自旋電子學 -----



從2007年諾貝爾物理獎巨磁阻現象談起

Spintronics materials and device

---- a quest from the Giant Magnetoresistance Effect, Nobel prize in Physics, 2007

Point Contact Andreev Reflection,

Current Perpendicular to Plane resistance, Spin transfer torque in magnetic nanostructures, and spin pumping effect Shang-Fan Lee (李尚凡)

S. Y. Huang (黃斯衍), C. Yu (于 淳), T. W. Chiang (江典蔚), L. K. Lin (林呂圭), L. J. Chang (張良君), Faris B. Y. C. Chiu (邱昱哲), Y. L. Chen(陳彥霖), Y. H. Chiu (邱亦欣) Institute of Physics, Academia Sinica

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Spintronics :



Electronics with electron spin as an extra degree of freedom Generate, inject, process, and detect spin currents

•Generation: ferromagnetic materials, spin Hall effect, spin pumping effect etc.

•Injection: interfaces, heterogeneous structures, tunnel junctions

Process: spin transfer torque

•Detection: Giant Magnetoresistance, Tunneling MR

科學月刊 38, 898 (2007). 物理雙月刊 30, 116 (2008). 科學人 87, 82 (2009).



2007 Nobel prize in Physics



2007年諾貝爾物理獎得主 左 亞伯 · 費爾(Albert Fert) 與右彼得 · 葛倫貝格(Peter Grünberg) (圖片資料來源: Copyright © Nobel Web AB 2007/ Photo: Hans Mehlin)



鐵磁性元素:鐵 Fe, 鈷 Co, 鎳 Ni, 釓 Gd, 鏑 Dy, 錳 Mn, 鈀 Pd ?? Elements with ferromagnetic properties 合金, alloys 錳氧化物 MnOx

н														2 He			
Li ³	Be ⁴											B 5	C ⁶	7 N	0 ⁸	9 F	10 Ne
л Na	12 Mg										Al	14 Si	015 P	5 ¹⁶	17 Cl	18 Ar	
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	.38 Sr	Y ³⁹	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	Ag ⁴⁷	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba	57 La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 T1	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	89 Ac	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Uun								

- 58	59	60	61	62	63	64	65	66	67	68	69	70	71
Ce	Pr	Nd	\mathbf{Pm}	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
90	91	92	93	- 94	95	96	97	- 98	- 99	100	101	102	103
Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	\mathbf{Fm}	Md	No	Lr



Solar system



s, p electron orbital



Orbital viewer

Platonic solid



From Wikipedia

In geometry, a Platonic solid is a <u>convex polyhedron</u> that is <u>regular</u>, in the sense of a <u>regular polygon</u>. Specifically, the faces of a Platonic solid are <u>congruent</u> regular polygons, with the same number of faces meeting at each <u>vertex</u>; thus, all its edges are congruent, as are its vertices and angles. There are precisely five Platonic solids (shown below):

The name of each figure is derived from its number of faces: respectively 4, 6, 8, 12, and 20.

<u>The aesthetic beauty and symmetry of the Platonic solids have made them a</u> <u>favorite subject of geometers</u> for thousands of years. They are named for the <u>ancient Greek philosopher Plato who theorized that the classical elements were</u> <u>constructed from the regular solids.</u>





3d transition metals: Mn atom has 5 d ↑ electrons Bulk Mn is NOT magnetic.



3d electron distribution in real space

Co atom has 5 d \uparrow electrons and 2 d \downarrow electrons Bulk Co is magnetic.







A f_1 n = 1(b) A $L = \frac{1}{2}\lambda_1$



One-dimensional resonance

Two-dimensional resonance



Stoner criterion for ferromagnetism:



I N(E_F) > 1, I is the Stoner exchange parameter and N(E_F) is the density of states at the Fermi energy.





For the non-magnetic state there are identical density of states for the two spins. For a ferromagnetic state, $N \uparrow > N \downarrow$. The polarization is indicated by the thick blue arrow.

