

CP violation in charged Higgs production and decays in the Complex 2HDM

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Based on: A.A, H. Eberl, E. Ginina, K. Christova , JHEP'11

Plan

Complex 2HDM: Motivations

parametrization of C2HDM and constraints

CP violation in charged Higgs production $bg \rightarrow tH^-$ and
decays $H^\pm \rightarrow tb, W^\pm h_{1,2}$

CP violation in neutral Higgs decays $h_1 \rightarrow \tau^+ \tau^-$, ...

Conclusions

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Those large CP violating phases can give contributions to the EDM which exceed the experimental upper bound.

With 2HDM $\Phi_{1,2}$, CP can be violated either **explicitly** or **spontaneously** in the Higgs sector

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EW phase transition with 4th generation requires 2 $SU(2)$ doublet Higgs fields

[Y.Kikukawa, M. Kohda, J.Yasuda, Prog.Theor.Phys'09]

Parameterization of C2HDM and constraint

$$\begin{aligned} V = & m_{11}^2 (\Phi_1^+ \Phi_1) + m_{22}^2 (\Phi_2^+ \Phi_2) + \lambda_1 (\Phi_1^+ \Phi_1)^2 + \\ & \lambda_2 (\Phi_1^+ \Phi_1)^2 + \lambda_3 (\Phi_1^+ \Phi_1)(\Phi_2^+ \Phi_2) + \lambda_4 |\Phi_1^+ \Phi_2|^2 \\ & + \{m_{12}^2 (\Phi_1^+ \Phi_2) + h.c\} + [\lambda_5 (\Phi_1^+ \Phi_2)^2 + h.c] \end{aligned}$$

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- One can have: **ExplicitCP** if $\Im(m_{12}^4 \lambda_5^*) \neq 0$
- For $\Im(m_{12}^4 \lambda_5^*) = 0$: we can have **SpontaneousCP** if:
 $|\frac{m_{12}^2}{\lambda_5 v_1 v_2}| < 1$; $\langle \Phi_1 \rangle = v_1$, $\langle \Phi_2 \rangle = v_2 e^{i\theta}$, the minimum occurs for:

$$\cos \theta = \frac{m_{12}^2}{\lambda_5 v_1 v_2} ; \lambda_5 \neq 0$$

Stability condition $\frac{\partial^2 V}{\partial \theta^2} > 0 \Rightarrow \lambda_5 > 0$,

parameterization of C2HDM

$$\Phi_1 = \begin{pmatrix} \varphi_1^+ \\ (v_1 + \eta_1 + i\chi_1)/\sqrt{2} \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \varphi_2^+ \\ (v_2 + \eta_2 + i\chi_2)/\sqrt{2} \end{pmatrix}.$$

The physical Higgs eigenstates are obtained as follows.

The charged Higgs H^\pm and the charged Goldstone fields G^\pm are a mixture of $\varphi_{1,2}^\pm$:

$$\begin{aligned} H^\pm &= -\sin \beta \varphi_1^\pm + \cos \beta \varphi_2^\pm, \\ G^\pm &= \cos \beta \varphi_1^\pm + \sin \beta \varphi_2^\pm, \end{aligned}$$

$$\tan \beta = v_2/v_1.$$

The neutral physical Higgs states are obtained:

- One rotates the imaginary parts of: (χ_1, χ_2) into (G^0, η_3) :

$$\begin{aligned} G^0 &= \cos \beta \chi_1 + \sin \beta \chi_2, \\ \eta_3 &= -\sin \beta \chi_1 + \cos \beta \chi_2, \end{aligned}$$

G^0 is the Goldstone boson. The CP-odd η_3 mixes with the neutral CP-even components $\eta_{1,2}$.

- $\mathcal{M}_{ij}^2 = \partial^2 V_{\text{Higgs}} / (\partial \eta_i \partial \eta_j)$, $i, j = 1, 2, 3$
 $\mathcal{R} \mathcal{M}^2 \mathcal{R}^T = \text{diag}(M_{H_1^0}^2, M_{H_2^0}^2, M_{H_3^0}^2)$, $M_{H_1^0} \leq M_{H_2^0} \leq M_{H_3^0}$
with $(H_1^0, H_2^0, H_3^0)^T = \mathcal{R} (\eta_1, \eta_2, \eta_3)^T$
The mass eigenstates H_i^0 have a mixed CP structure.

\mathcal{R} is parametrized by three rotation angles α_i , $i = 1, 2, 3$:

$$\begin{aligned} \mathcal{R} &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_3 & s_3 \\ 0 & -s_3 & c_3 \end{pmatrix} \begin{pmatrix} c_2 & 0 & s_2 \\ 0 & 1 & 0 \\ -s_2 & 0 & c_2 \end{pmatrix} \begin{pmatrix} c_1 & s_1 & 0 \\ -s_1 & c_1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \\ &= \begin{pmatrix} c_1 c_2 & s_1 c_2 & s_2 \\ -(c_1 s_2 s_3 + s_1 c_3) & c_1 c_3 - s_1 s_2 s_3 & c_2 s_3 \\ -c_1 s_2 c_3 + s_1 s_3 & -(c_1 s_3 + s_1 s_2 c_3) & c_2 c_3 \end{pmatrix}, \end{aligned}$$

with $s_i = \sin \alpha_i$ and $c_i = \cos \alpha_i$,

$$-\frac{\pi}{2} < \alpha_1 \leq \frac{\pi}{2}; \quad -\frac{\pi}{2} < \alpha_2 \leq \frac{\pi}{2}; \quad 0 \leq \alpha_3 \leq \frac{\pi}{2}.$$

Scalar potentiel parameters

The potential has **12 real parameters**: 2 real masses:
 $m_{11,22}^2$, 2 VEVs, 4 reals: $\lambda_{1,2,3,4}$, 2 complex: λ_5, m_{12}^2 .

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remains: 8 real independent parameters:

$\lambda_{1,2,3,4}, \text{ Re}(\lambda_5), \text{ Re}(m_{12}^2), \tan\beta, \text{ Im}(m_{12}^2).$

or

$M_{H_1^0}, M_{H_2^0}, M_{H^+}, \alpha_1, \alpha_2, \alpha_3, \tan\beta, \text{ Re}(m_{12}).$

$$M_{H_3^0}^2 = \frac{M_{H_1^0}^2 R_{13}(R_{12} \tan\beta - R_{11}) + M_{H_2^0}^2 R_{23}(R_{22} \tan\beta - R_{21})}{R_{33}(R_{31} - R_{32} \tan\beta)},$$

Higgs couplings to gauge bosons

The interactions relevant to our study are:

$$\mathcal{C}(H_i^0 WW) = \cos \beta R_{i1} + \sin \beta R_{i2},$$

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One can derive the **following sum rules**:

$$\mathcal{C}(H_i^0 WW)^2 + |\mathcal{C}(H_i^0 W^+ H^-)|^2 = 1 \quad \text{for each } i = 1, 2, 3$$

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For a fixed i , if $|\mathcal{C}(H_i^0 W^+ H^-)|^2$ is suppressed, then

$(\sin \beta R_{i1} - \cos \beta R_{i2})^2 \approx 0$ and $R_{i3}^2 \approx 0$

$\Rightarrow H_i^0$ is dominantly a CP-even state.

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For a fixed i , if $|\mathcal{C}(H_i^0 W^+ H^-)|^2$ is suppressed,
the second sum rule $\Rightarrow \mathcal{C}(H_j^0 WW)^2 \approx 0$ for $j \neq i$.

Higgs couplings to fermions

if Φ_1 and Φ_2 couple to all fermions

$$\mathcal{L}_{Yukawa}^{2HDM} = -h_{ij}^{d,1}(\overline{\Psi_q^L})_i \Phi_1 d_j^R - h_{ij}^{u,1}(\overline{\Psi_q^L})_i \tilde{\Phi}_1 u_j^R + (\Phi_1 \longleftrightarrow \Phi_2)$$

The mass term is: $M_{ij}^q = h_{ij}^{q,1} v_1 + h_{ij}^{q,2} v_2$

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We would have FCNC at tree level!

