



# Spin current & spin pumping effect

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J. Kwo

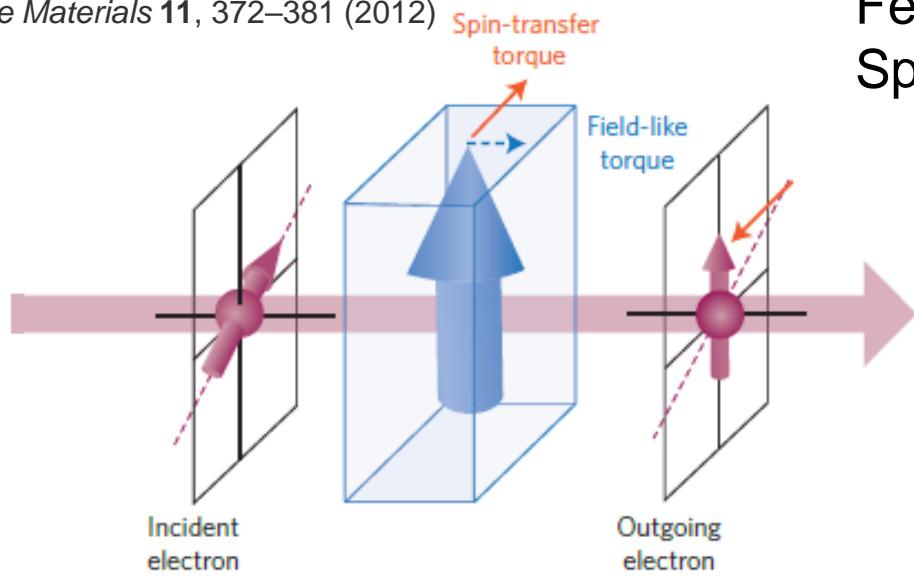
Department of Physics, National Tsing Hua University

# Outline

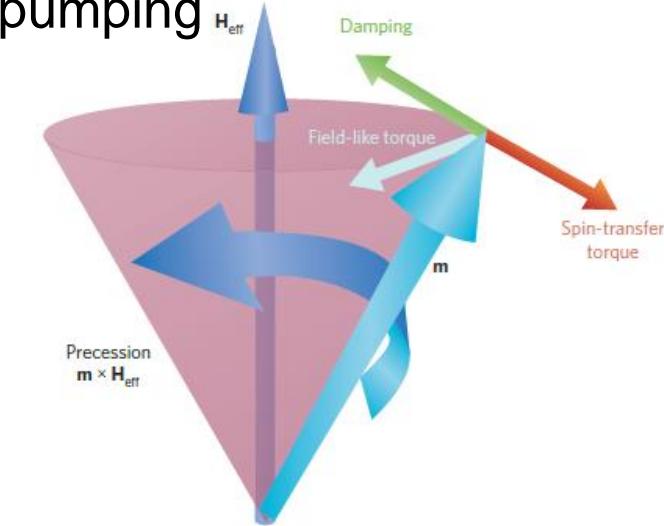
- **Introduction to spin current and spin transfer torques**
- **Measuring spin Hall angle and IEE length**
  - Spin pumping
  - Spin-torque ferromagnetic resonance (ST-FMR)
  - Modulation of magnetization damping (MOD)

# Spin transfer torques

Nature Materials 11, 372–381 (2012)



Ferromagnetic resonance (FMR)  
Spin pumping



LLG equation with torque terms:

$$\frac{\partial \mathbf{m}}{\partial t} = -y\mathbf{m} \times H_{eff} + \alpha\mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t} + \boldsymbol{\tau}$$

Damp-like torque:

$$-\frac{\gamma\hbar}{2eM_s V} \mathbf{m} \times (\mathbf{m} \times I_s)$$

A. Brataas, et al., Nat. Mater. 11, 372 (2012)

Field-like torque:

$$-\frac{\gamma\hbar}{2eM_s V} \mathbf{m} \times I_s$$

# Spin current

$$\mathbf{Q} = \mathbf{v} \otimes \mathbf{s}$$

$$= \frac{\hbar^2}{2m} \operatorname{Im}(\psi^* \boldsymbol{\sigma} \otimes \nabla \psi)$$

For a spinor plane-wave wavefunction in x direction:

$$\psi = \frac{e^{ikx}}{\sqrt{\Omega}} \operatorname{Im}(a|\uparrow\rangle + b|\downarrow\rangle)$$

$$Q_{xx} = \frac{\hbar^2 k}{2m\Omega} 2 \operatorname{Re}(ab^*)$$

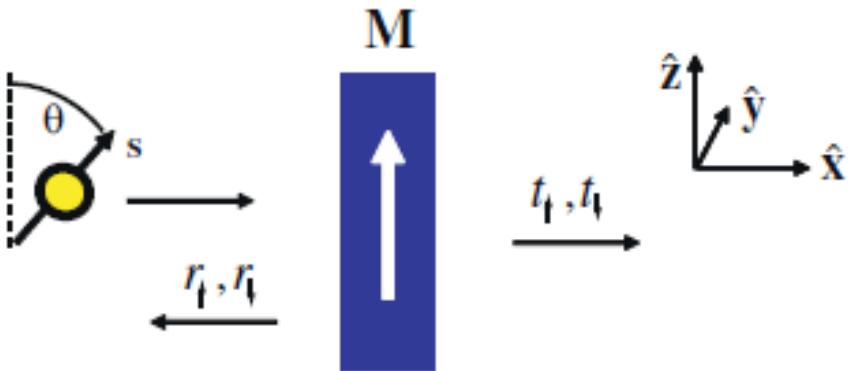
$$Q_{xy} = \frac{\hbar^2 k}{2m\Omega} 2 \operatorname{Im}(ab^*)$$

$$Q_{xz} = \frac{\hbar^2 k}{2m\Omega} 2 \operatorname{Re}(|a|^2 - |b|^2)$$

Conservation of angular momentum  
Spin transfer torque:

$$\begin{aligned}\mathbf{N}_{st} &= - \int_{pillbox} d^2 R \hat{\mathbf{n}} \cdot \mathbf{Q} \\ &= - \int_{pillbox} d^3 r \nabla \cdot \mathbf{Q}\end{aligned}$$

$$\psi_{in} = \frac{e^{ikx}}{\sqrt{\Omega}} (\cos(\theta/2) |\uparrow\rangle + \sin(\theta/2) |\downarrow\rangle)$$



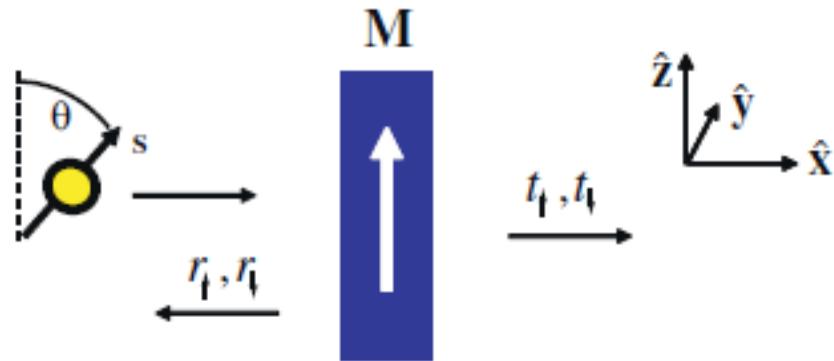
$$\psi_{trans} = \frac{e^{ikx}}{\sqrt{\Omega}} (t_{\uparrow} \cos(\theta/2) |\uparrow\rangle + t_{\downarrow} \sin(\theta/2) |\downarrow\rangle)$$

$$\psi_{refl} = \frac{e^{-ikx}}{\sqrt{\Omega}} (r_{\uparrow} \cos(\theta/2) |\uparrow\rangle + r_{\downarrow} \sin(\theta/2) |\downarrow\rangle)$$

$$\mathbf{Q}_{in} = \frac{\hbar^2 k}{2m\Omega} [\sin(\theta) \hat{\mathbf{x}} + \cos(\theta) \hat{\mathbf{z}}]$$

$$\begin{aligned} \mathbf{Q}_{trans} &= \frac{\hbar^2 k}{2m\Omega} \sin(\theta) \operatorname{Re}(t_{\uparrow} t_{\downarrow}^*) \hat{\mathbf{x}} + \frac{\hbar^2 k}{2m\Omega} \sin(\theta) \operatorname{Im}(t_{\uparrow} t_{\downarrow}^*) \hat{\mathbf{y}} \\ &\quad + \frac{\hbar^2 k}{2m\Omega} \left( |t_{\uparrow}|^2 \cos^2(\theta/2) - |t_{\downarrow}|^2 \sin^2(\theta/2) \right) \hat{\mathbf{z}} \end{aligned}$$

$$\begin{aligned} \mathbf{Q}_{refl} &= -\frac{\hbar^2 k}{2m\Omega} \sin(\theta) \operatorname{Re}(r_{\uparrow} r_{\downarrow}^*) \hat{\mathbf{x}} - \frac{\hbar^2 k}{2m\Omega} \sin(\theta) \operatorname{Im}(r_{\uparrow} r_{\downarrow}^*) \hat{\mathbf{y}} \\ &\quad - \frac{\hbar^2 k}{2m\Omega} \left( |r_{\uparrow}|^2 \cos^2(\theta/2) - |r_{\downarrow}|^2 \sin^2(\theta/2) \right) \hat{\mathbf{z}} \end{aligned}$$



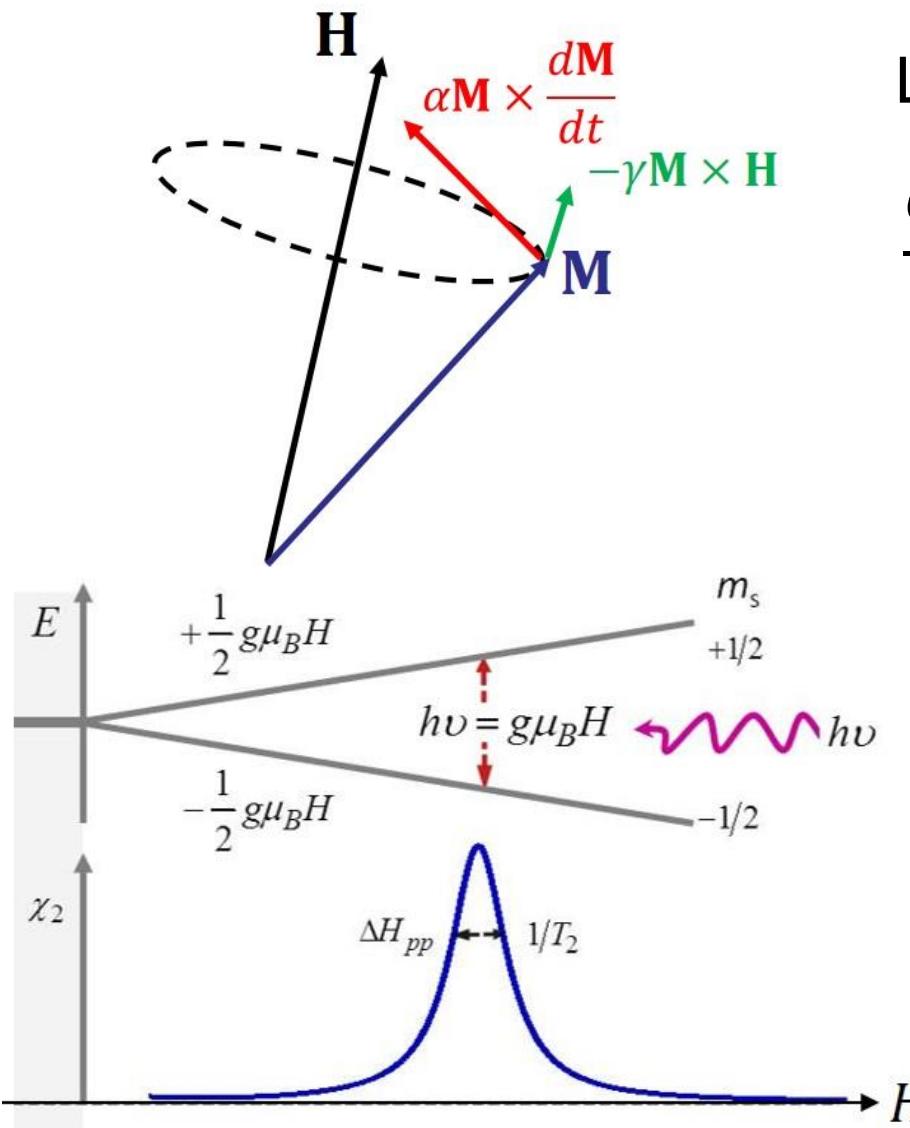
$$\begin{aligned}
 \mathbf{N}_{st} &= A\hat{\mathbf{x}} \cdot (\mathbf{Q}_{in} + \mathbf{Q}_{refl} - \mathbf{Q}_{trans}) \\
 &= \frac{A\hbar^2 k}{2m\Omega} \sin(\theta) \left[ 1 - \text{Re}(t_{\uparrow}^* t_{\downarrow} + r_{\uparrow} r_{\downarrow}^*) \right] \hat{\mathbf{x}} \\
 &\quad \text{Damp-like torque} \\
 &- \frac{A\hbar^2 k}{2m\Omega} \sin(\theta) \left[ \text{Im}(t_{\uparrow}^* t_{\downarrow} + r_{\uparrow} r_{\downarrow}^*) \right] \hat{\mathbf{y}} \\
 &\quad \text{Field-like torque}
 \end{aligned}$$

$$\begin{aligned}
 |t_{\uparrow}|^2 + |r_{\uparrow}|^2 &= 1 \\
 |t_{\downarrow}|^2 + |r_{\downarrow}|^2 &= 1
 \end{aligned}$$

## Spin mixing conductance

$$\begin{pmatrix} a' \\ b' \end{pmatrix} = \begin{pmatrix} G_{\uparrow\uparrow} & G_{\uparrow\downarrow} \\ G_{\downarrow\uparrow}^* & G_{\downarrow\downarrow} \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} \quad \text{Re}(G_{\uparrow\downarrow}) \gg \text{Im}(G_{\uparrow\downarrow}) \text{ for metals}$$

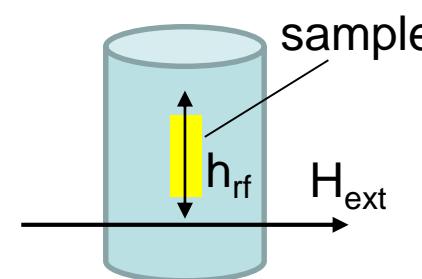
# Ferromagnetic resonance (FMR)



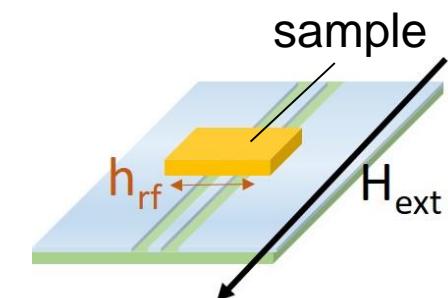
Landau–Lifshitz–Gilbert equation

$$\frac{d\mathbf{M}}{dt} = -\gamma\mathbf{M} \times \mathbf{H} + \alpha\mathbf{M} \times \frac{d\mathbf{M}}{dt}$$