Schematic plot for the energy band structure of 3d transition metals.

Spin-dependent conduction in Ferromagnetic metals (Two-current model) First suggested by Mott (1936) Experimentally confirmed by I. A. Campbell and A. Fert (~1970)

At low temperature

$$\rho = \frac{\rho_{\uparrow} \rho_{\downarrow}}{\rho_{\uparrow} + \rho_{\downarrow}}$$

At high temperature

$$\rho = \frac{\rho_{\uparrow} \rho_{\downarrow} + \rho_{\uparrow\downarrow} (\rho_{\uparrow} + \rho_{\downarrow})}{\rho_{\uparrow} + \rho_{\downarrow} + 4\rho_{\uparrow\downarrow}}$$



Spin mixing effect equalizes two currents

Magnetic coupling in multilayers



Long-range incommensurate magnetic order in a Dy-Y multilayer M. B. Salamon, Shantanu Sinha, J. J. Rhyne, J. E. Cunningham, Ross W. Erwin, Julie Borchers, and C. P. Flynn, Phys. Rev. Lett. 56, 259 - 262 (1986)
Observation of a Magnetic Antiphase Domain Structure with Long-Range Order in a Synthetic Gd-Y Superlattice C. F. Majkrzak, J. W. Cable, J. Kwo, M. Hong, D. B. McWhan, Y. Yafet, and J. V. Waszczak, C. Vettier, Phys. Rev. Lett. 56, 2700 - 2703 (1986)
Layered Magnetic Structures: Evidence for Antiferromagnetic Coupling of Fe Layers across Cr Interlayers P. Grünberg, R. Schreiber, Y. Pang, M. B. Brodsky, and H. Sowers, Phys. Rev. Lett.

P. Grünberg, R. Schreiber, Y. Pang, M. B. Brodsky, and H. Sowers, Phys. Rev. Lett. 57, 2442 - 2445 (1986)



Coupling in **Wedge-shaped** Fe/Cr/Fe Fe/Au/Fe Fe/Ag/Fe J. Unguris, R. J. Celotta, and D. T. Pierce





Fig. 2.58. Dependence of saturation field on Ru spacer layer thickness for several series of $Ni_{81}Fe_{19}/Ru$ multilayers with structure, 100 Å Ru/[30 Å $Ni_{81}Fe_{19}/Ru(t_{Ru})]_{20}$, where the topmost Ru layer thickness is adjusted to be $\simeq 25$ Å for all samples





Fig. 2.11. Fermi surface of Cu in the (100) plane in the extended zone scheme. Arrows indicate values of $2(k_F - G)$ for reciprocal lattice vectors G which can give rise to oscillations with periods greater than π/k_F





Fig. 2.41. A schematic expanded view of the sample structure showing the Fe(001) single-crystal whisker substrate, the evaporated Cr wedge, and the Fe overlayer. The arrows in the Fe show the magnetization direction in each domain. The z-scale is expanded approximately 5000 times. (From [2.206])





Fig. 2.43. SEMPA image of the magnetization M_y (axes as in Fig. 2.41) showing domains in (a) the clean Fe whisker, (b) the Fe layer covering the Cr spacer layer evaporated at 30 °C, and (c) the Fe layer covering a Cr spacer evaporated on the Fe whisker held at 350 °C. The scale at the bottom shows the increase in the thickness of the Cr wedge in (b) and (c). The arrows at the top of (c) indicate the Cr thicknesses where there are phase slips. The region of the whisker imaged is about 0.5 mm long



Fig. 2.44. The effect of roughness on the inertlayer exchange coupling is shown by a comparison of (a) the oscillations of the RHEED intensity along the bare Cr wedge with (b) the SEMPA magnetization image over the same part of the wedge

Aliasing





Fig. 2.10. RKKY-like oscillating exchange coupling with period λ (solid line) showing the longer period oscillation (dashed line) obtained by sampling the function only at integral values of the spacing, *a*, between atomic planes, i.e. "aliasing". From [2.21]