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Symétrie Z_2 (Théorème de Glashow-Weinberg):

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up	Φ_2	Φ_2	Φ_2	Φ_2
down	Φ_2	Φ_1	Φ_1	Φ_2
lepton	Φ_2	Φ_1	Φ_2	Φ_1

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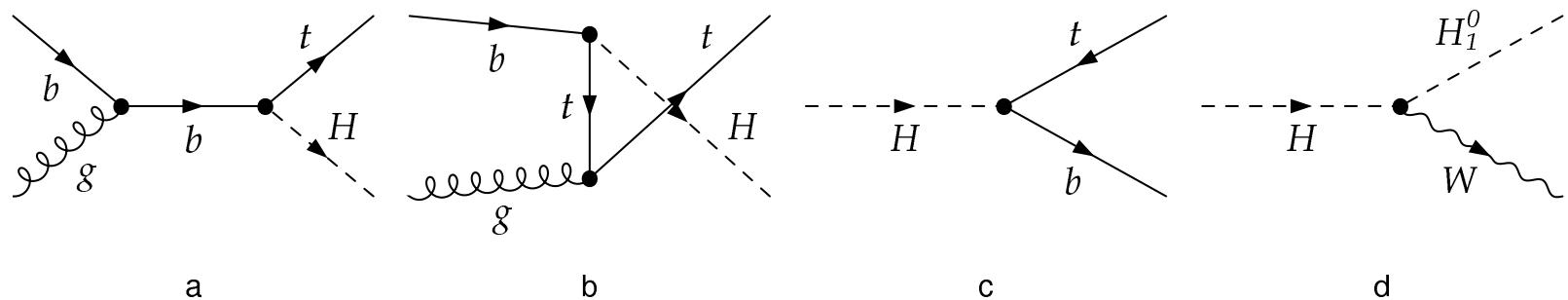
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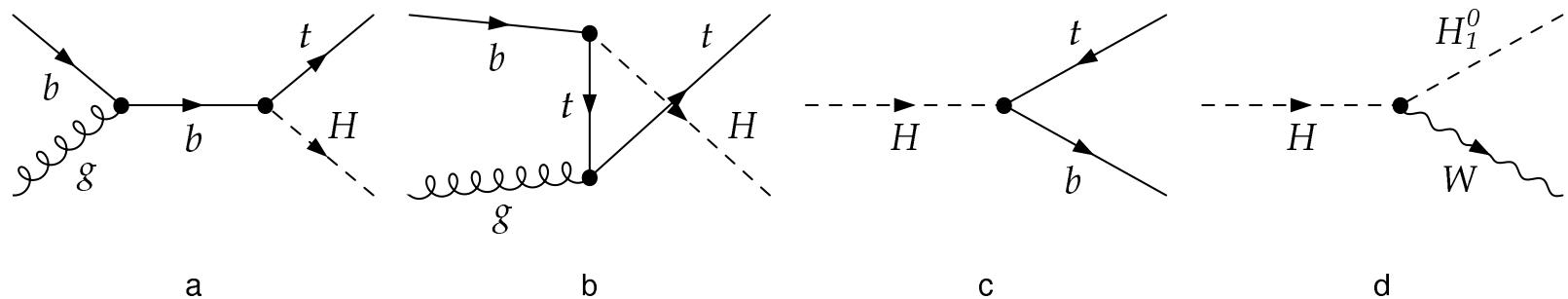
$$H_i b \bar{b} = -i \frac{g m_b}{2m_W} \left(\frac{R_{i1}}{\cos \beta} - i R_{i3} \tan \beta \gamma_5 \right)$$

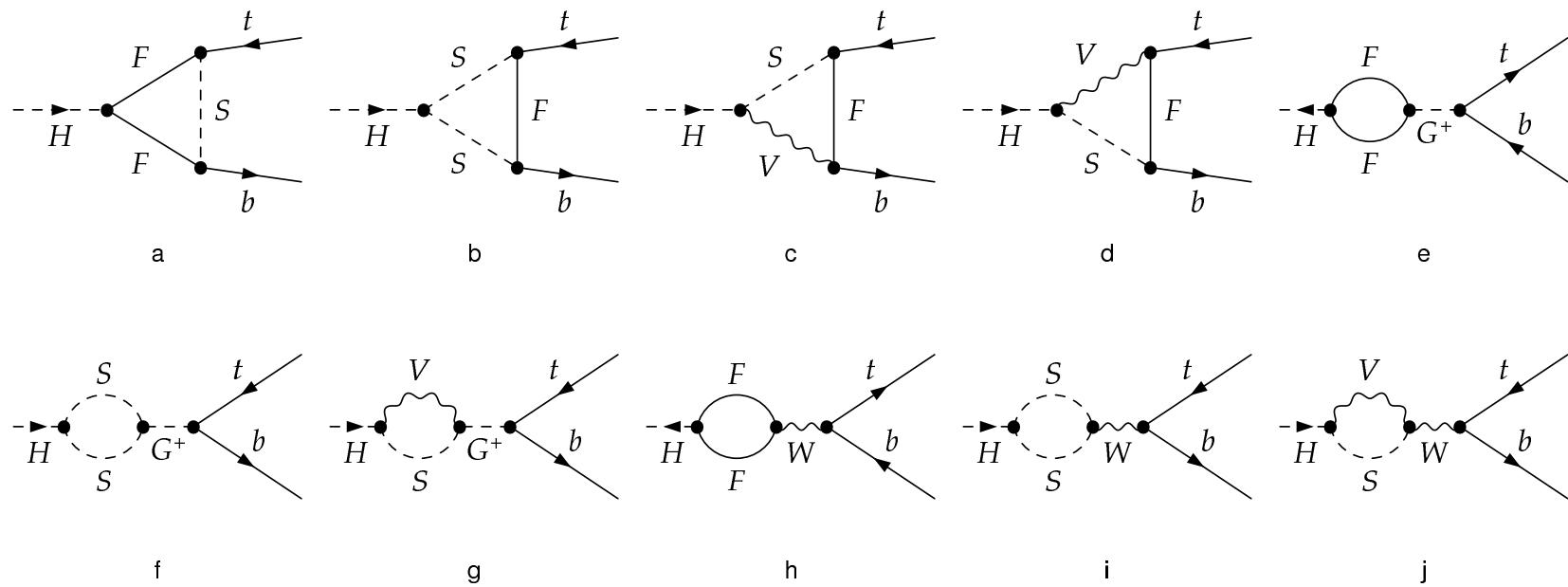
$$H_i t \bar{t} = -i \frac{g m_t}{2m_W} \left(\frac{R_{i2}}{\sin \beta} - i R_{i3} \cot \beta \gamma_5 \right)$$