Cavity



Coplanar waveguide



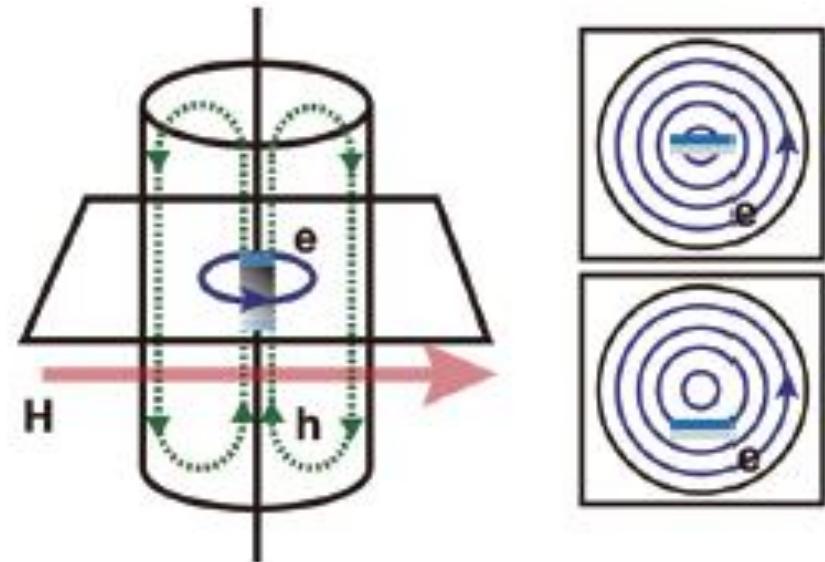
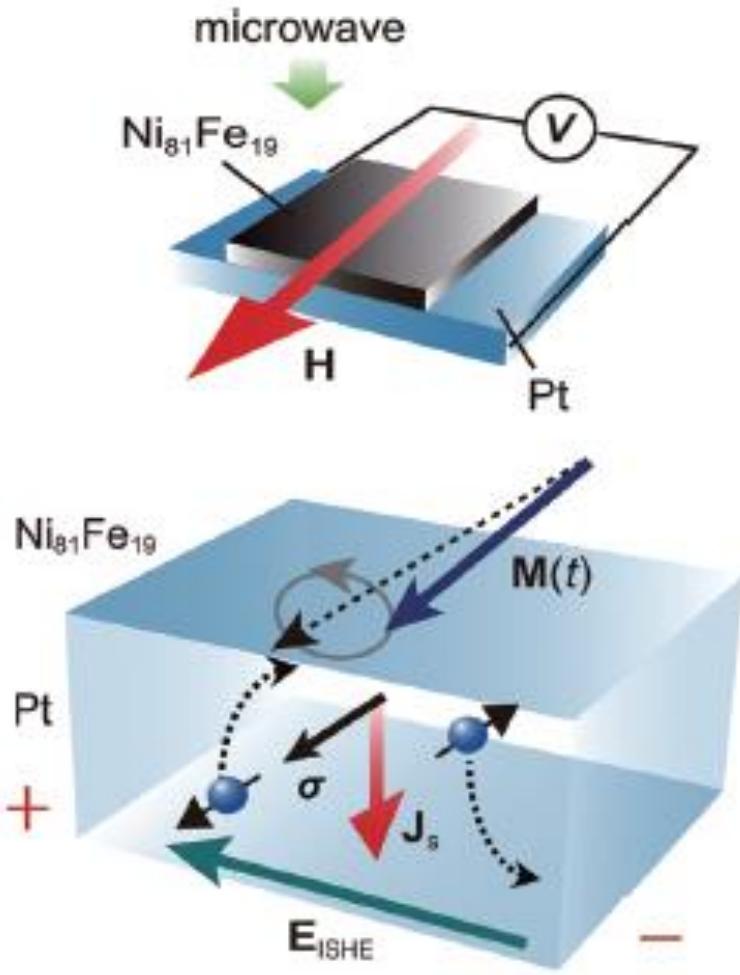
Application:

Measurement of **magnetic anisotropy**

Measurement of **damping constant  $\alpha$**

**Spin pumping**

# Spin pumping



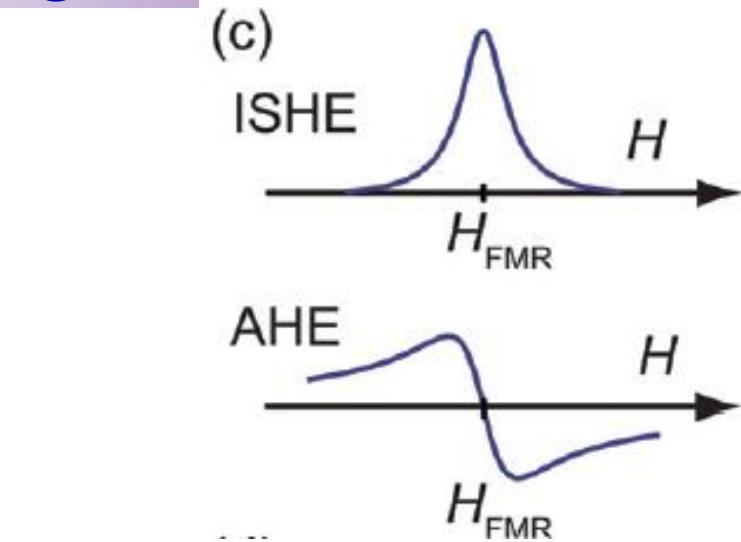
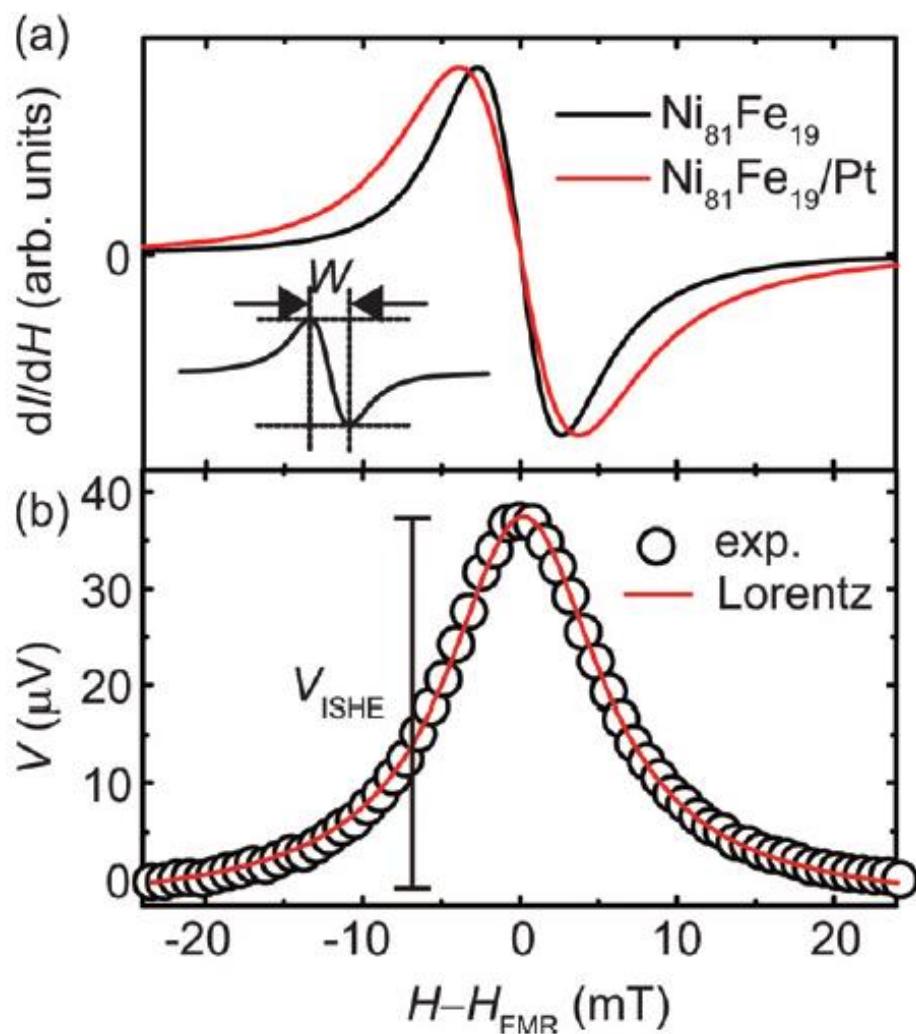
Spin current projected along  $H_{\text{ext}}$ :

$$j_s = \frac{\omega}{2\pi} \int_0^{2\pi/\omega} \frac{\hbar}{4\pi} g_r^{\uparrow\downarrow} \frac{1}{M_s^2} \left[ \mathbf{M}(t) \times \frac{d\mathbf{M}(t)}{dt} \right]_z dt$$

$$\begin{aligned} V_{\text{ISHE}} &\propto J_c \propto \theta_{\text{SH}} J_s \times \sigma \propto \theta_{\text{SH}} J_s \times M \\ &\propto \theta_{\text{SH}} J_s \times H \propto \theta_{\text{SH}} \sin \theta_H, \end{aligned}$$

- E. Saitoh et al., Appl. Phys. Lett. **88**, 182509 (2016)  
K. Ando, et al., J. Appl. Phys. **109**, 103913 (2011)  
H. Nakayama, et al., Phys. Rev. B **85**, 144408 (2012)

# A phenomenological model



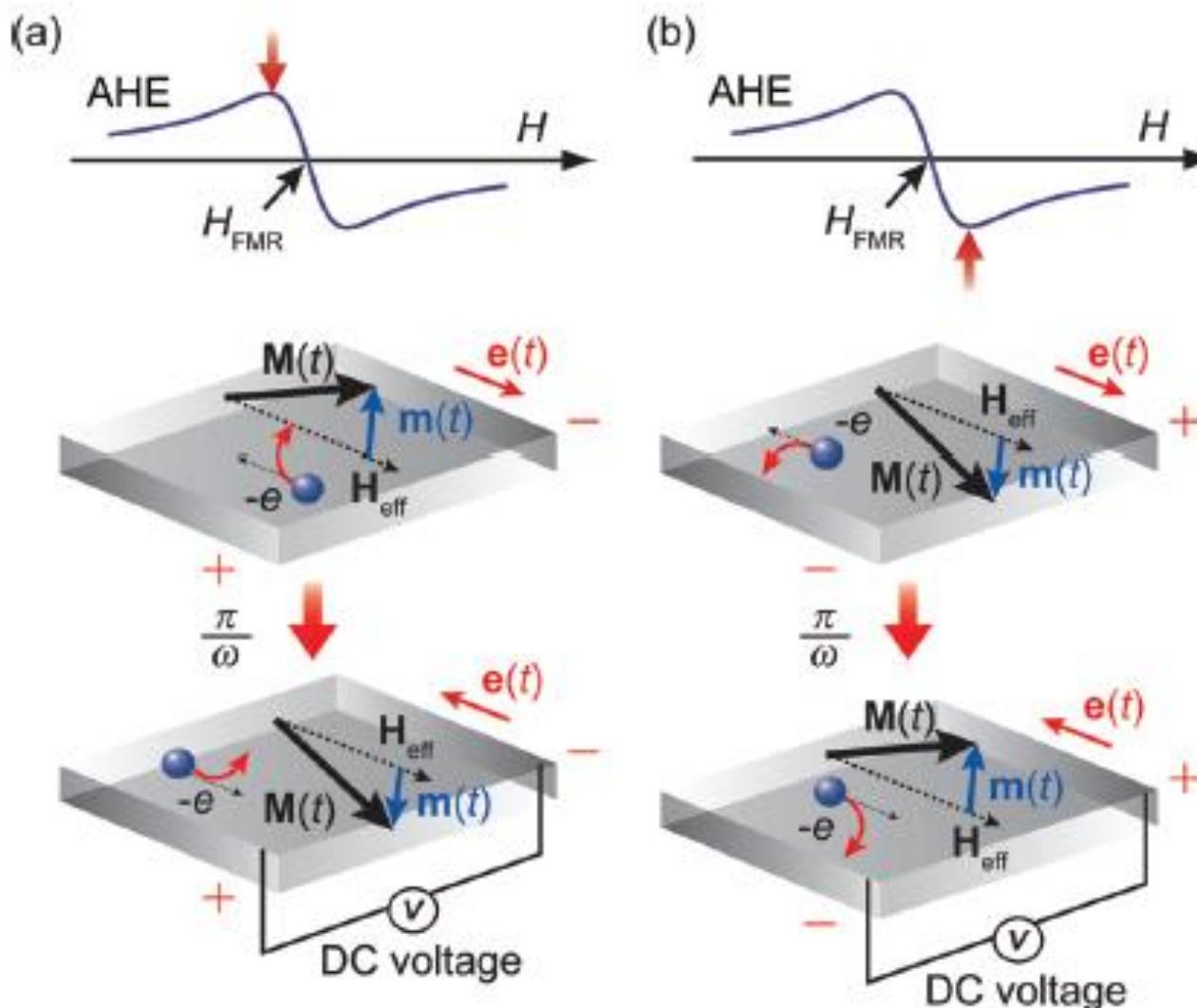
$$V = V_{ISHE} \frac{\Gamma^2}{(H - H_0)^2 + \Gamma^2} + V_{AHE} \frac{-2\Gamma(H - H_0)}{(H - H_0)^2 + \Gamma^2}$$

$$g_r^{\uparrow\downarrow} = \frac{2\sqrt{3}\pi M_s \gamma d_F}{g \mu_B \omega} (W_{F/N} - W_F)$$

$$\text{or } g_r^{\uparrow\downarrow} = \frac{4\pi M_s d_F}{g \mu_B} (\alpha_{F/N} - \alpha_F)$$

E. Saitoh et al., Appl. Phys. Lett. **88**, 182509 (2016)  
 K. Ando, et al., J. Appl. Phys. **109**, 103913 (2011)  
 H. Nakayama, et al., Phys. Rev. B **85**, 144408 (2012)

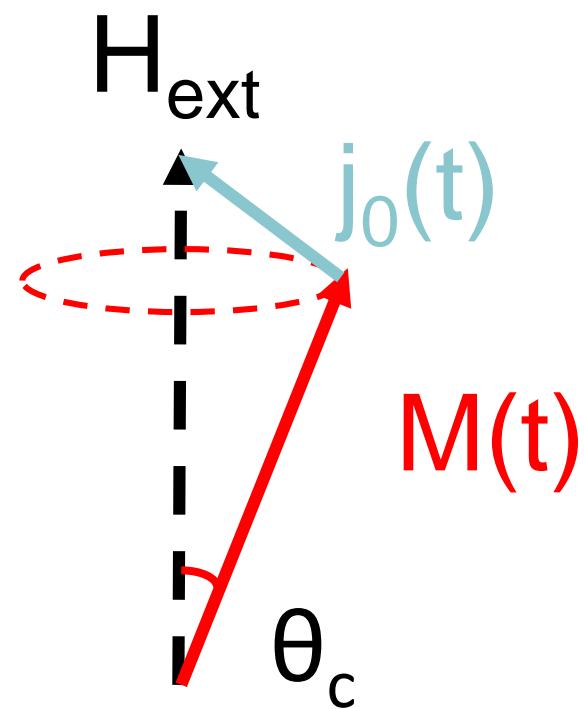
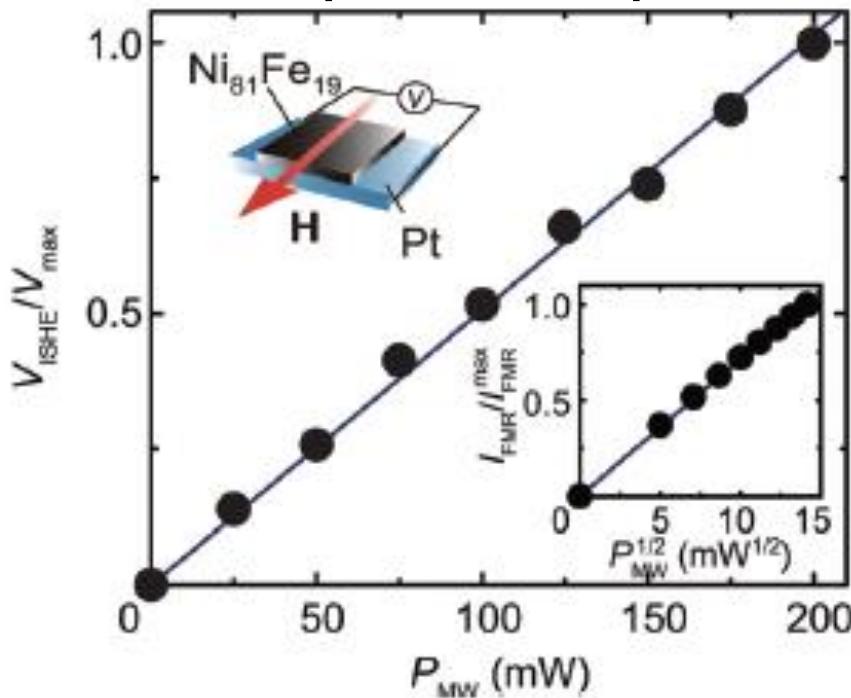
# Antisymmetric lineshape from AHE or AMR



Phase shift between the microwave and magnetization determine the polarity.

