

Fabry-Perot Resonator for Hard X-Rays

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Research Team

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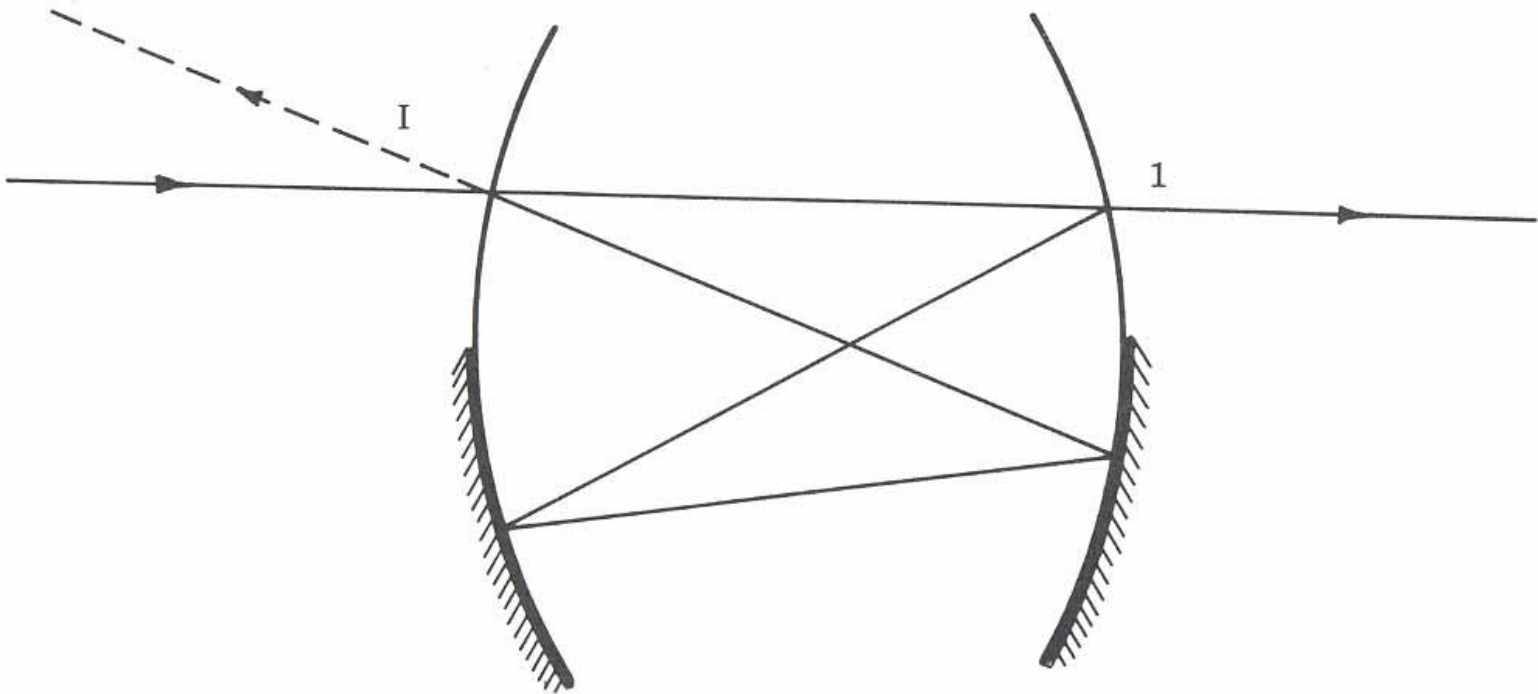
¹Department of Physics, National Tsing Hua University (NTHU), Hsinchu, Taiwan, R.O.C. 300

²National Synchrotron Radiation Research Center (NSRRC), Hsinchu, Taiwan, R.O.C. 300

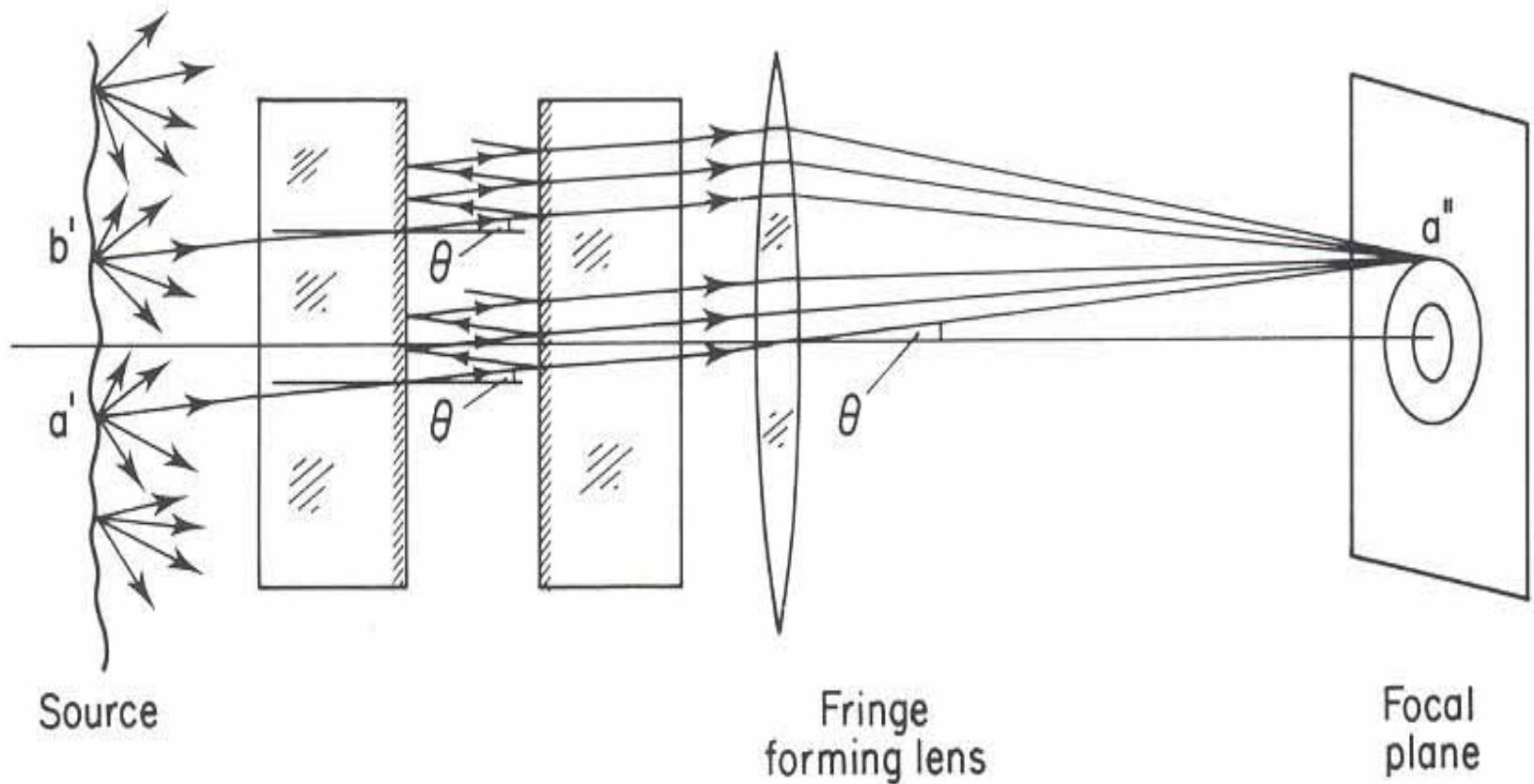
³Spring-8/JASRI, Mikazuki, Hyogo 679-5198, Japan