Feynman Diagrams

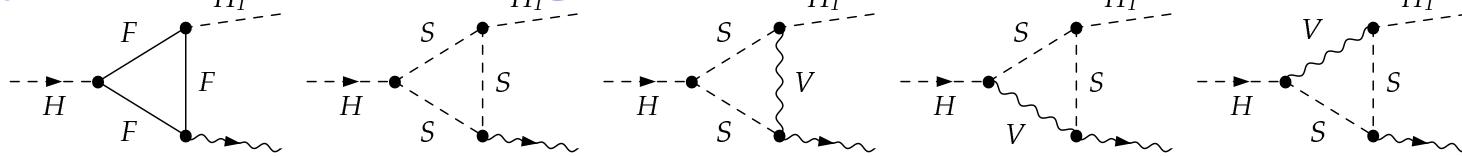


Feynman Diagrams



$$H^\pm \rightarrow tb$$


Feynman Diagrams: $H^\pm \rightarrow W^\pm H_i$



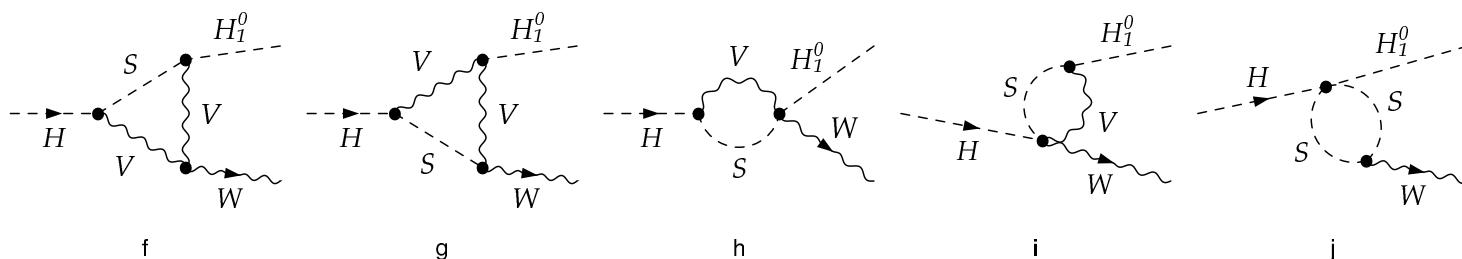
a

b

c

d

e



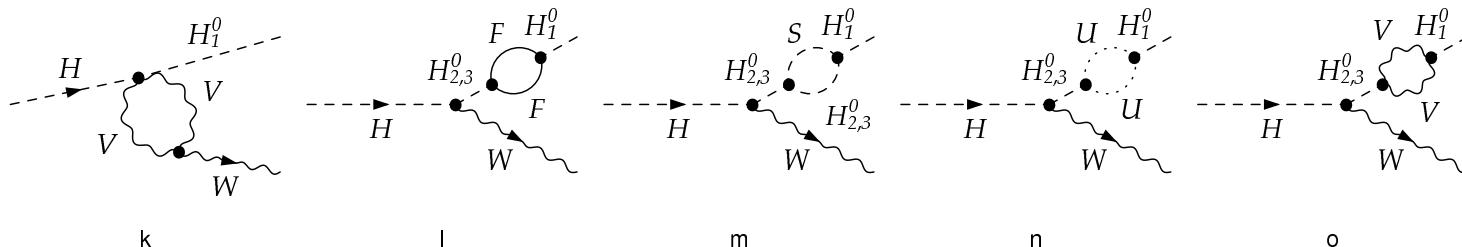
f

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h

i

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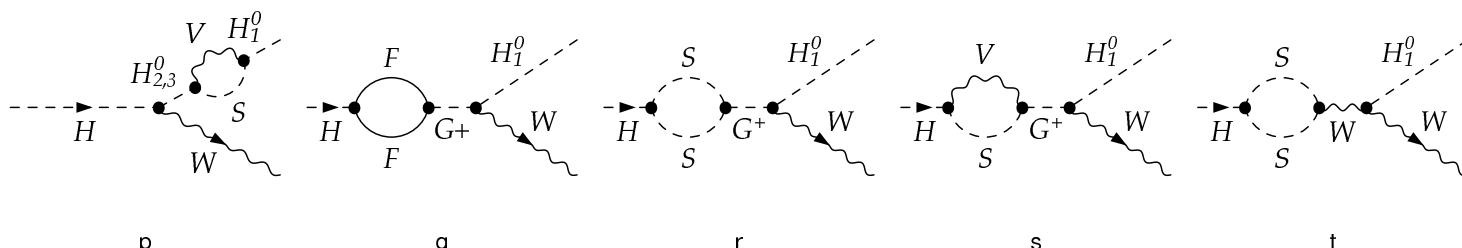
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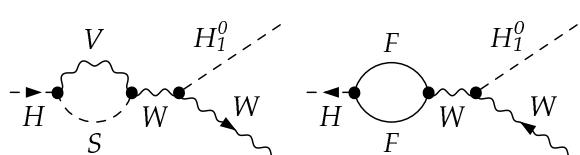
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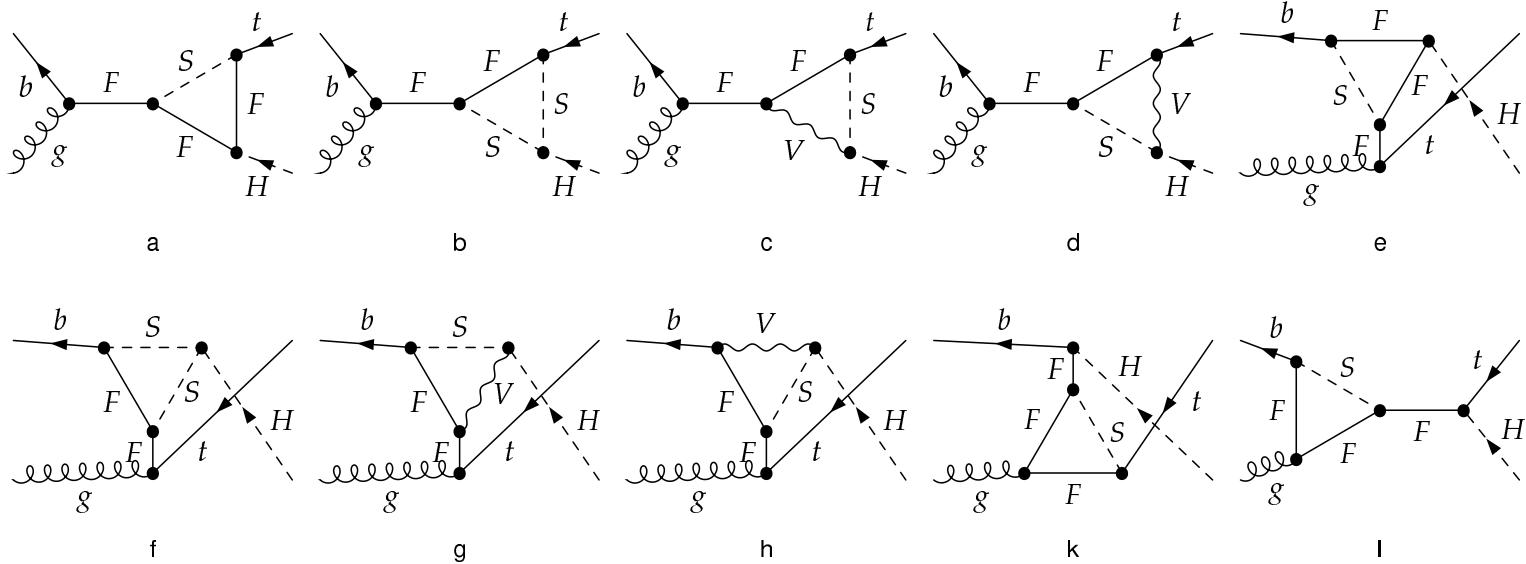
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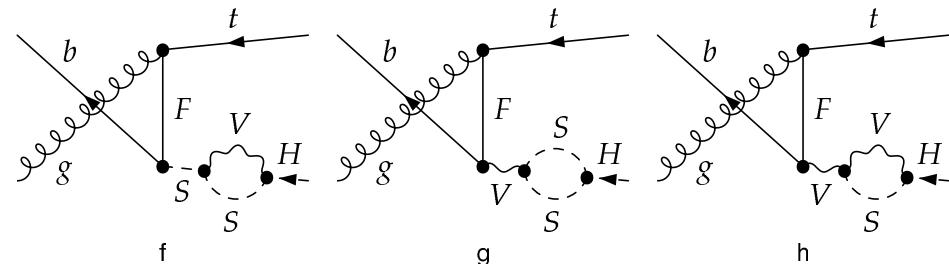
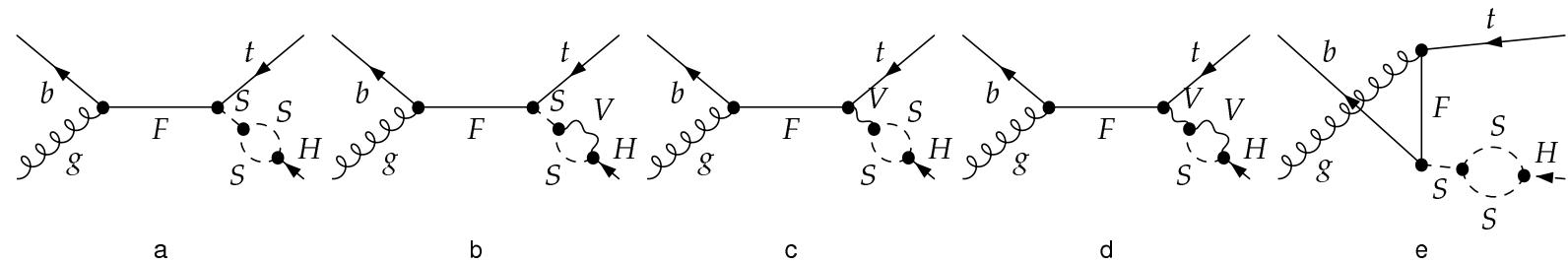
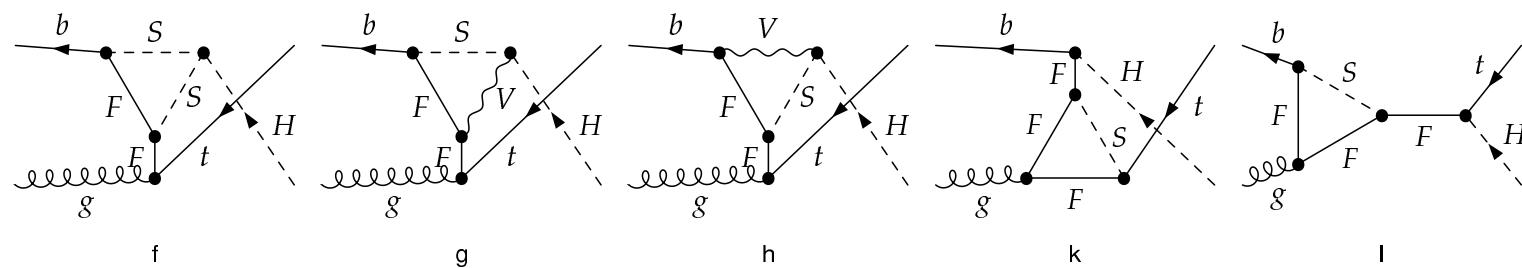
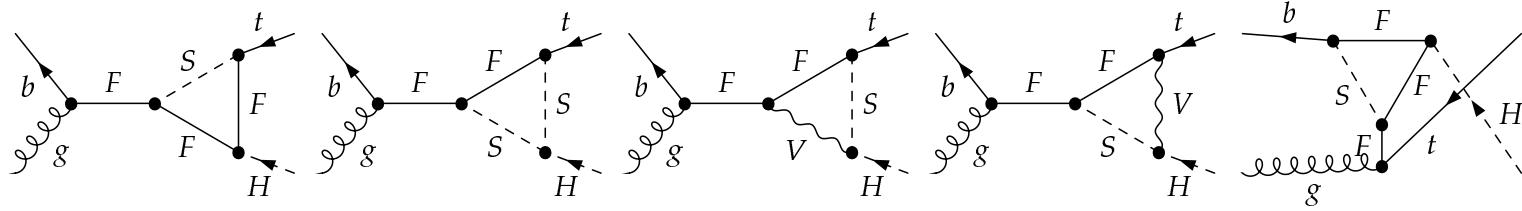
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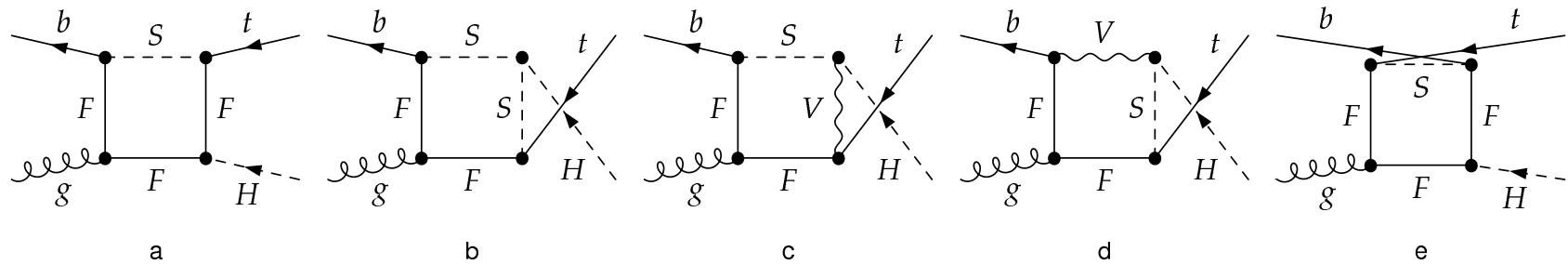
Feynman Diagrams: vetex & selfenergies