# Small cone angle (linear) regime

## Linear power dependence

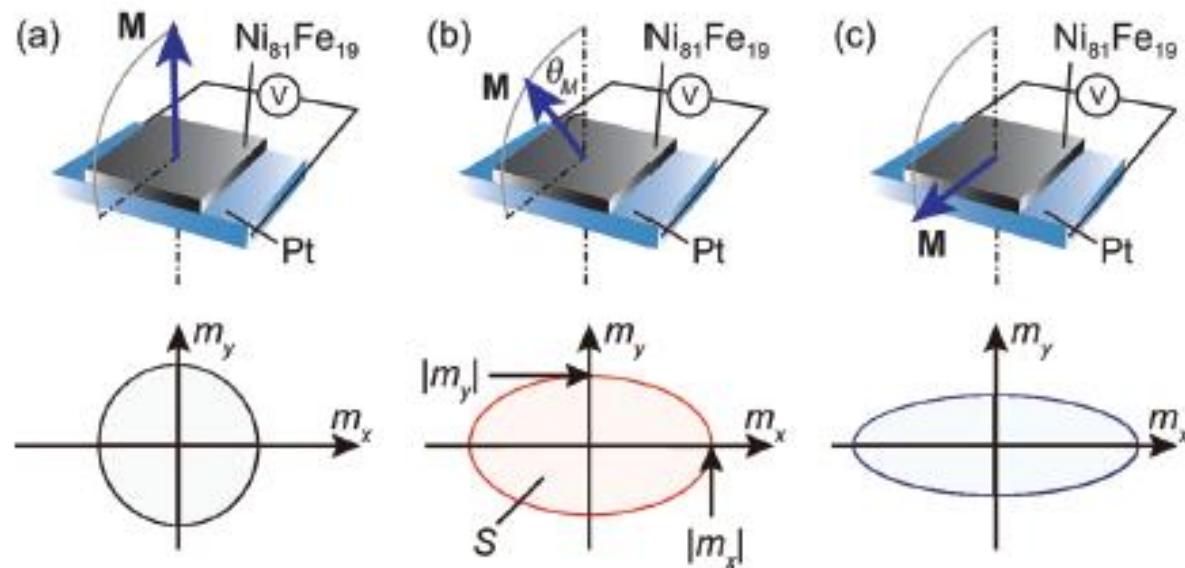


$$j_0 = \frac{g_r^{\uparrow\downarrow} \gamma^2 h_{rf}^2 \hbar \left[ 4\pi M_s \gamma + \sqrt{(4\pi M_s)^2 \gamma^2 + 4\omega^2} \right]}{8\pi\alpha^2 \left[ (4\pi M_s)^2 \gamma^2 + 4\omega^2 \right]}$$
$$= g_r^{\uparrow\downarrow} fP \left( \frac{\gamma h_{rf}}{2\alpha\omega} \right)^2 = g_r^{\uparrow\downarrow} fP \theta_c^2, \text{ where } h_{rf}^2 \propto \text{power}$$

# The P factor

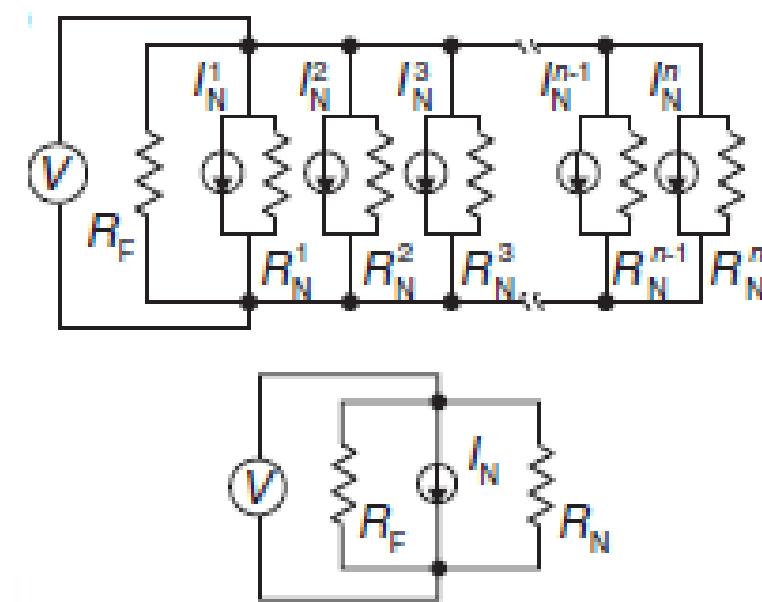
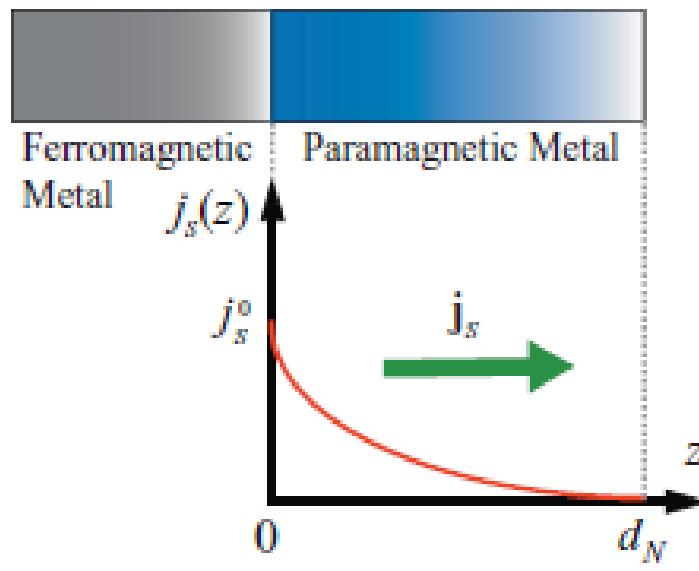
$$P = \frac{2\omega \left[ 4\pi M_s \gamma + \sqrt{(4\pi M_s)^2 \gamma^2 + 4\omega^2} \right]}{(4\pi M_s)^2 \gamma^2 + 4\omega^2}$$

can be viewed as a correction factor.



The pumped spin current is proportional to the trajectory area.  
Spin pumping is an adiabatic process. (think about the Carnot engine.)

# Spin distribution in normal metals

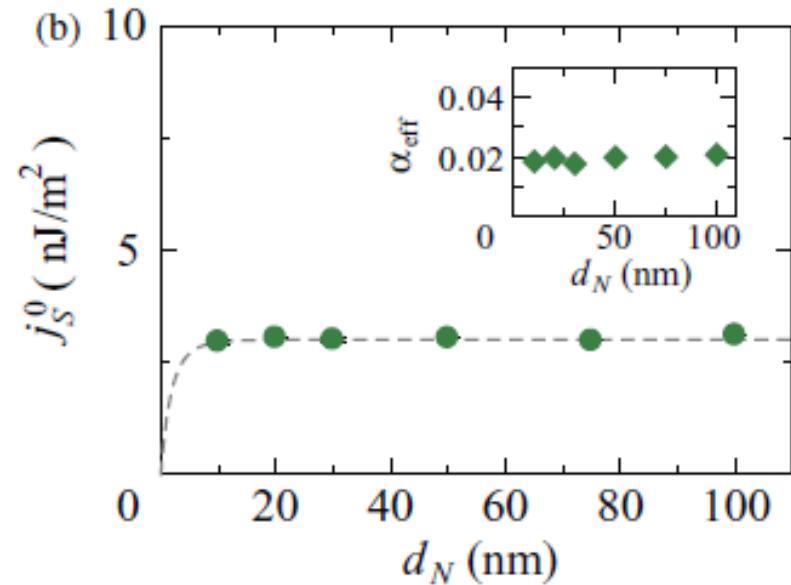
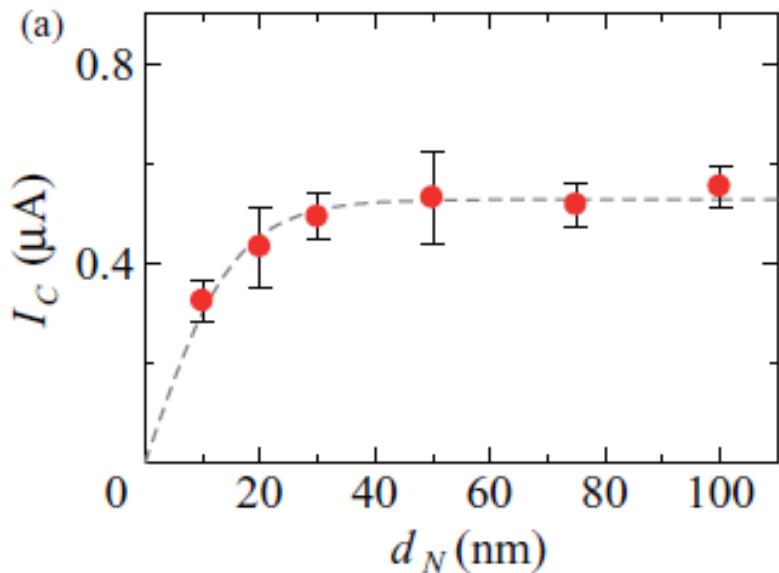


Spin Hall effect acts as a charge current source.

Solving the spin diffusion equation...

$$j_s(z) = \frac{\sinh[(d_N - z)/\lambda_N]}{\sinh(d_N/\lambda_N)} j_s^0$$

# Thickness dependence



$$\langle j_c \rangle = \frac{1}{d_N} \int_0^{d_N} j_c(y) dy$$

$$= \theta_{SH} \left( \frac{2e}{\hbar} \right) \frac{\lambda_N}{d_N} \tanh \left( \frac{d_N}{2\lambda_N} \right) j_s^0$$

Spin backflow depends on the spin diffusion length.

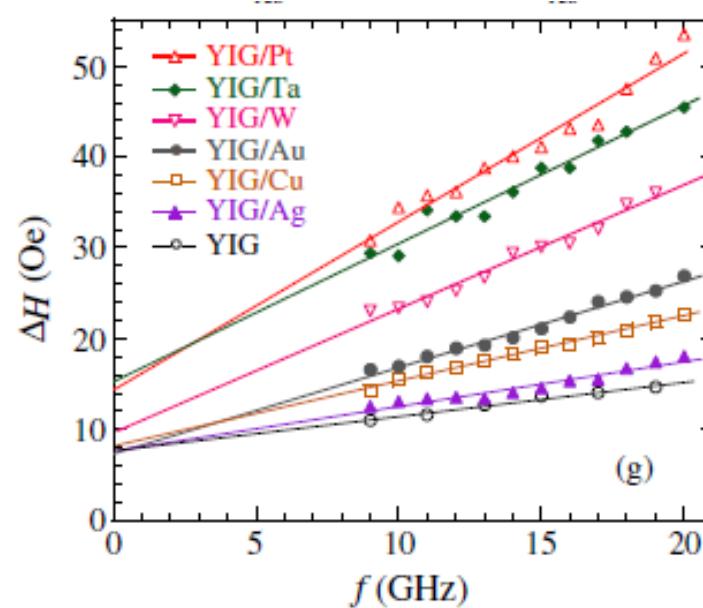
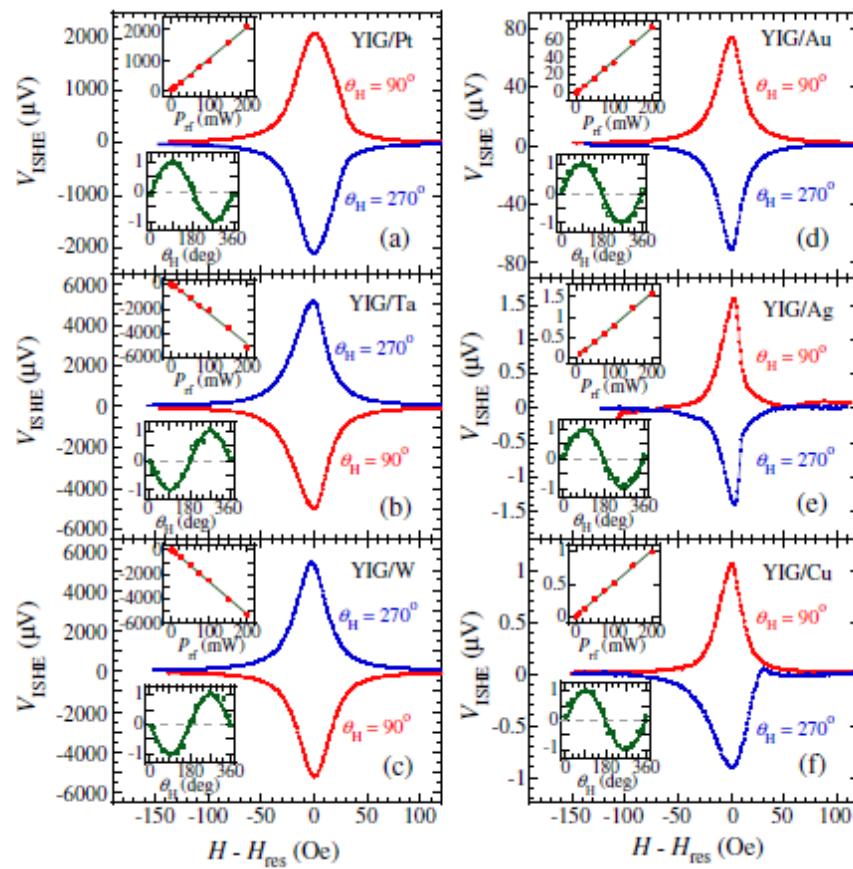
Need to get the thickness dependence data to calculate the spin Hall angle

