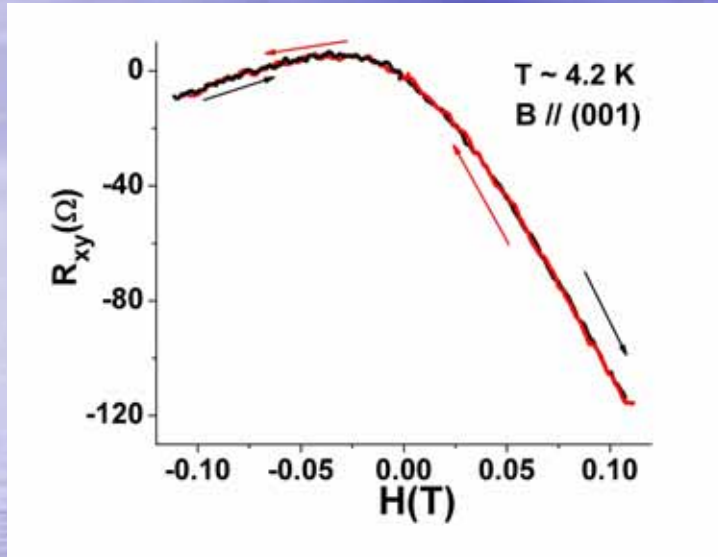
- Thermal Gradient



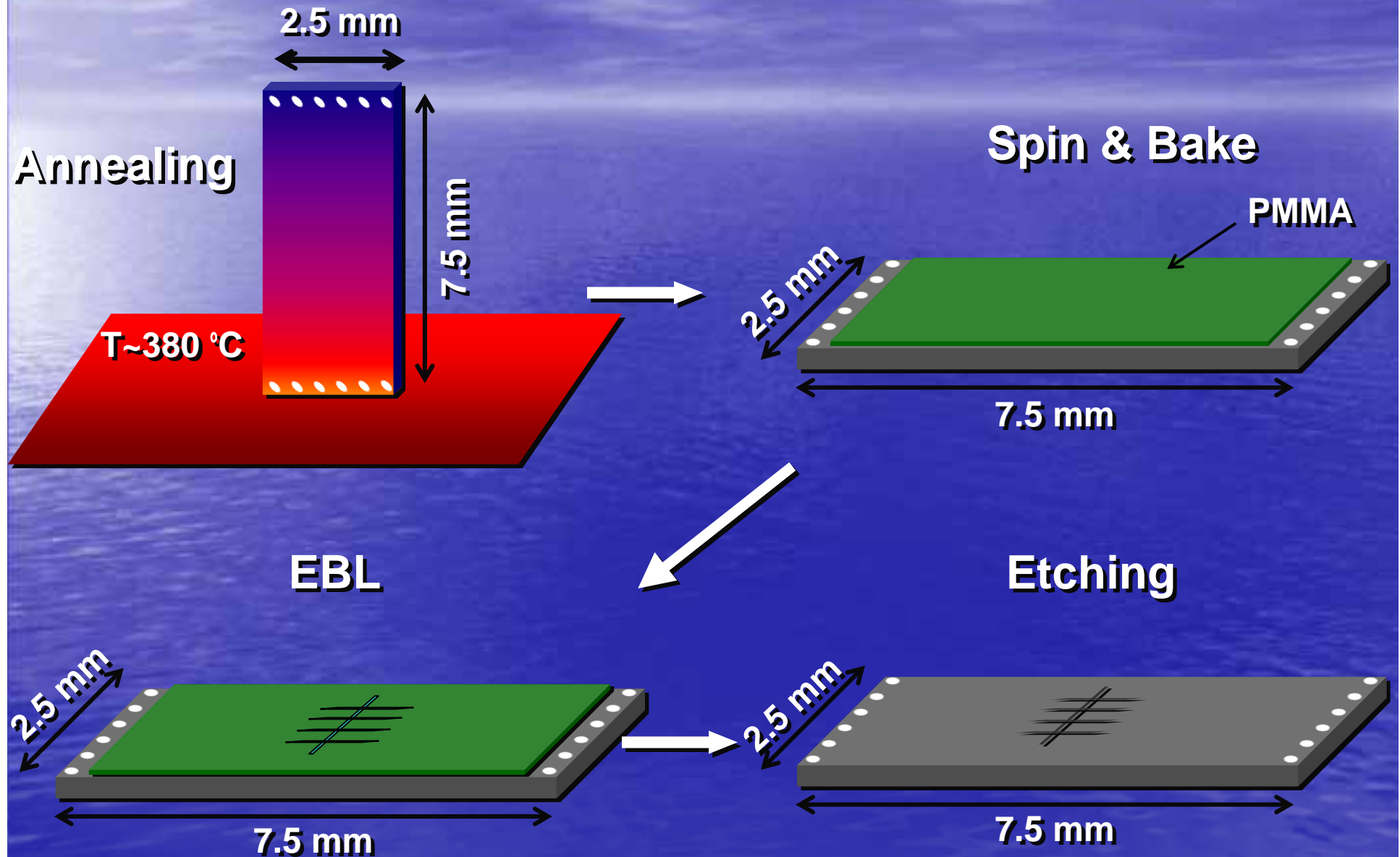
Ohmic contact to $\text{Ga}_{1-x}\text{Mn}_x\text{As}$



Ohmic contact to $\text{Ga}_{1-x}\text{Mn}_x\text{As}$

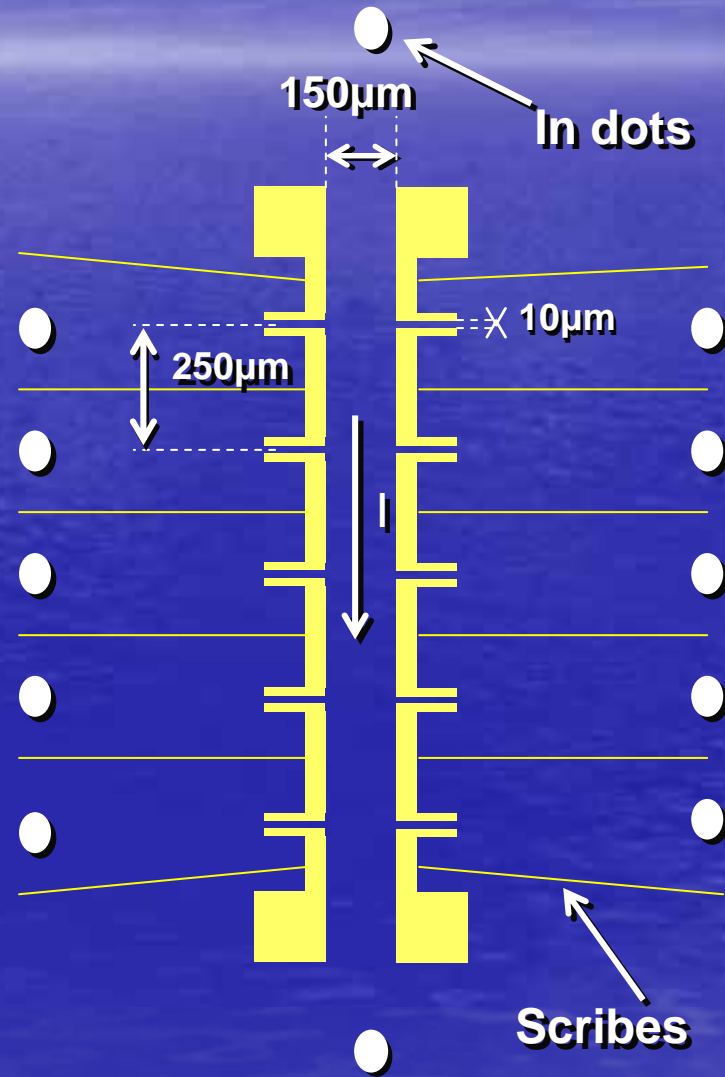
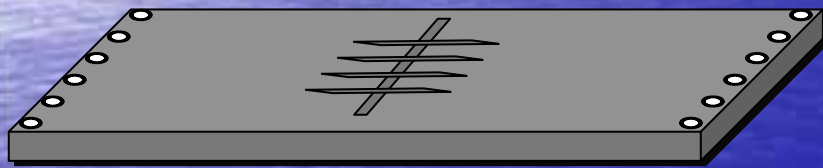