Feynman Diagrams: vetex & selfenergies



Feynman Diagrams: boxes



CP violating asymmetries

Decay rate asymmetries $A_{D,f}^{CP}$, defined by:

$$A_{D,f}^{CP} (H^\pm \rightarrow f) = \frac{\Gamma(H^+ \rightarrow f) - \Gamma(H^- \rightarrow \bar{f})}{2\Gamma^{\text{tree}}(H^+ \rightarrow f)}, \quad f = t\bar{b}; W^\pm H_i^0$$

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Asymmetries A_f^{CP} for production and subsequent decays:

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In the narrow width approximation:

$$A_f^{CP} = A_P^{CP} + A_{D,f}^{CP}$$

Constraints

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Theoretical constraints:

Potential bounded from below:

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad \lambda_3 + \sqrt{\lambda_1 \lambda_2} > 0, \quad \lambda_4 + \lambda_4 - |\lambda_5| + \sqrt{\lambda_1 \lambda_2} > 0$$

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Perturbative unitarity constraints:

$$\left| \left(\lambda_1 + \lambda_2 \pm \sqrt{(\lambda_1 - \lambda_2)^2 + 4|\lambda_5|^2} \right) \right| < 16\pi,$$

$$\left| \left(\lambda_1 + \lambda_2 \pm \sqrt{(\lambda_1 - \lambda_2)^2 + 4\lambda_4^2} \right) \right| < 16\pi,$$

$$\left| 3(\lambda_1 + \lambda_2) \pm \sqrt{9(\lambda_1 - \lambda_2^2 + 4(\lambda_3 + \lambda_4)^2)} \right| < 16\pi,$$

$$|\lambda_3 \pm \lambda_4| < 8\pi, \quad |\lambda_3 \pm |\lambda_5|| < 8\pi, \quad |\lambda_3 + 2\lambda_4 \pm |\lambda_5|| < 8\pi.$$

Only $|\lambda_5|$ is constrained not the CP phase

Numerics: $H^\pm \rightarrow tb$

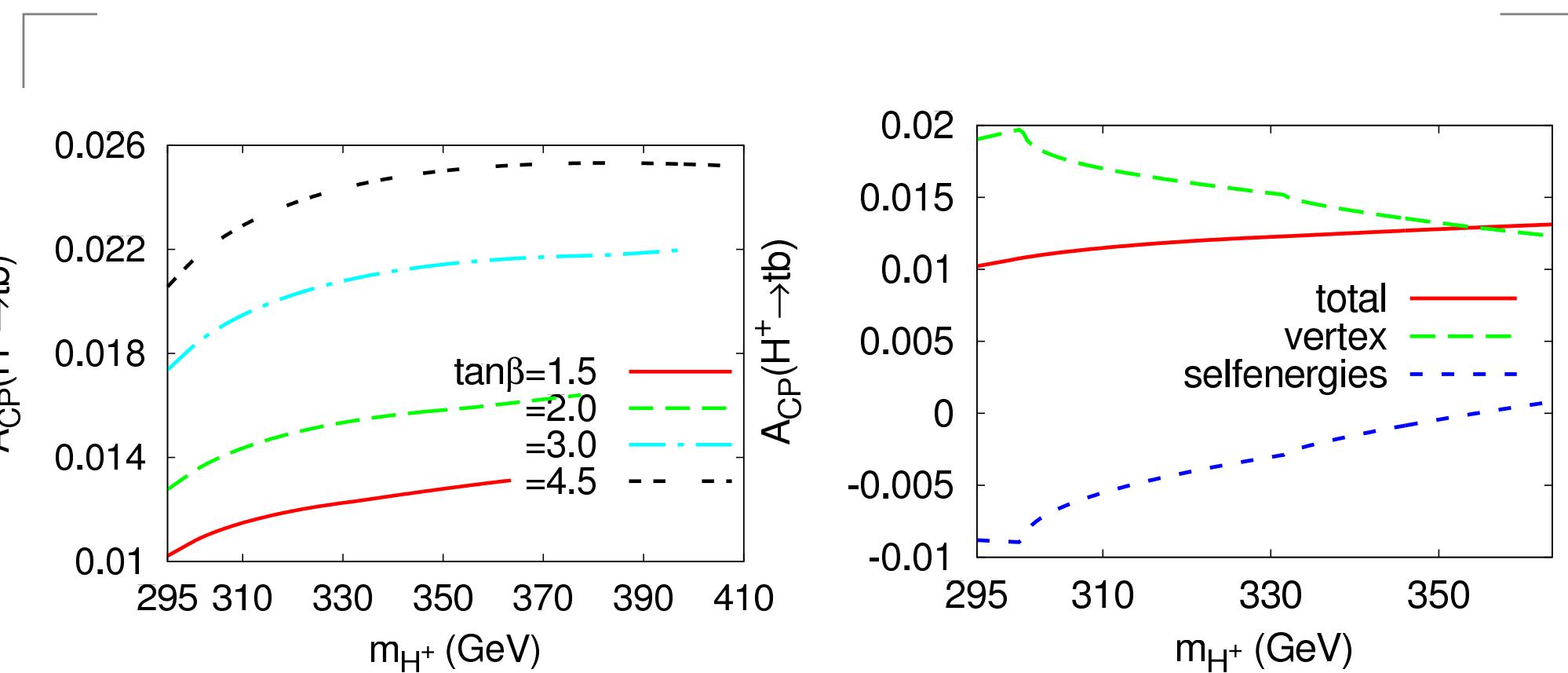


Figure 1: Left: $A_{D,tb}^{CP}$ as a function of M_{H^\pm} . $M_{H_1^0, H_2^0} = 120, 220$ GeV, $\text{Re}(m_{12}) = 170$ GeV, $\alpha_1 = 0.8$, $\alpha_2 = -0.9$ and $\alpha_3 = \pi/3$.