# Scaling of Spin Hall Angle in 3d, 4d, and 5d Metals from $\text{Y}_3\text{Fe}_5\text{O}_{12}$ /Metal Spin Pumping

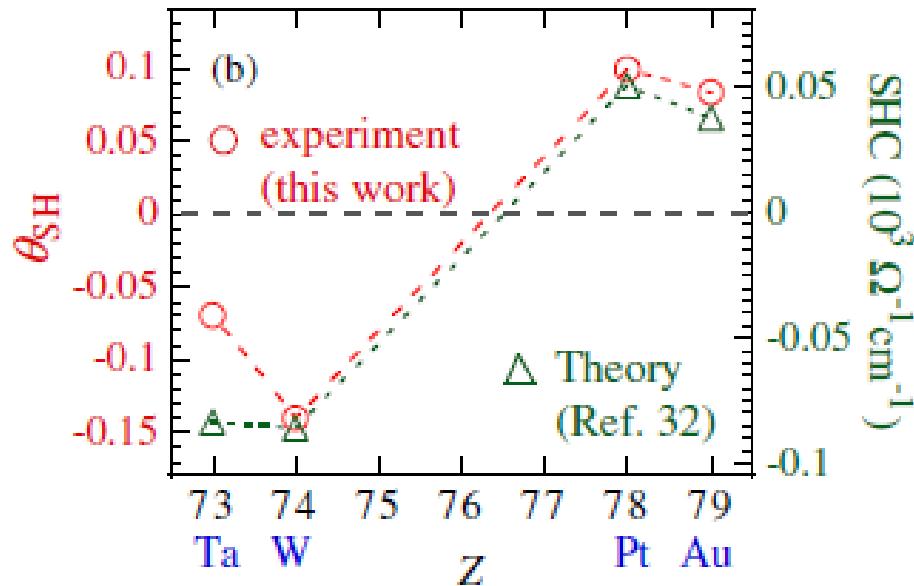
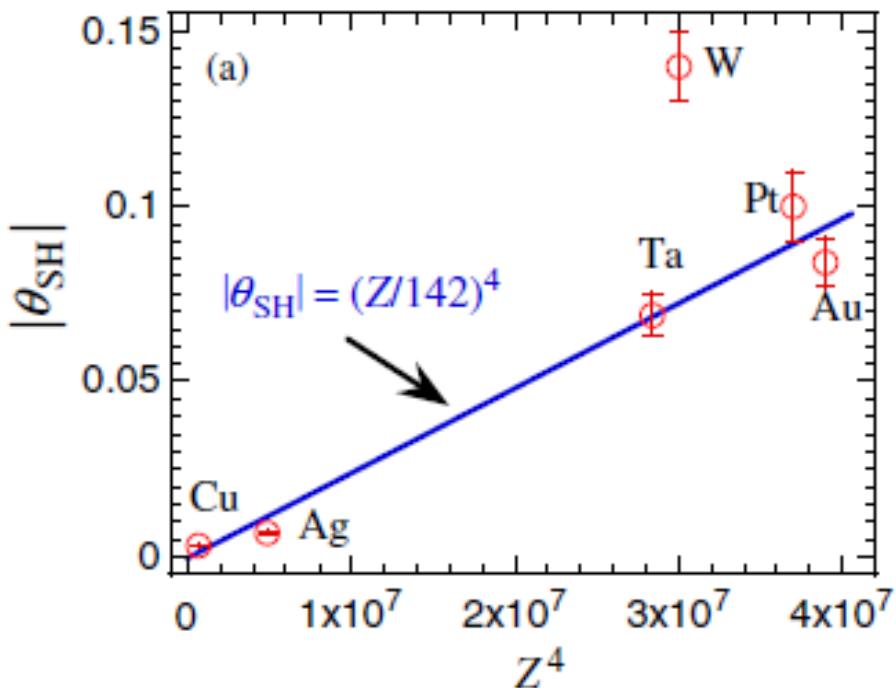
H. L. Wang,<sup>1</sup> C. H. Du,<sup>1</sup> Y. Pu,<sup>1</sup> R. Adur,<sup>1</sup> P. C. Hammel,<sup>1,\*</sup> and F. Y. Yang<sup>1,†</sup>

<sup>1</sup>*Department of Physics, The Ohio State University, Columbus, Ohio 43210, USA*

(Received 23 September 2013; revised manuscript received 24 December 2013; published 15 May 2014)



Bilayer	$V_{\text{ISHE}}$	$\Delta H$ change	$\alpha_{\text{sp}}$	$\rho(\Omega m)$	$g_{\uparrow\downarrow}(\text{m}^{-2})$	$\lambda_{\text{SD}}(\text{nm})$	$\theta_{\text{SH}}$	$J_s(\text{A/m}^2)$
YIG/Pt	2.10 mV	24.3 Oe	$(3.6 \pm 0.3) \times 10^{-3}$	$4.8 \times 10^{-7}$	$(6.9 \pm 0.6) \times 10^{18}$	7.3	$0.10 \pm 0.01$	$(2.0 \pm 0.2) \times 10^7$
YIG/Ta	-5.10 mV	16.5 Oe	$(2.8 \pm 0.2) \times 10^{-3}$	$2.9 \times 10^{-6}$	$(5.4 \pm 0.5) \times 10^{18}$	1.9	$-0.071 \pm 0.006$	$(1.6 \pm 0.2) \times 10^7$
YIG/W	-5.26 mV	12.3 Oe	$(2.4 \pm 0.2) \times 10^{-3}$	$1.8 \times 10^{-6}$	$(4.5 \pm 0.4) \times 10^{18}$	2.1	$-0.14 \pm 0.01$	$(1.4 \pm 0.1) \times 10^7$
YIG/Au	72.6 $\mu\text{V}$	5.50 Oe	$(1.4 \pm 0.1) \times 10^{-3}$	$4.9 \times 10^{-8}$	$(2.7 \pm 0.2) \times 10^{18}$	60	$0.084 \pm 0.007$	$(7.6 \pm 0.7) \times 10^6$
YIG/Ag	1.49 $\mu\text{V}$	1.30 Oe	$(2.7 \pm 0.2) \times 10^{-4}$	$6.6 \times 10^{-8}$	$(5.2 \pm 0.5) \times 10^{17}$	700	$0.0068 \pm 0.0007$	$(1.5 \pm 0.1) \times 10^6$
YIG/Cu	0.99 $\mu\text{V}$	3.70 Oe	$(8.1 \pm 0.6) \times 10^{-4}$	$6.3 \times 10^{-8}$	$(1.6 \pm 0.1) \times 10^{18}$	500	$0.0032 \pm 0.0003$	$(4.6 \pm 0.4) \times 10^6$



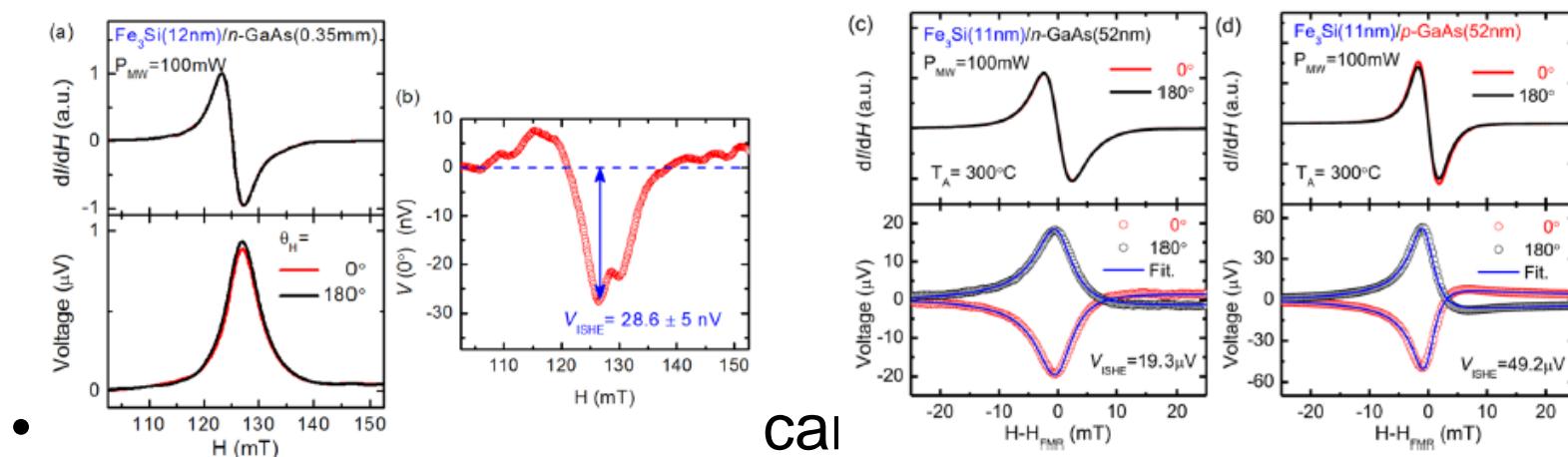
Spin Hall angles strongly depend on the d-electron count.

	<i>T</i> (K)	$\lambda_{sd}$ (nm)	$\sigma_{NM}$ ( $10^6$ S/m)	$\alpha_{SH}$ (%)		<i>T</i> (K)	$\lambda_{sd}$ (nm)	$\sigma_{NM}$ ( $10^6$ S/m)	$\alpha_{SH}$ (%)
Al	4.2	$455 \pm 15$	10.5	$0.032 \pm 0.006$	Mo	10	10	3.03	-0.20
	4.2	$705 \pm 30$	17	$0.016 \pm 0.004$		10	10	0.667	-0.075
Au	295	$86 \pm 10$	37	11.3	Nb	10	$8.6 \pm 1.3$	2.8	$-(0.8 \pm 0.18)$
	295	83	37	3		295	$35 \pm 3^*$	4.66	$-(0.05 \pm 0.01)$
	4.5	$65^*$	48.3	$<2.3$		10	$5.9 \pm 0.3$	1.1	$-(0.87 \pm 0.20)$
	295	$36^*$	25.7	$<2.7$		295	$13 \pm 2$	2.2	$1.2 \pm 0.4$
	295	$35 \pm 4$	28	$7.0 \pm 0.1$		295	$9^*$	1.97	1.0
	295	$27 \pm 3$	14	$7.0 \pm 0.3$		295	$15 \pm 4^*$	4.0	$0.64 \pm 0.10$
	295	$25 \pm 3$	14.5	$12 \pm 4$		295	$5.5 \pm 0.5$	5	$1.2 \pm 0.3$
	295	$50 \pm 8$	16.7	$0.8 \pm 0.2$		295	$2.0 \pm 0.1$	3.7	$0.8 \pm 0.20$
	<10	$40 \pm 16$	25	$1.4 \pm 0.4$	Pt	295		6.41	0.37
	295	$35 \pm 3^*$	25.2	$0.35 \pm 0.03$		5	8	8.0	0.44
AuW	295	35	20	$0.25 \pm 0.1$		295	7	5.56	0.9
	295	$35 \pm 3^*$	5.25	$1.6 \pm 0.1$		10	$11 \pm 2$	8.1	$2.1 \pm 0.5$
	295	$35 \pm 3^*$	7	$0.335 \pm 0.006$		10	$\sim 10$	8.1	2.4
	295	$35^*$		$1.1 \pm 0.3$		295	$7^*$	6.4	8.0
	295	60	20.4	$8.4 \pm 0.7$		295	$10 \pm 2^*$	2.4	$1.3 \pm 0.2$
	295	1.9	1.75	>10		295	$10^*$	2	4.0
	295	700	15	$0.7 \pm 0.1$		295	$3.7 \pm 0.2$	2.42	$8 \pm 1$
	Bi	$0.3 \pm 0.1$	-	>0.3		295	$8.3 \pm 0.9$	$4.3 \pm 0.2$	$1.2 \pm 0.2$
		-	$2.4 \pm 0.3(I)$	$-(7.1 \pm 0.8)(I)$		295	$7.7 \pm 0.7$	$1.3 \pm 0.1$	$1.3 \pm 0.1$
Cu	295		$50 \pm 12(V)$	$1.9 \pm 0.2(V)$		295	$1.5 - 10^*$	$2.45 \pm 0.1$	$3^{+4}_{-1.5}$
						295	4	4	$2.7 \pm 0.5$
	295	500	16	$0.32 \pm 0.03$		295	$8 \pm 1^*$	1.02	$2.012 \pm 0.003$
	10	5–30		$2.1 \pm 0.6$		295	$1.3^*$	2.4	$2.1 \pm 1.5$
CuIr				$0.7(Ta) \cdot 2.6(Ir)$		295	1.2		$8.6 \pm 0.5$
CuMn T						295	$14^*$		$12 \pm 4$

1. The larger spin Hall angles, the shorter spin diffusion lengths.
  2. Depending on techniques, materials preparation and geometry, the calculated spin Hall angle can vary by 1 order of magnitude.
  3. Rashba effect (broken inversion symmetry) at the interface adds complexity to analyses.
- |                |     |          |                   |                |     |     |     |                 |               |
|----------------|-----|----------|-------------------|----------------|-----|-----|-----|-----------------|---------------|
| $\text{IrO}_2$ | 300 | $3.8(P)$ | $0.5(P), 0.18(A)$ | $4(P), 6.5(A)$ | $W$ | 295 | 2.1 | $0.55$          | $-14 \pm 1$   |
|                |     |          |                   |                |     | 295 |     | $0.38 \pm 0.06$ | $-(33 \pm 6)$ |

# Spurious effects

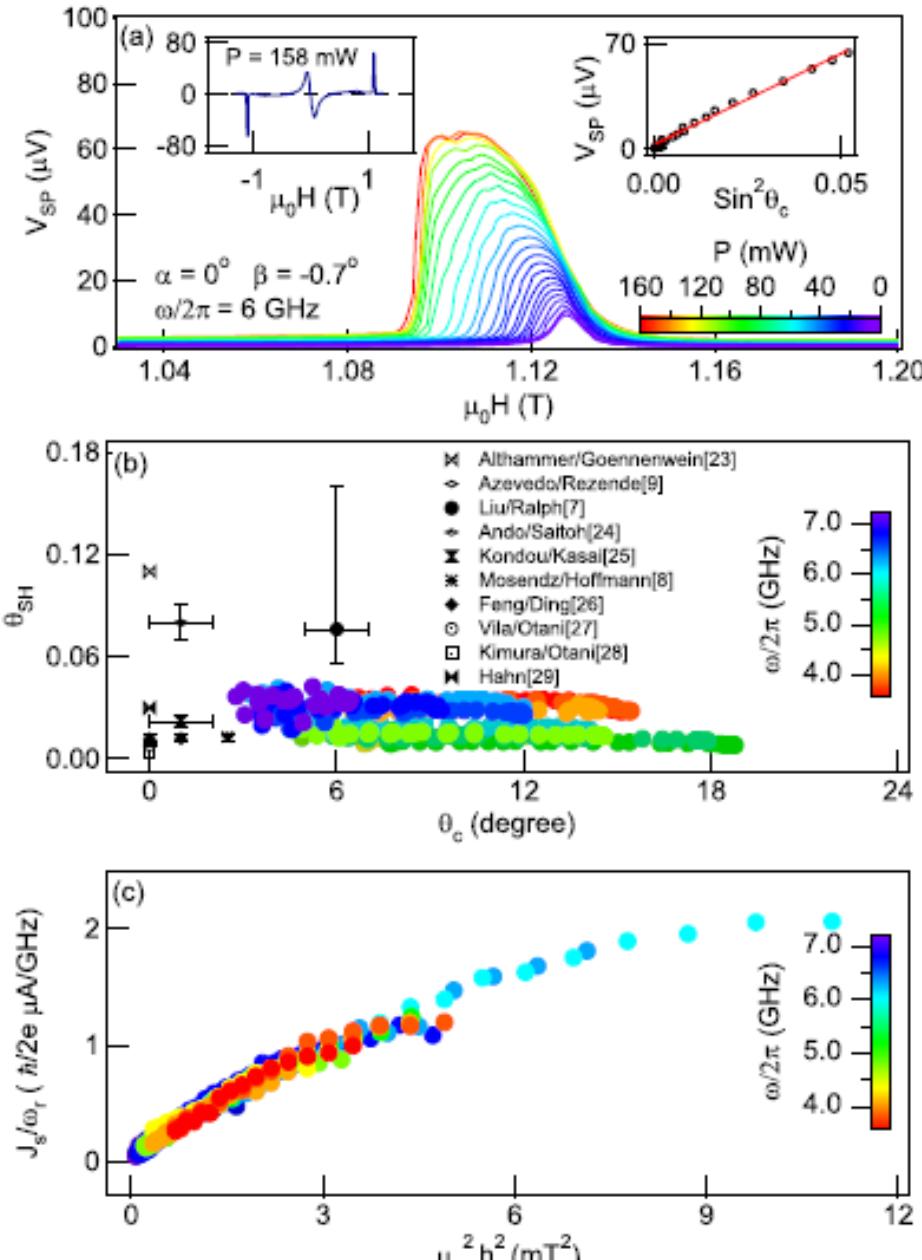
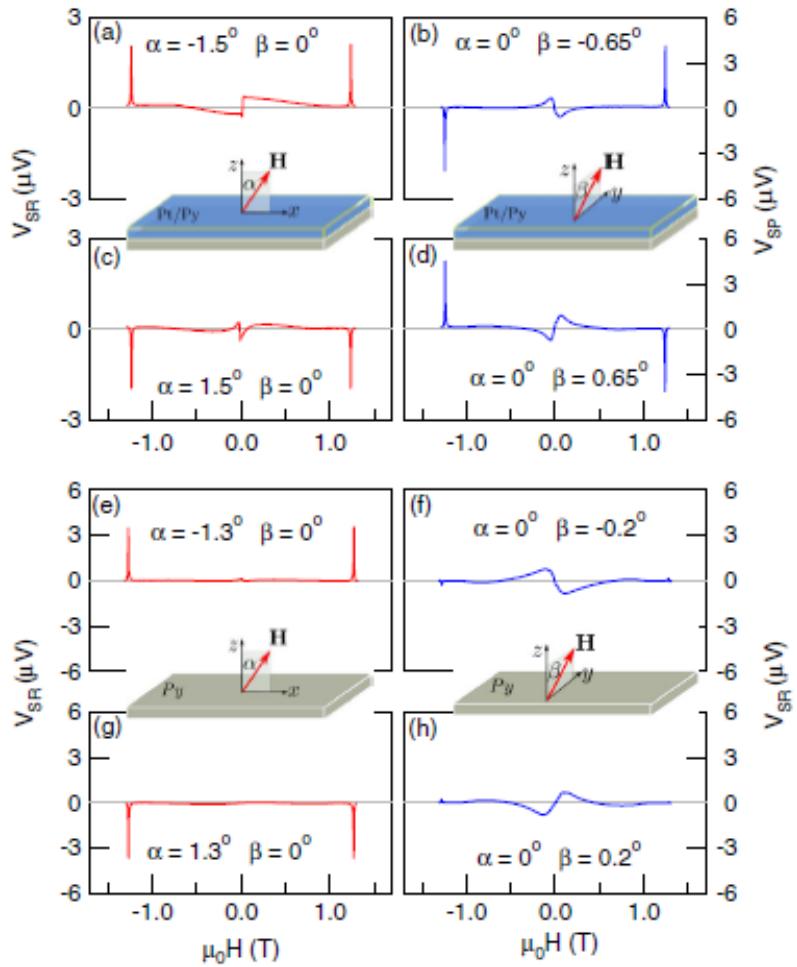
- Microwave induced Seebeck effect in semiconductor.