SAMPLE PREPARETION



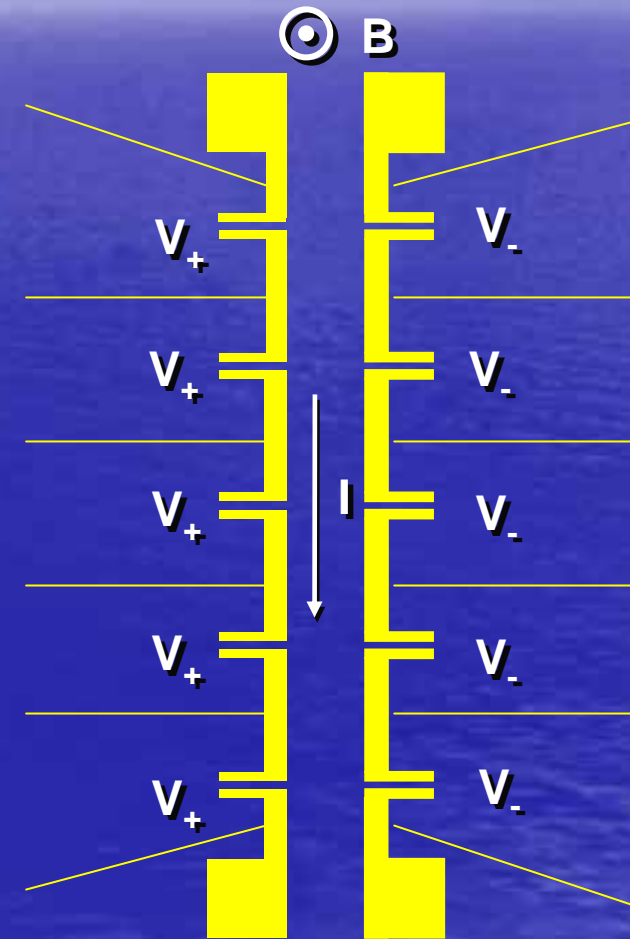
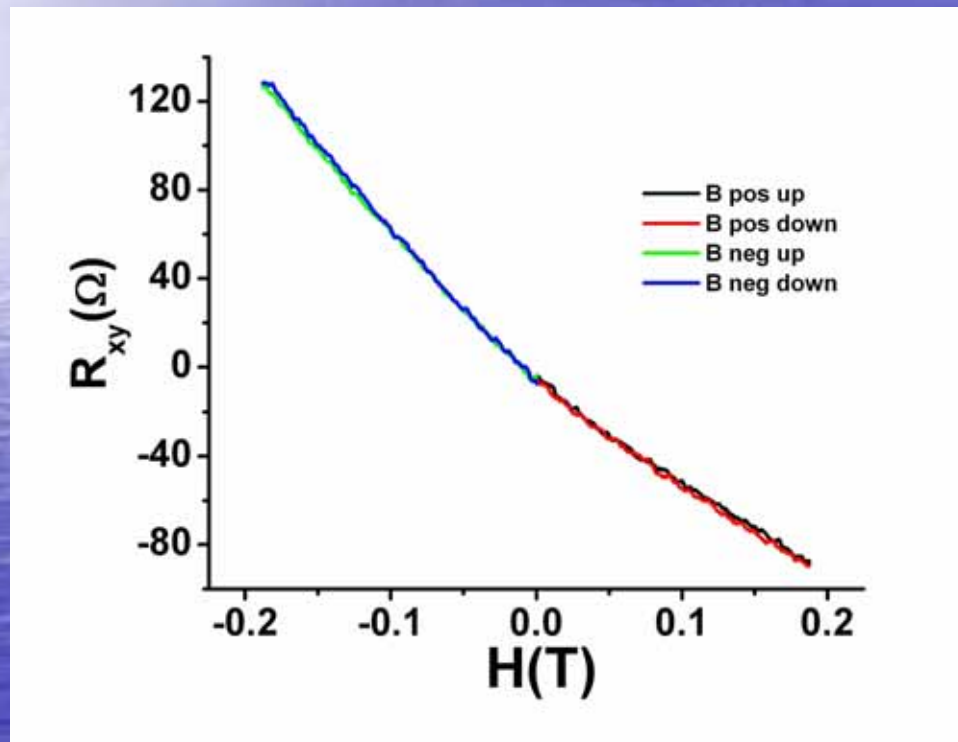
SAMPLE PREPARATION

- Hall Bar Pattern



MAGNETO-TRANSPORT MEASUREMENTS

- 4.2 K Measurements



MAGNETO-TRANSPORT MEASUREMENTS

- Lag Removal

$$I_{Magnet} - I_{Ramper} = -I' \left(1 - e^{-t/\tau} \right) \tau$$

$$I_{Magnet} - I_{Ramper} = I' e^{-t/\tau} \tau$$

- Anti-symmetrization

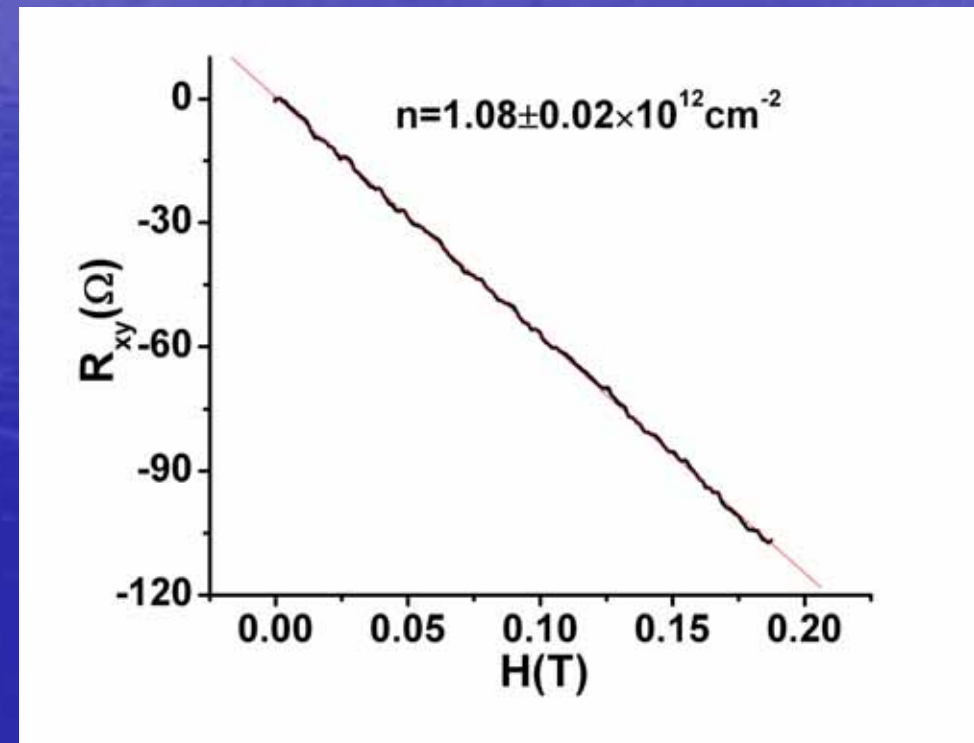
$$R_{xy}(B) = \left(R_{xy}(B+) - R_{xy}(B-) \right) / 2$$