⁴Spring-8/RIKEN, Mikazuki, Hyogo 679-5148, Japan

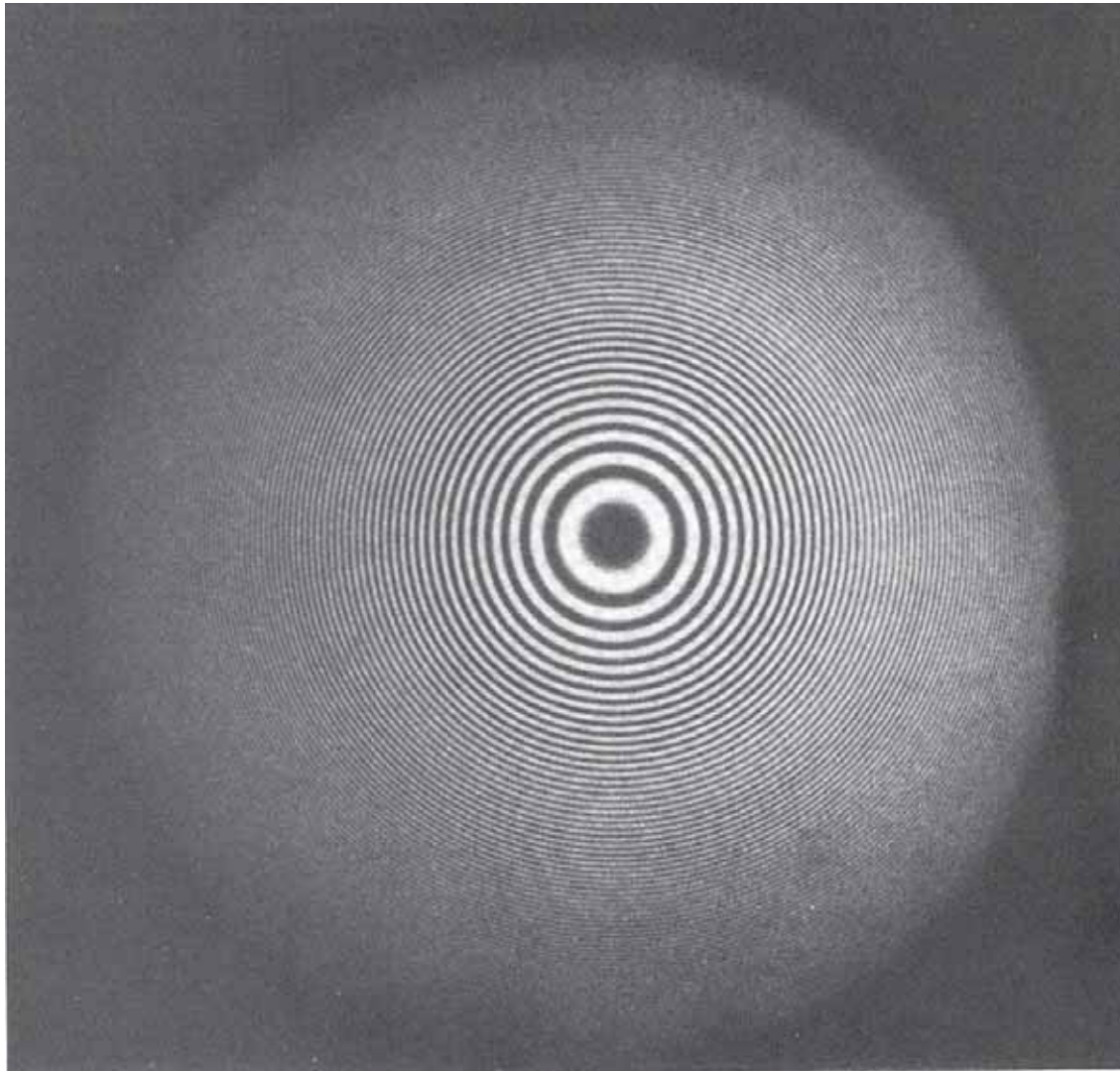
Optical Fabry-Parot Interferometer



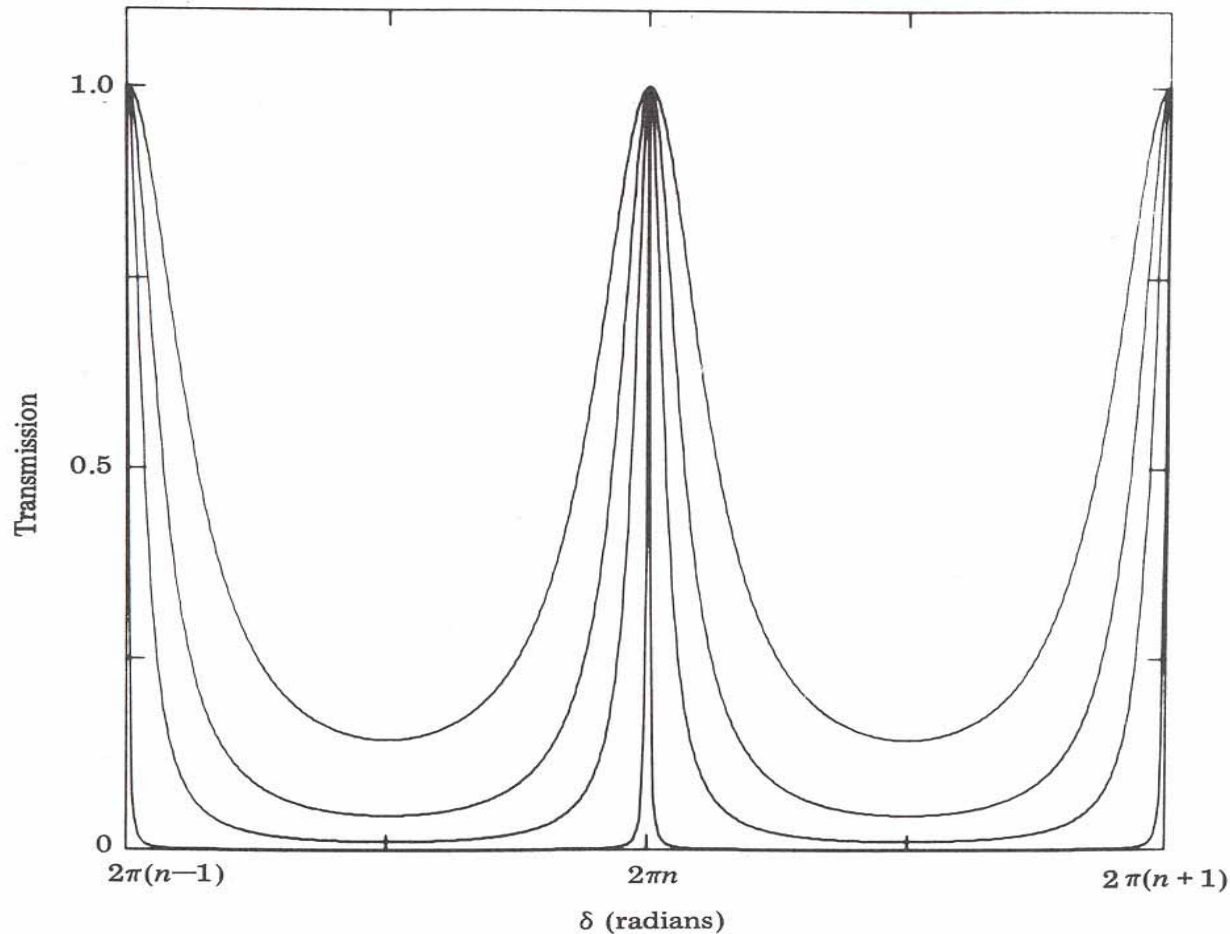
Optical Fabry-Parot Interferometer



Transmitted radiation of a Fabry-Perot etalon

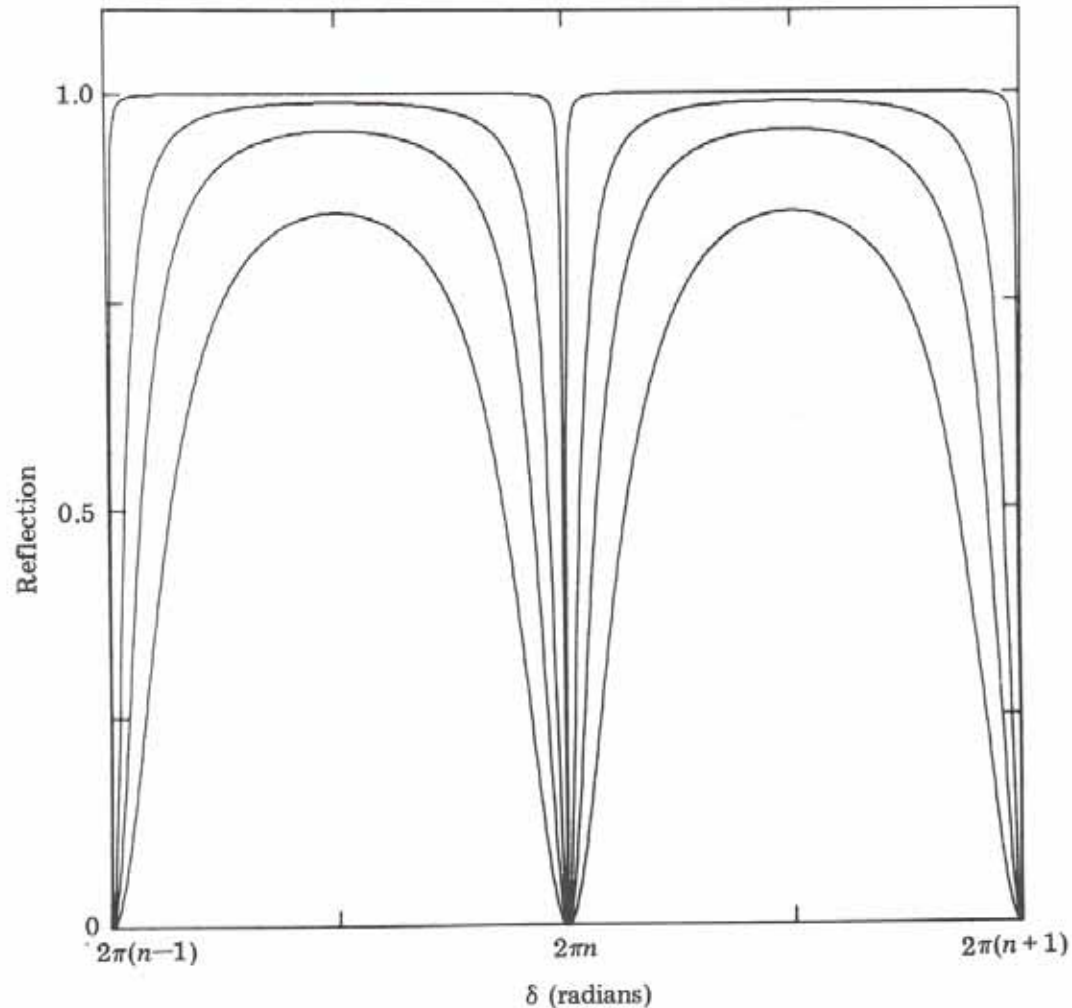


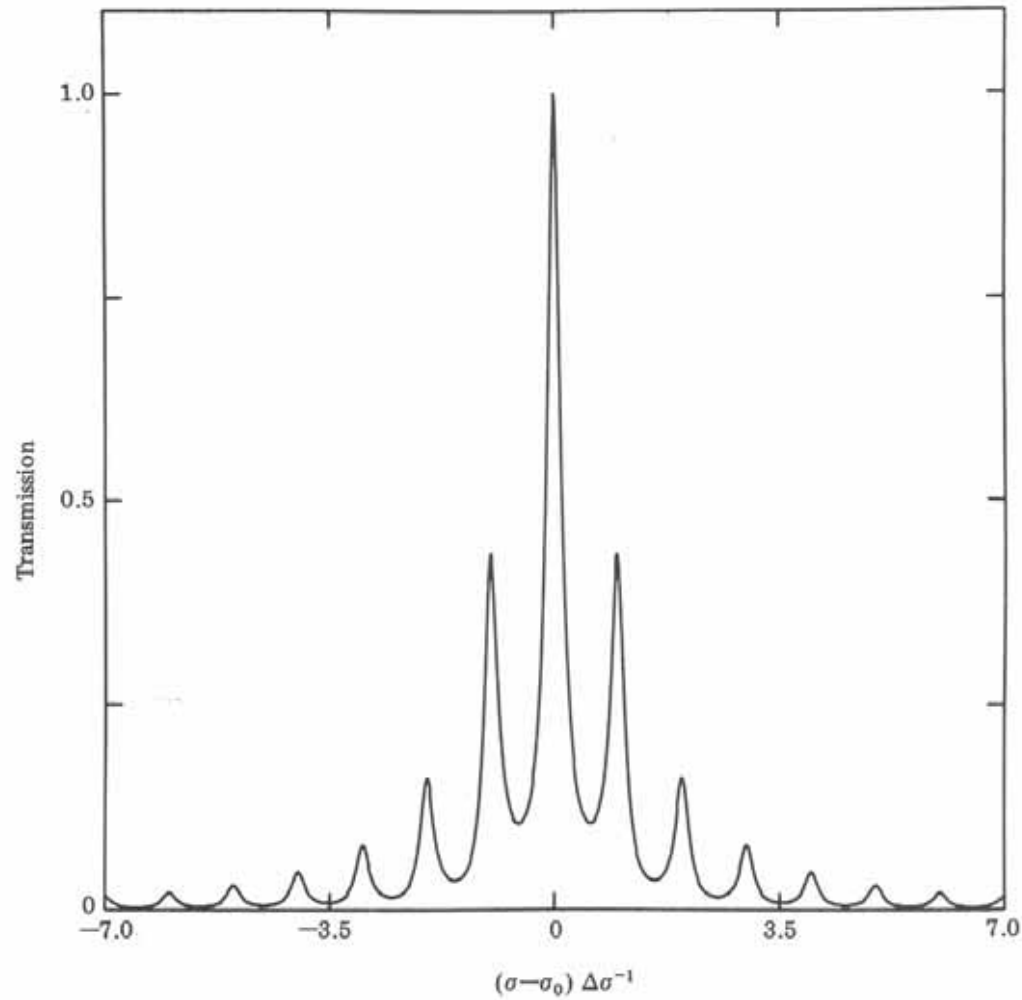
Transmitted radiation of a Fabry-Perot etalon as a function of the phase retardation of the beams for various reflectivities.



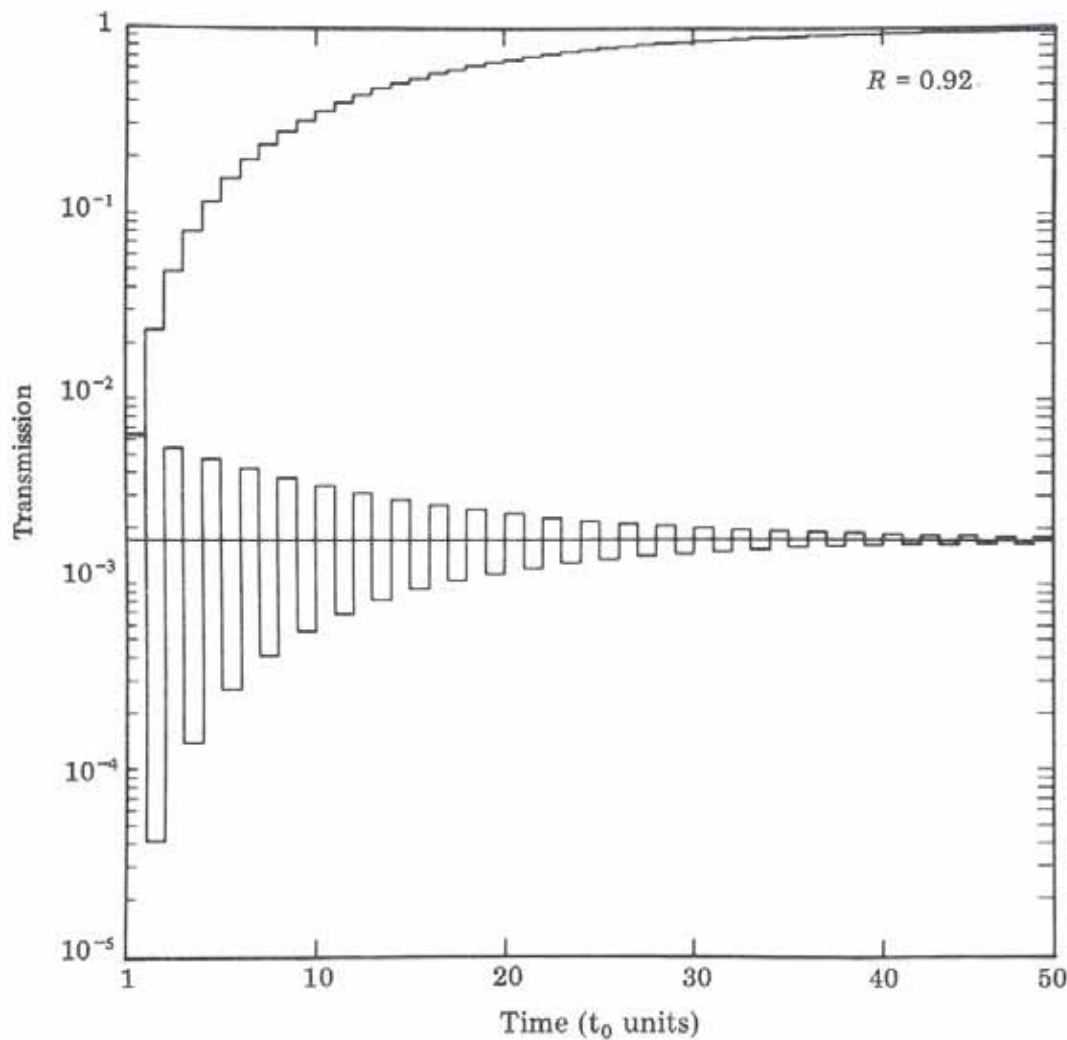
$$\delta = 2\pi (2 R d \cos \theta) / \lambda$$

Reflected radiation of a Fabry-Parot etalon as a function of the phase retardation of the beams.





**Transmission of an etalon combined
with a Lorentzian filter.**



δt is a pulse of length ; and t_r is response time.

Response of an etalon to a pulse of length δt greater than t_r .

Literature (for X-rays)

1. Bond, W. L., Duguay, M. A. & Rentzepis, P. M.
“Proposed resonator for an X-ray laser”.
Appl. Phys. Lett. **10**, 216-218 (1967).
2. Deslattes, R. D.
“X-ray monochromators and resonators from single crystals”.
Appl. Phys. Lett. **12**, 133-135 (1968).
3. Liss, K. D., Hock, R., Gomm, M., Waibel, B., Magert, A., Krisch, M. & Tucoulou, R.
“Storage of X-ray Photons in a crystal resonator”.
Nature **404**, 371-373 (2000).
4. Shvyd'ko, Yu. V., Lerche, M., Wille, H.-C., Gerdau, E., Lucht, M. & Rutter, H.D.
“X-ray interferometer with microelectronvolt resolution”.
Phys. Rev. Lett. **90**, 013904(1)-013904(4) (2003).

Gamma-Ray Lasers (proposals)

- Baldwin, G.C. & Solem, J.C.

“Approaches to the Development of Gamma-Ray Lasers”

Rev. Mod. Phys. 53, 687 (1981)

Photon channeling in crystals

Standing-wave fields in crystals

2. Baldwin, G.C. & Solem, J.C.

“Recoilless Gamma-Ray Lasers”

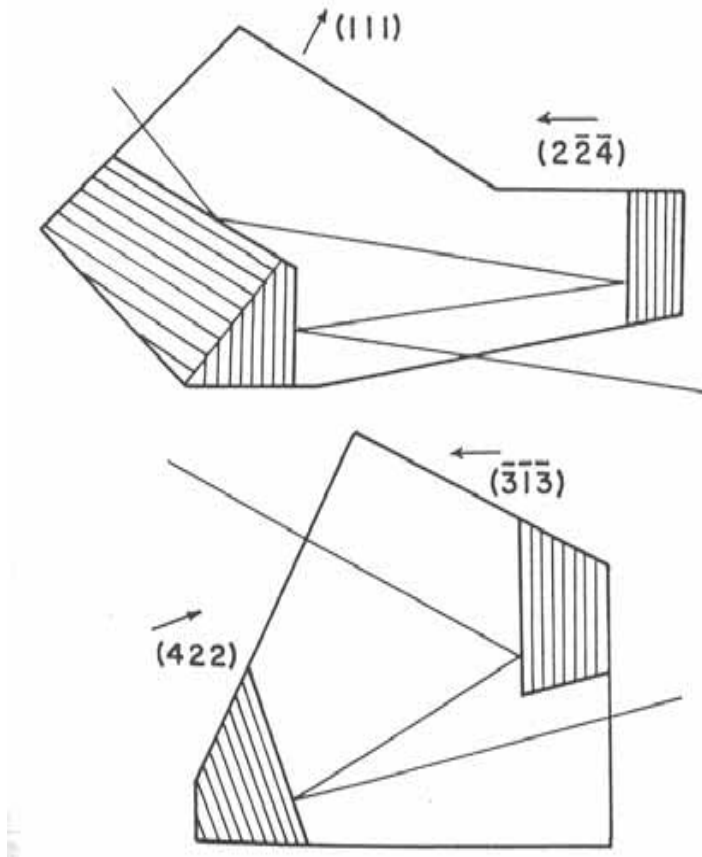
Rev. Mod. Phys. 69, 1085 (1997)

Crystals as resonators

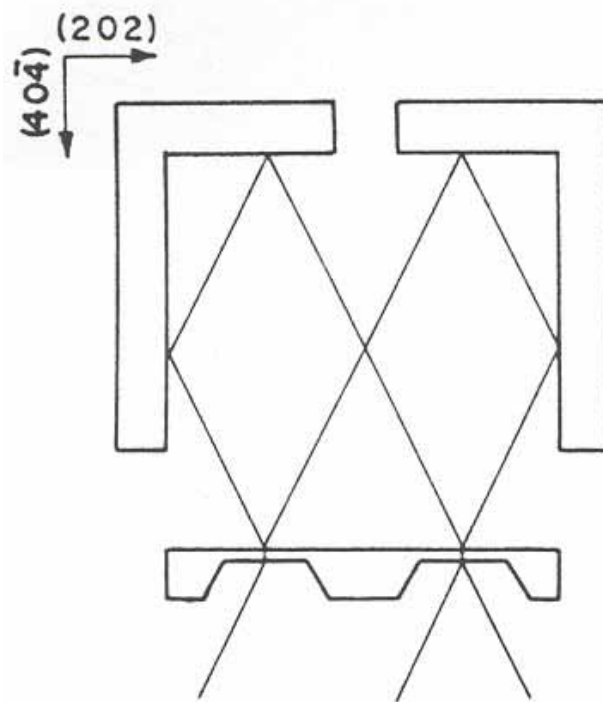
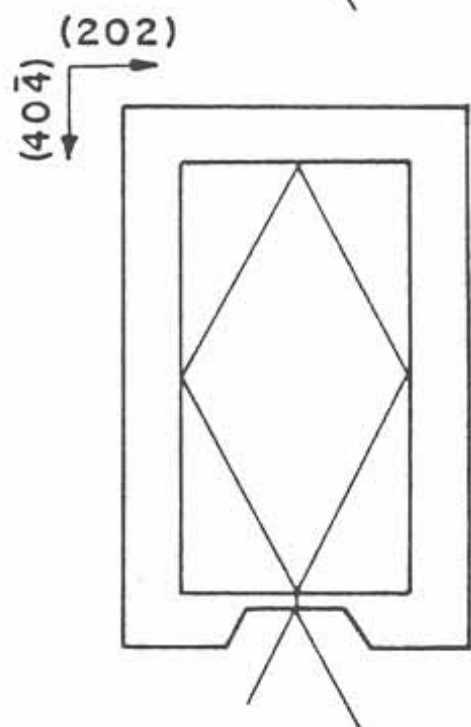
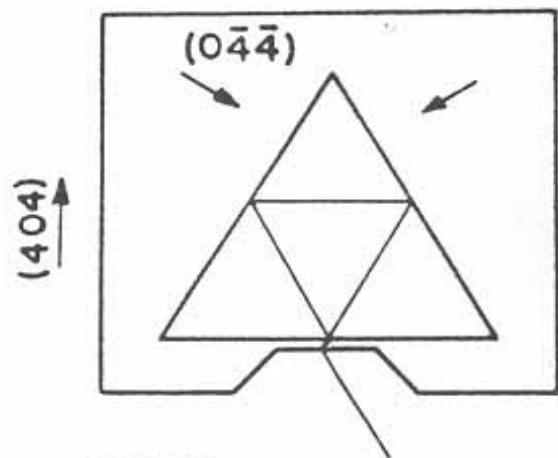
Literature (for X-rays)