Different aspect of Magnetoresistance Anisotropic MR (異向磁阻) Giant MR (巨磁阻– CPP, CIP) Tunneling MR (穿隧磁阻)



Discovery of Giant MR -- Two-current model combines with magnetic coupling in multilayers



Spin-dependent transport structures.(A) Spin valve. (B) Magnetic tunnel junction. (from Science)

Schematic illustration of GMR





"short circuit effect" of one spin channel results in small resistance in parallel configuration

Electron potential landscape in a F/N multilayer



Intrinsic potential + Scattering potentials due to • Impurities

Vacancies

•

• Lattice mismatches

•Can we distinguish the interface effect from the bulk effect?

Transport geometry



 CIP resistance can be measured easily, CPP resistance needs special techniques.

From CPP resistance in metallic multilayers, one can measure interface resistances, spin diffusion lengths, and polarization in ferromagnetic materials, etc. Valet and Fert model of CPP-GMR



Based on the Boltzmann equation A semi-classical model with spin taken into consideration

$$j_{+(-)} = \frac{1}{e\rho_{+(-)}} \frac{\partial\mu_{+(-)}}{\partial x}$$

$$j_{+} + j_{-} = j_{e}$$

$$\frac{\partial(j_{+} - j_{-})}{\partial x} = \frac{2eN(E_{F})\Delta\mu}{\tau_{sf}}$$

$$\frac{\partial^{2}\mu_{+(-)}}{\partial x} - \frac{\mu_{+(-)}}{\tau_{sf}} = 1^{F} - [\lambda^{F}]$$

 l_{sf}^2

 ∂z^2

$$l_{sf}^{F} = \left[\lambda_{sf}^{F} / 3(\lambda_{\uparrow}^{-1} + \lambda_{\downarrow}^{-1})\right]^{1/2}, \quad l_{sf}^{N} = \left[\lambda_{sf}^{N} \lambda / 6\right]^{1/2}$$

Spin accumulation at the interface is important Spin diffusion length, instead of mean free path, is the dominant physical length scale





How to Determine the Spin Polarization





Andreev reflection: A conversion of normal current to supercurrent occuring at a metallic N/S interface.



When N is ferromagnetic, only part of the electrons are paired.

The suppression of Andreev reflection due to spin polarization serves as a probe of the degree of spin polarization. ✓ Spin Polarization Determined by PCAR Measurement



✓ Dilute magnetic semiconductor (Ga,Mn)As









 $P=0.74, Z=0.04, \Delta=0.85 meV, \chi=4.0$





Black open circles with spreading resistance fits (blue solid lines) and the extracted PCAR spectra (red dashed line) after removing the contribution of spreading resistances in (a) as-grown GaMnAs P=0.76 (b) annealed GaMnAs P=0.74



R.J. Soulen, J.M. Broussard, B. Nadgorny, T. Ambrose, Science 282, 85(1998)

Magnetic Nano-structures



Single Magnetic Domain Wall Resistance Phase diagram of magnetization reversals Edge roughness effect on domain wall mobility Current driven magnetization reversals

Possible applications:
Magnetic sensors, Reading heads
Magnetic RAM
Logic operation



Atomic Force Microscope (AFM) Magnetic Force Microscope (MFM) images





Single Magnetic Domain Wall Resistance



齐府究院 . **Phase diagram of magnetization reversals** INSTITU 0 PHYSICS Acc.V Spot Magn WD 5.00 kV 3.0 50000x 4.7 Acc.V Spot Magn WD 5.00 kV 3.0 50000x 4.7 (a) 1.4 1.2 Acc.V Spot Magn WD | 10.0 kV 2.0 50000x 4.7 Η 1 μm 1.0 8.0 % 0.8 % 0.6 % one - step 0.4 🔺 two - step P3 0.2 ☆ calculated one - step 0.20 calculated two - step 0.0 200 -200 400 -400 0 0.15 width (µm) 1.4 or S 0.10 1.2 1.0 P2 **P2** (%) 0.8 0.6 0.05 ☆ 0.4 0.00 0.2 0.3 0.1 0.2 b/a 0.0 -200 -400 Ó 200 400

H (Oe)

Magnetization reversal characteristics in NiFe elliptical ring arrays

The magnetization reversal processes of single layer nanoscale elliptical ring arrays are examined. For various aspect ratios and thicknesses, transition between singlestep and double-step magnetization reversals was measured to form phase diagrams.