- Density & Mobility

$$n = 1.08 \times 10^{12} \text{ cm}^{-2}$$

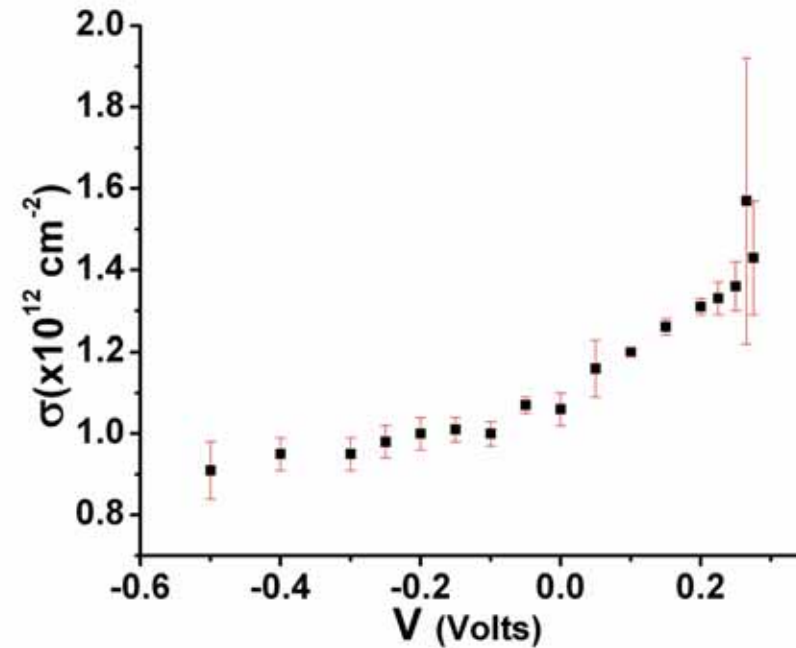
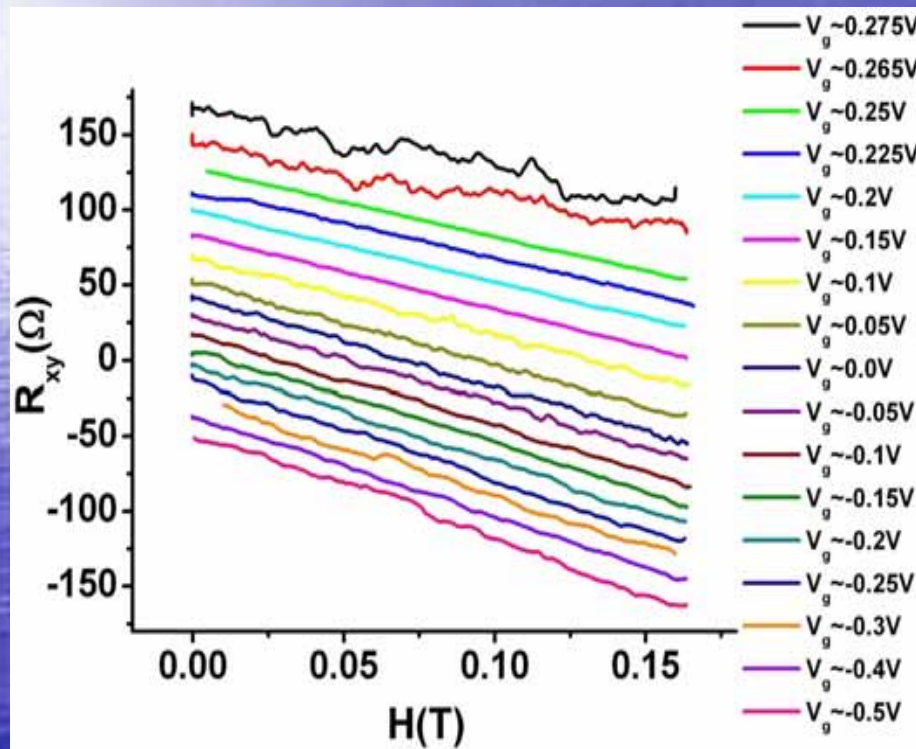
$$\mu = 575 \text{ cm}^2 / \text{Vs}$$

n-Type Electrons!



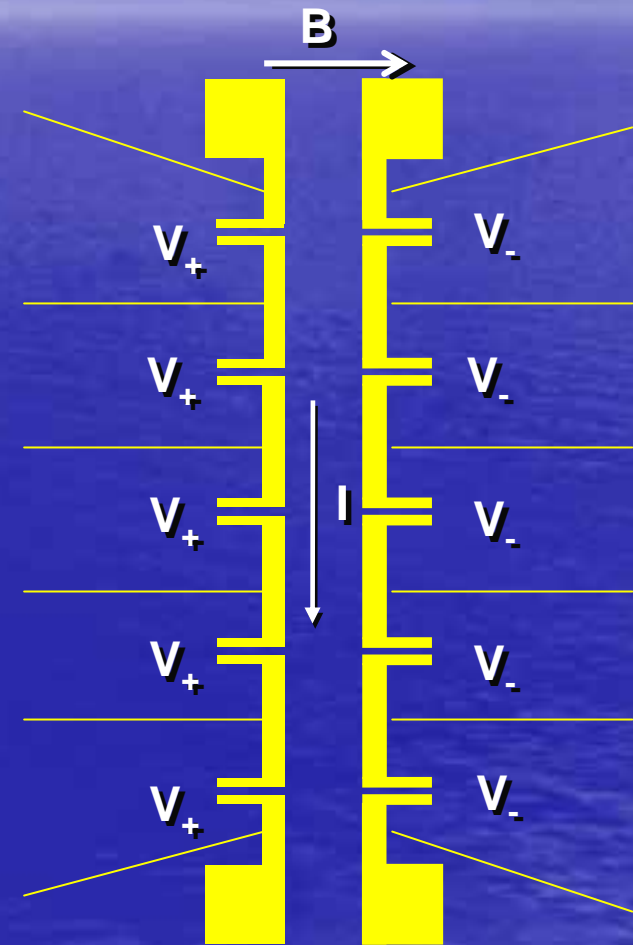
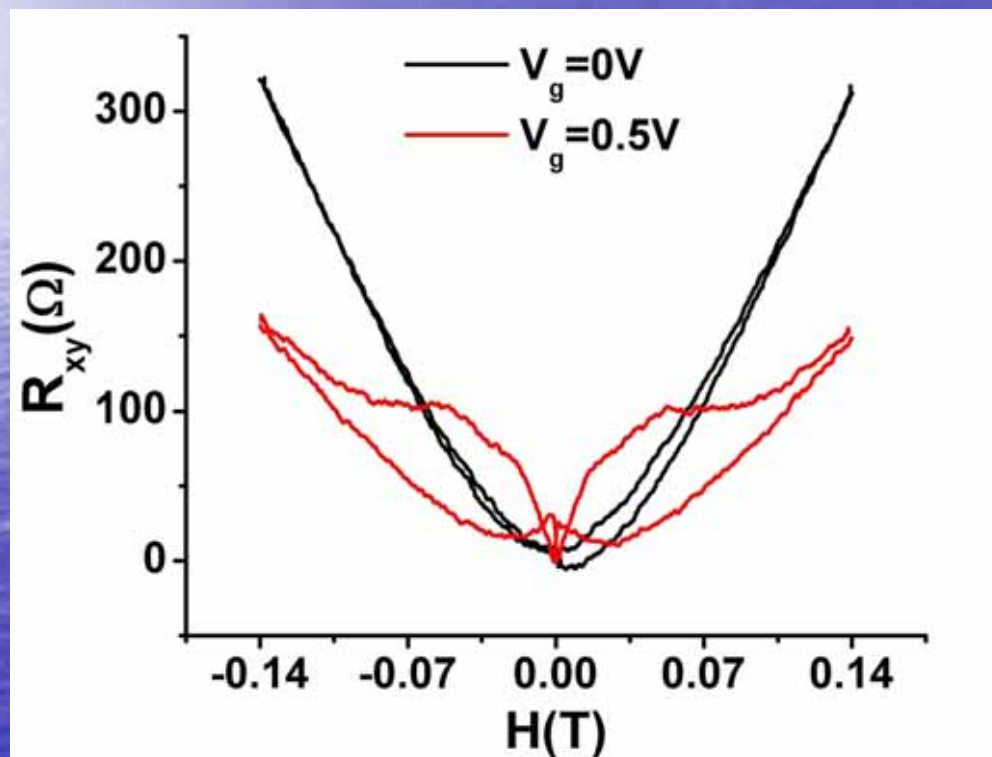
MAGNETO-TRANSPORT MEASUREMENTS