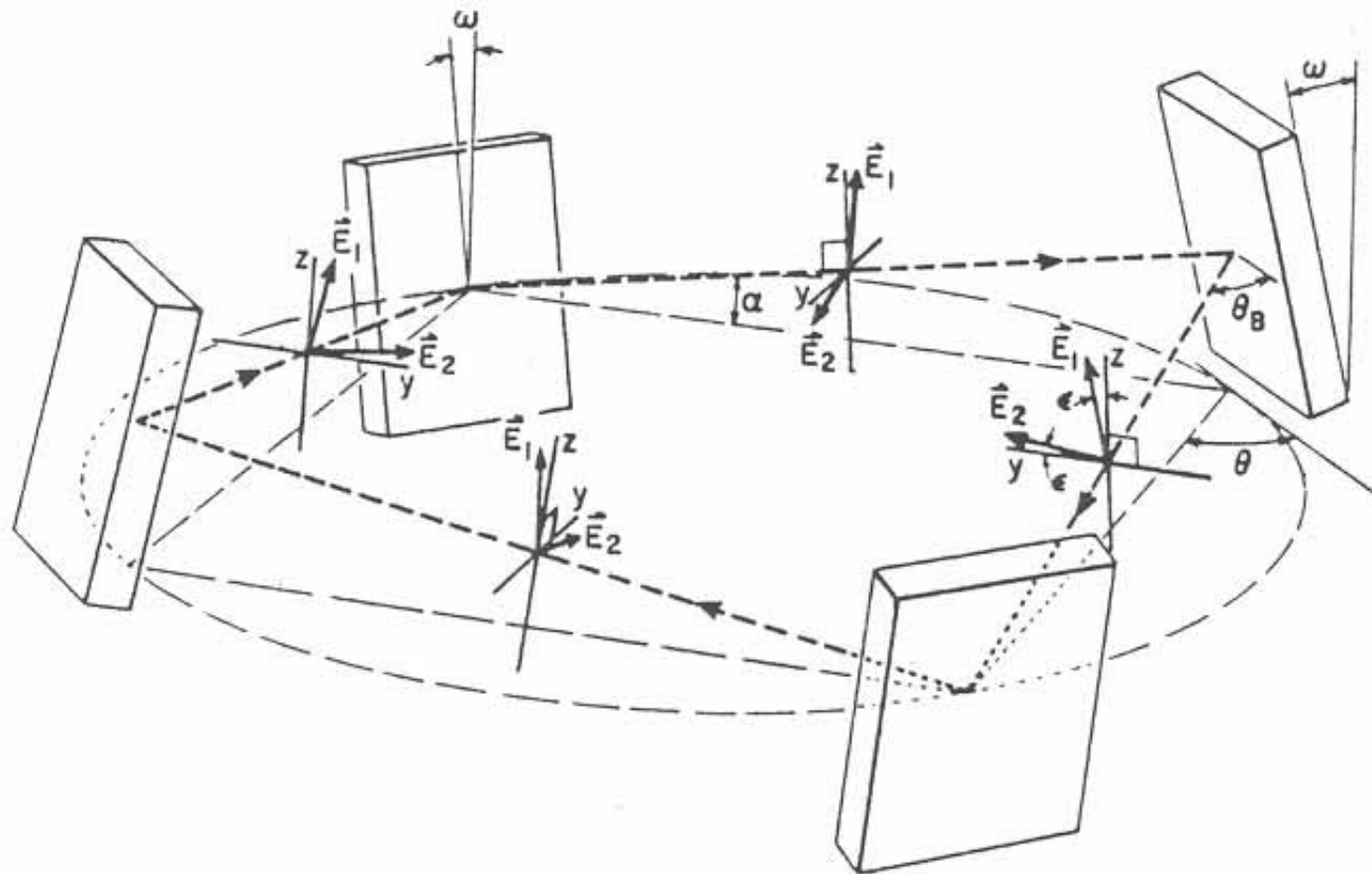
1. Bond, W. L., Duguay, M. A. & Rentzepis, P. M.
“Proposed resonator for an X-ray laser”.
Appl. Phys. Lett. **10**, 216-218 (1967).
2. Deslattes, R. D.
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3. Liss, K. D., Hock, R., Gomm, M., Waibel, B., Magert, A., Krisch, M.
& Tucoulou, R.
“Storage of X-ray Photons in a crystal resonator”.
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Rutter, H.D.
“X-ray interferometer with microelectronvolt resolution”.
Phys. Rev. Lett. **90**, 013904(1)-013904(4) (2003).

Proposed X-ray Cavity Geometry

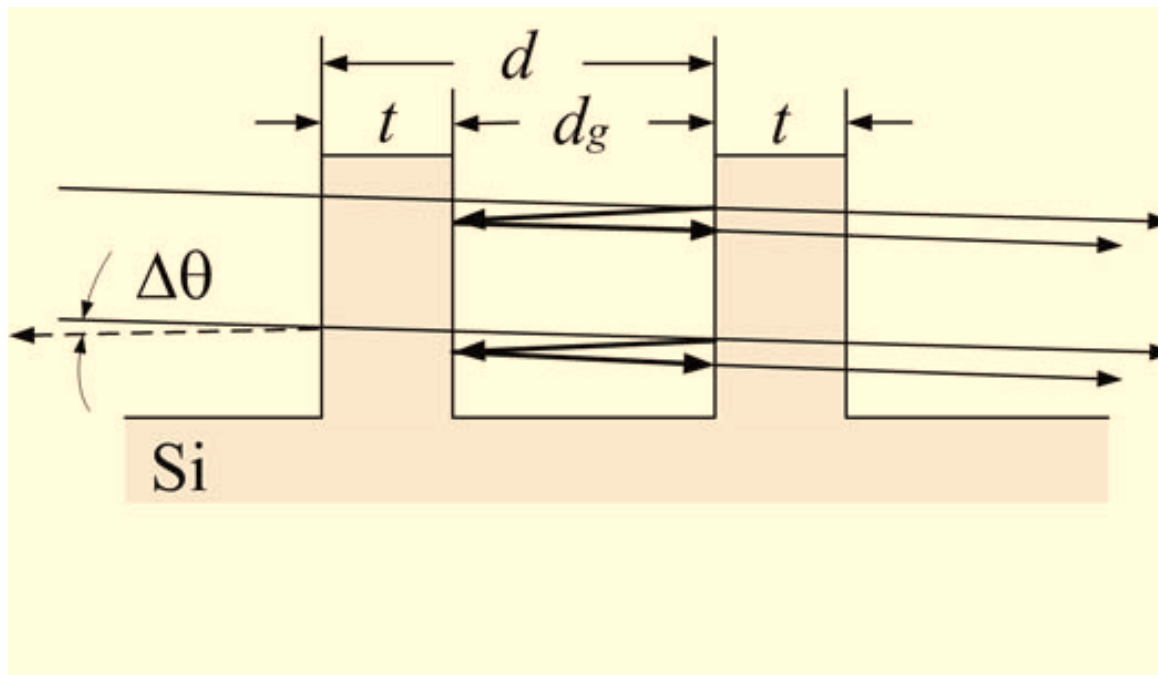


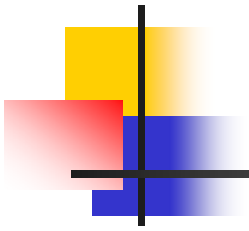
Deslattes, *Appl. Phys. Lett.* **12**,
133 (1968)





X-ray Fabry-Perot resonator



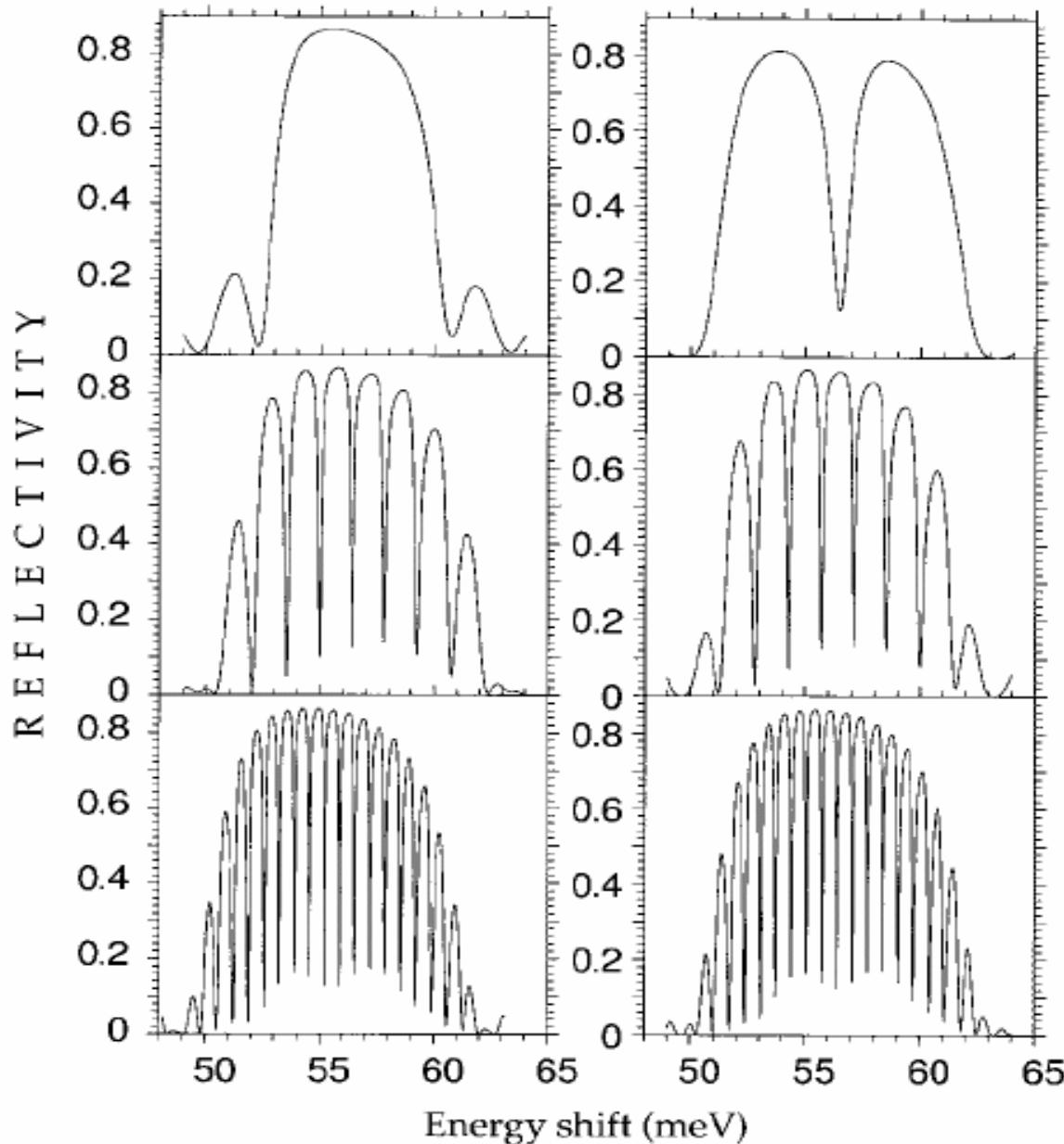


X-ray Fabry-Perot resonator

Cavity resonance occurs when an incident X-ray is reflected back and forth coherently , both **spatially and temporally** , between the two plates , thus generating interference frings .

X-ray back diffraction (Bragg angle=90 deg.)

Theoretical calculation



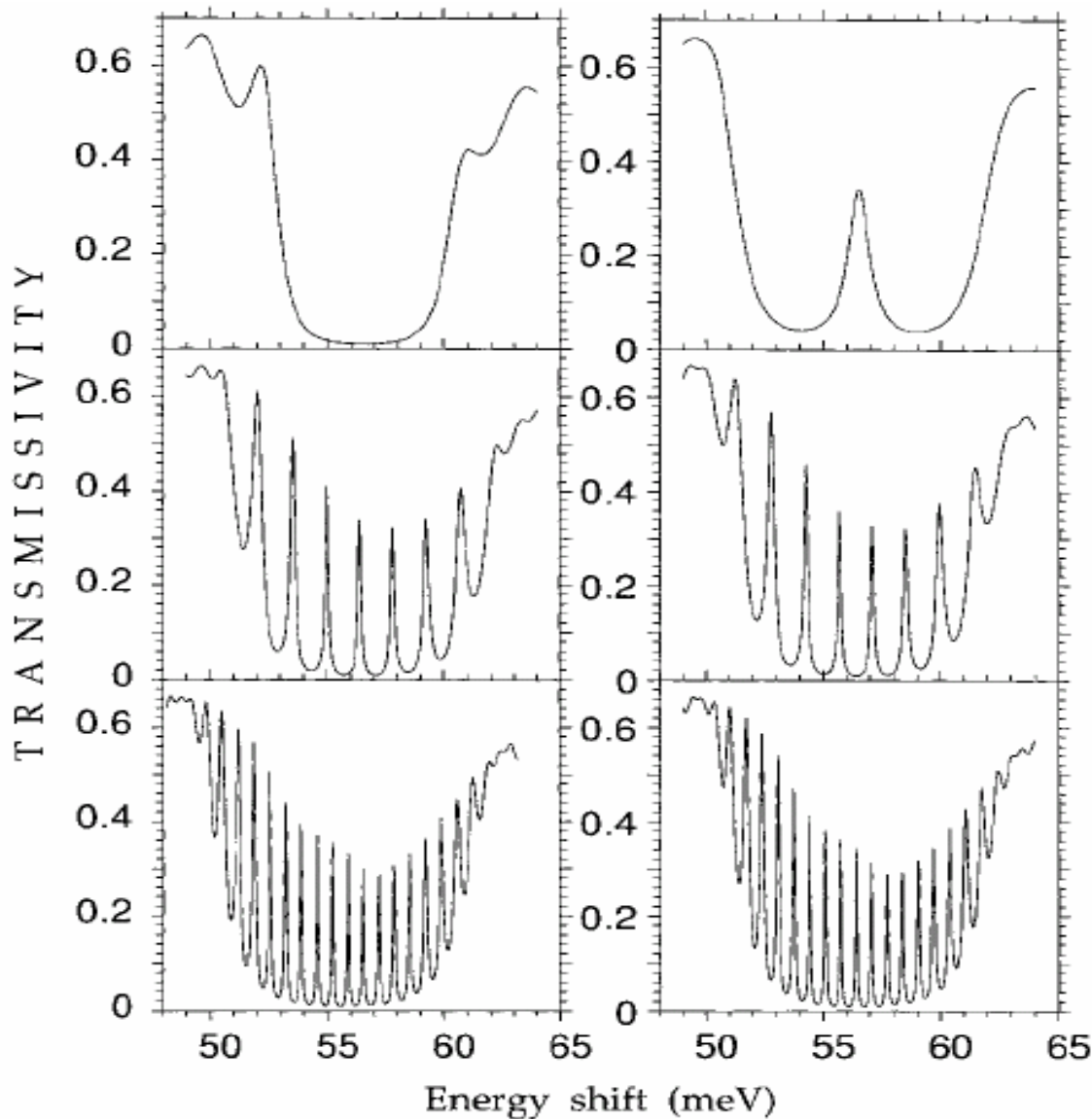
Reflectivity of an X-ray Fabry-Perot interferometer with the same parameters as the transmissivity

Resonance fringes appearing inside the energy gap in energy scan (the total reflection range in angle scan)

Pendellosung for thin crystal plates

Defect states (photonic crystals)

Theoretical calculation



Transmissivity of an X-ray Fabry-Perot interferometer as function of the X-ray energy E with respect to the Bragg energy $E_B = 14.4125 \text{ keV}$.