Right: Cancellation for $\tan\beta = 1.5$.

Numerics: $H^\pm \rightarrow W^\pm H_1$

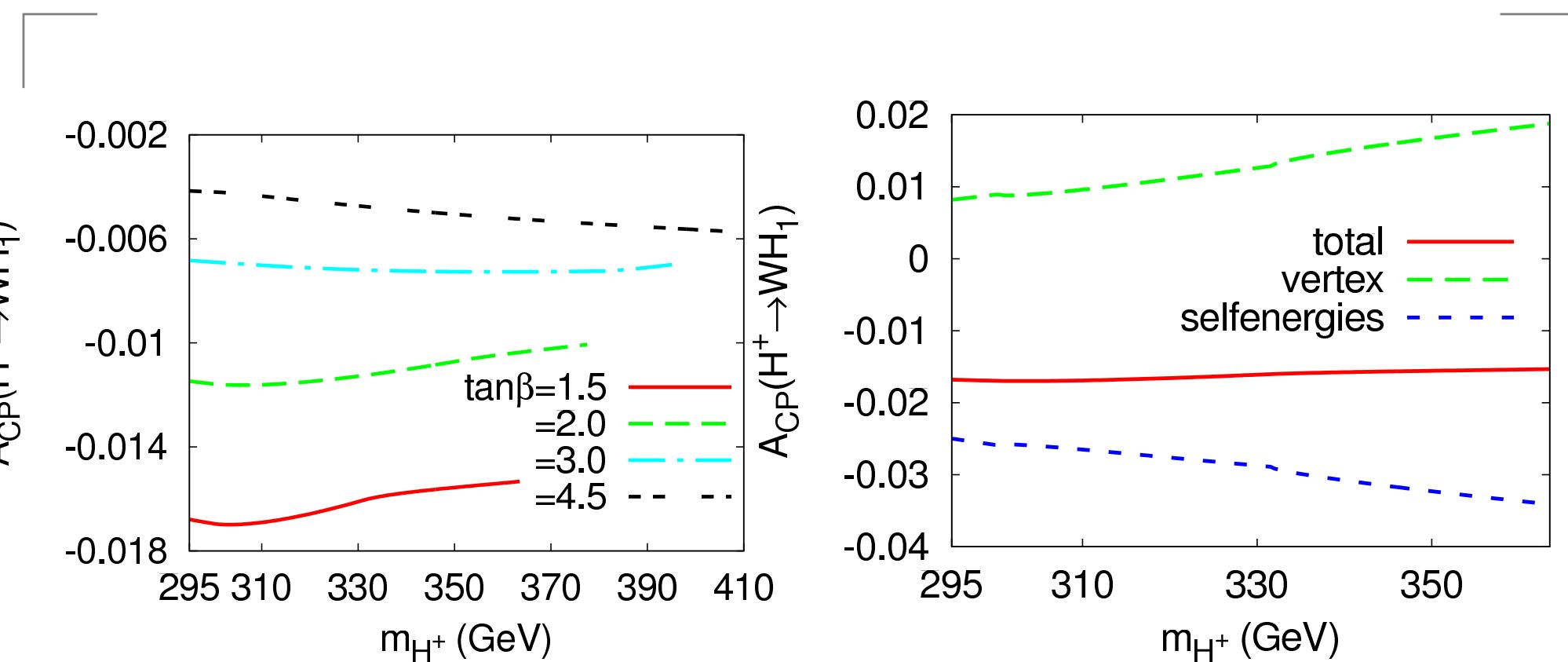


Figure 2: Left: $A_{D,WH_1^0}^{CP}$ as a function of M_{H^+} .
 Right: Cancellation in $A_{D,WH_1^0}^{CP}$ for $\tan\beta = 1.5$.

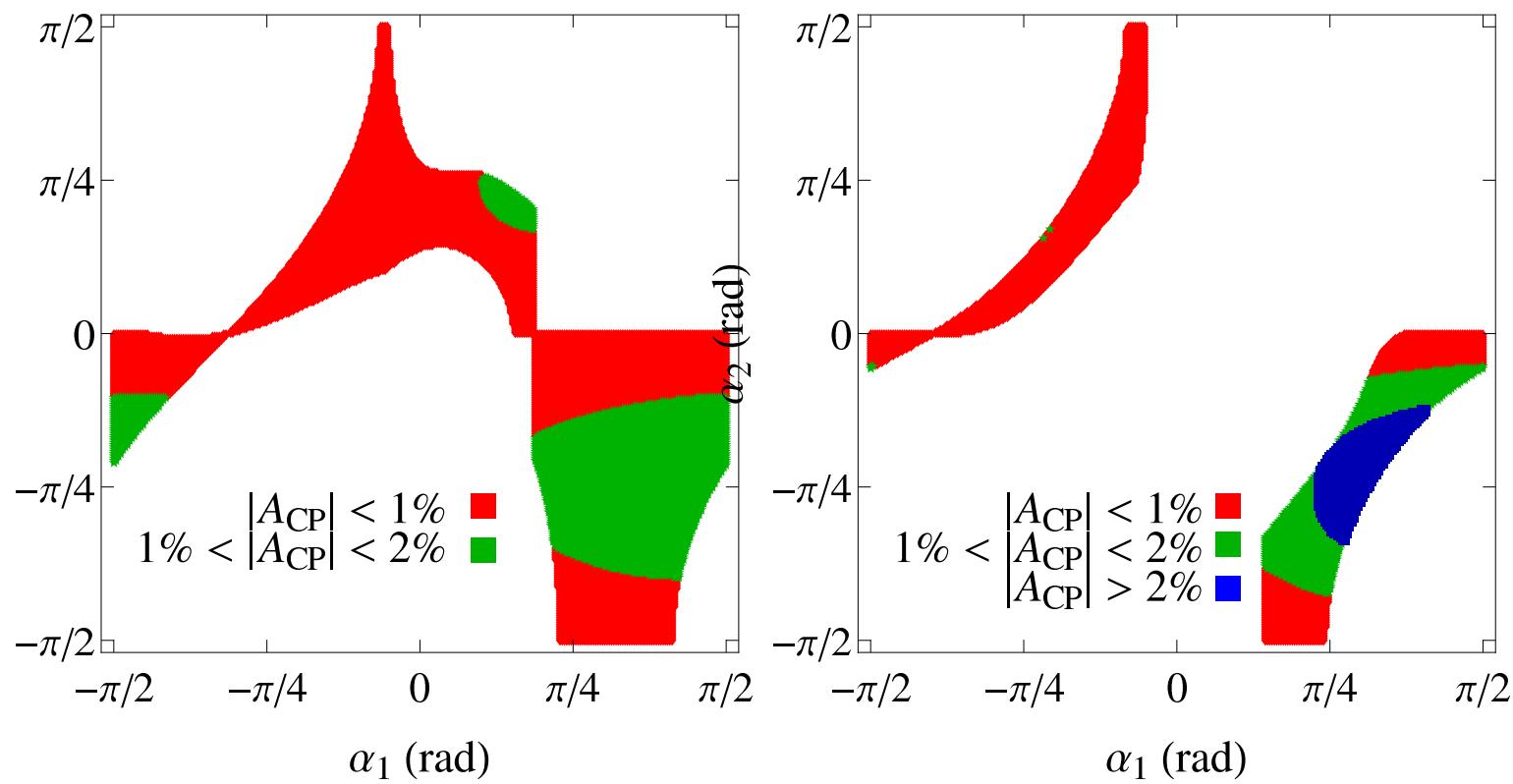


Figure 3: The allowed regions in (α_1, α_2) plan together with $|A_{D,tb}^{CP}|$. $M_{H_1^0, H_2^0, H^\pm} = 120, 220, 350$ GeV, $\text{Re}(m_{12}) = 170$ GeV, and $\alpha_3 = \pi/3$. On the top left plot $\tan \beta = 1.5$ and $\tan \beta = 3$