- Gating



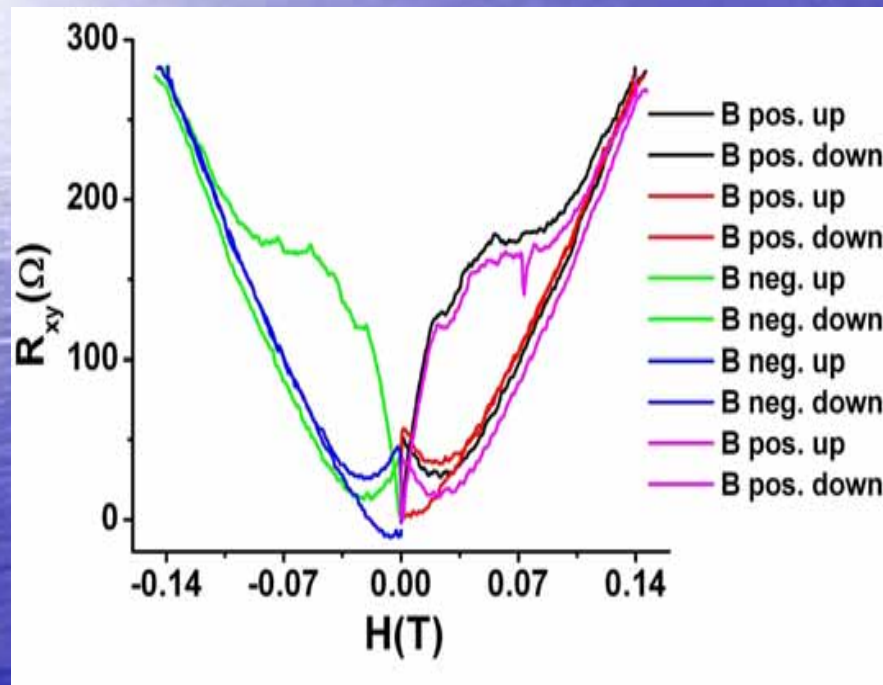
MAGNETO-TRANSPORT MEASUREMENTS

- 0.3 K Measurements

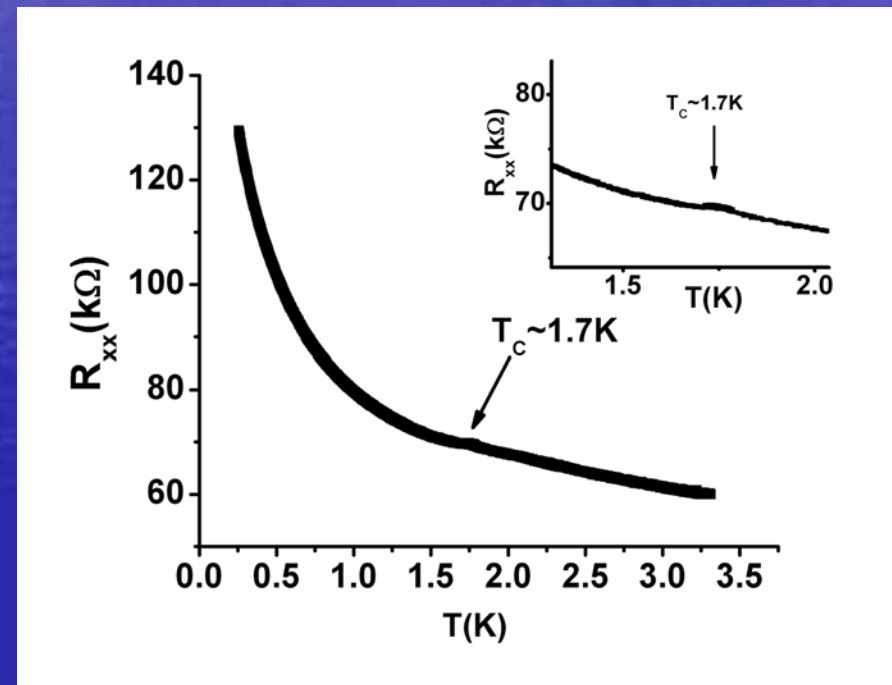


MAGNETO-TRANSPORT MEASUREMENTS

- Hysteresis

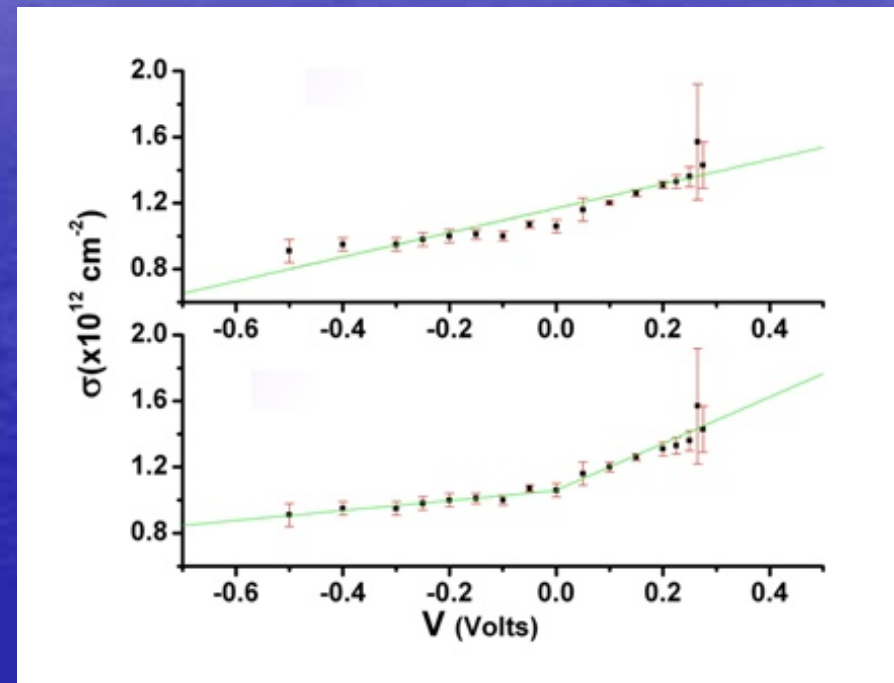
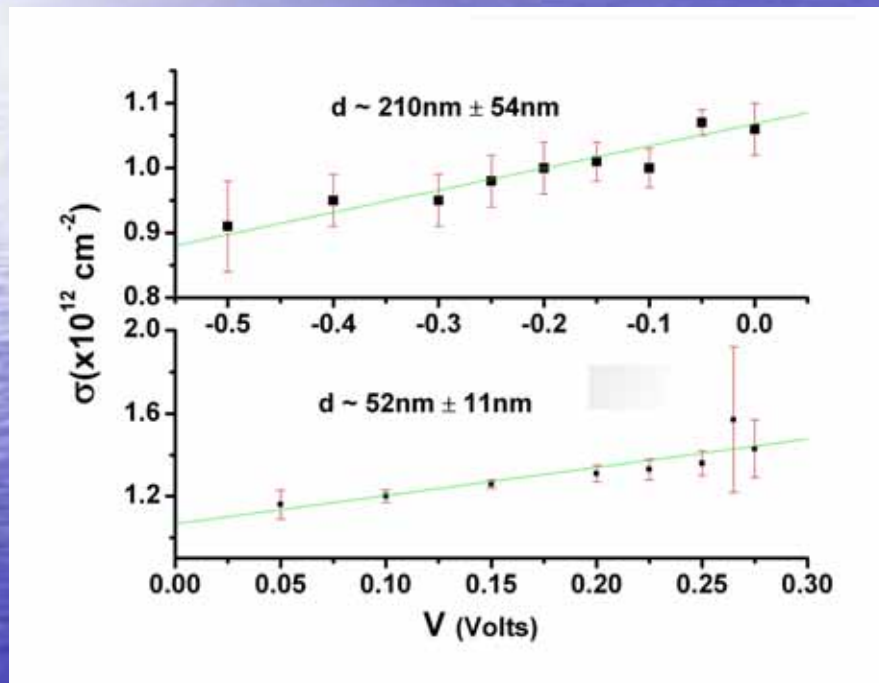