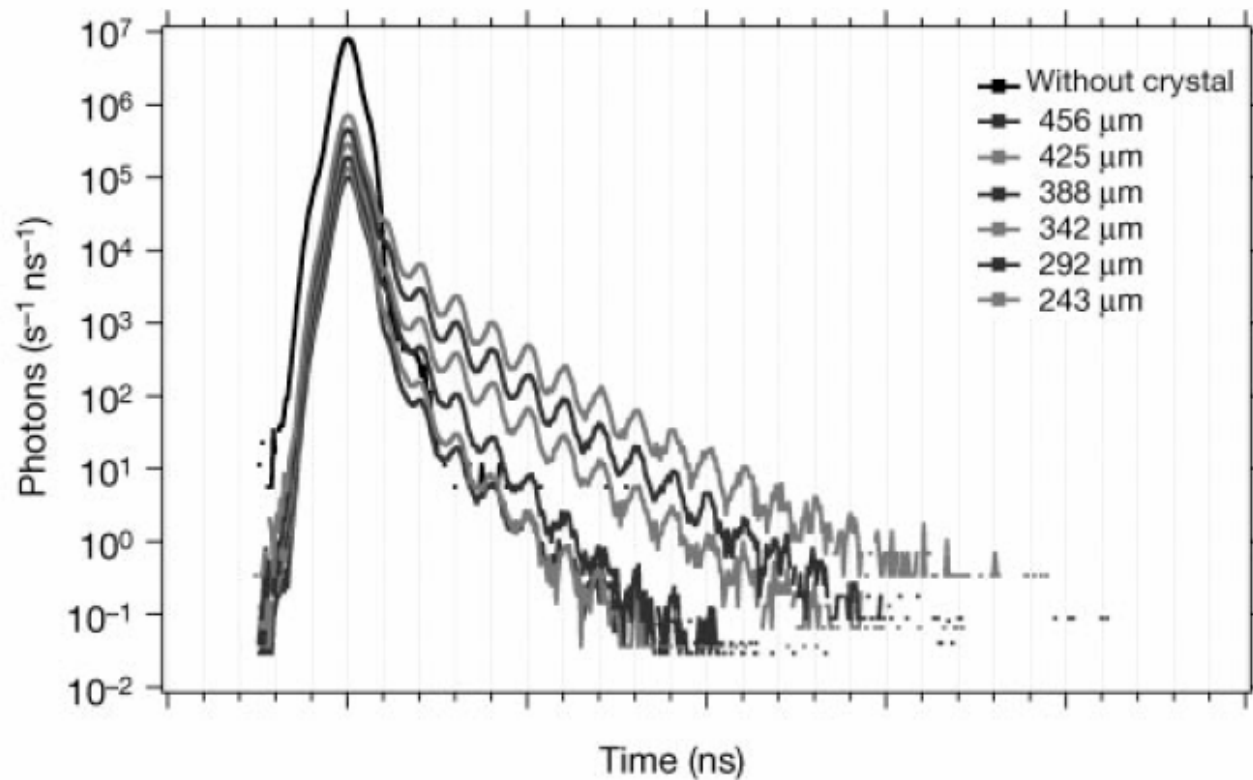
Normal incidence is assumed to the reflecting planes (1,3,-4,28) of sapphire (Al_2O_3)

crystal plates of thickness $d_1 = d_2 = 100 \mu\text{m}$ separated by a gap of thickness $d_g = 0$ (top), 0.5 mm (middle) and 1 mm (bottom).

The relative shift of crystal lattices in the mirrors is $s = 0$ (left) and $s = 0.5$ (right)

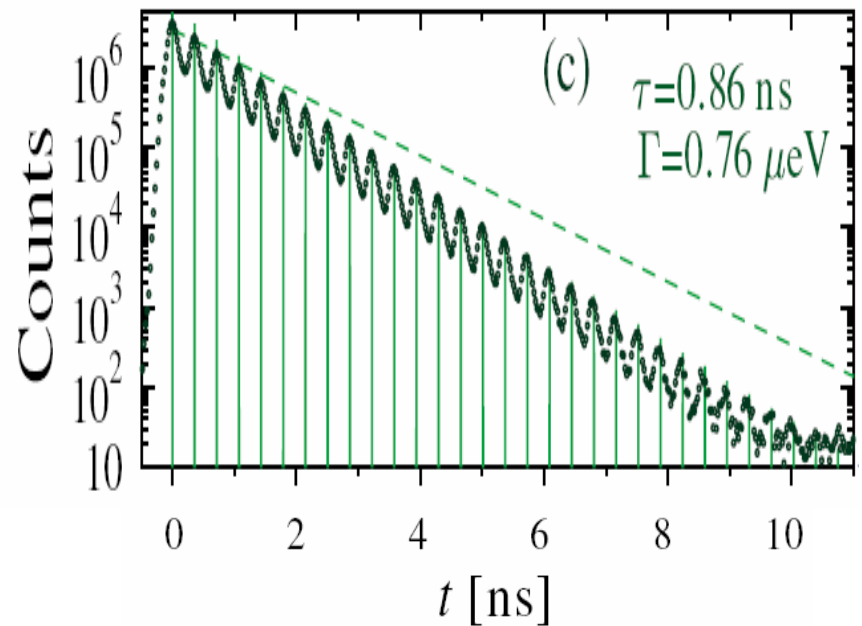
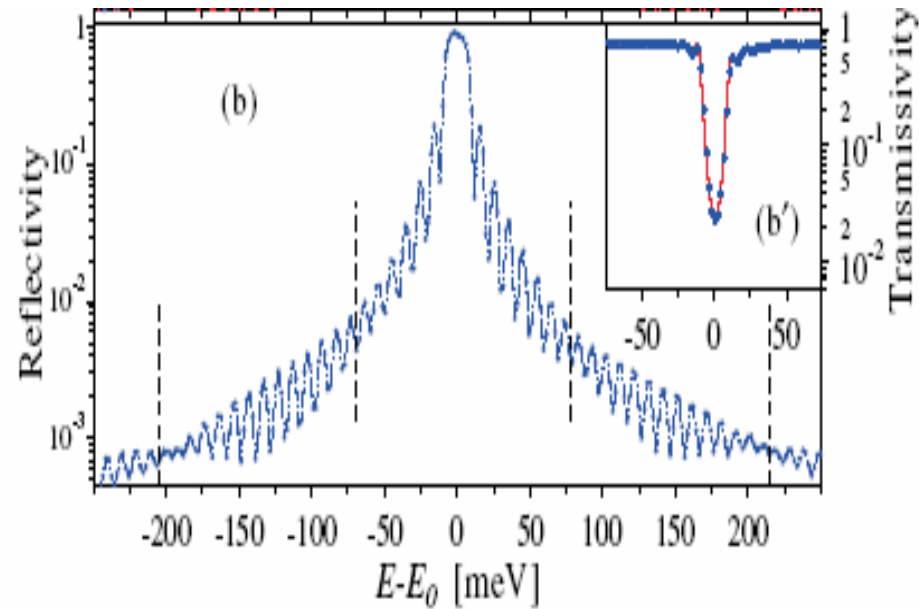
K.-D. Liss et al. (Nature 2001)

$d_G = 15 \text{ cm}$ $t = 243 \text{ } \mu\text{m} \sim 456 \text{ } \mu\text{m}$ $\Delta E/E \sim 10^{-7}$



Shvyd'ko et al (PRL 2003):

$$d_G = 0.5 \text{ cm} \quad t_1 = 63 \mu\text{m} \quad t_2 = 59 \mu\text{m} \quad \Delta E/E \sim 10^{-7}$$



X-ray Cavity Research in Phys. Dept. NTHU

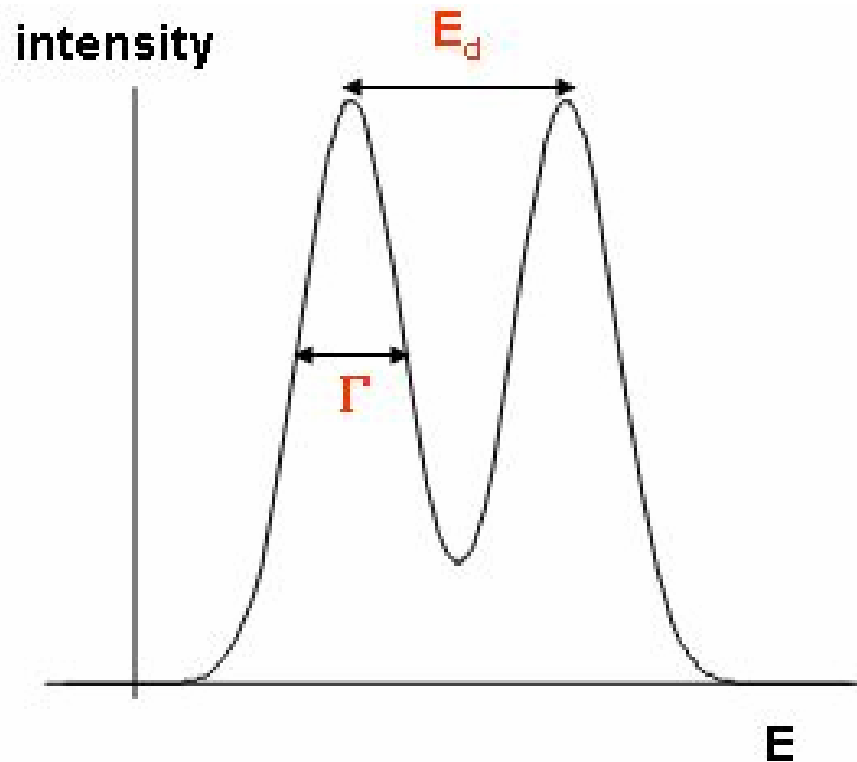
1984 Seminar on “Feasibility of X-ray lasers”

1997 First two crystals prepared

1999~2003 Experiments at beamline 19XU,
Spring-8 (3 more crystals prepared)

2004 Experiments at beamline 12XU, NSRRC
beamline at Spring-8 (4 more crystals
prepared)

Resolution of two spectral components



Criteria for observing cavity resonance fringes

- a. $\Delta E < E_d$ (ΔE = the energy resolution of the incident X-ray beam ; $E_d = hc/2d$)
- b. $\Delta E < \Gamma$
- c. $\Gamma < E_d$
- d. $\Delta t > t_f / 2\pi$ ($\Delta t = \hbar / \Delta E$, the coherent time of the incident beam ; $t_f = h / E_d = 2d / c$)
- e. $\ell_L = \langle \lambda^2 / \Delta\lambda \rangle = \langle \lambda / (\Delta E / E) \rangle > 2d$

4-crystal Monochromator



Energy resolution :

$$\Delta E = 0.36 \text{ meV}$$

$$\Delta E/E = 2.5 \times 10^{-8}$$

at 14.4388 keV

(0.8588 Å)

1 step = 0.005 arcsec.

= 58.548 μeV

◎ Cavity size :

$t=25 \text{ um} \sim 100 \text{ um}$, $d_g=40 \sim 150 \text{ um}$, $d=t+d_g=65 \text{ um} \sim 250 \text{ um}$

$$\Delta E (=0.36 \text{ meV}) < E_d (=3.6 \text{ meV})$$

Criterion (a) is satisfied.

$$\Delta E (=0.36 \text{ meV}) < \Gamma (=1.60 \text{ meV})$$

Criterion (b) is satisfied.

$$\Gamma (=1.60 \text{ meV}) < E_d (=3.6 \text{ meV})$$

Criterion (c) is satisfied.

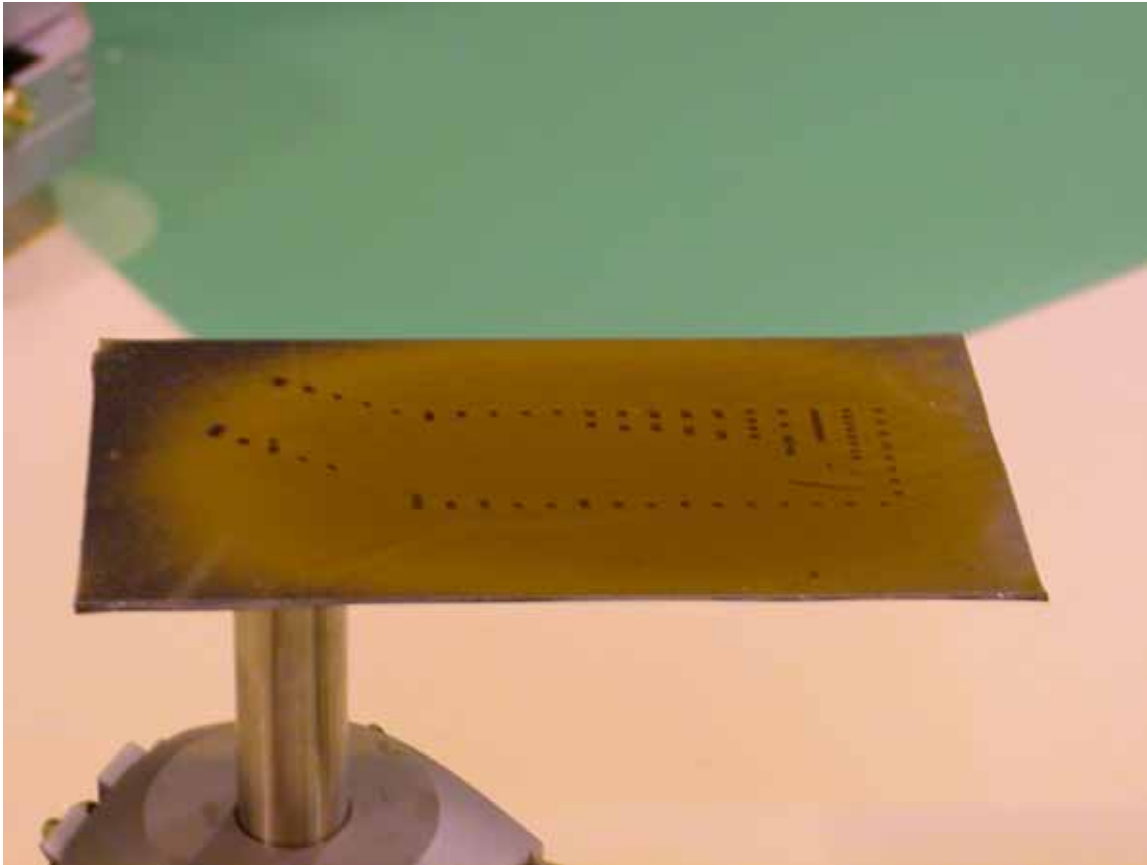
$$\Delta t (=1.8 \text{ ps}) > t_f / 2\pi (=0.1 \text{ ps})$$

Criterion (d) is satisfied.

$$l_L (=1717 \text{ um}) > 2d (=340 \text{ um})$$

Criterion (e) is satisfied.