- - the boundary conditions, phase shift between E and B field can strongly affect voltage signals.

- Self-induced ISHE and spin backflow. (can be prevented by YIG)

# Universal Method for Separating Spin Pumping from Spin Rectification Voltage of Ferromagnetic Resonance



# Spin-torque ferromagnetic resonance (ST-FMR)

PRL 106, 036601 (2011)

PHYSICAL REVIEW LETTERS

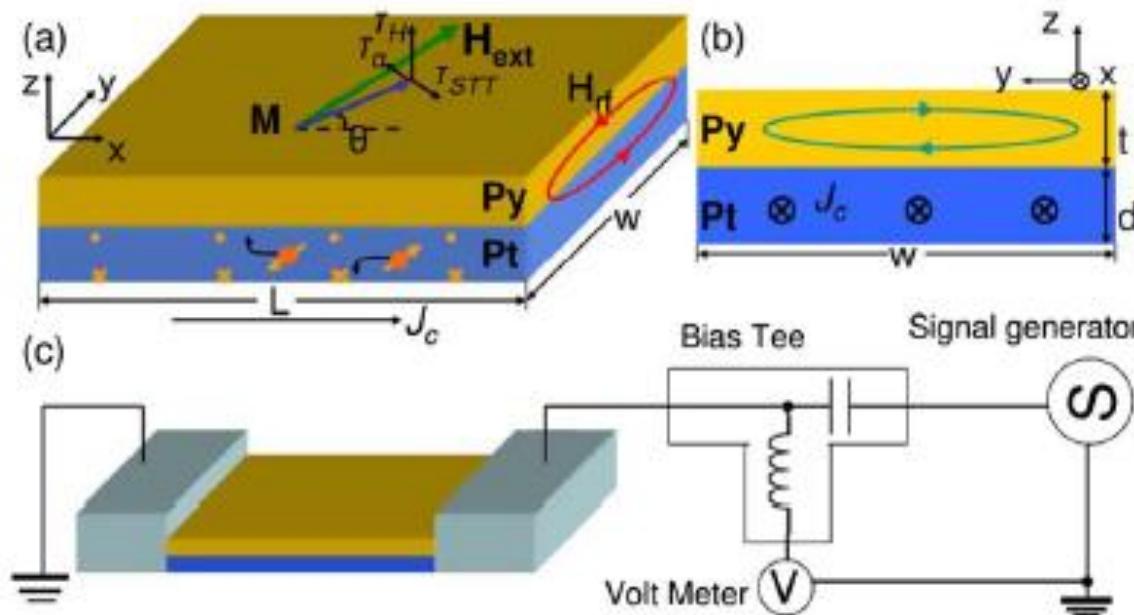
week ending  
21 JANUARY 2011

## Spin-Torque Ferromagnetic Resonance Induced by the Spin Hall Effect

Luqiao Liu, Takahiro Moriyama, D. C. Ralph, and R. A. Buhrman

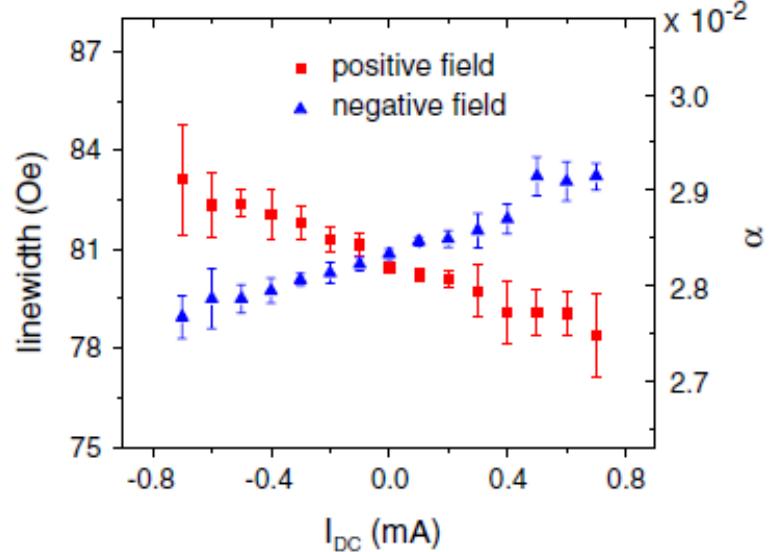
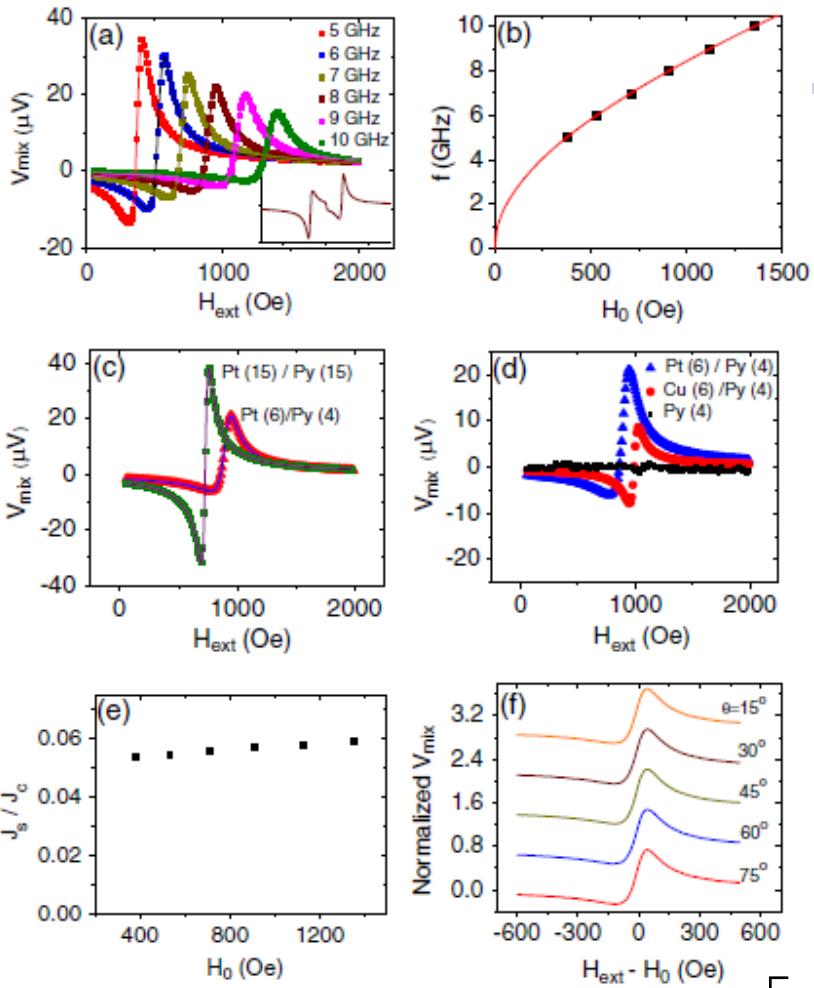
Cornell University, Ithaca, New York, 14853

(Received 12 October 2010; published 20 January 2011)



$$\frac{d\hat{m}}{dt} - \gamma \hat{m} \times \vec{H}_{eff} + \alpha \hat{m} \times \frac{d\hat{m}}{dt} + \gamma \frac{\hbar}{2e\mu_0 M_s t} J_{S,rf} \left( \hat{m} \times \hat{\sigma} \times \hat{m} \right) - \gamma \hat{m} \times \vec{H}_{rf}$$

Anti-damp torques



Rely on AMR to generate voltage signals. Not suitable for magnetic insulator.  
Special case: Pt/YIG, Ta/YIG...

$$V_{mix} = -\frac{1}{4} \frac{dR}{d\theta} \frac{\gamma I_{rf} \cos \theta}{\Delta 2\pi (df/dH)|_{H_{ext}=H_0}} \left[ S \frac{\Delta^2}{\Delta^2 + (H_{ext} - H_0)^2} + A \frac{(H_{ext} - H_0)\Delta}{\Delta^2 + (H_{ext} - H_0)^2} \right]$$

$$\frac{J_{S,rf}}{J_{C,rf}} = \frac{S}{A} \frac{e\mu_0 M_S t d}{\hbar} \left[ 1 + \left( \frac{4\pi M_{eff}}{H_{ext}} \right) \right]^{1/2}$$

The spin Hall angle can be determined from the relative magnitude of the two components.

# Modulation of magnetization damping (MOD)

PRL 101, 036601 (2008)

PHYSICAL REVIEW LETTERS

week ending  
18 JULY 2008

## Electric Manipulation of Spin Relaxation Using the Spin Hall Effect

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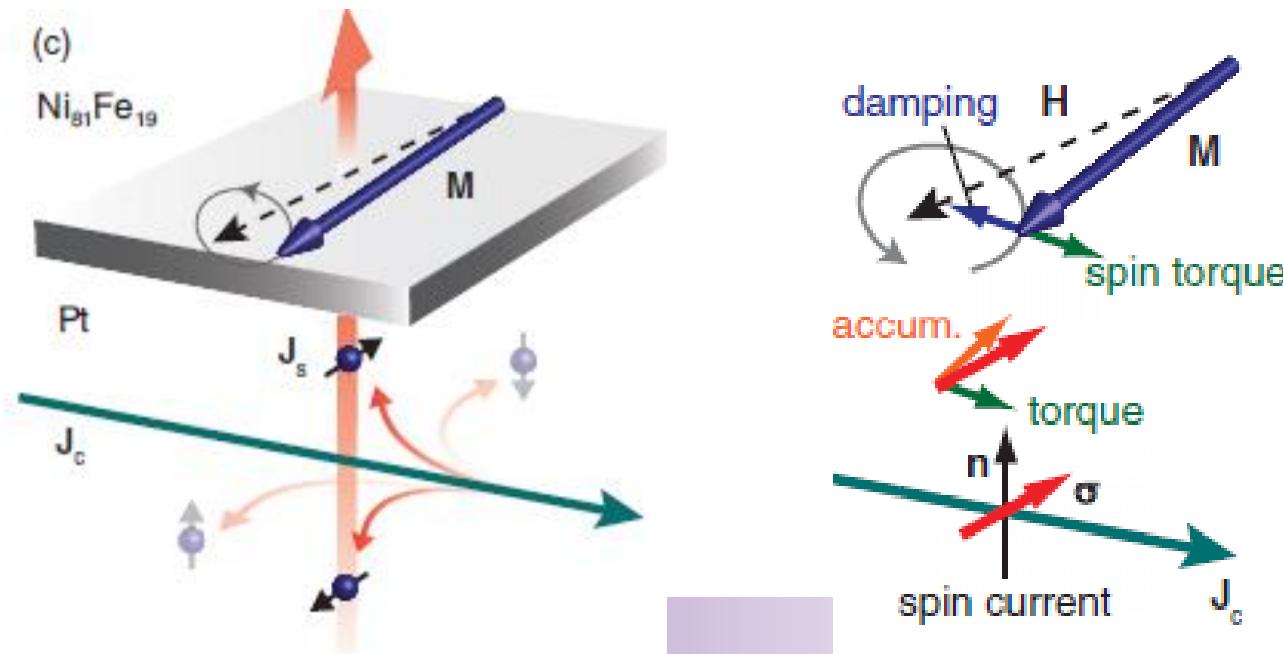
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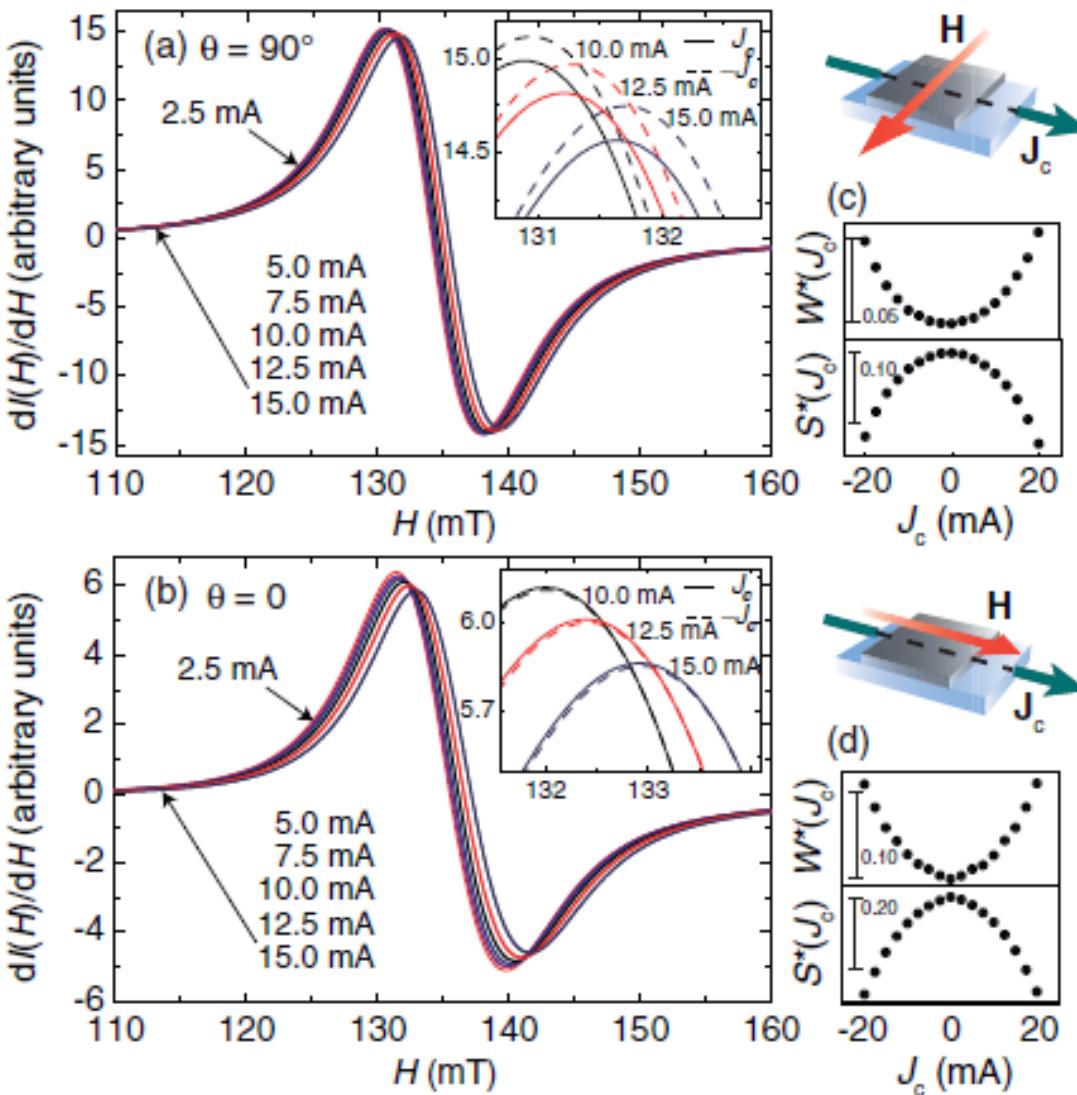
<sup>3</sup>*CREST, Japan Science and Technology Agency, Kawaguchi, Saitama 332-0012, Japan*