- Curie Temperature



MAGNETO-TRANSPORT MEASUREMENTS

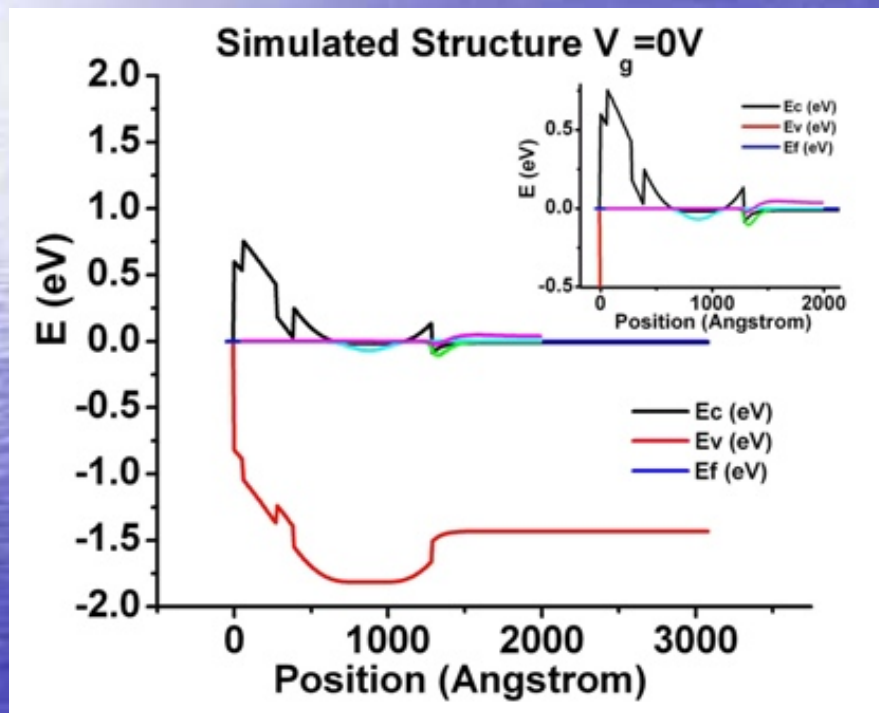
- Two slopes vs. one slope model



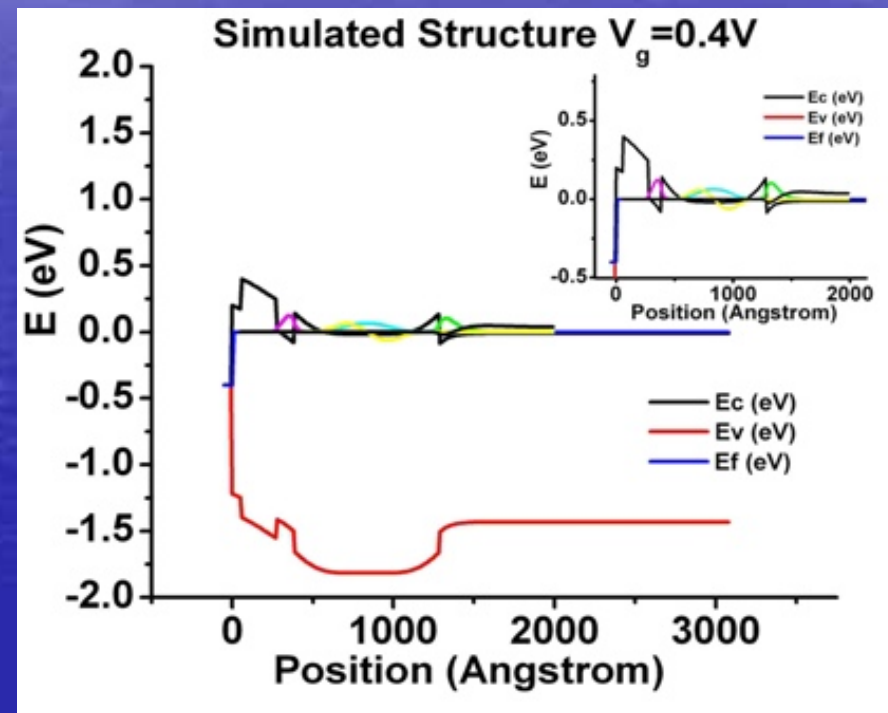
F-test confidence level greater than 99.9%

MAGNETO-TRANSPORT MEASUREMENTS

- Simulations



$$V_g = 0V$$

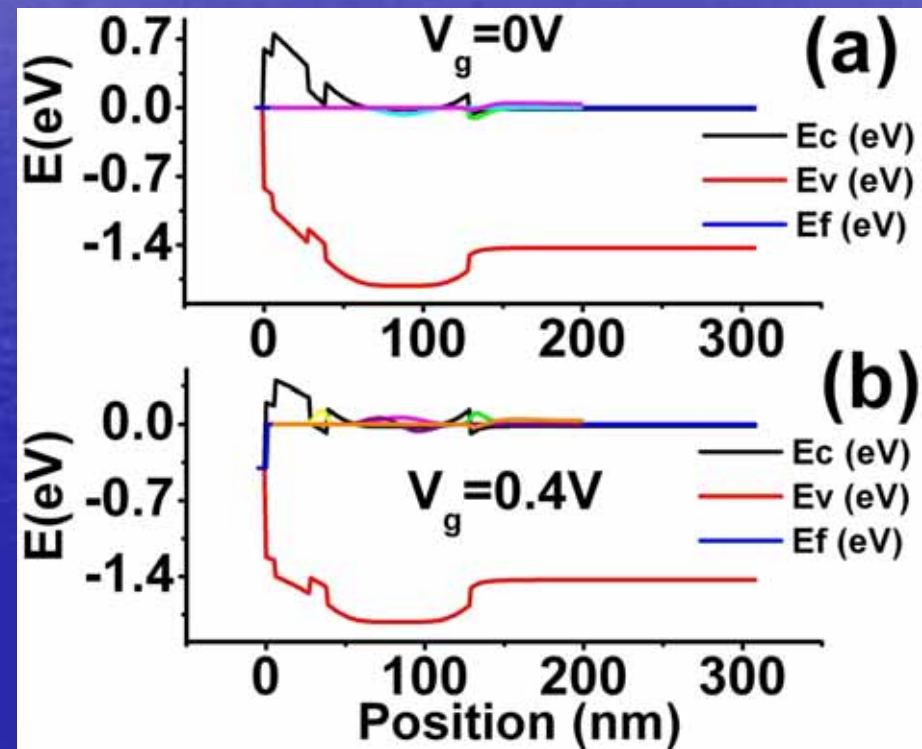
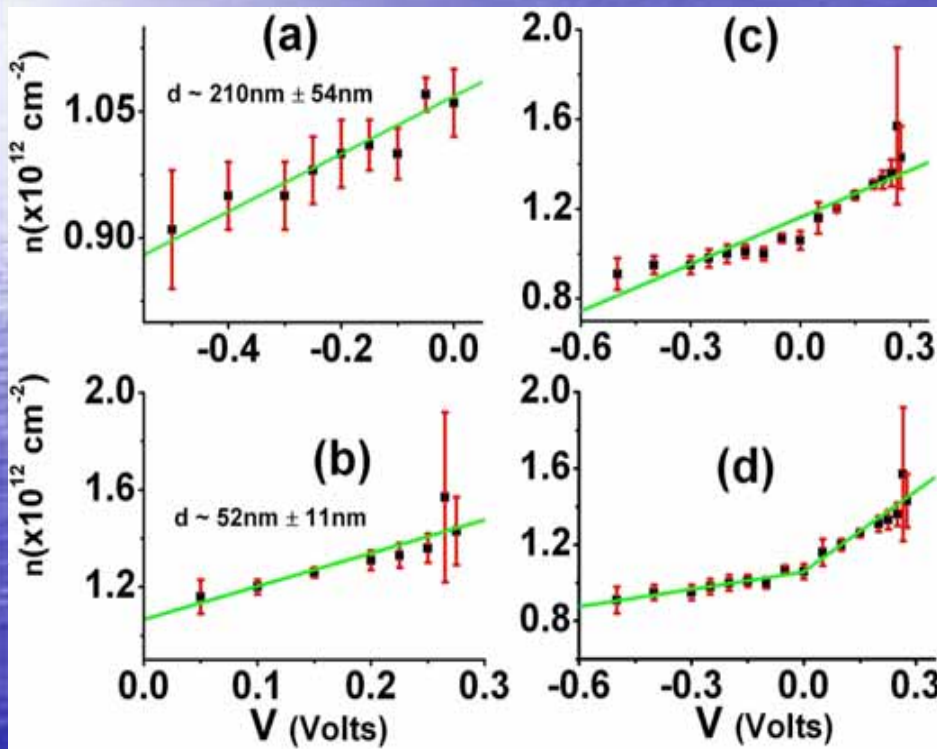


$$V_g = 0.4V$$

MAGNETO-TRANSPORT MEASUREMENTS

Two slopes vs. one slope model

Simulations



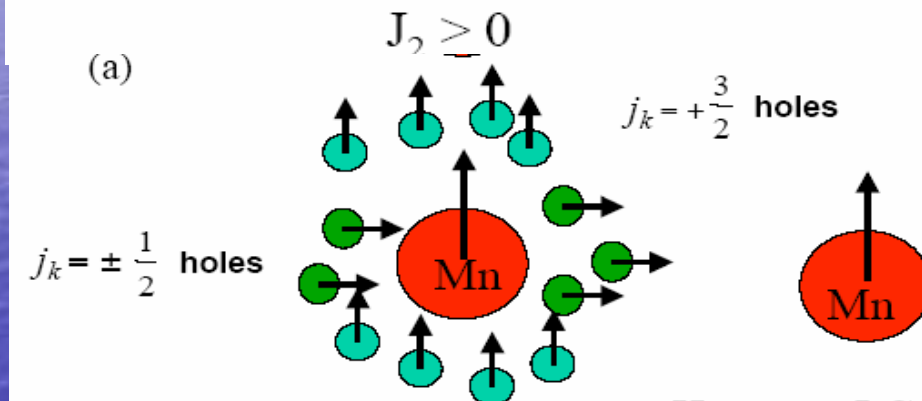
F-test confidence level greater than 99.9%