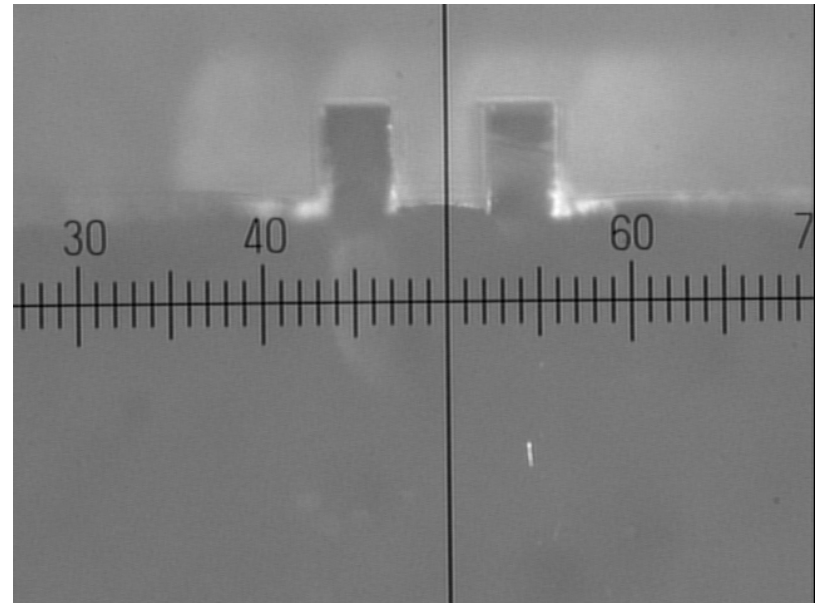
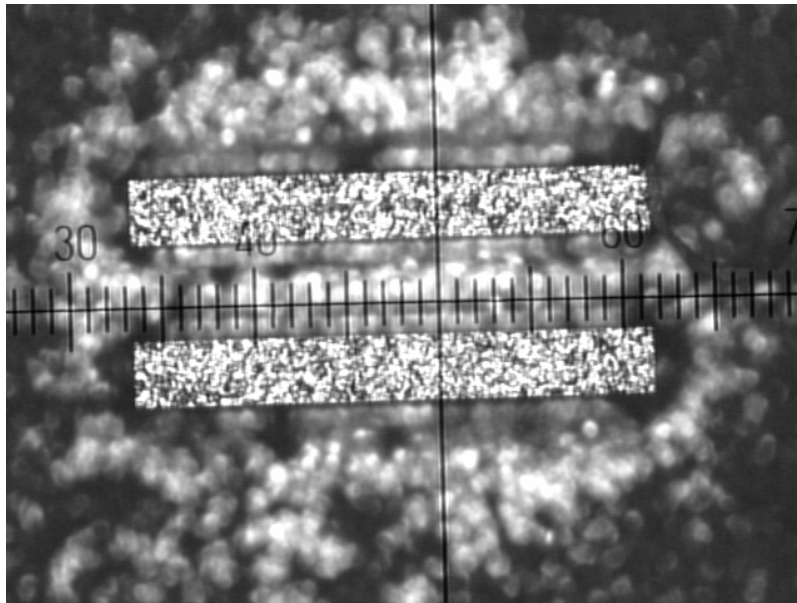
Crystal Cavities (Si)



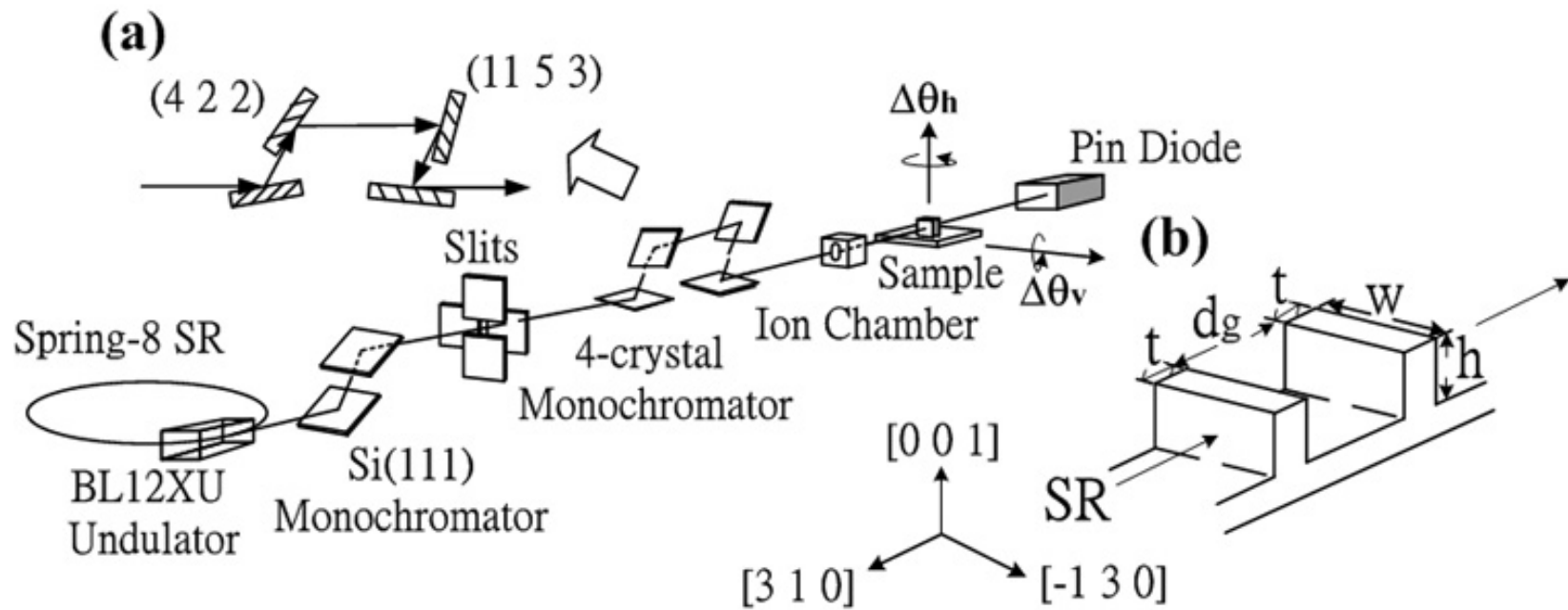
Lithography

Ion-beam dry
etching

Top-view & side-view



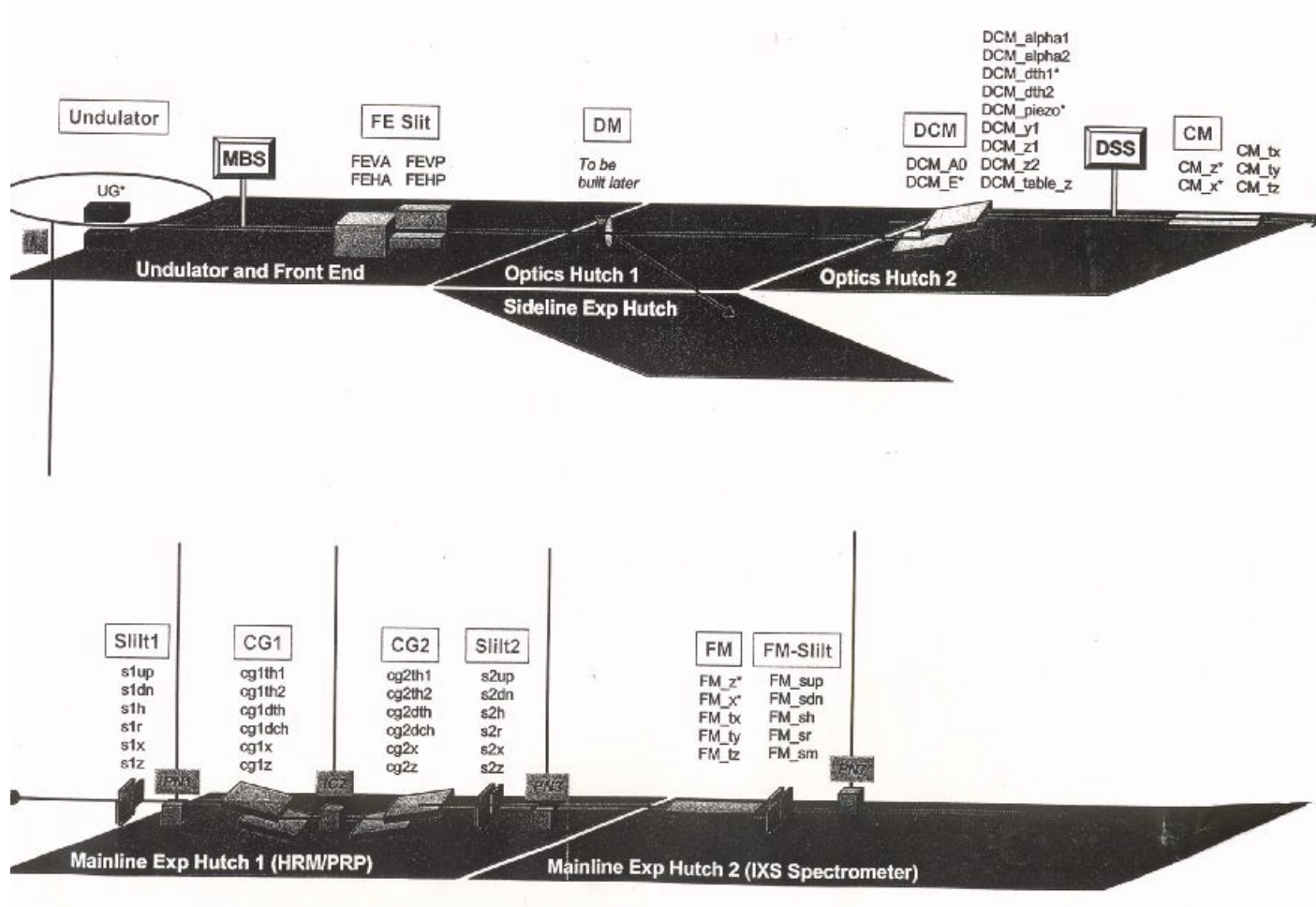
Experimental set-up



Spring-8 (Super Photon ring-8 GeV) Japan



8 GeV; $\gamma = 15,700$; 1.44 km circumference



A Huber 8-circle diffractometer



1 step=0.0005 deg.

$$\Delta T = 0.1^{\circ} \text{C}$$

At 14.4388 keV, a 24-beam diffraction takes place



9 coplanar diffractions C1 – C9

C1: (040), (4-40), (480), (8-40), (880), (12 0 0)

C2: (6-4-2), (682)

C3: (022), (12 2 -2)

C4: (60-6), (646)

C5: (426), (82-6)

C6: (42-6), (826)

C7: (606), (646)

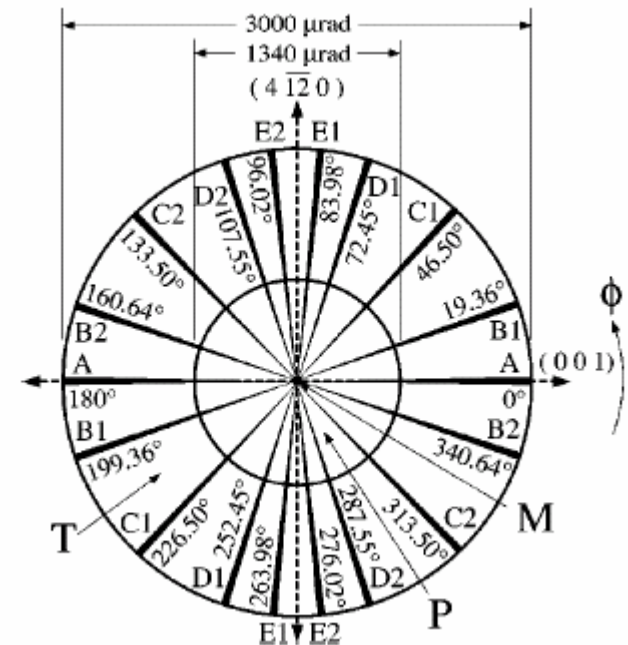
C8: (02-2), (12 2 2)

C9: (6-42), (68-2)

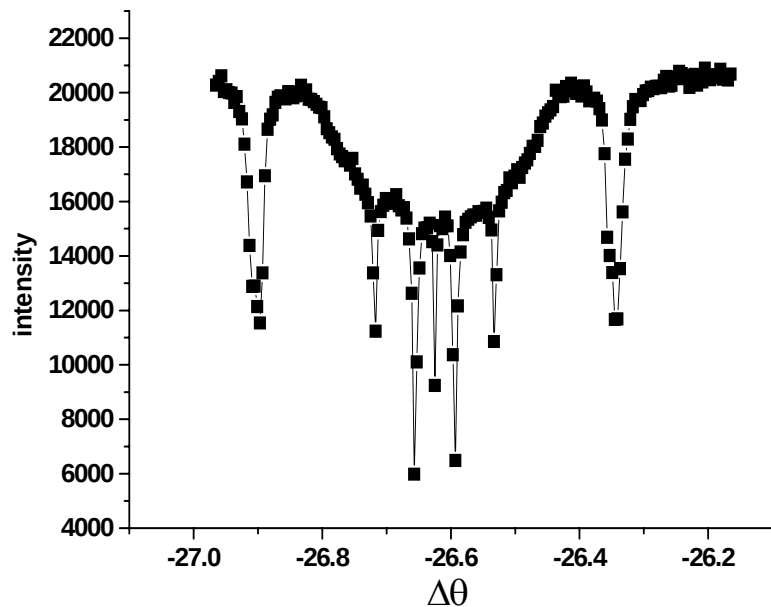
(000) and (12 4 0) reflections (back diffraction)