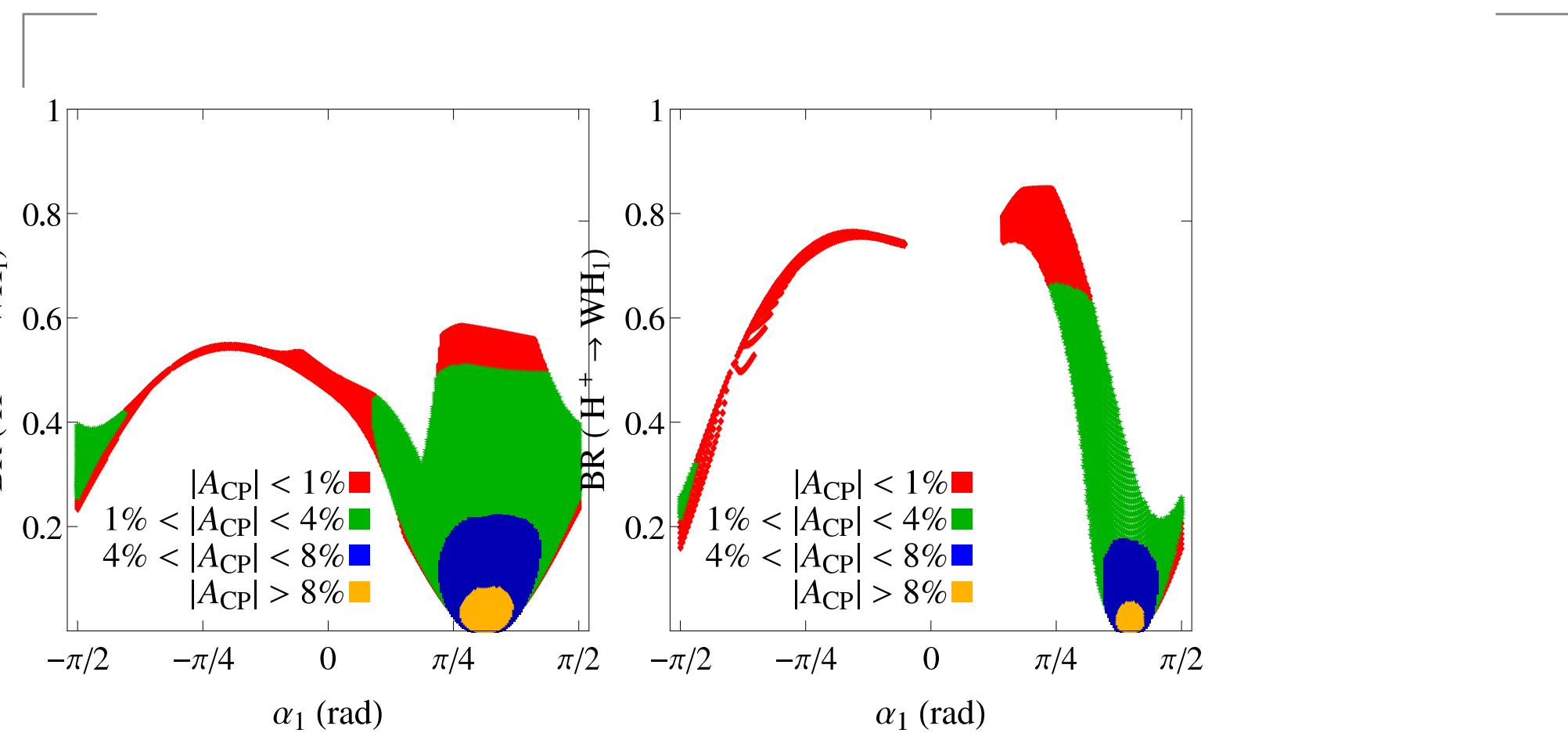


Figure 4: The $\text{BR}(H^+ \rightarrow W^+ H_1^0)$ as a function of α_1 with α_2 in the allowed parameter range, $\tan \beta = 1.5$ (left), $\tan \beta = 3$ (right)

Production: $pp \rightarrow tH^+$

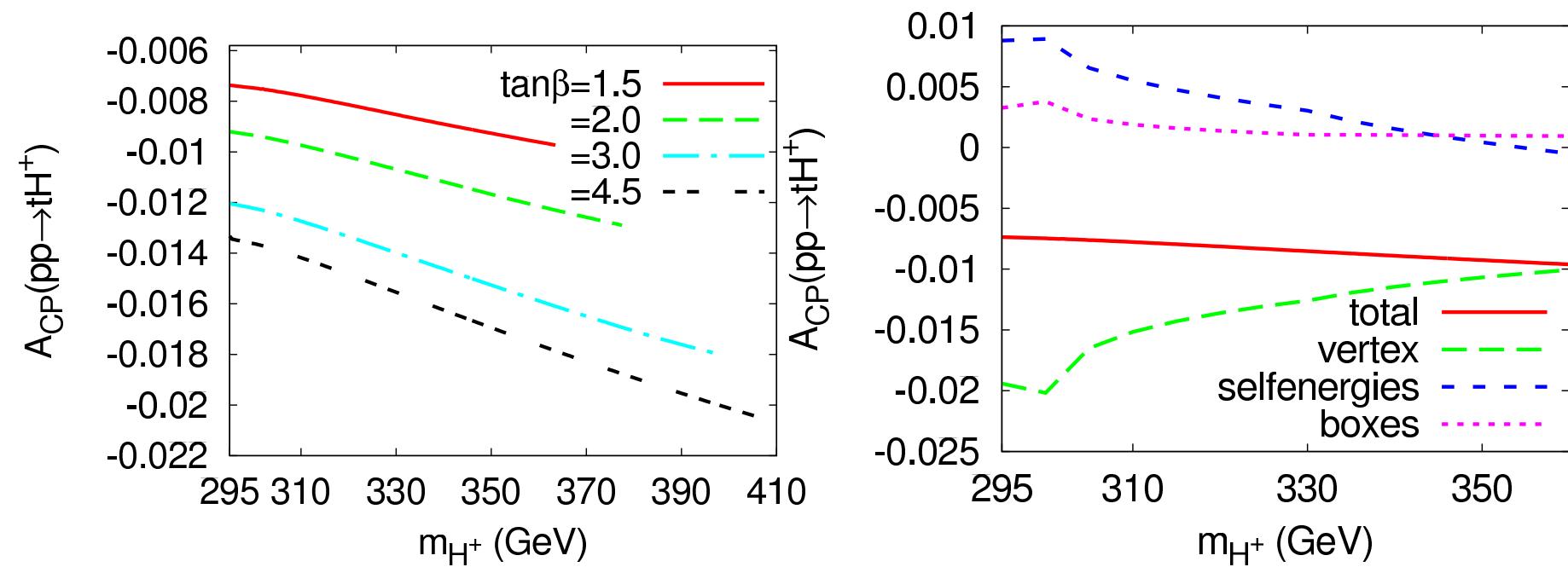


Figure 5: A_P^{CP} as a function of m_{H^\pm} with $M_{H_1^0, H_2^0} = 120, 220$ GeV, $\text{Re}(m_{12}) = 170$ GeV, $\alpha_1 = 0.8$, $\alpha_2 = -0.9$ and $\alpha_3 = \pi/3$; Right: cancellation in A_P^{CP} as a function of M_{H^+} for $\tan\beta = 1.5$