Heisenberg Exchange Anisotropy

Spin-Orbit—Second Order Perturbation

P-type

$$H_{12} = -J_1 \mathbf{S}_1 \cdot \mathbf{S}_2 + J_2 \mathbf{S}_1 \cdot \mathbf{r}_{12} \mathbf{S}_2 \cdot \mathbf{r}_{12}$$



From: Randy Fishman

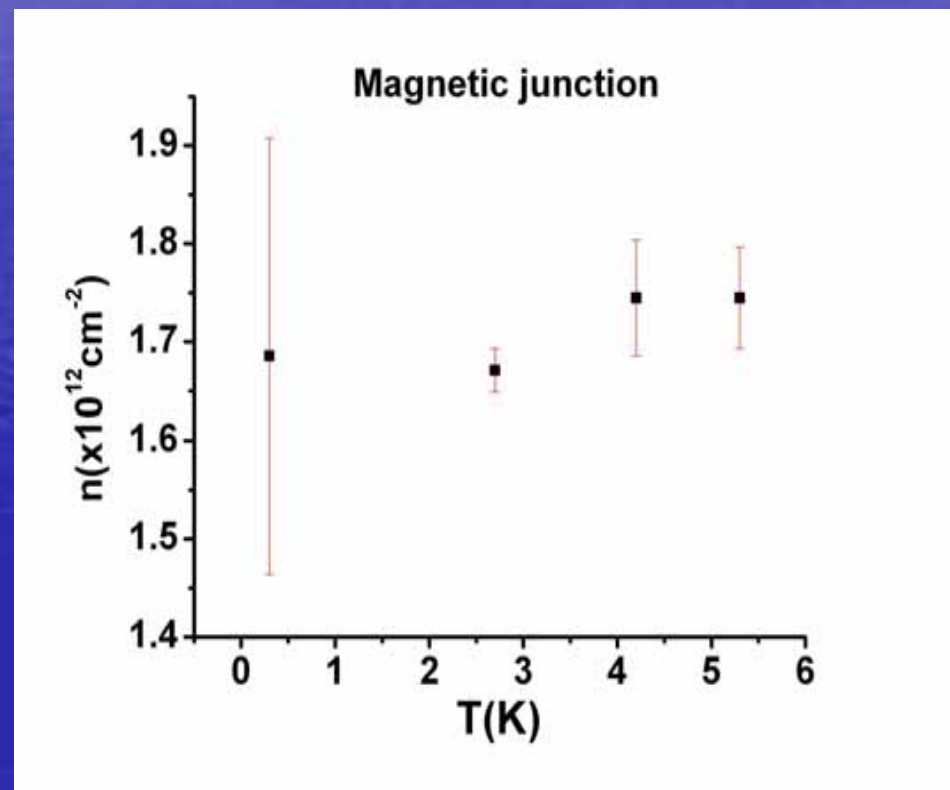
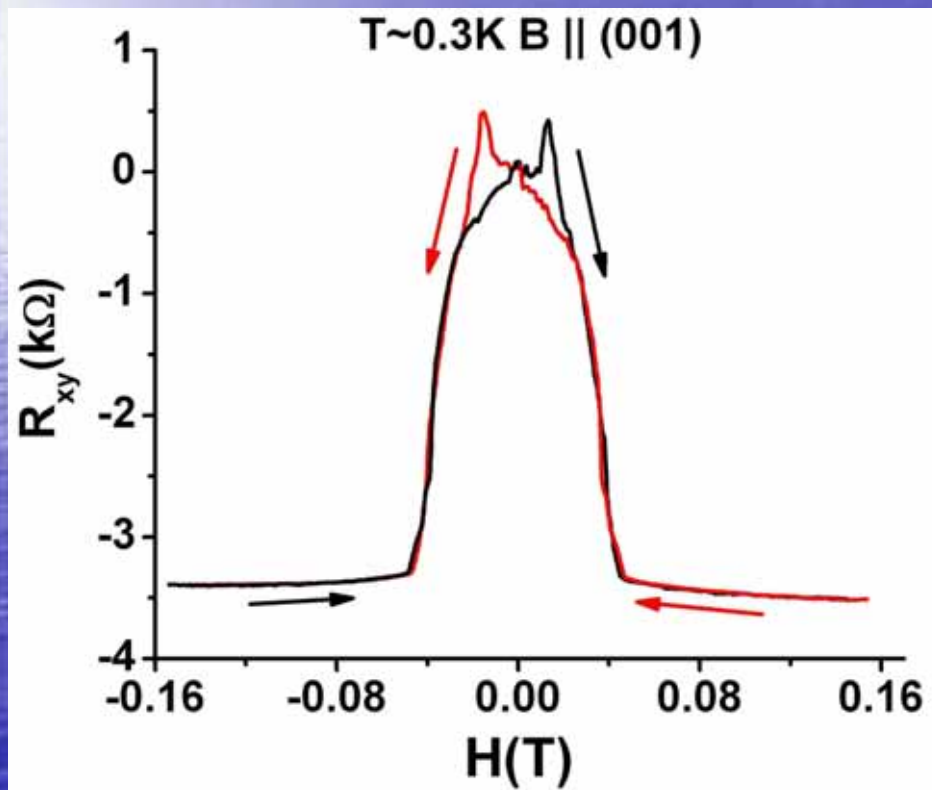
Dipole-Dipole Interaction ($\sim 100\mu\text{eV}$)

N-type

$$\mathbf{H} = -\frac{\mu_0}{4\pi r_{jk}^3} (3(\mathbf{m}_j \cdot \mathbf{e}_{jk})(\mathbf{m}_k \cdot \mathbf{e}_{jk}) - \mathbf{m}_j \cdot \mathbf{m}_k)$$

MAGNETO-TRANSPORT MEASUREMENTS

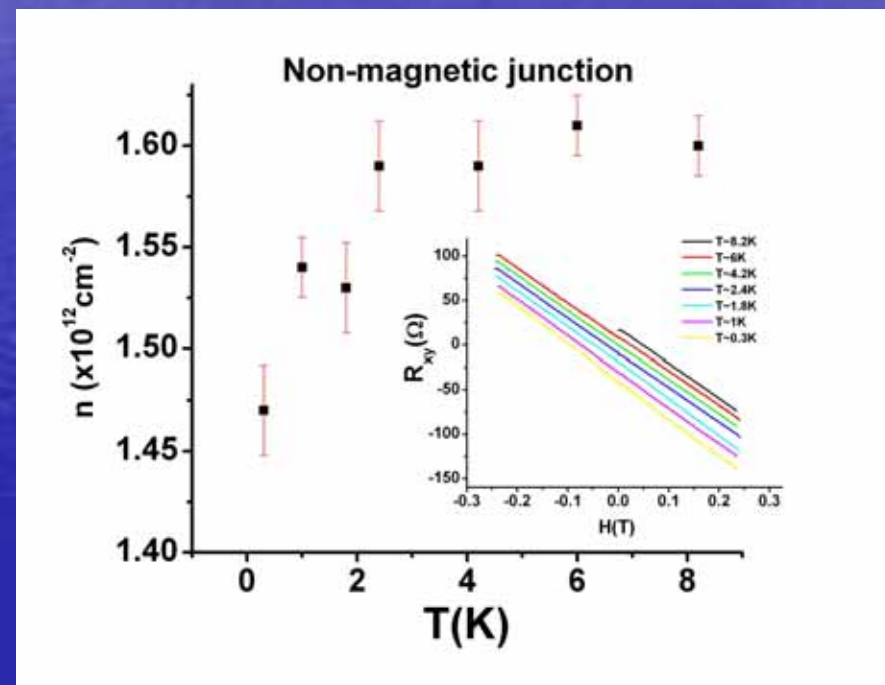
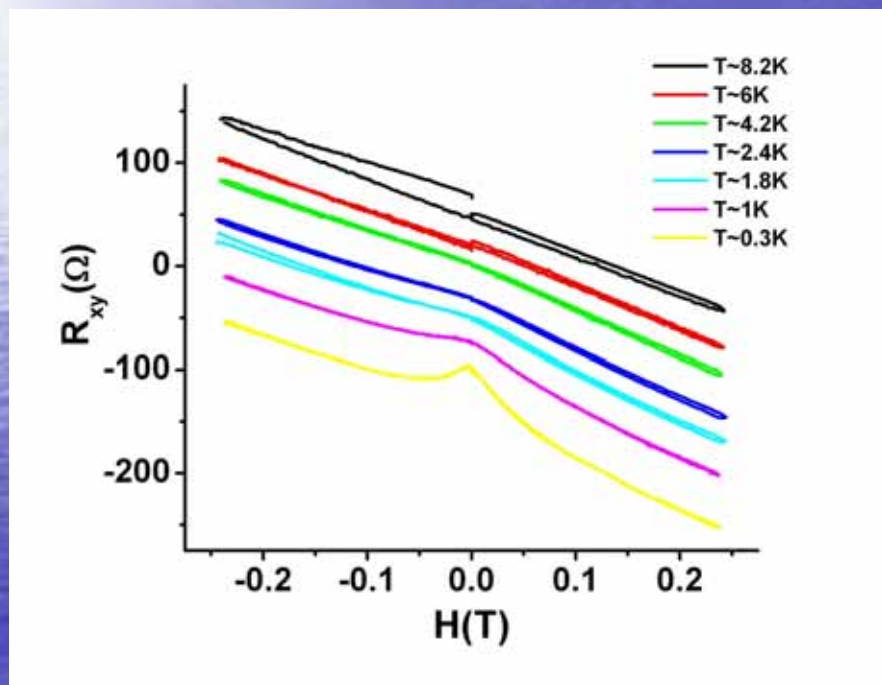
- Anomalous Hall Effect