At 14.4388 keV, a 24-beam diffraction takes place

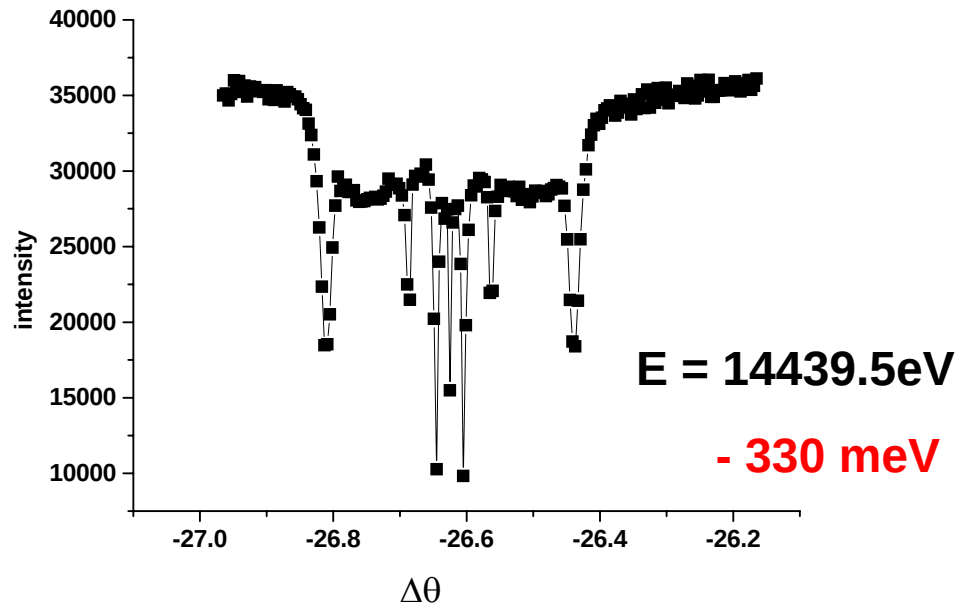
No.	(hkl)	$\tilde{\theta}_B$ (°)	ϕ_{ref} (°)	No.	(hkl)	$\tilde{\theta}_B$ (°)	ϕ_{ref} (°)
1	(8 2 6)	53.729	6.017	12	(4 2 $\bar{6}$)	36.271	186.017
2	(6 0 6)	42.130	17.548	13	(6 4 $\bar{6}$)	47.870	197.548
3	(12 2 2)	77.079	43.492	14	(0 2 $\bar{2}$)	12.921	223.492
4	(6 4 2)	36.271	68.432	15	(6 8 2)	53.729	248.432
5	(12 0 0)	71.565	90.000	16	(0 4 0)	18.435	270.000
6	(4 4 $\bar{0}$)	26.565	90.000	17	(8 8 0)	63.435	270.000
7	(8 4 $\bar{0}$)	45.000	90.000	18	(4 8 0)	45.000	270.000
8	(6 4 2)	36.271	111.568	19	(6 8 2)	53.729	291.568
9	(12 2 2)	77.079	136.508	20	(0 2 2)	12.921	316.508
10	(6 0 6)	42.130	162.452	21	(6 4 6)	47.870	342.452
11	(8 2 $\bar{6}$)	53.729	173.983	22	(4 2 6)	36.271	353.983



The comparison of $\Delta\theta$ -scans

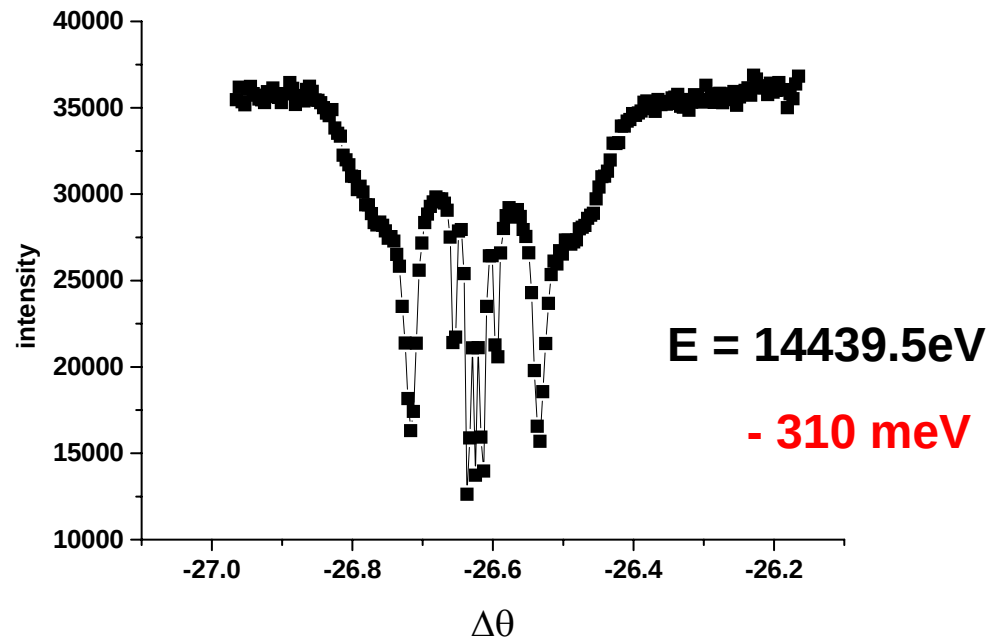


E = 14439.5eV - 350 meV



E = 14439.5eV

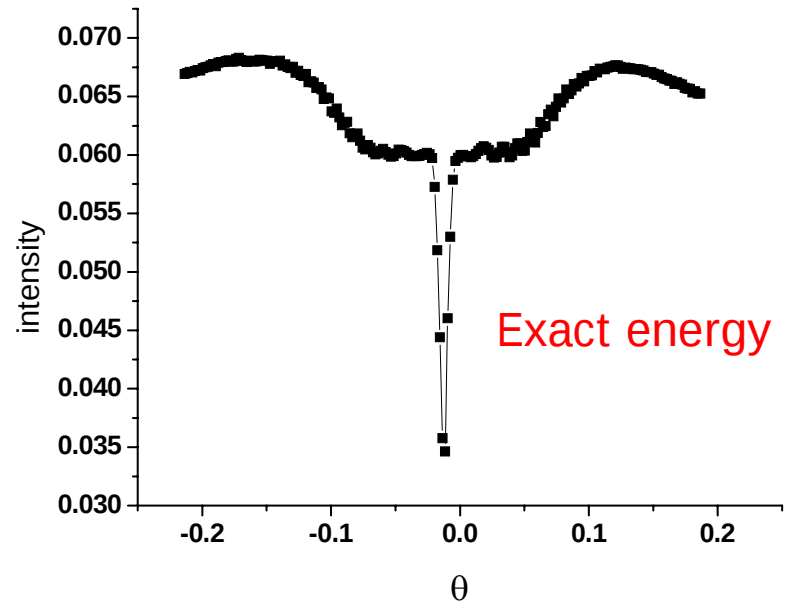
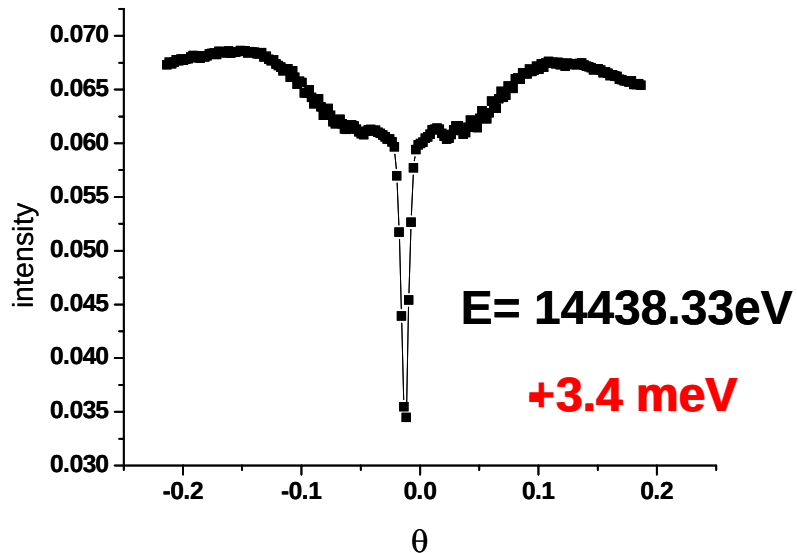
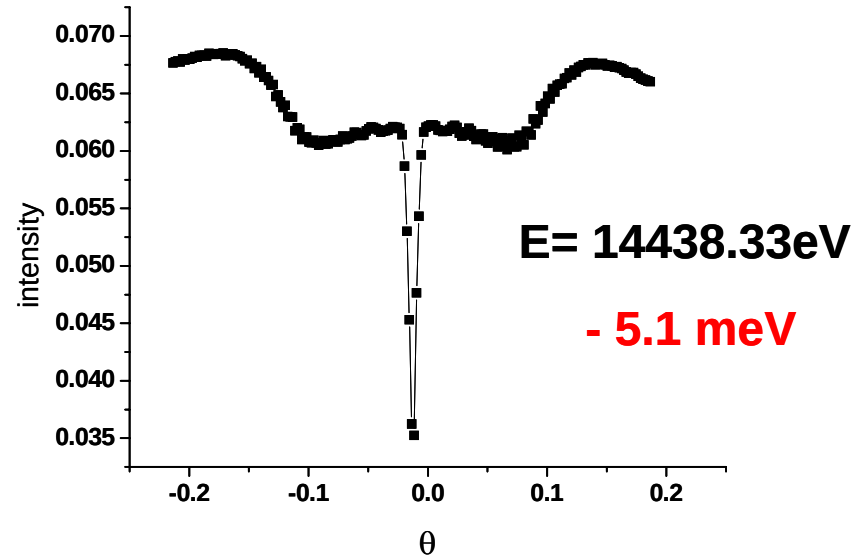
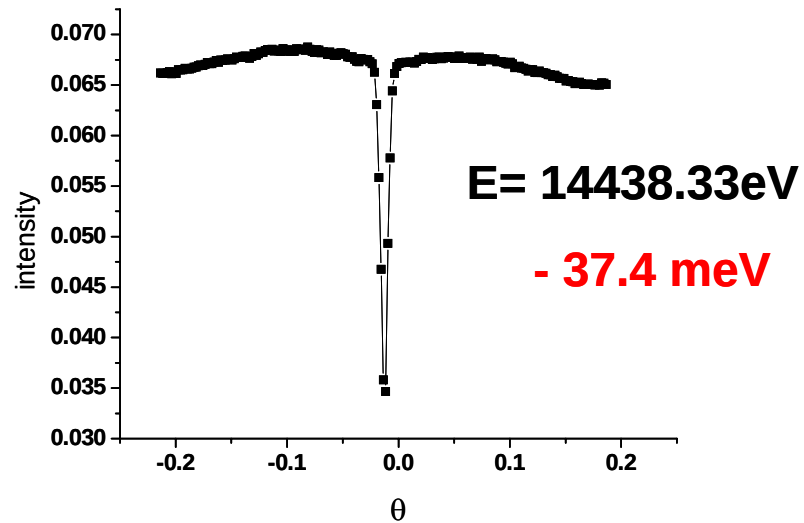
- 330 meV