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(Received 17 March 2008; published 18 July 2008)



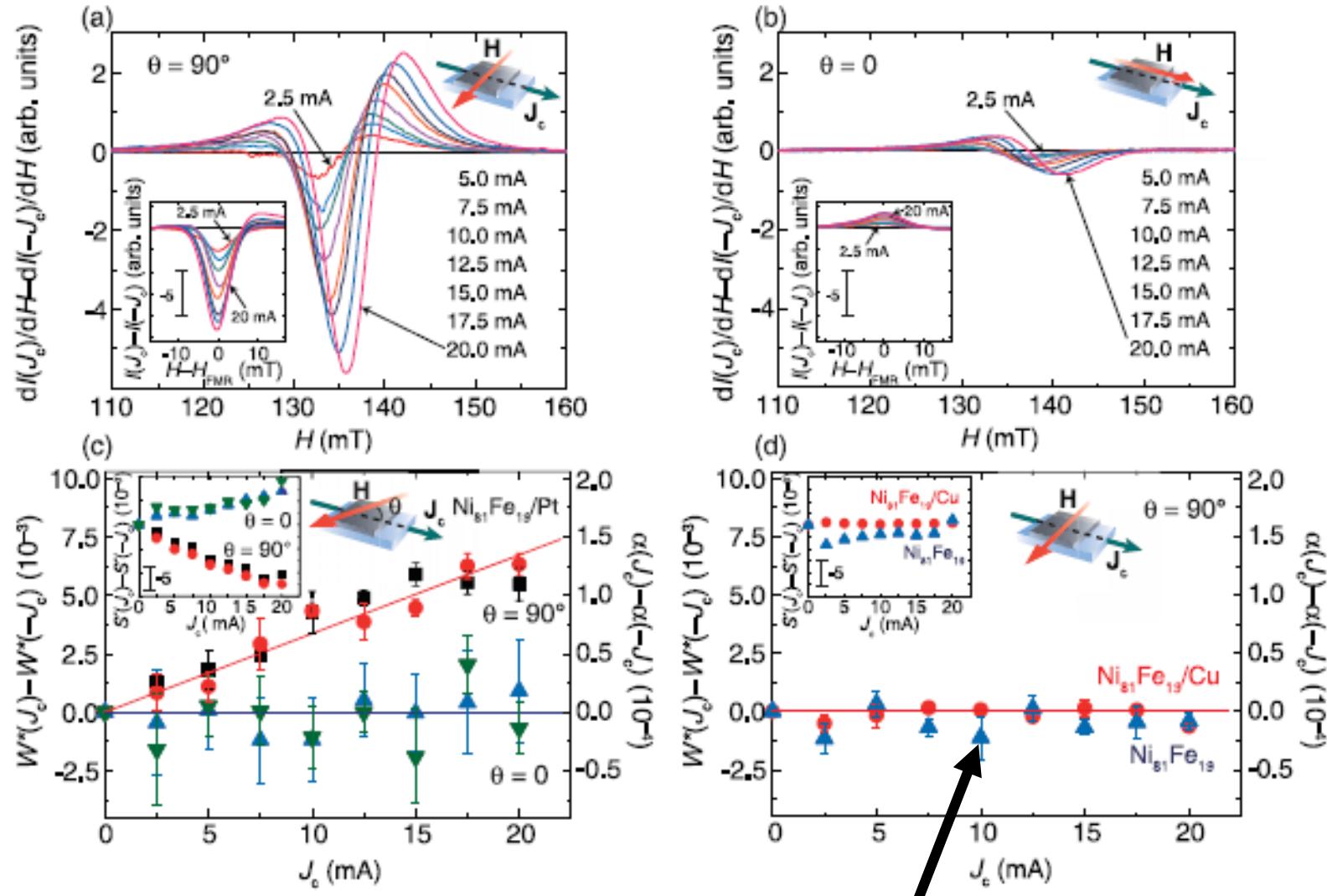
# Modulation of magnetization damping (MOD)



Thermal effects on FMR spectra can be serious.

Need to change the in-plane field angle to separate the spin-transfer effect from the thermal effect.

# Modulation of magnetization damping (MOD)



Controlled sample Py/Cu: Cu  
 has small spin Hall angle.





# Investigation of interfacial and spin transport properties of topological insulator/magnetic insulator heterostructures by spin pumping

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# Outline

## Introduction

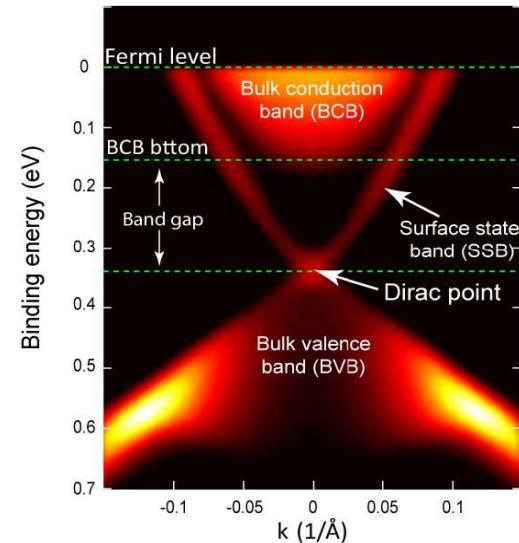
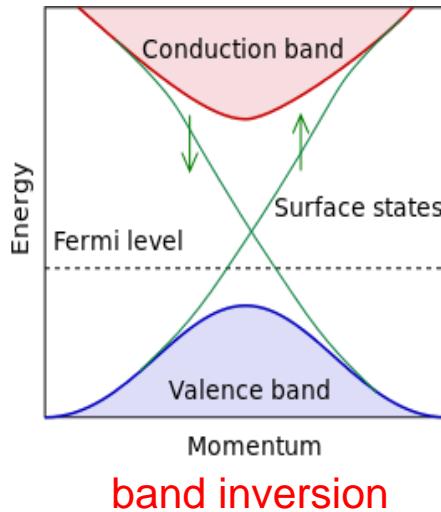
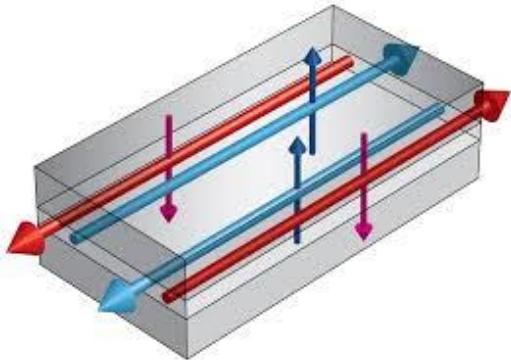
- Spin pumping in topological insulators (TIs)
- Magnetic proximity effect (MPE) in TI/magnetic insulator heterostructures

## Experimental results

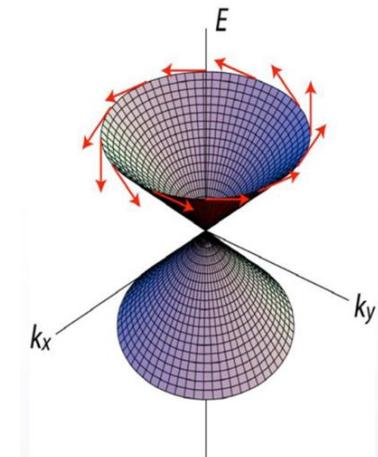
- Spin pumping and spin-to-charge conversion (SCC) in TI/ferromagnetic metals and Py/Al<sub>2</sub>O<sub>3</sub>/Bi<sub>2</sub>Se<sub>3</sub>
- Surface-state-modulated magnetization dynamics in Bi<sub>2</sub>Se<sub>3</sub>/YIG
- Signatures of MPE in Bi<sub>2</sub>Se<sub>3</sub>/YIG and zero-field FMR
- Negative magnetoresistance (MR) and exchange gap opening in Bi<sub>2</sub>Se<sub>3</sub>/ReIG
- Spin pumping and SCC in transferred Bi<sub>2</sub>Se<sub>3</sub>/Au/YIG

## Conclusions

# Topological insulators (TI)

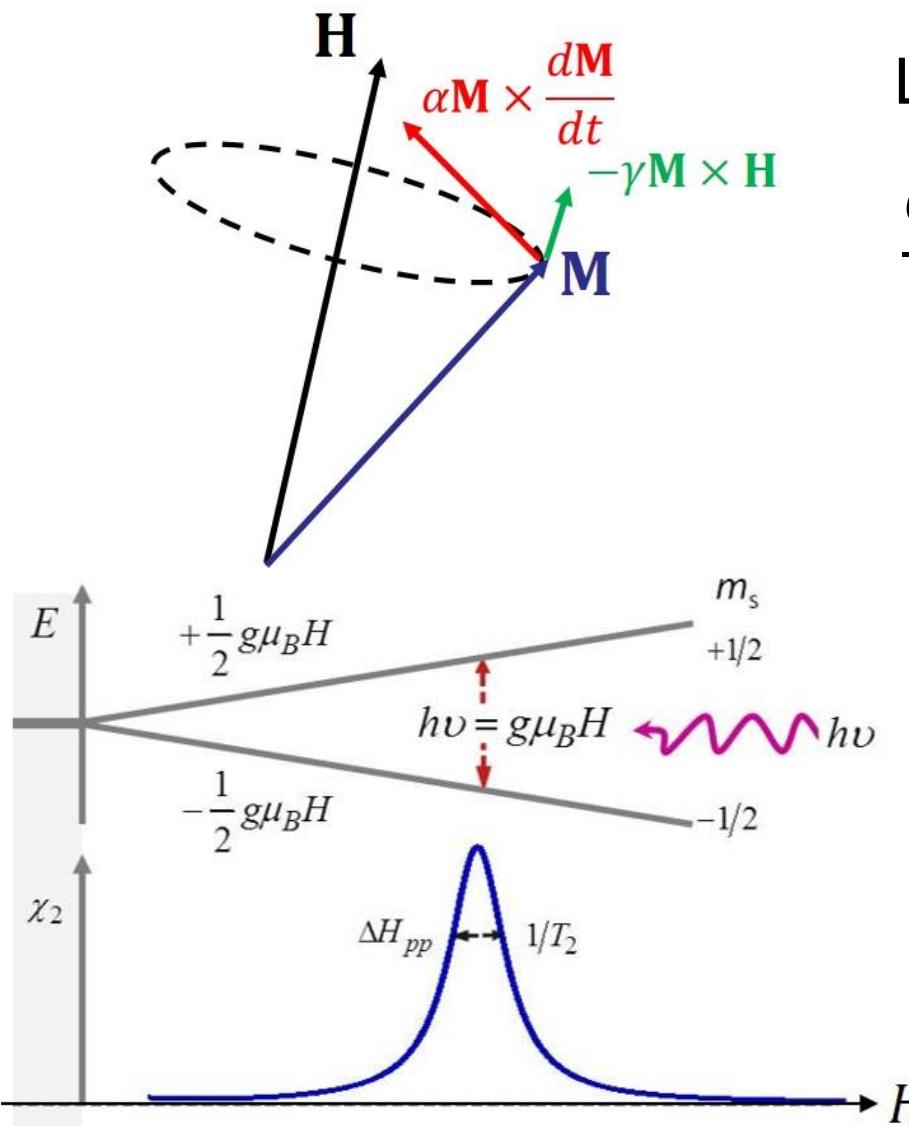


Electronic band structure along K- $\Gamma$ -K of undoped  $\text{Bi}_2\text{Se}_3$  by ARPES, Y. L. Chen et al, Science, (2010).



- Extraordinary physical properties
  - Quantum spin Hall state
  - Strong spin orbit coupling + time-reversal symmetry  
⇒ Spin-momentum locking
- Applications
  - Low dissipation spintronics and spin-caloritronics
  - High spin-charge conversion device, such as a “spin battery”.
  - Interface of TI and superconductor - Majorana fermion, quantum computation

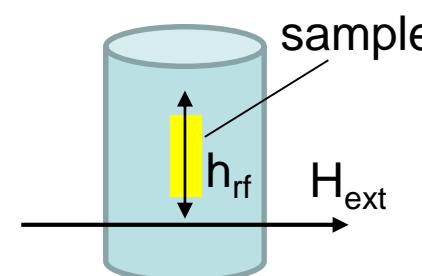
# Ferromagnetic resonance (FMR)



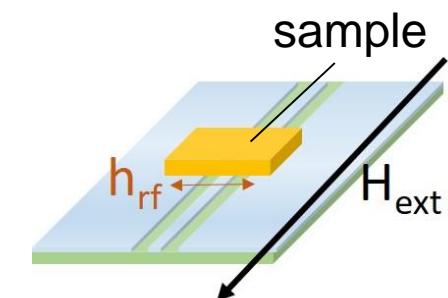
Landau–Lifshitz–Gilbert equation

$$\frac{d\mathbf{M}}{dt} = -\gamma \mathbf{M} \times \mathbf{H} + \alpha \mathbf{M} \times \frac{d\mathbf{M}}{dt}$$