Production: $pp \rightarrow tH^+$

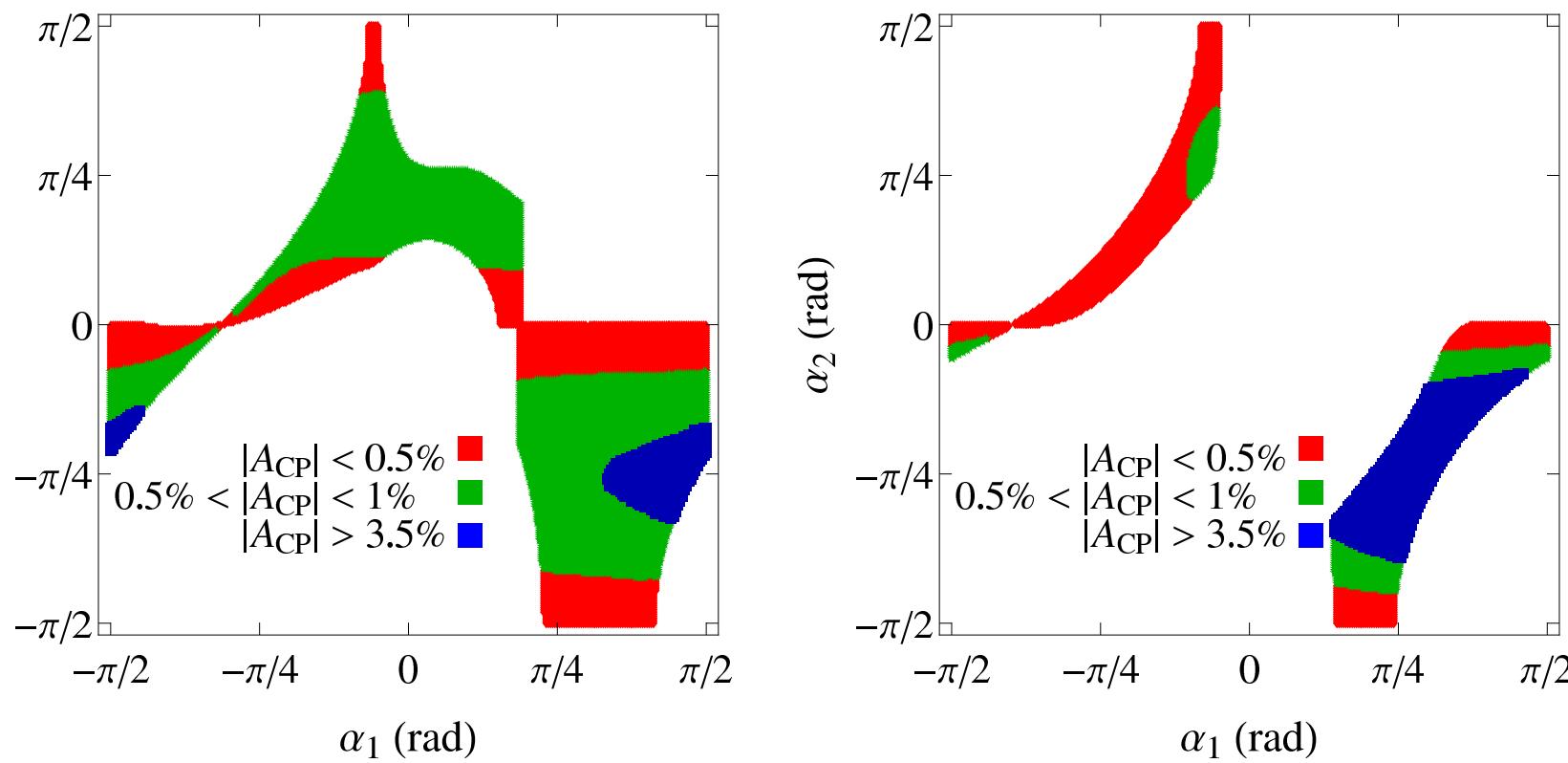
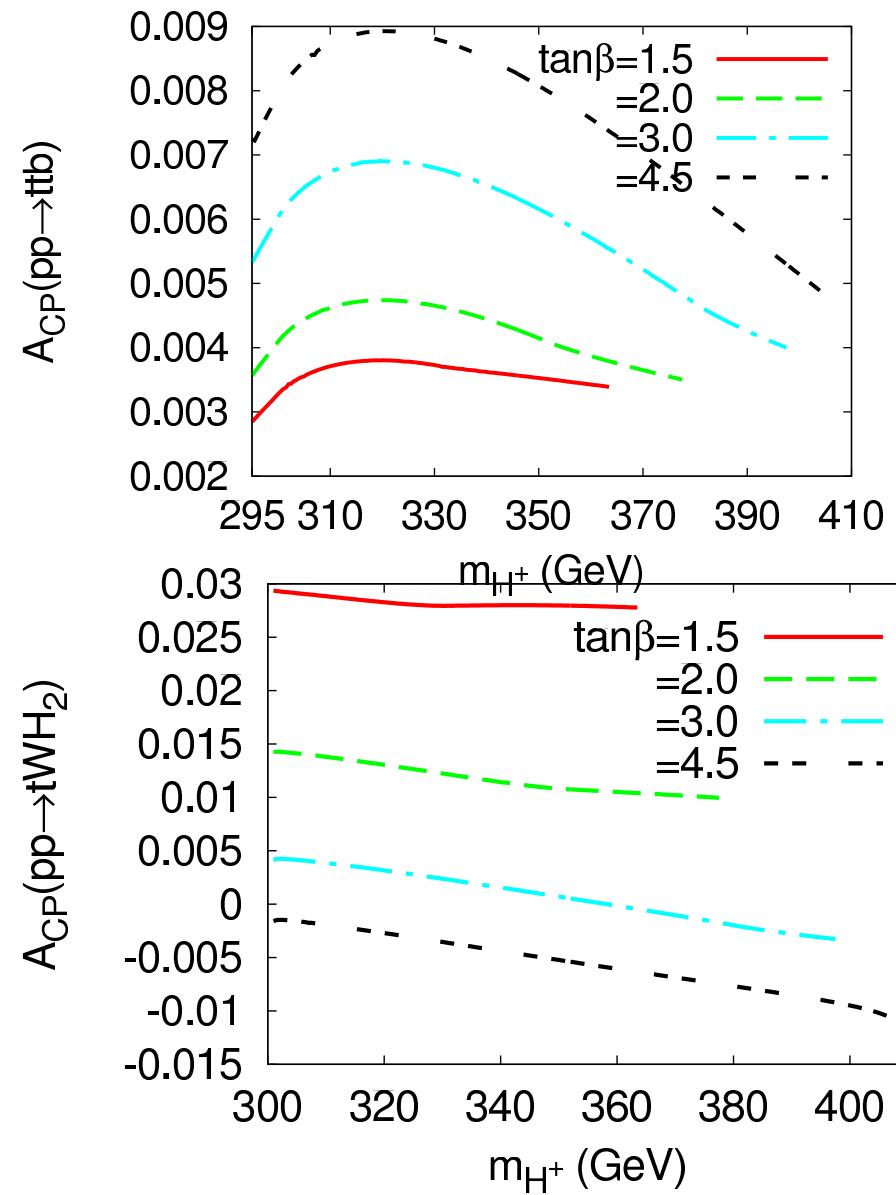
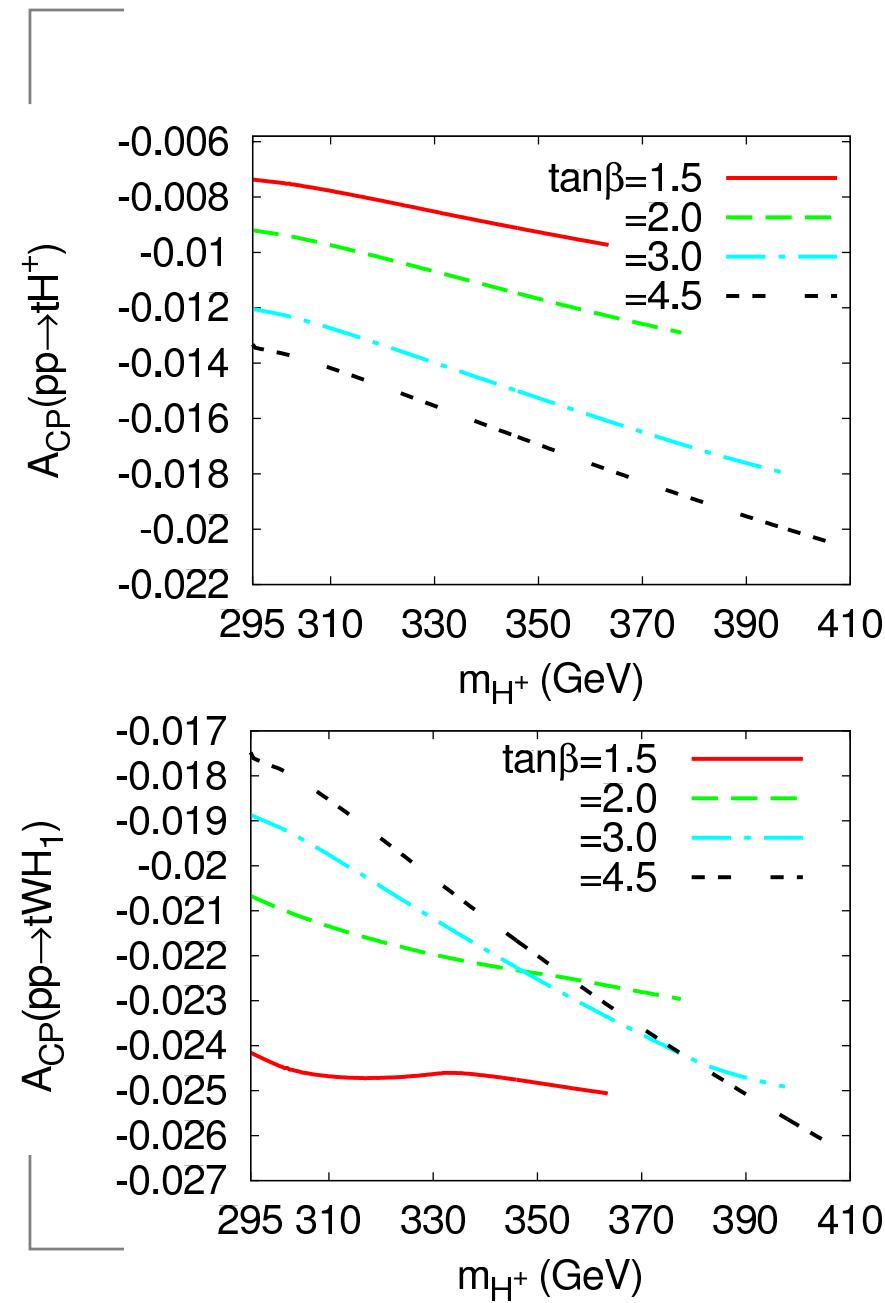