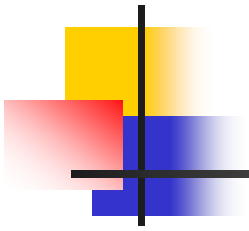


E = 14439.5eV

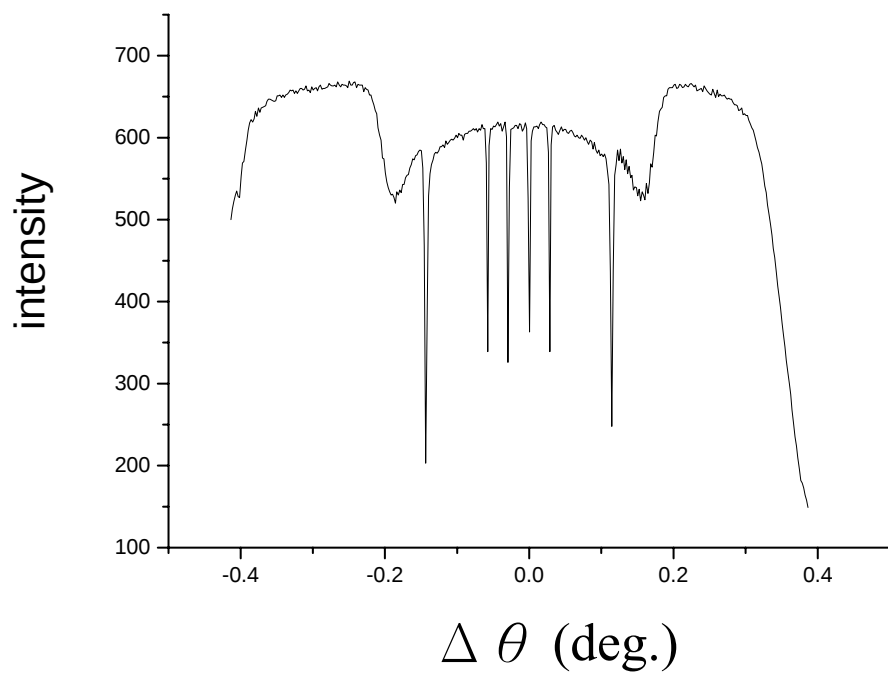
- 310 meV

The comparison of $\Delta\theta$ -scans

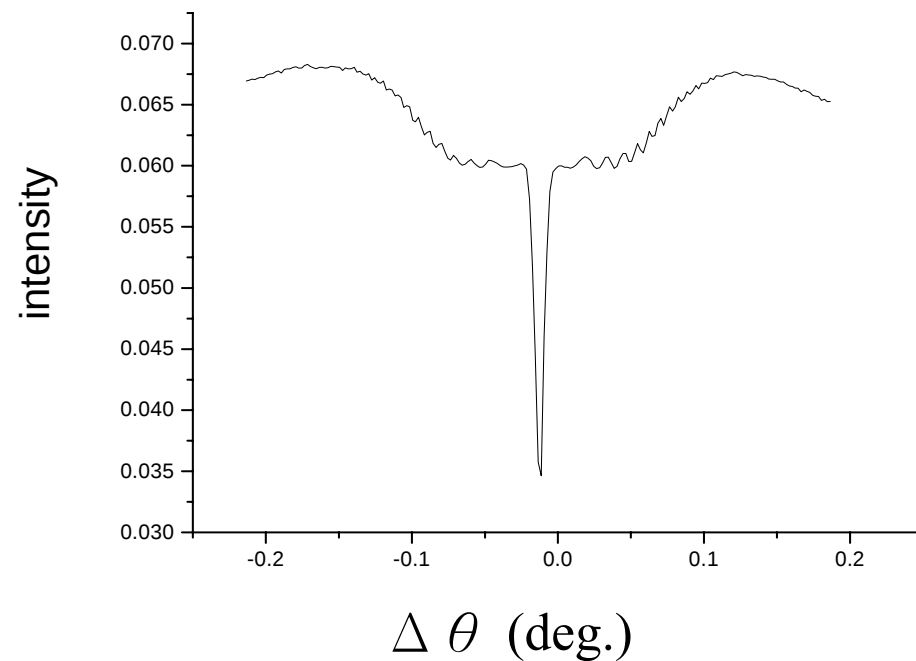




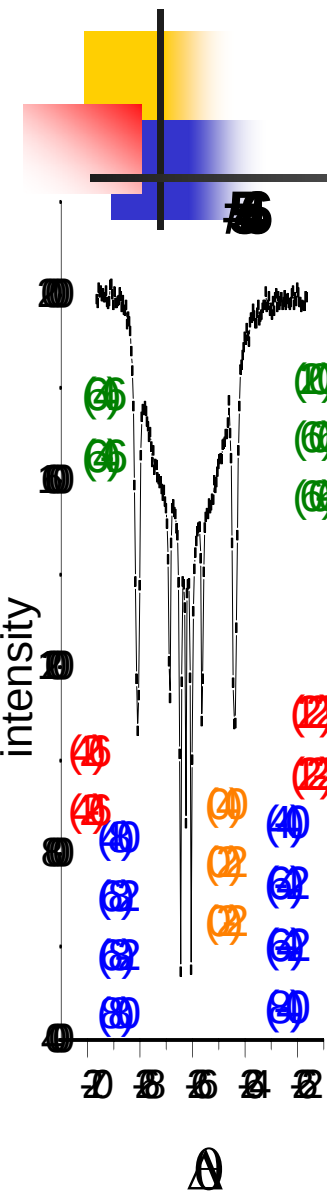
$\Delta \theta$ -scans



$E \neq E_0 = 14.4388$ keV

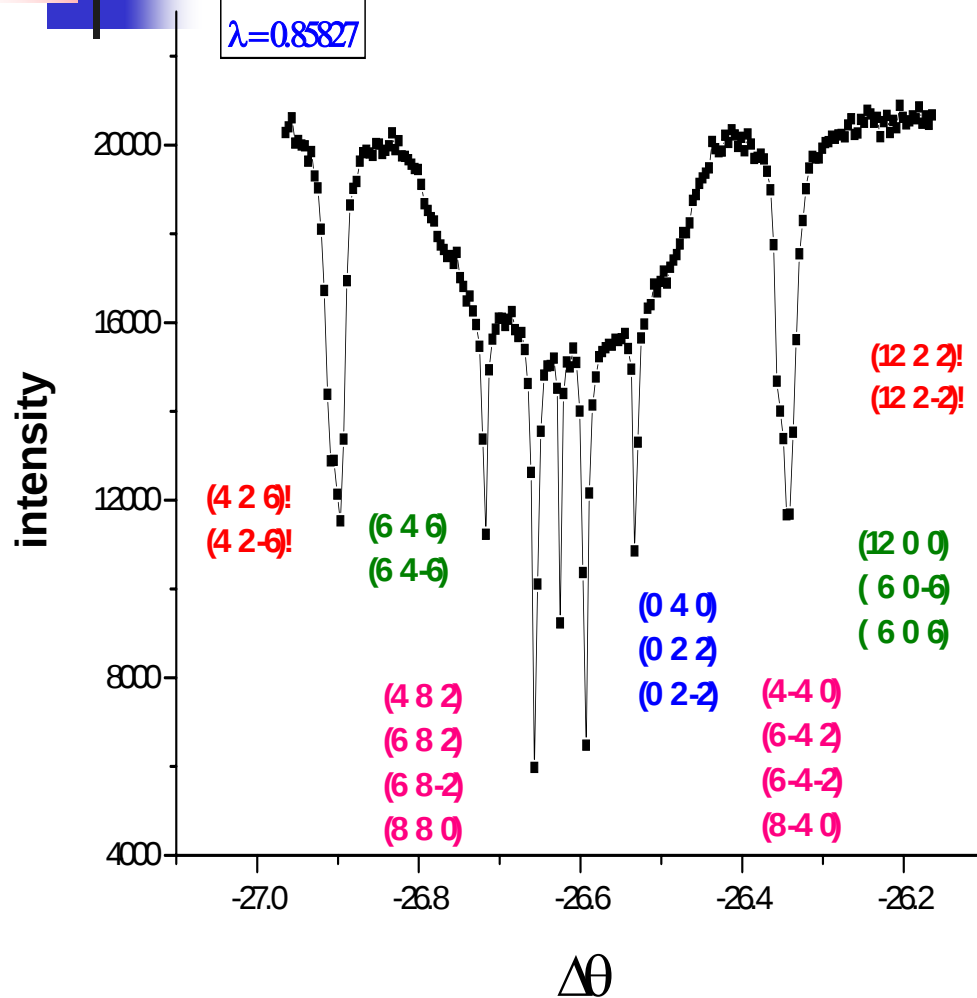


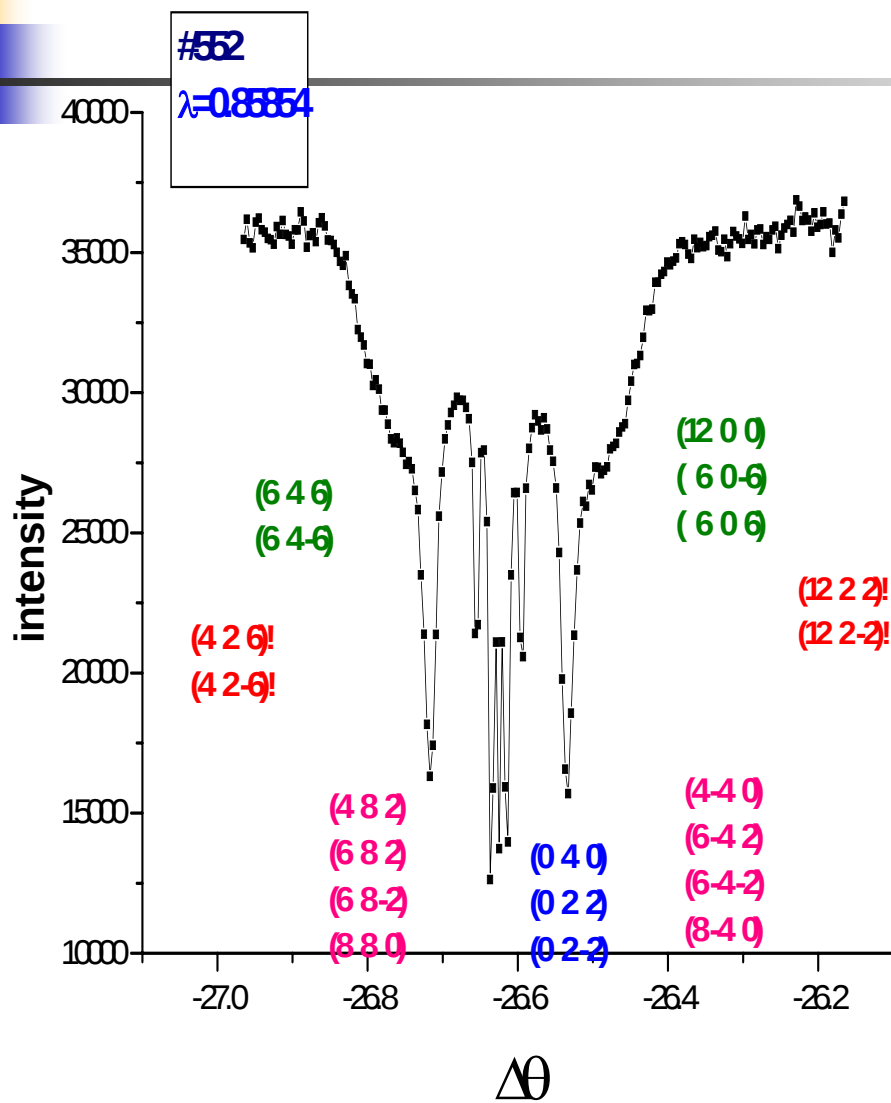
$E = E_0 = 14.4388$ keV



#549

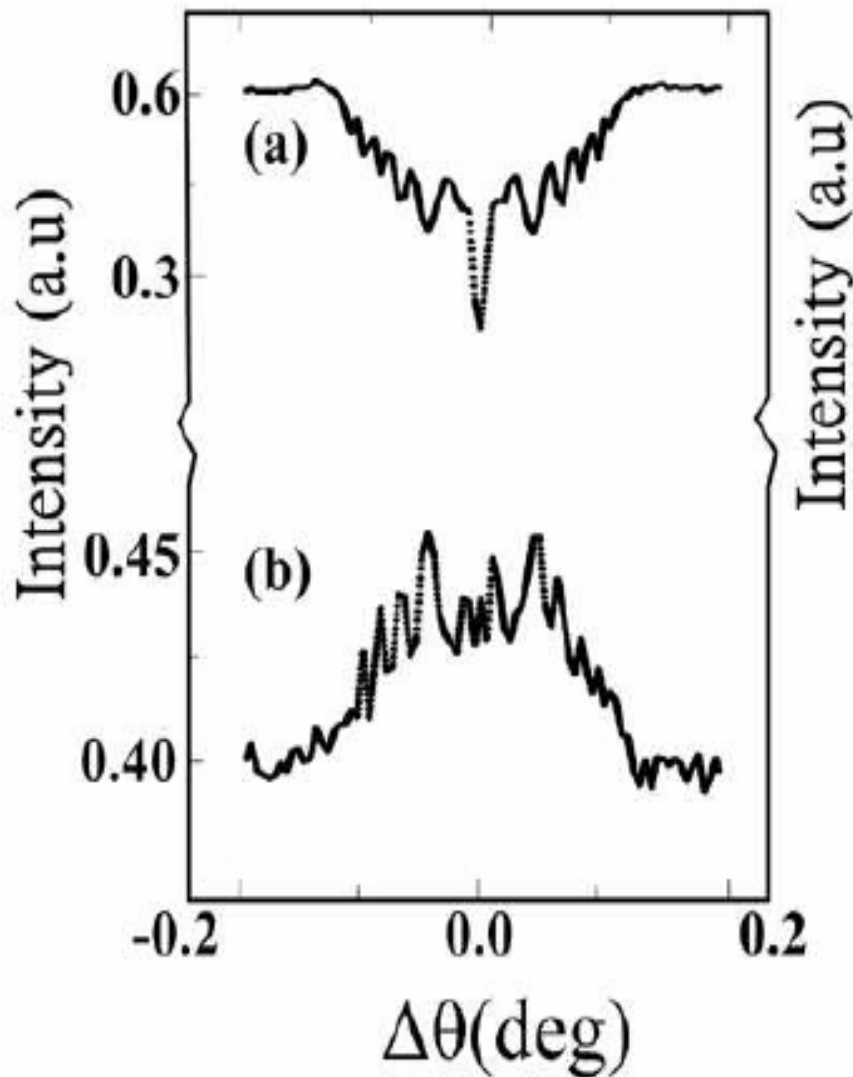
$\lambda=0.85827$





$\Delta \theta$ - scans at $\Delta E = 9 \text{ meV}$

The $\Delta \theta$ -scan at 0.002 deg./step

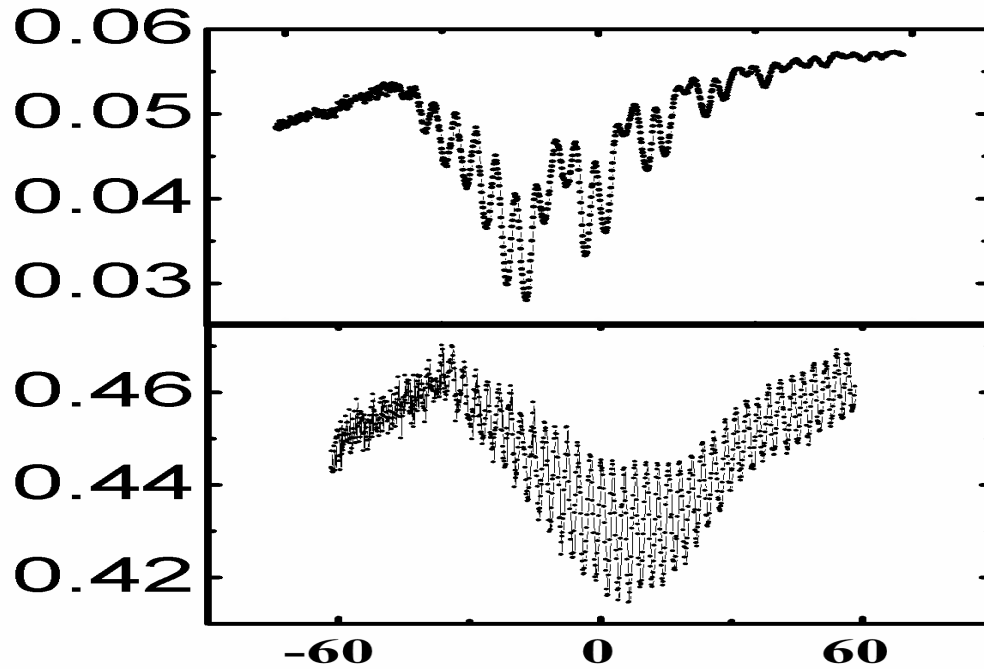


(a) Forward-transmitted
(0 0 0) beam

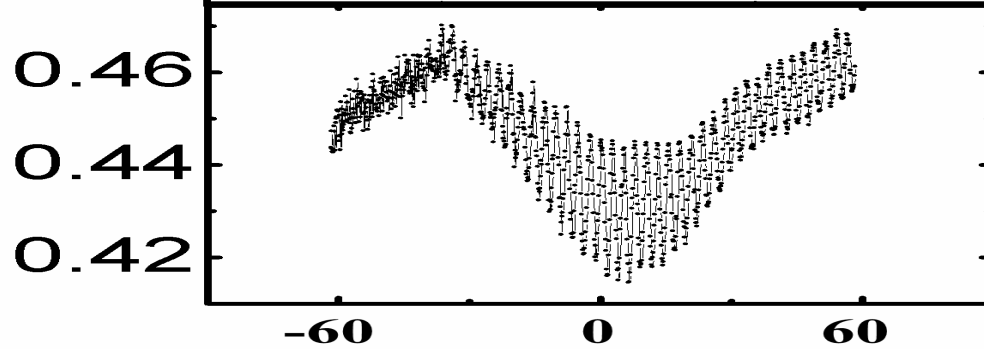
(b) Back-reflected
(12 4 0) beam

Energy scans

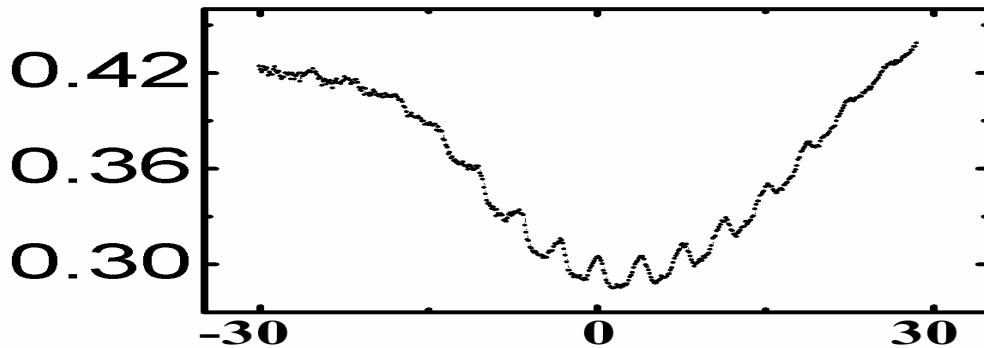
Intensity(a.u)



Double_thinner
plate (70/100)



Double_thicker
Plate (100/150)



8-plate
(25/150)

ΔE (meV)

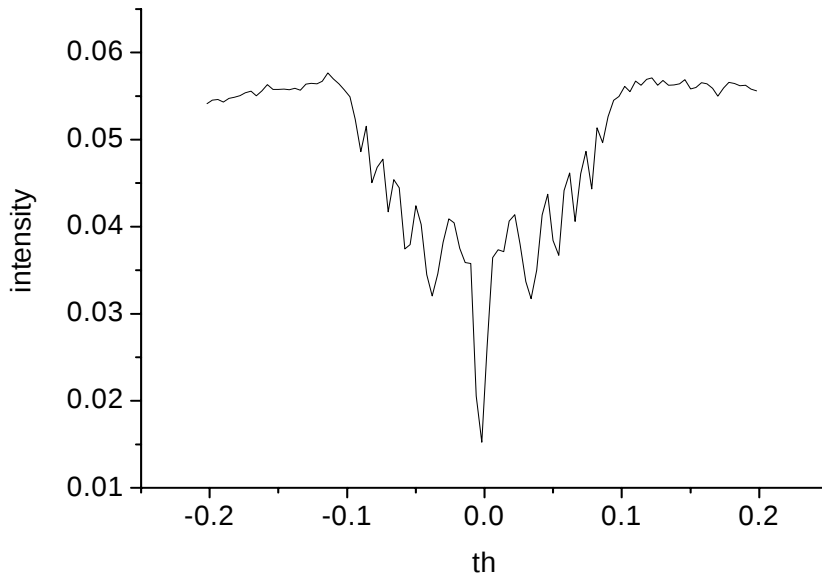
The energy ΔE scan (1 step=58.548 μ eV)

The spectral width Γ =1.60 meV of fringes.