Scanning electron microscope images of selected samples (a) aspect ratio r=3.3 and (b) r=8 arrays of elliptical rings. The edge-to-edge distance in the long axis direction is fixed at 3 μ m.





Figure 2. [(a)-(h)] The MOKE signals for 20 nm NiFe elliptical rings arrays of fixed width 100 nm and circumference 6.3µm for applied field parallel to the long axis of varied aspect ratios. Figure 3. Phase diagram of elliptical ring reversal behavior and the field range of the vortex state Δ Hv as functions of the aspect ratio r and thickness t for the applied field parallel to the long axis. The solid and open circles represent two-step and single-step switching, respectively.



Edge roughness effect on domain wall mobility



Spin transfer Torque



(tranport of magnetization by an electrical curent)

- fundamentals

- switching of magnetization by spin transfer torque applications (STT-RAM, reprogrammable devices)

 microwave oscillations by spin transfer and applications to telecommunications


Concept of spin transfer (Slonczewski 1996)



S



The transverse spin component is lost by the conduction electrons, but is actually transferred to the global SPIN \overline{S} of the layer \rightarrow rotation of \overline{S}

$$\dot{\boldsymbol{S}}_{1,2} = (\boldsymbol{I}_{e} \boldsymbol{g}/\boldsymbol{e}) \, \boldsymbol{\hat{s}}_{1,2} \times (\boldsymbol{\hat{s}}_{1} \times \boldsymbol{\hat{s}}_{2})$$

Current-induced magnetization reversal by the spin-transfer torque can be understood in terms of collision of particles with material-dependent angular momentum transfer efficiencies.



Spin transfer torque





Trilayered pillar or tunnel junction



Tunnel junction ≈ **50x170** nm²



Two regimes of spin transfer

1) Magnetization switching by spin transfer



Applications: writing a memory, etc

2) Sustained precession of the magnetization of the free layer and generation of radiofrequency oscillations

Polarizer magnetization



Free layer magnetization

Applications: spin transfer nanooscillators (NSTOs) for communications (telephone, radio, radar) Applications of magnetic switching by spin transfer Switching of reprogrammable devices (example: STT-RAM) To replace M-RAM (switching by external magnetic field : nonlocal, risk of « cross-talk » limiting integration, too large currents) Current **STT-RAM :**«Electronic» reversal by spin pulse transfer from an electrical current Bit Line Free layer Bipolar MTJ Write Pulse / Pinned laver Read Bias Word Line Generator Transistor

Sense Amp. Ref. Source : SpinRAM SONY, IEEE 2005

Regime of steady precession for tunnel junctions

Tunnel junction \approx 50x170 nm²





CoFeB/MgO/CoFeB junction (J.Grollier, AF et al 2008, collaboration S. Yuasa et al, AIST)



Regime of sustained vortex motion

point contact







Advantages:

-direct oscillation in the microwave range (0.5-40 GHz)

-agility: control of frequency by dc current amplitude

- high quality factor

- small size ($\approx 0.1 \mu m$) (on-chip integration, chip to chip com., microwave assisted writiing in HDD)

-Needed improvements

-- Increase of power by synchronization of a large number N of STOs (x N²)