Magnetic junction

MAGNETO-TRANSPORT MEASUREMENTS

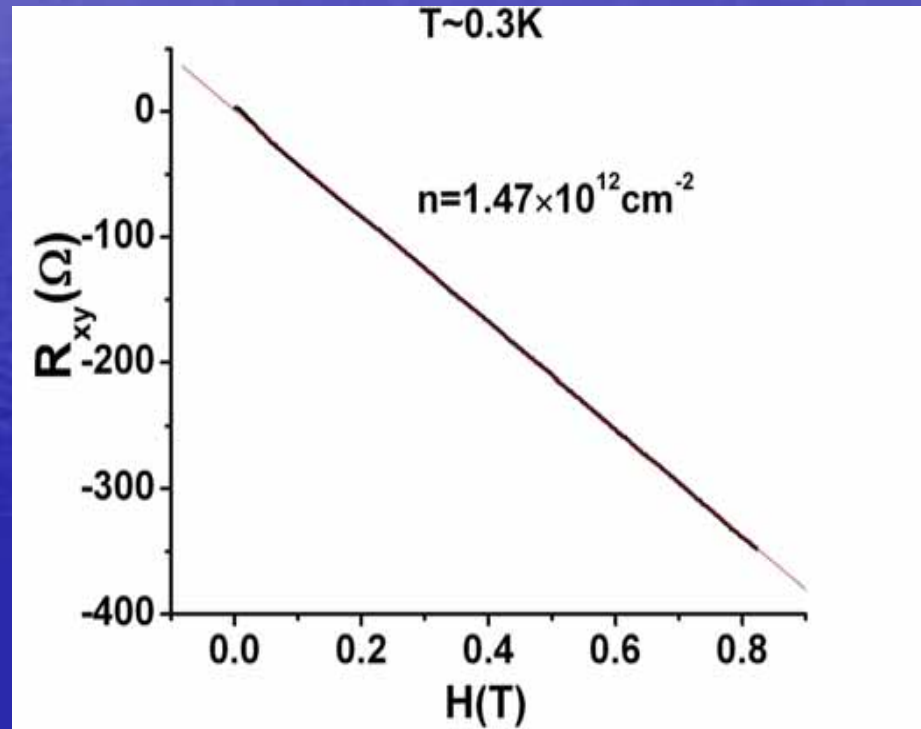
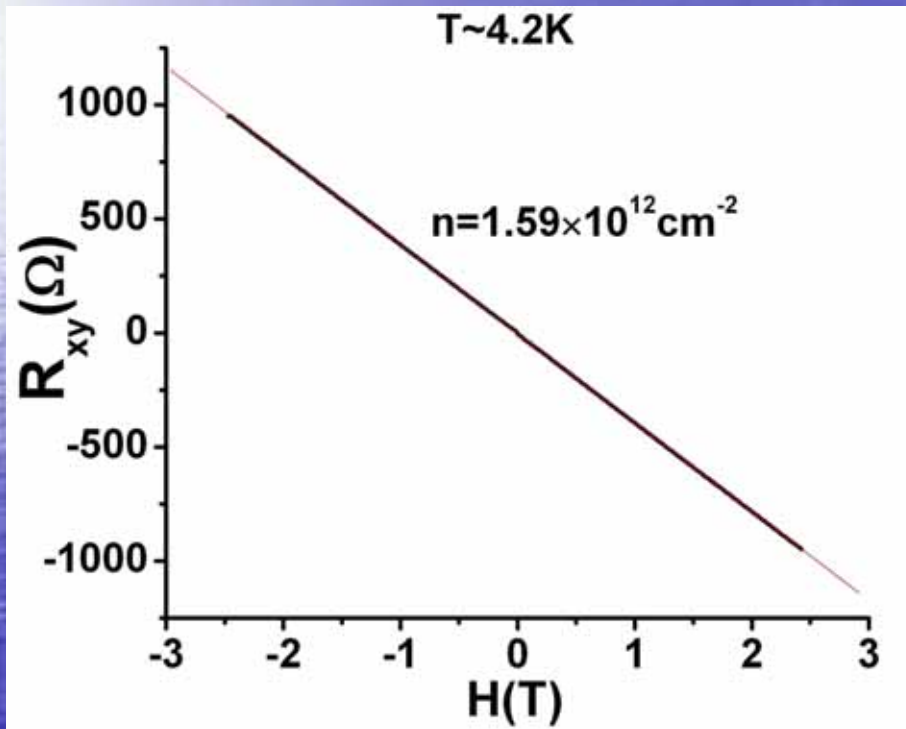
- Anomalous Hall Effect