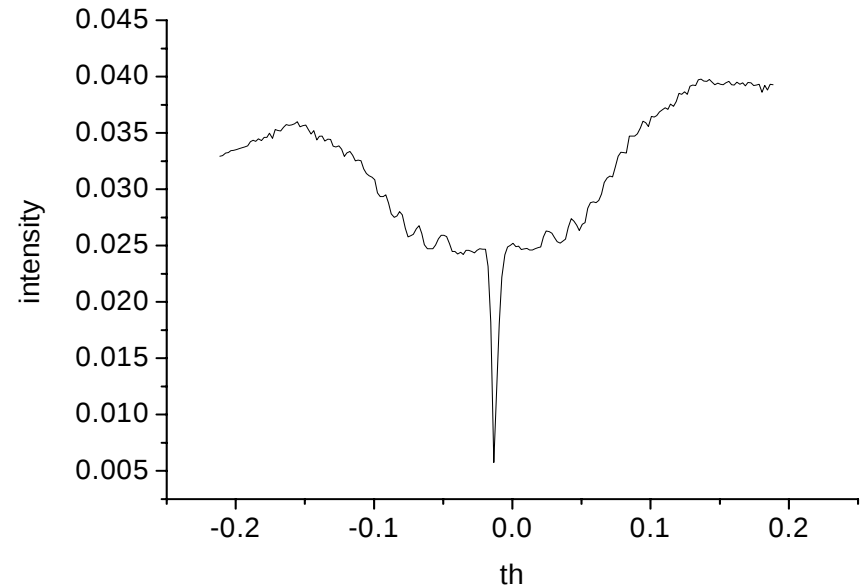
Finesse, $F=E_d/\Gamma$ = 2.3
(designed value $F= 4.0$ with
 $R= 50\%$ $T=50\%$)

Absorption

The $\Delta \theta$ -scans show obvious oscillations, even not at the exact energy.

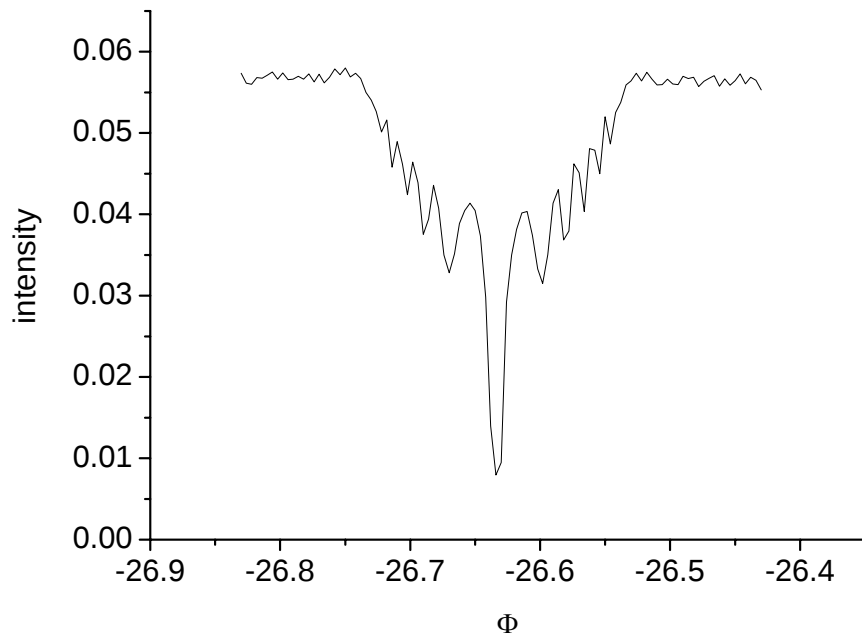


Double_thinner plate

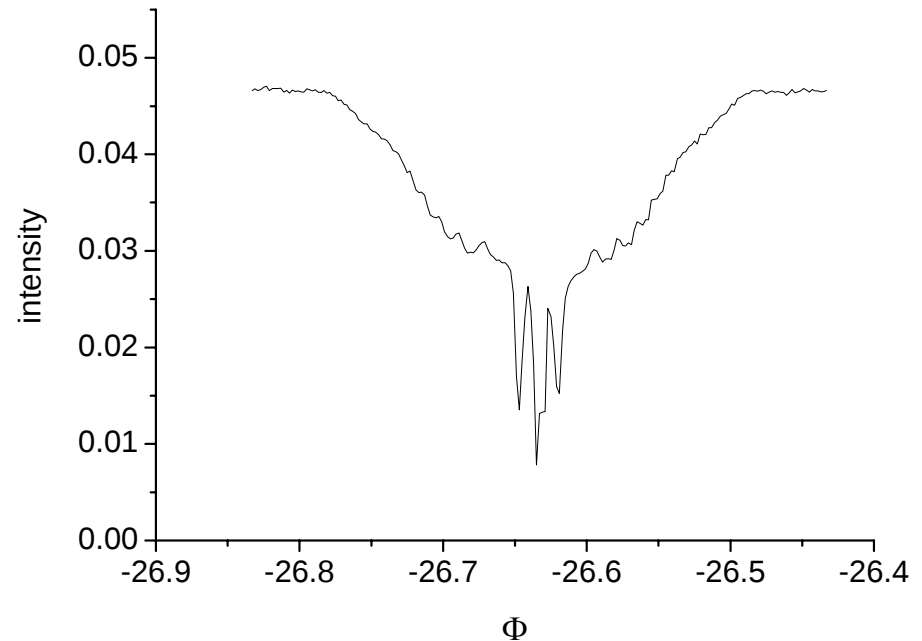


8-plate

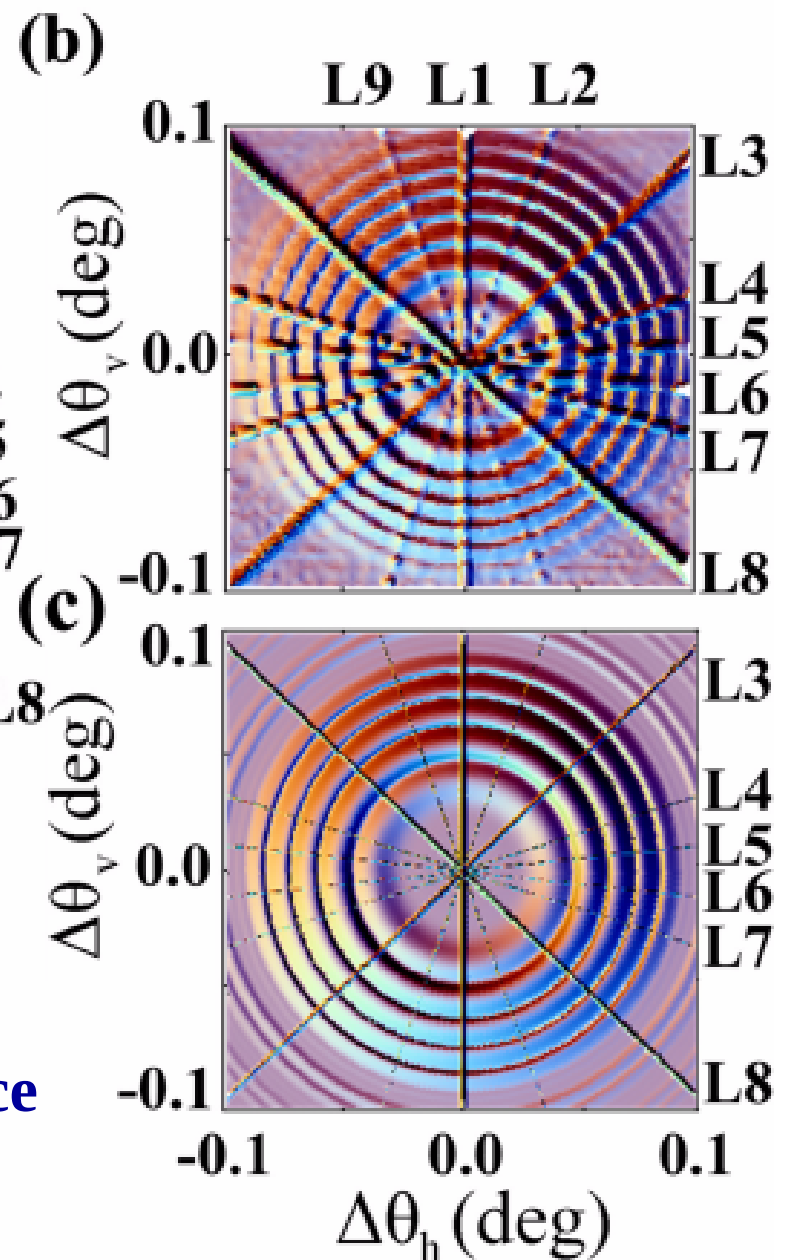
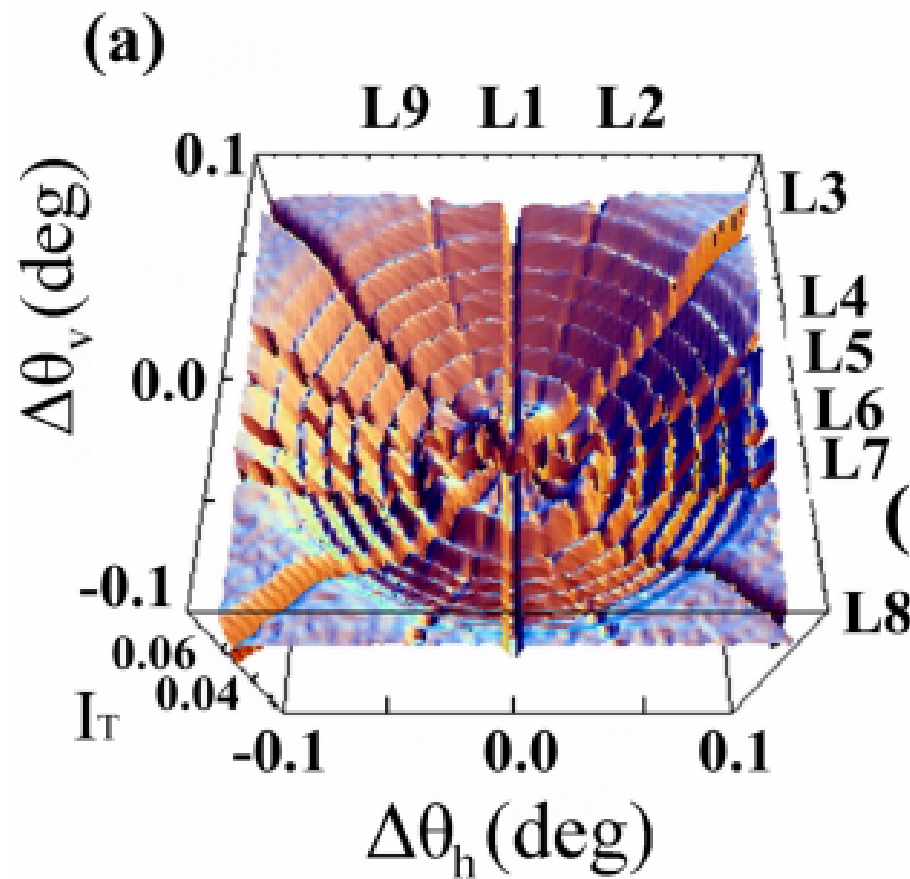
The $\Delta \phi$ -scans show obvious oscillations,
even not at the exact energy.



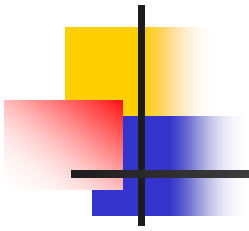
Double_thinner plate



8-plate



Intensity distribution of resonance interference at $\Delta E = 12\text{meV}$



Shvyd'ko et al (PRL 2003):

$\Delta E (=2 \text{ meV}) > E_d (=12.4 \text{ ueV})$ Criterion (a) is not satisfied.

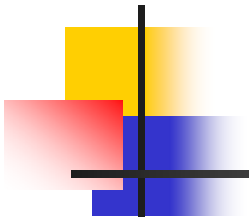
$\Delta E (=2 \text{ meV}) > \Gamma (=0.64 \text{ ueV})$ Criterion (b) is not satisfied.

$\Gamma (=0.64 \text{ ueV}) < E_d (=12.4 \text{ ueV})$ Criterion (c) is satisfied.

$\Delta t (=0.33 \text{ ps}) < t_f/2 \pi (=53 \text{ ps})$ Criterion (d) is not satisfied.

$l_L (=310 \text{ um}) < 2d (=100000 \text{ um})$ Criterion (e) is not satisfied.

Pendellosung fringes due to diffraction from thin crystals (60 um).



K.-D. Liss et al. (Nature 2001)

$\Delta E (=3.7 \text{ meV}) > E_d (=4.12 \text{ ueV})$ Criterion (a) is not satisfied.

$\Delta E (=3.7 \text{ meV}) ? \Gamma$ (no information about Γ , but should be smaller than $E_d = 4.12 \text{ ueV}$ for observable fringes). Criterion (b) is not likely to be satisfied.

$\Gamma ? E_d$ (No information about Γ).

$t (=0.18 \text{ ps}) < t_f / 2 (=159 \text{ ps})$ Criterion (d) is not satisfied.

$l_L (=170 \text{ um}) < 2d (=300000 \text{ um})$ Criterion (e) is not satisfied.

Conclusion

- (1) Resonance of X-rays always takes place in a normal incident X-ray diffraction from two parallel crystal plates in a monolithic crystal. Although the resonance fringes are always there, it is, however, very difficult to be observed.

For a normal incidence X-ray cavity, the required conditions for observing fringes:

Spatial coherence: photon emittances (1 deg.)

Temporal coherence: $\Delta t > t_f / 2\pi$

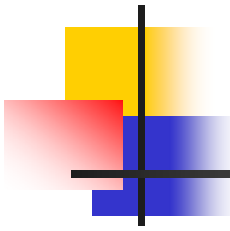
$$\ell_L \geq 2d$$

Conclusion

(2) The current experiments extend the spectral range of Fabry-Perot resonators (interferometers) from the visible spectra to hard X-ray and near-gamma ray regime

Conclusion (Applications):

1. Since the fixed phase relation between the forward transmitted and the back-reflected beams and the narrow energy and angular widths of X-rays from the cavity, this crystal cavity can be used for [phase-contrast and high-resolution X-ray optics](#), such as [high-resolution monochromator](#) using the back reflection and [narrow-band filter](#) with the transmission.
2. Application for [high-resolution X-ray scattering, spectroscopy, and phase-contrast microscopy](#) in many physical, chemical, and biological studies, such as investigation of [dynamics of solids, liquids, and bio-molecules](#), [precise measurements of wavelength and lattice constant](#), etc.
3. Crystal cavities of the present type with better finesse might be useful for the development toward [hard X-ray \(or gamma-ray\) lasers](#), if suitable lasing materials could be developed.
4. [Seeding for Free electron lasers](#)



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Thank you for your attention !!