-Optimization of the emission linewidth

Programmable AND (OR) logic element operated by spin torque transfer

Area : 200*600 nm²

Au 100 nm	
CoFeB 6 nm	
Cu 7 nm	
Py 30 nm	
Cu 80 nm	
substract	
Layer struct	ure









$$\begin{split} I_{P \rightarrow AP} &= 14 \text{ mA}, I_{AP \rightarrow P} = \textbf{-8.7 mA} \\ \text{Input signal 1 (} I_{P \rightarrow AP} / 2 < I = 8 \text{ mA} < I_{P \rightarrow AP}) \\ \text{Input signal 0 (} I = 0 \text{ mA}) \\ \text{Refresh current (} I = \textbf{-11 mA} > I_{AP \rightarrow P}) \end{split}$$



Two channels input

Ch1

Ch2



	rinte										
	input	refresh									
Ch 1 (mA)	0 (0)	(-11)	1 (8)	(-11)	0 (0)	(-11)	1 (8)	(-11)	1 (8)	(-11)	
Ch 2 (mA)	0 (0)	(0)	1 (8)	(0)	1 (8)	(0)	1 (8)	(0)	0 (0)	(0)	
State	L		н		L		н		L		

Another spin transfer effect: displacement of a wall between magnetic domains



Magnetization to the right \rightarrow

← Magnetization to the left



Domain walls in a magnetic nano-stripe for the massive memories of tomorrow ? (IBM project, replacement of hard discs ?)



The information is stored by domain walls located on periodic notches: No wall = "0", Wall = "1"







D4EZ6

FA1304

N

S

ASTC/D4EZA





The information is stored by domain walls located on periodic notches: No wall = "0", Wall = "1"

Edge Roughness effect on the magnetization reversal process of spin valve submicron wires



Non-local measurement



Spin diffusion length
Hanle effect
Spin Hall effect & Inverse Spin Hall effect

Spin Pumping (spin battery)

Pure spin currentSpin Hall effect & Inverse Spin Hall effect

Spin Hall Effect: Electron flow generates transverse spin current



Now observed at room temperature in ZnSe

The extrinsic SHE is due to asymmetry in electron scattering for up and down spins. – spin dependent probability difference in the electron trajectories The Intrinsic SHE is due to topological band structures

Pure Spin Currents: The Johnson Transistor



First Experimental Demonstrations

■ T = 4.2 K

• T = 293 K

λ_N=1,000 nm

2,000

1,500





南北院

Cu film: $\lambda_s = 1 \ \mu m$ (4.2 K)

Jedema et al., Nature 410, 345 (2001)

Spin Hall Angle



 $\gamma = \frac{\sigma_{SH}}{\sigma_c} \quad \longleftarrow \quad \text{spin Hall conductivity} \\ \leftarrow \quad \text{charge conductivity}$

stronger spin orbit interaction \longrightarrow larger γ

Goal:

• experiments to quantify γ

Importance:

- understanding the effect of SO coupling on electron transport
- recognizing materials for spintronics applications

Spin Pumping -- dynamic behavior in F/N bilayers



Ferromagnetic Resonance (FMR) described by

• Landau-Lifshitz-Gilbert

 $\dot{\mathbf{m}} = -\gamma \mathbf{m} \times \mathbf{H}_{\text{eff}} + \mathbf{m} \times \left(\tilde{\alpha} \dot{\mathbf{m}} \right)$

In the FMR condition, the steady magnetization precession in a F is maintained by balancing the absorption of the applied microwave and the dissipation of the spin angular momentum --the transfer of angular momentum from the local spins to conduction electrons, which polarizes the conduction-electron spins.



Spin accumulation gives rise to spin current in neighboring normal metal



PRL 100, 067602 (2008)

week ending 15 FEBRUARY 2008

2.0F

Tunnel Barrier Enhanced Voltage Signal Generated by Magnetization Precession of a Single Ferromagnetic Layer

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感院 物

HILA SINICA

F



2.8GHz

2.6GHz

2.4GHz

2.2GHz

2GHz

1.8GHz

0

H (Oe)

50

100

-50



APPLIED PHYSICS LETTERS 96, 022502 (2010)

Suppression of spin-pumping by a MgO tunnel-barrier

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A real spin transistor?