Figure 6: The allowed parameter regions in the (α_1, α_2) plane in the C2HDM together with $|A_P^{CP}|$.

Production and decays



CPV in neutral Higgs decays into fermion

At the LHC, the expected accuracy for $h \rightarrow \tau^+ \tau^-$ is about 20% .

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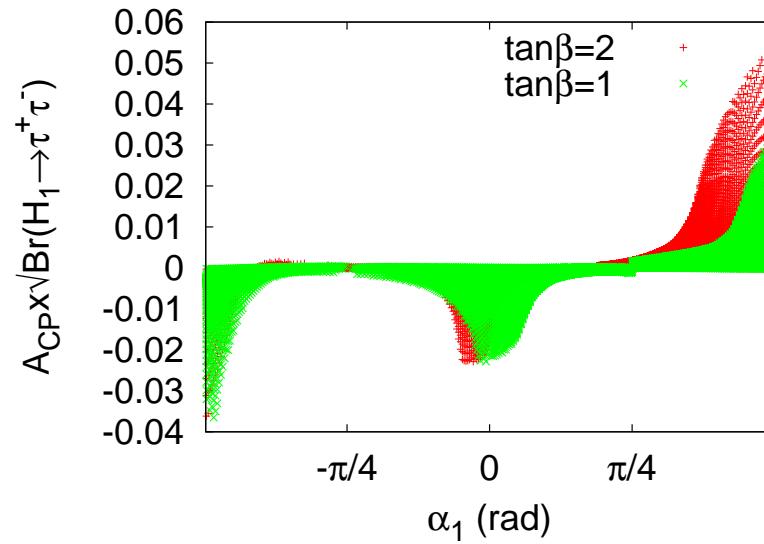
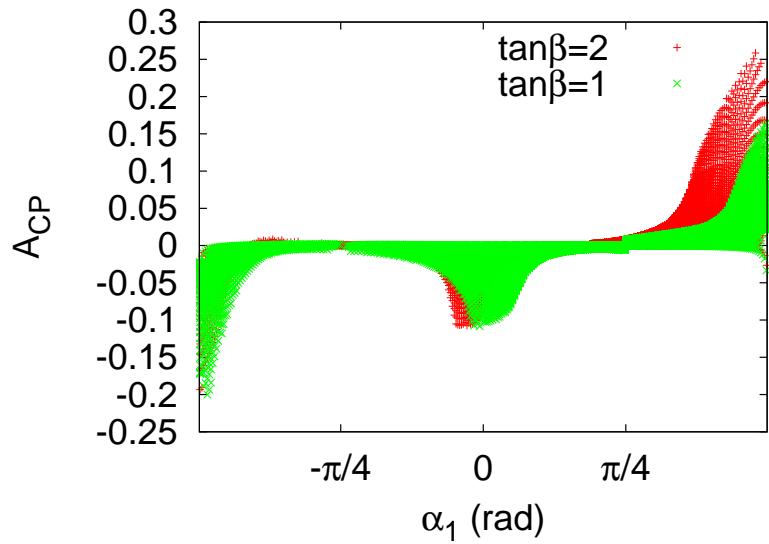
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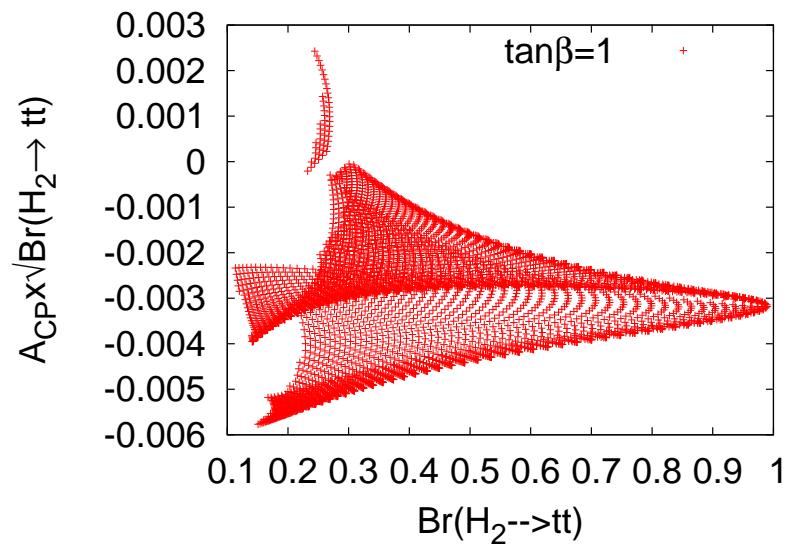
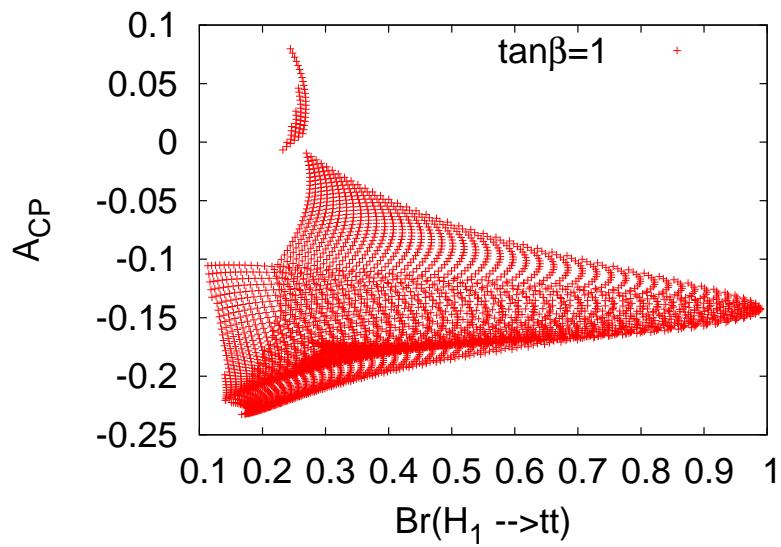
$Br(H_1 \rightarrow \tau^+ \tau^- \& b\bar{b})$ suppressed for $\alpha_2 \approx 0$ and $\alpha_1 \approx \pm\pi/2$

$$H_1 b\bar{b} = -i \frac{gm_b}{2m_W c_\beta} (\cos \alpha_1 \cos \alpha_2 - i \sin \alpha_2 \sin \beta \gamma_5)$$

$H_1 \rightarrow \tau^+ \tau^-$



$H_2 \rightarrow t\bar{t}$



Production: $pp \rightarrow tH^+$

- In C2HDM with softly broken Z_2 , the complex m_{12}^2 parameter of the tree-level potential gives CPV in $pp \rightarrow H^\pm t + X$, and H^\pm to tb , and to WH_i , $i=1,2$
- The parameters space of C2HDM is severely constrained by vacuum stability, perturbative unitarity ... CPA cannot be greater than $\sim 3\%$.
- In the CMSSM , the CPVA can reach more than 20%. However, at the LHC they will have roughly same statistical significance. Not enough for a clear observation at the LHC.
- need for SLHC!
- Calculations have been done with FeynArts & FormCalc. A new model file has been created and corresponding fortran drivers have been written and tested.