Non-magnetic junction

MAGNETO-TRANSPORT MEASUREMENTS

- Anomalous Hall Effect



Non-magnetic junction

MAGNETO-TRANSPORT MEASUREMENTS

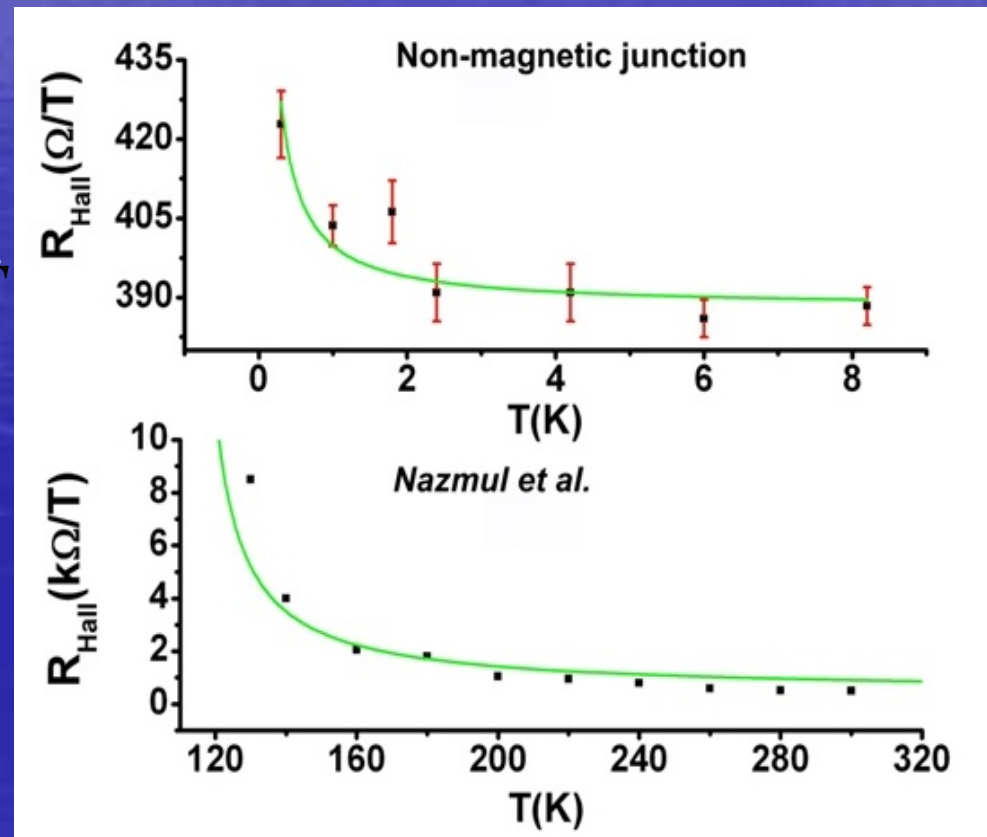
- Anomalous Hall Effect

$$R_H = R_O + R_S \frac{C}{\mu_0 (T - T_C)}$$

$$R_{S-NMJ} = 2.73 \pm 0.58 \times 10^{-11} \Omega / T$$

$$R_{S-Naz} = 4.46 \pm 0.76 \times 10^{-7} \Omega / T$$

$$r = \frac{R_{S-Naz}}{R_{S-NMJ}} \approx 16000$$



MAGNETO-TRANSPORT MEASUREMENTS

- Anomalous Hall Effect

$$R_{Hall} = -\frac{1}{en_{HJ}} \frac{qr^2 + 1}{(qr + 1)^2}$$

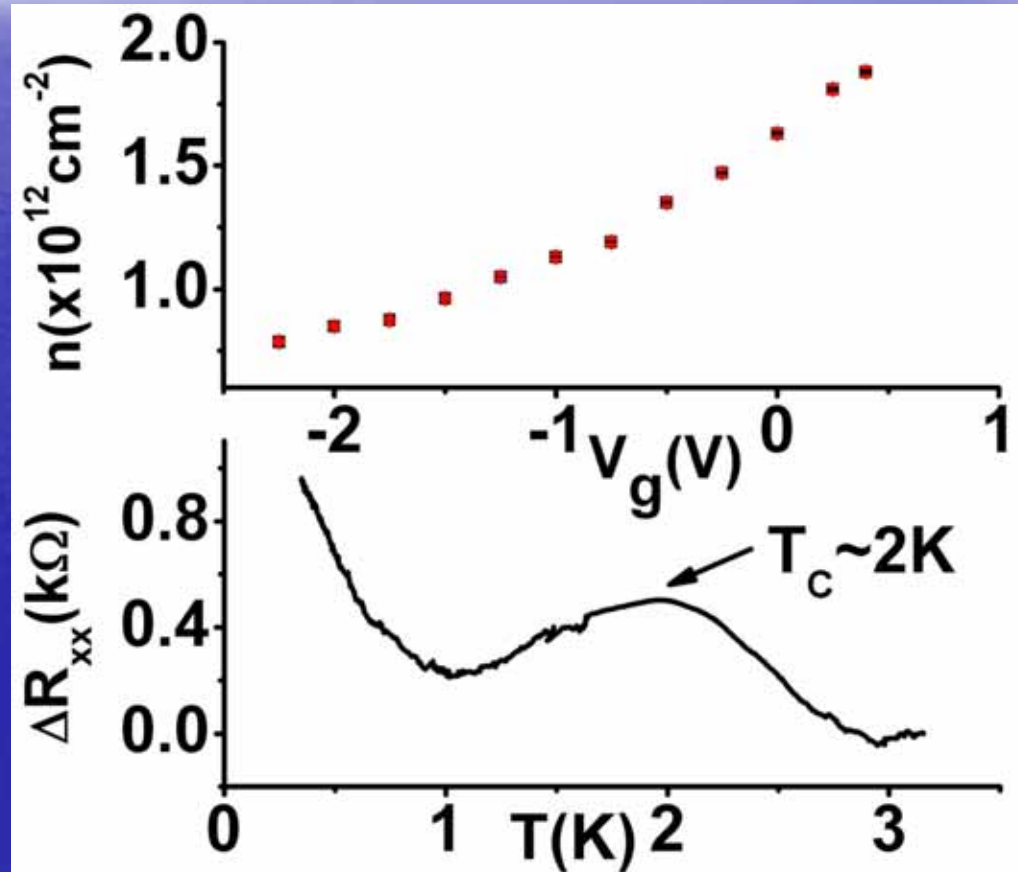
$$q = \frac{n_{QW}}{n_{HJ}}, \quad r = \frac{\mu_{QW}}{\mu_{HJ}}$$

$$\frac{\partial(1/R_{Hall})}{\partial n_{QW}} = e \frac{(q^2 r^4 + 2qr^2 + 2r - r^2)}{(qr^2 + 1)^2}$$

$$q \approx 2.5, \quad r \approx 0.22$$

$$\frac{R_{S-Naz.}}{R_{S-NMJ}} \approx 1800$$

$$R_{S-NMJ}$$



Conclusions & Future Directions

- We have successfully designed a 2D Ferromagnetic gas with excellent gating capabilities
- We can make ohmic contact to the 2D gas without destroying the Ferromagnetism
- We have shown the first clear evidence of electron-mediated ferromagnetism in GaMnAs
- We have set the first clear bound on the AHE in an electron mediated DMS compared to a hole mediated DMS
- Domain size study
- Simpler structure with better mobility
- First ferromagnetic quantum dot

Spin-Orbit: Skew-Scattering (extrinsic-disorder)

$$H_1 = \left[-\frac{\nabla^2}{2m} + V_{dis}(\mathbf{r}) \right] \delta_{\sigma\sigma'} - M_z \tau_{\sigma\sigma'}^z - i(g_\sigma/4\pi n_\sigma) [\tau_{\sigma\sigma'} \cdot (\nabla V_{dis} \times \nabla)]$$

$$n_\sigma = (k_{F\sigma}^2/4\pi)$$

$$\begin{aligned} \sigma_{xy}^{ss(0)} &= e^2 \sum_{\sigma} \tau_{\sigma\sigma}^z D_{\sigma}^{(0)} N_{\sigma} \sqrt{w_{\sigma}} g_{\sigma} / (1 + \frac{1}{2} g_{\sigma}^2) \\ &= \frac{e^2}{4} \sum_{\sigma} \tau_{\sigma\sigma}^z \left(\frac{n_{\sigma}}{n_{imp}} \right) \frac{1}{\sqrt{w_{\sigma}}} \frac{g_{\sigma}}{(1 + g_{\sigma}^2/2)^2} \end{aligned}$$

$$\sigma_{xy}^{ss(0)} / \sigma_{\alpha\alpha}^{(0)} \simeq \left(\frac{M_z}{\epsilon_F} \right) V_0 N_0 \langle g_0 \rangle_{\sigma}$$

$$\rho_{xy} = \frac{\sigma_{xy}}{\sigma_{xx}^2 + \sigma_{yy}^2} \simeq \frac{\sigma_{xy}}{\sigma_{xx}} \rho_{xx}$$

Spin-Orbit: Side-Jump-Scattering

$$\mathbf{v} = \frac{d}{dt} \mathbf{r} = -i[\mathbf{r}, H_1] = \frac{\mathbf{p}}{m} + (g_\sigma / 4\pi n_\sigma)(\boldsymbol{\tau}_{\sigma\sigma} \times \nabla V_{dis})$$

$$\sigma_{xy}^{sj} = (e^2 / 2\pi) \sum_{\sigma} [g_\sigma / (1 + \frac{1}{2}g_\sigma^2)] \tau_{\sigma\sigma}^z$$

AHE: Berry Phase (intrinsic)

$$\chi(\mathbf{k}) = - \int_c^{\mathbf{k}} d\mathbf{k}' \cdot \mathbf{X}(\mathbf{k}')$$

$$\mathbf{X}(\mathbf{k}) = \int_{\text{cell}} d^2r u_{n\mathbf{k}}^*(\mathbf{r}) i\nabla_{\mathbf{k}} u_{n\mathbf{k}}(\mathbf{r})$$

$$\boldsymbol{\Omega}(\mathbf{k}) = \nabla_{\mathbf{k}} \times \mathbf{X}(\mathbf{k})$$

$$\dot{\mathbf{k}} = e\mathbf{E} + e\dot{\mathbf{r}} \times \mathbf{B}$$

$$\dot{\mathbf{r}} = \nabla_{\mathbf{k}} \epsilon_{n\mathbf{k}} - e\mathbf{E} \times \boldsymbol{\Omega}$$

$$\mathbf{j}_H = -e^2 n \langle \boldsymbol{\Omega} \rangle \times \mathbf{E} \rightarrow \sigma_{xy}^B = e^2 n \langle \Omega_z \rangle$$

$$\langle \boldsymbol{\Omega} \rangle = n^{-1} \sum_{\mathbf{k}\sigma} \boldsymbol{\Omega}_{\sigma}(\mathbf{k}) f(\epsilon_{\mathbf{k}\sigma})$$

$$\sigma_{AH} = -\frac{2e^2}{\hbar V} \sum_{n,\mathbf{k}} f_{n,\mathbf{k}} \text{Im} \left\langle \frac{\partial u_{n,\mathbf{k}}}{\partial k_x} \middle| \frac{\partial u_{n,\mathbf{k}}}{\partial k_y} \right\rangle$$