Switch function – OK Current amplification? No

Dissipationless spin current from a new material?

Topological insulator



Topological insulators

•A **topological insulator** is a material conducting on its boundary but behaves as an insulator in its bulk.

•The conducting channel(s) are guaranteed by timereversal symmetry, topologically protected, will not be affected by local impurities etc, and thus robust.



Band insulator
Mott insulator
Kondo insulator
Topological insulator



Why the word 'topological'?

Topological order: a pattern of longrange quantum entanglement in quantum states, can be described by a new set of quantum numbers, such as ground state degeneracy, quasiparticle fractional statistics, edge states, topological entropy, etc.

 Landau symmetry breaking

describes classical orders in materials. But it failed to describe the chiral spin state, which was proposed (but failed) to explain HTS.



 Z2 topological quantum number
 Chern numbers (陳省身) explains Quantum Hall Effect (from Foucault pendulum to Chern numbers)

 $1/2\pi \int_{s} K \, \mathrm{d}A = 2 \, (1 - g)$



How to become a topological insulator?

Or, how to cross from an intrinsic insulator to a topological insulator? Or, how to build the edge conducting states?

- Spin-orbit effect
- Lattice constant adjustment

To get inversion states and Dirac cone on the boundary.



Carriers in these states have their spin locked at a right-angle to their momentum. At a given energy the only other available electronic states have opposite spin, so scattering is strongly suppressed and conduction on the surface is nearly dissipationless.



A MISTILLE ACADEMINATION OF A HYSICS ACADEMINATION OF A HYSICA ACADEMI

States of matter. (**Top**) Electrons in an insulator are bound in localized orbitals (left) and have an energy gap (right) separating the occupied valence band from the empty conduction band. (Middle) A two-dimensional quantum Hall state in a strong magnetic field has a bulk energy gap like an insulator but permits electrical conduction in onedimensional "one way" edge states along the sample boundary. (Bottom) The quantum spin Hall state at zero magnetic field also has a bulk energy gap but allows conduction in spinfiltered edge states.

A zoo of Hall effects



□ Hall effect --- $B \perp I$, $V \perp I$ $R_H = \frac{-n\mu_e^2 + p\mu_h^2}{e(n\mu_e + p\mu_h)^2}$ □ Anomalous (Extra-ordinary) Hall effect

extra voltage proportional to magnetization

- **D** Planar Hall effect --- in-plane field, $V \perp I$
- $\Box \text{ (Integer) Quantum Hall effect --- } \sigma = \nu \frac{e^2}{h},$ B \perp I, V \perp I in 2D electron gas
- Fractional Quantum Hall effect electrons bind magnetic flux lines
- **Spin Hall effect** --- $B = 0, V \perp I$
- Quantum Spin Hall effect --- 2D topological insulator





Edwin Hall's 1878 experiment was the first demonstration of the Hall effect. A magnetic field *B* normal to a gold leaf exerts a Lorentz force on a current *I* flowing longitudinally along the leaf. That force separates charges and builds up a transverse "Hall voltage" between the conductor's lateral edges. Hall detected this transverse voltage with a voltmeter that spanned the conductor's two edges.

PhysicsToday, Aug 2003, p38



Figure 1. Spatial separation is at the heart of both the quantum Hall (QH) and the quantum spin Hall (QSH) effects. (a) A spinless one-dimensional system has both a forward and a backward mover. Those two basic degrees of freedom are spatially separated in a QH bar, as illustrated by the symbolic equation "2 = 1 + 1." The upper edge contains only a forward mover and the lower edge has only a backward mover. The states are robust: They will go around an impurity without scattering. (b) A spinful 1D system has four basic channels, which are spatially separated in a QSH bar: The upper edge contains a forward mover with up spin and a backward mover with down spin, and conversely for the lower edge. That separation is illustrated by the symbolic equation "4 = 2 + 2."