Cavity



Coplanar waveguide



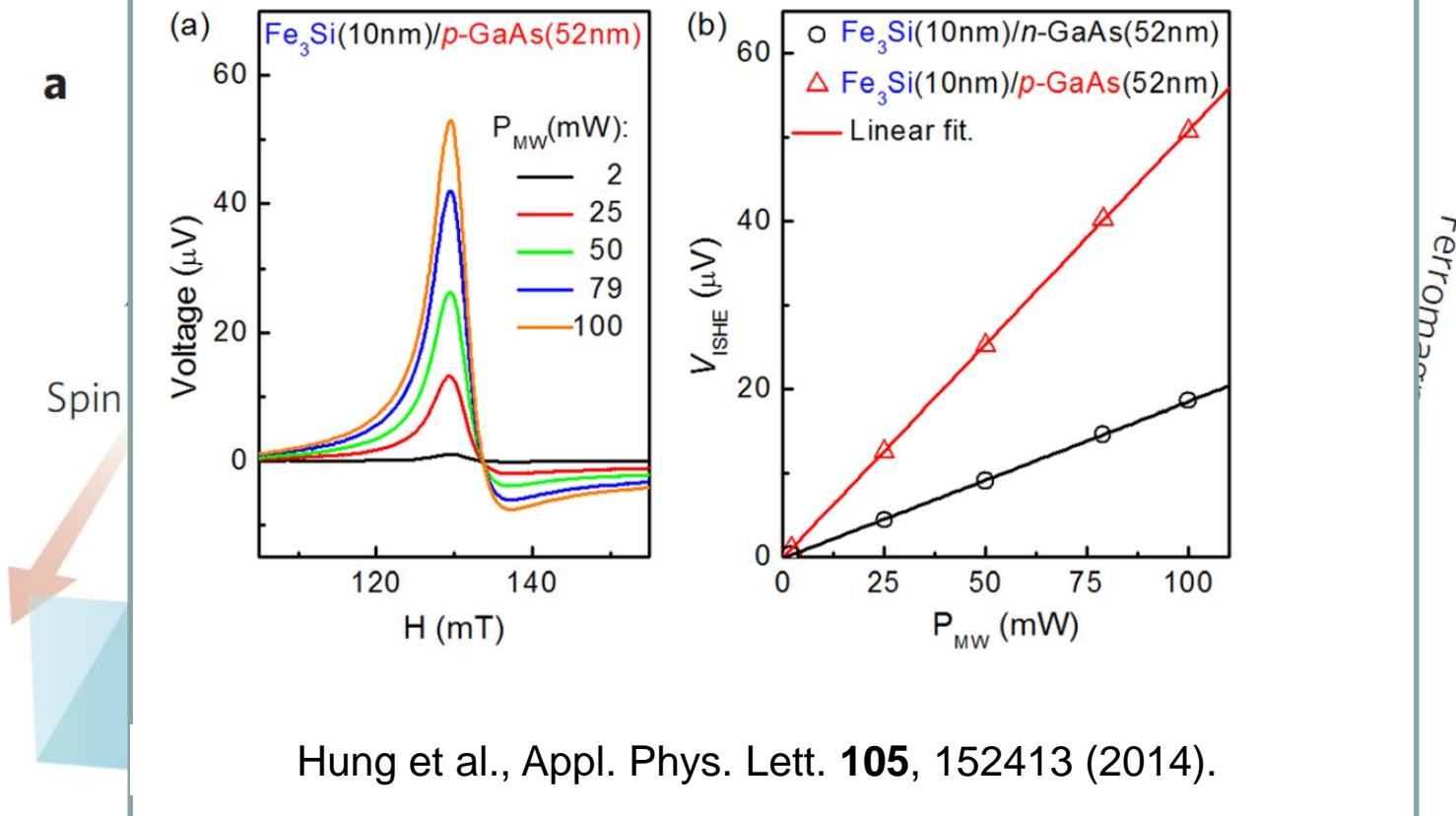
Application:

Measurement of **magnetic anisotropy**

Measurement of **damping constant  $\alpha$**

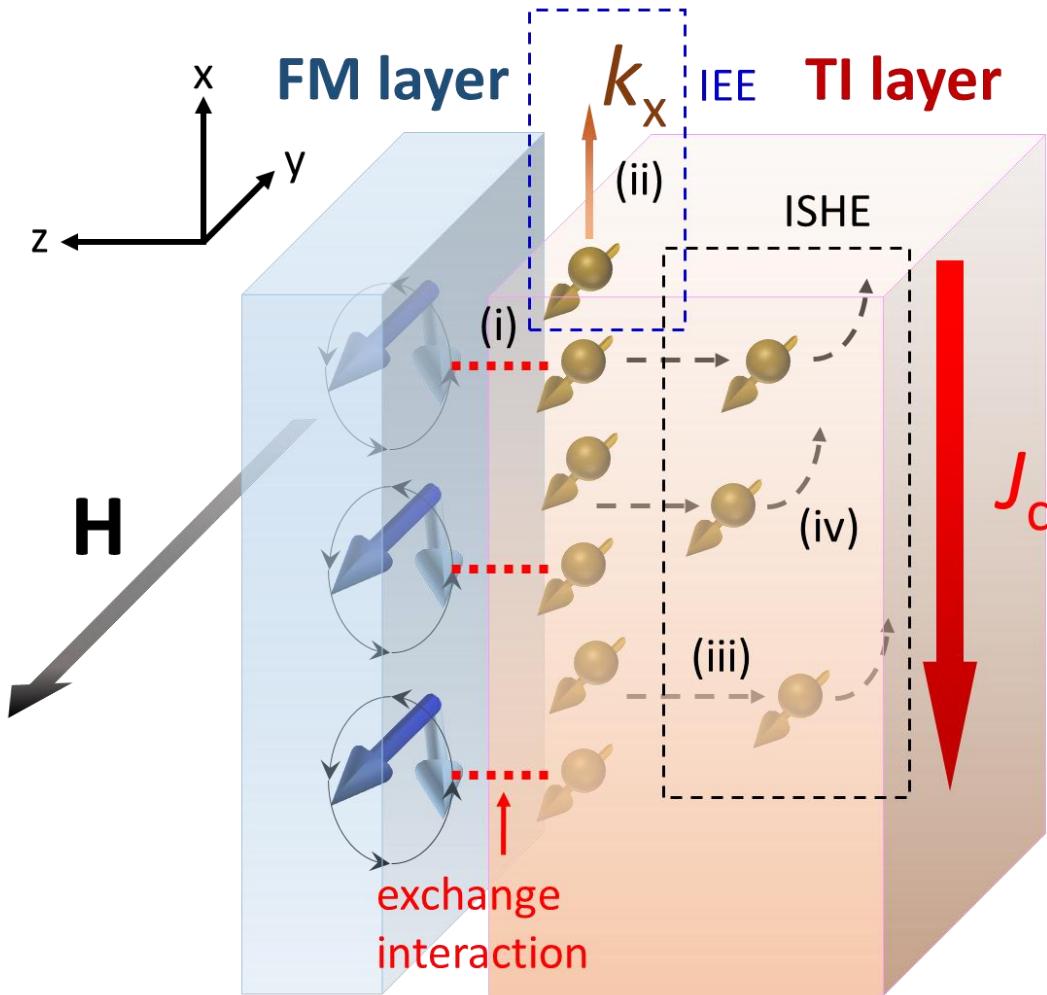
**Spin pumping**

# Spin pumping: a solution to impedance mismatch problem



Ando et al., Nat. Mater. **10**, 655 (2013).

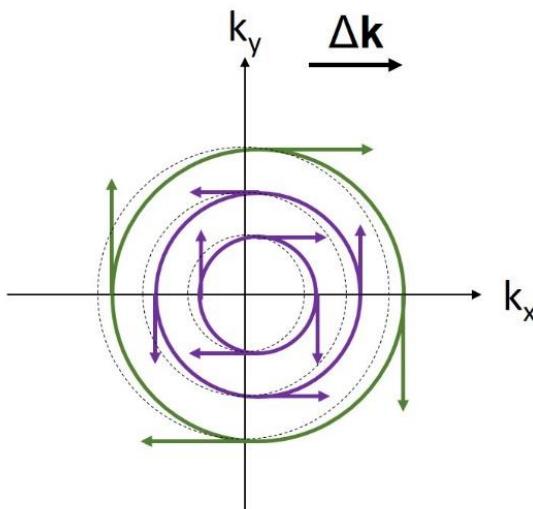
# Concept of "Spin pumping to TI" experiment



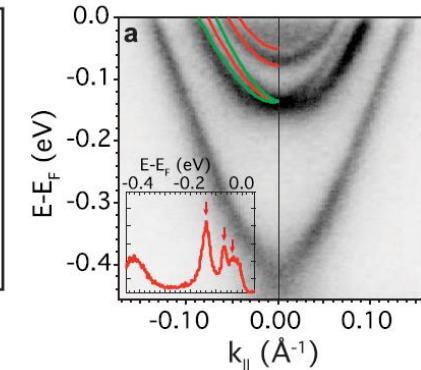
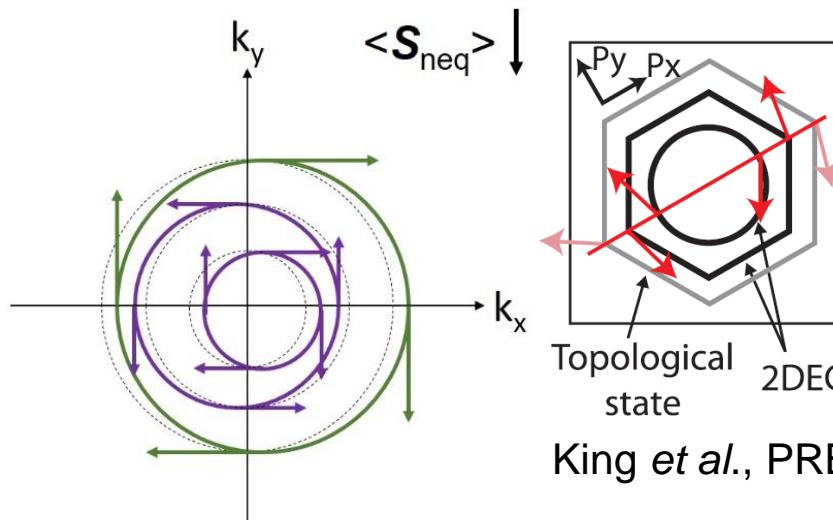
- (i) Spin injection to the TI layer by exchange interaction
- (ii) SCC by spin-momentum locking of TSS
- (iii) Spin diffusion to the TI bulk
- (iv) SCC by SHE of the TI bulk

# Spin-charge conversion in 2D systems

Edelstein effect



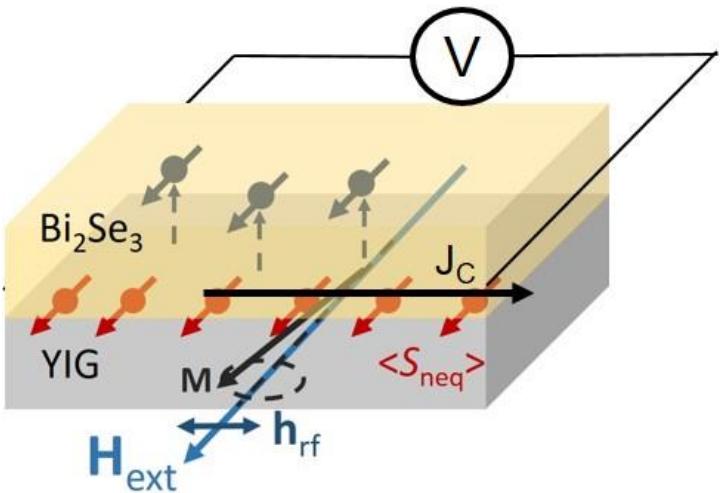
Inverse Edelstein effect



King *et al.*, PRB **107**, 096802 (2011).

	Inverse spin Hall effect (ISHE)	Inverse Edelstein effect (IEE)
location	bulk	surface
condition	Spin current normal to the interface	"non-equilibrium" spin density at interface
material	Normal metals and semiconductors including 3D TIs	TIs and Rashba materials possessing $k$ -dependent spin-polarized states

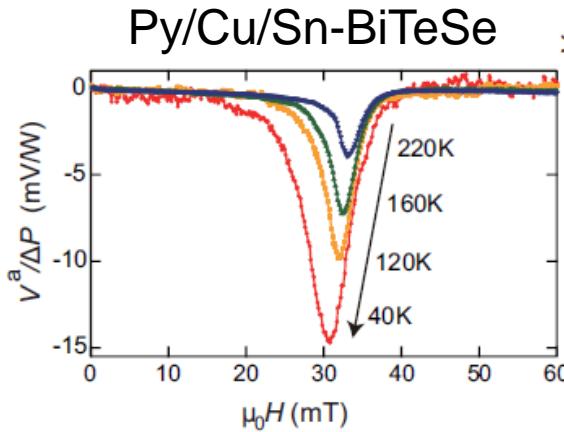
# Spin pumping as an effective way to probe the spin-momentum locking



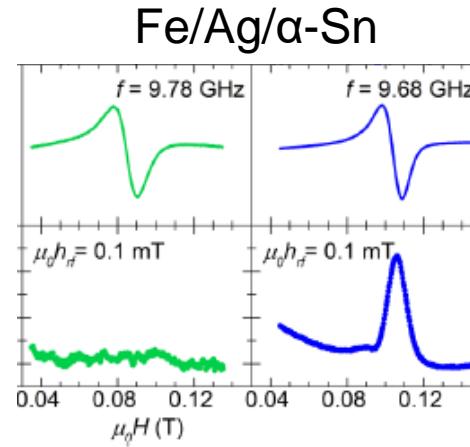
Spin pumping: a widely used spin injection method  
FMR in the magnetic layer  
→ Exchange interaction at the interface: transfer of spin angular momentum  
→ Spin accumulation at the interface  
→ Charge current generated via spin-momentum locking

Various material systems and experimental configurations have been reported.

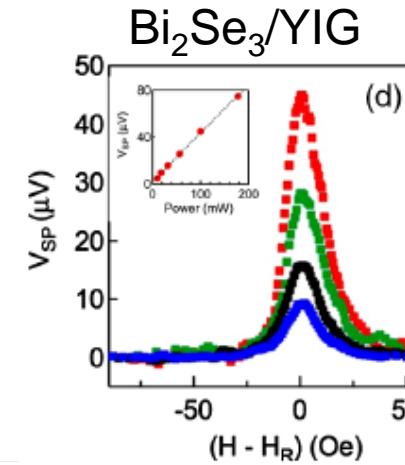
## E. Saitoh group



## A. Fert group



## N. Samarth group



# Challenges of spin pumping into TIs

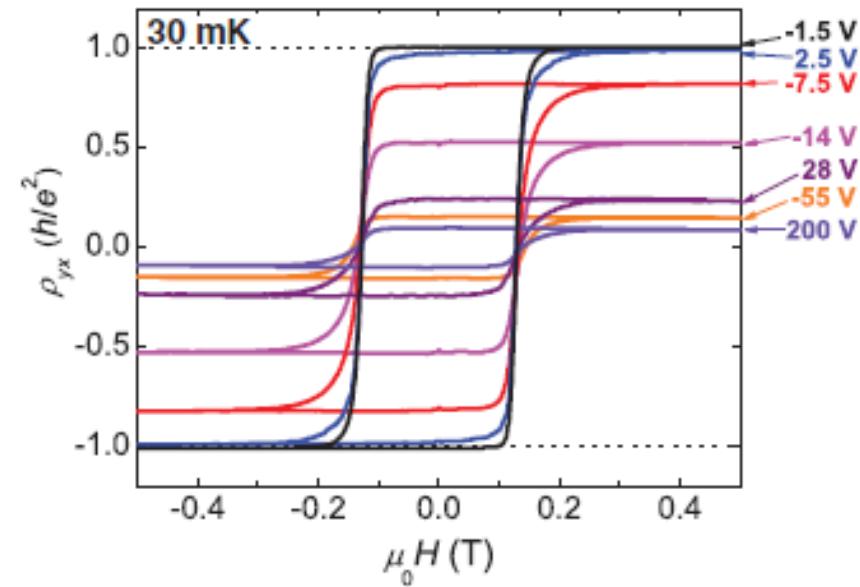
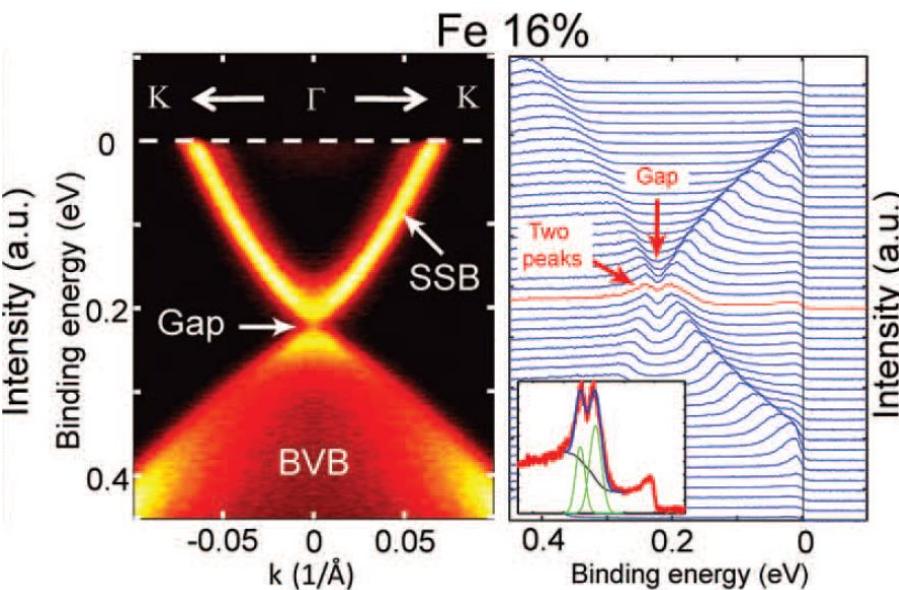
- Bulk conduction of TIs obscures the effect of topological surface states
- Large variation in reported effective spin Hall angle  $\theta_{\text{SH}}$ 
  - **0.022** in  $\text{Bi}_2\text{Se}_3/\text{Py}$  at 15 K (Deorani et al. (2014))
  - **$\sim 10^{-4}$**  in bulk insulating  $\text{Bi}_{1.5}\text{Sb}_{0.5}\text{Te}_{1.7}\text{Se}_{1.3}$  at 15 K (Shiomi et al. (2014))
  - **0.021-0.43** in  $\text{Bi}_2\text{Se}_3/\text{CoFeB}$  at RT (Jamali et al. (2015))
  - **0.27-0.62** in Fe/Ag/ $\alpha$ -Sn at RT (Rojas-Sánchez et al. (2016))
  - **$\sim 0.02$**  in  $\text{Bi}_2\text{Se}_3/\text{YIG}$  at RT (Wang et al. (2016))
- Current shunting effect by ferromagnetic metals in ST-FMR measurement