Figure 2. (a) On a lens with antireflection coating, light waves reflected by the top (blue line) and the bottom (red line) surfaces interfere destructively, which leads to suppressed reflection. (b)A quantum spin Hall edge state can be scattered in two directions by a nonmagnetic impurity. Going clockwise along the blue curve, the spin rotates by π ; counterclockwise along the red curve, by $-\pi$. A quantum mechanical phase factor of -1 associated with that difference of 2π leads to destructive interference of the two paths—the backscattering of electrons is suppressed in a way similar to that of photons off the antireflection coating.



Figure 3. Mercury telluride quantum wells are wo dimensional topological insulators. (a) The behavior of a mercury telluride-cadmium telluride quantum well depends on the thickness *d* of the HgTe layer. Here the blue curve shows the potential-energy well experienced by electrons in the conduction band; the red curve is the barrier for holes in the valence band. **Electrons and holes are trapped laterally by those** potentials but are free in the other two dimensions. For quantum wells thinner than a critical thickness d_{c} $\simeq 6.5$ nm, the energy of the lowest-energy conduction subband, labeled E1, is higher than that of the highest-energy valence band, labeled H1. But for d > $d_{\rm c}$, those electron and hole bands are inverted. (b) The energy spectra of the quantum wells. The thin quantum well has an insulating energy gap, but inside the gap in the thick quantum well are edge states, shown by red and blue lines. (c) Experimentally measured resistance of thin and thick quantum wells, plotted against the voltage applied to a gate electrode to change the chemical potential. The thin quantum well has a nearly infinite resistance within the gap, whereas the thick quantum well has a quantized resistance plateau at $R = h/2e^2$, due to the perfectly conducting edge states. Moreover, the resistance plateau is the same for samples with different widths, from 0.5 µm (red) to 1.0 µm (blue), proof that only the edges are conducting.

Fig. 1. Electronic band structure of undoped Bi2Se3 measured by ARPES. (A) The bulk conduction band (BCB), bulk valence band (BVB), and surface-state band (SSB) are indicated, along with the Fermi energy $(E_{\rm F})$, the bottom of the BCB $(E_{\rm B})$, and the Dirac point (E_D) . (B) Constant-energy contours of the band structure show the SSB evolution from the Dirac point to a hexagonal shape (green dashed lines). (C) Band structure along the K- Γ -K direction, where Γ is the center of the hexagonal surface Brillouin zone (BZ), and the K and M points [see (D)] are the vertex and the midpoint of the side of the BZ, respectively (14). The BCB bottom is ~190 meV above Ep and 150 meV below $E_{\rm F}$. (D) Photon energy-dependent FS maps (symmetrized according to the crystal symmetry). Blue dashed lines around the BCB FS pocket indicate their different shapes.

3 D topological insulators: Bi₂Sb₃, Bi₂Se₃, Bi₂Te₃, Sb₂Te₃. There is optical proof of the Dirac cone, but no transport evidence.





SCIENCE 329, 659 (2010)
Tunable multifunctional topological insulators in ternary Heusler compounds



Stanislav Chadov, Xiaoliang Qi, Jürgen Kübler, Gerhard H. Fecher, Claudia Felser, and Shou Cheng Zhang



Figure 1 | Comparison of the zinc-blende and the C1_b crystal structure. The zinc-blende (XY) structure is shown on the left, and the C1_b (XYZ) on the right. Yellow and blue spheres correspond to the main-group (Z) and transition (Y) elements, respectively. The orange spheres in C1_b stand for the additional stuffing (X) element.



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Figure 2 | Bandstructures of CdTe and HgTe compared with ScPtSb and ScPtBi Heuslers. Red colour marks the bands with Γ_8 symmetry, blue with Γ_6 . Comparison reveals obvious similarity between binary systems and their ternary equivalents: both CdTe and ScPtSb are trivial semiconductors with Γ_6 situated above Γ_8 , which sits at the Fermi energy (set to zero). Both HgTe and ScPtBi are topological with inverted band order; the band with Γ_6 symmetry is situated below Γ_8 .





Figure 3 | $E_{\Gamma_6} - E_{\Gamma_8}$ difference calculated for various Heuslers at their experimental lattice constants. HgTe and CdTe binaries are shown for comparison. Open squares mark the systems not reported in the literature. **a**, $E_{\Gamma_6} - E_{\Gamma_8}$ difference as a function of the lattice constant. Pairs of materials with well-matching lattices for the QSH quantum wells can be easily picked up along the same vertical lines. The borderline compounds (between trivial and topological) insulators (YPtSb, YPdBi, ScAuPb) are situated closer to the zero horizontal line. **b**, $E_{\Gamma_6} - E_{\Gamma_8}$ difference as a function of the average spin-orbit coupling strength represented by the average nuclear charge $\langle Z \rangle = (1/N) \sum_{i=1}^{N} Z(X_i)$, where N is 3 for ternaries and 2 for binaries.

а

High energy physicist stretches their imagination



- Dyon: an image electric charge and image magnetic monopole above a 3D TI surface, which is a behave with any possible statistics
- Anyon
- Axions
- Skyrmions

Noether's theorem symmetry implies conservation



Figure 5. Novel behavior is predicted for topological insulators. (a) When a topological insulator (TI, green) is coated by a thin ferromagnetic layer (gray), each electron (red sphere) in the vicinity of the surface induces an image monopole (blue sphere) right beneath it.¹² When one electron winds around another (red circle), it will experience the magnetic flux (arrows in the blue dome) carried by the image monopole of the other, so that the electron-monopole composite, called a dyon, obeys fractional statistics. (b) When a TI is coated by an *s*-wave superconductor (SC), the superconducting vortices are Majorana fermions—they are their own antiparticles. Exchanging or braiding Majorana vortices, as sketched here, leads to non-abelian statistics.¹⁷ Such behavior could form the basis for topological quantum computing.

Dynamical axion field in topological magnetic insulators



Suggest attenuated total reflection (ATR) measurements



Figure 2 | Axionic polariton and ATR experiment. a, The dispersion of the axionic polariton. The grey area indicates the forbidden band between frequencies m and $\sqrt{m^2 + b^2}$ (see text), within which light cannot propagate in the sample. The red dotted line shows the bare photon dispersion $\omega = c'k$. b, Set-up for the ATR experiment. Without an external magnetic field, the incident light can transmit through the sample. c, When an external magnetic field is applied parallel to the electric field of light, the incident light will be totally reflected if its frequency lies within the forbidden band.

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Demonstration of TI

- On the surface of a 3D TI, induced magnetic gap leads to novel quantum Hall state --- topological magnetoelectric effect?
- Induced superconducting gap ---Majorana fermion states --- topological quantum computation?

Fig. 2. Illustration of the experimental setup to measure the image monopole. A magnetic layer is deposited on the surface of the topological insulator, as indicated by the layer with blue arrows. (The same layer is drawn in Figs. 3 and 4.) A scanning MFM tip carries a magnetic flux ϕ and a charge q. A charged impurity is confined on the surface with charge Q and distance D out of the surface. By scanning over the voltage V and the distance r to the impurity, the effect of the image monopole magnetic field can be measured (see text).

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Fig. 3. Illustration of the fractional statistics induced by image monopole effect. Each electron forms a dyon with its image monopole. When two electrons are exchanged, an AB phase factor is obtained (which is determined by half of the image monopole flux) and leads to statistical transmutation.





Present and future impact of spintronics





Summary



GMR effect – charge can be controlled by magnetization (spin).

STT (spin transfer torque) effect

magnetization can be controlled by spin polarized current.
New materials with high spin polarization, low saturation moments,
high Curie temperature are needed.

Pure spin current – will it be realized in circuits?