**Ferrimagnetic insulator YIG with high thermal stability is an ideal spin source.**

# Breaking the time-reversal-symmetry of TI surface state

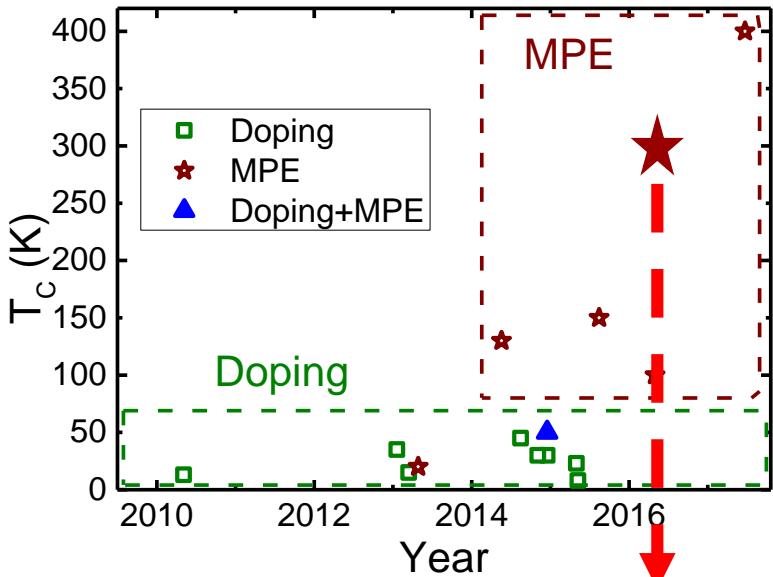
## Experimental observations

1. Gap opening of TI surface states
2. Quantum anomalous Hall effect (QAHE)
3. Topological magnetoelectric effect

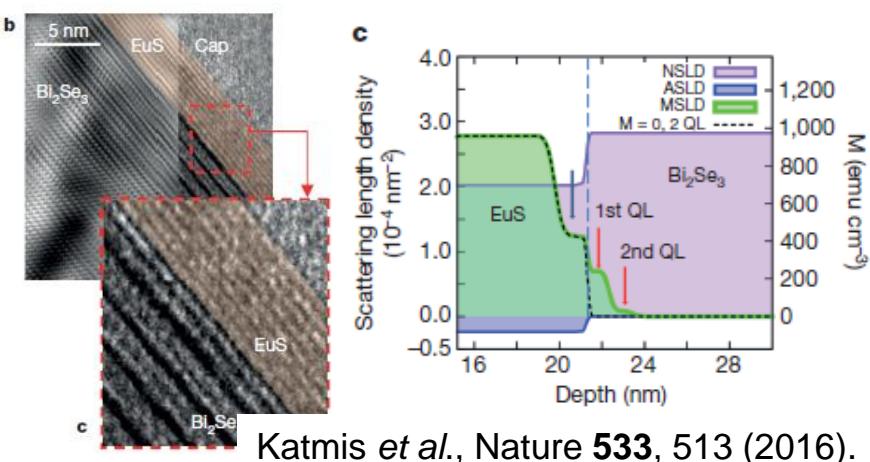


Chen et al., Science **329**, 659 (2010).  
Chang et al., Science **340**, 167 (2013).

# Magnetic proximity effect (MPE) in TI/magnetic layer heterostructures



Discovery of RT MPE in  $\text{EuS}/\text{Bi}_2\text{Se}_3$ , exhibiting an interfacial PMA.



Katmis *et al.*, Nature 533, 513 (2016).

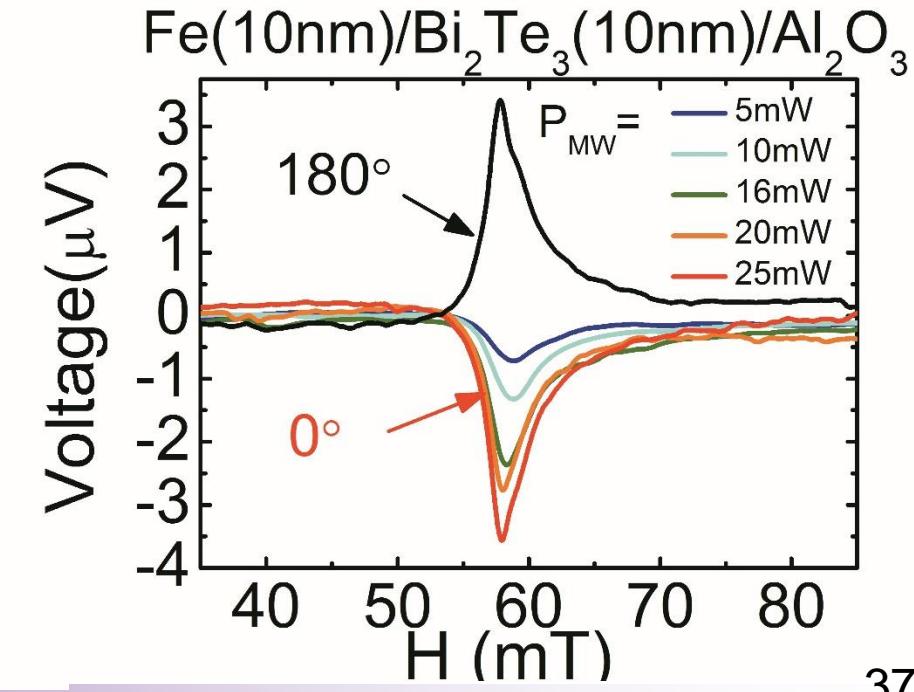
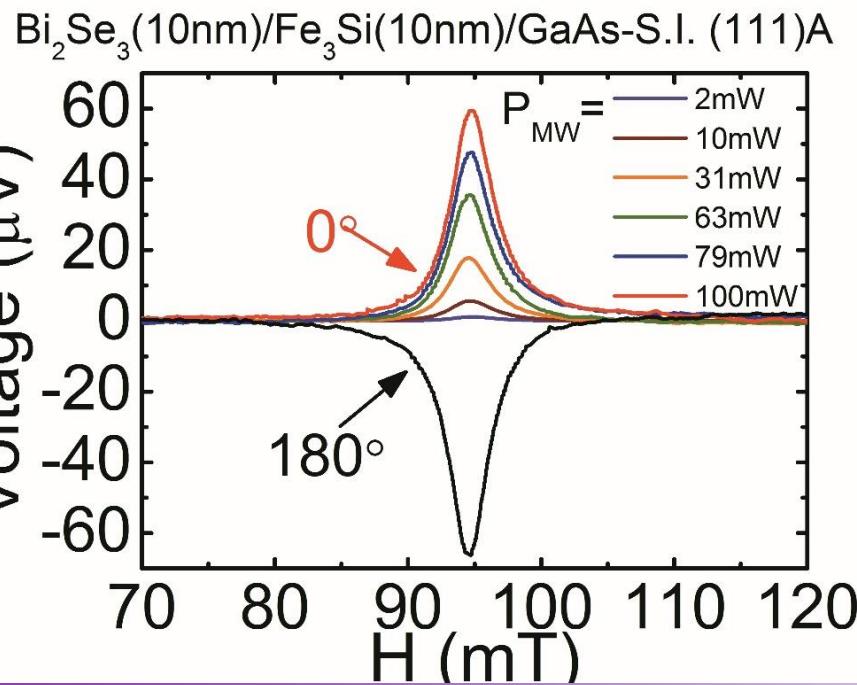
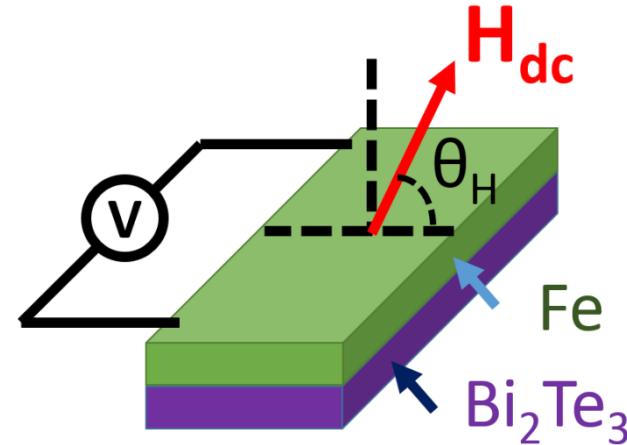
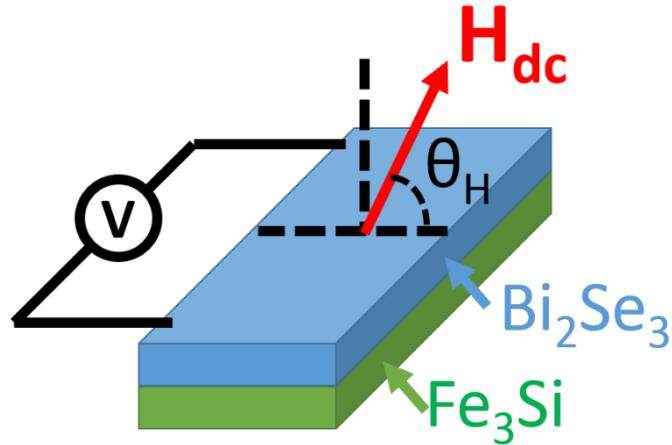
Advantages of using the MPE to break time reversal symmetry:

- Higher  $T_c$  than that of magnetic doping
- No crystal defects
- Uniform magnetization

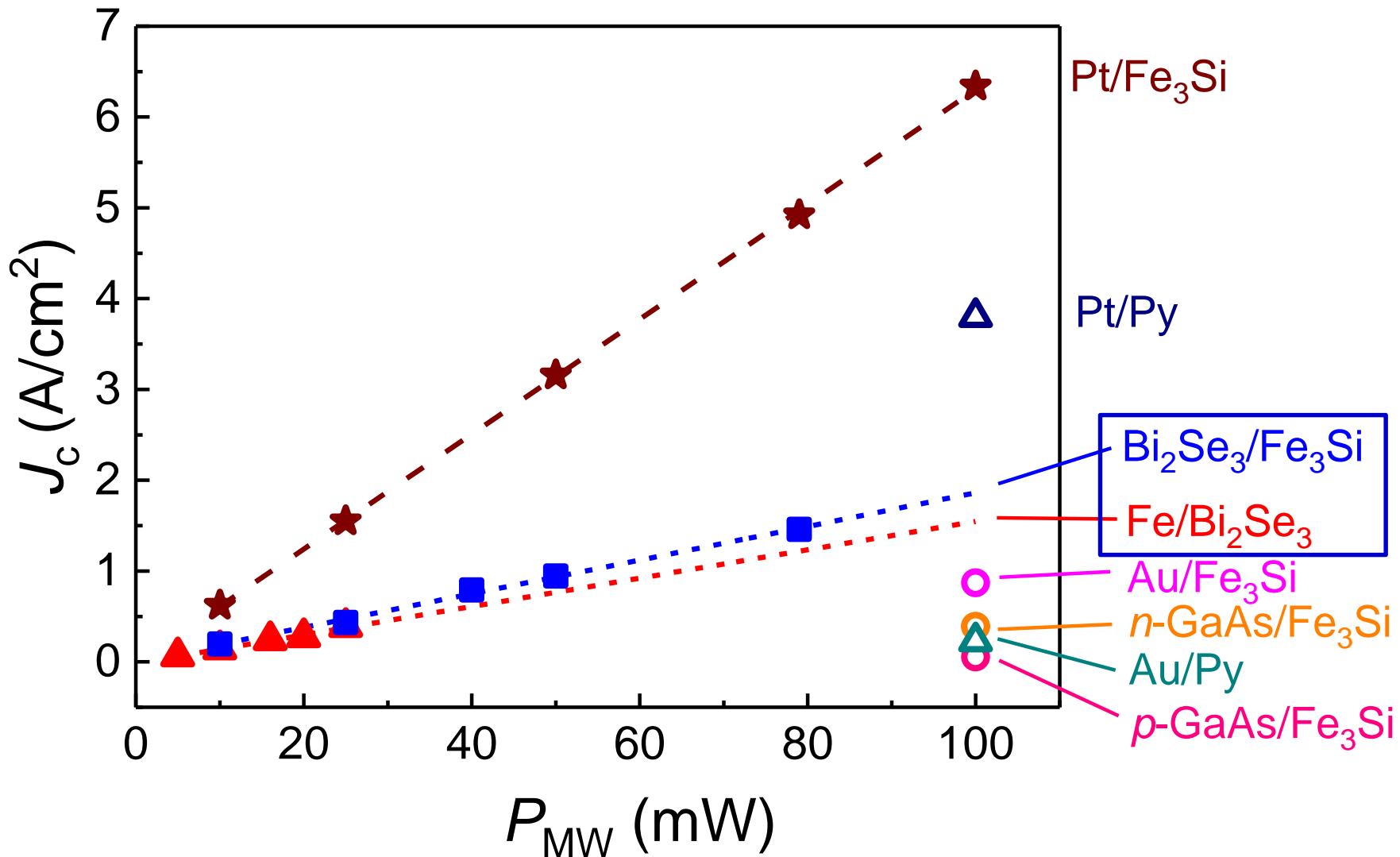
How about MPE and the interfacial magnetic anisotropy in  $\text{Bi}_2\text{Se}_3/\text{YIG}$ ?

**High  $T$  IMA and low  $T$  PMA!**

# Spin Pumping in $\text{Bi}_2\text{Se}_3/\text{Fe}_3\text{Si}$ and $\text{Fe}/\text{Bi}_2\text{Te}_3$ Structures



# Converted Charge Current Density Comparison



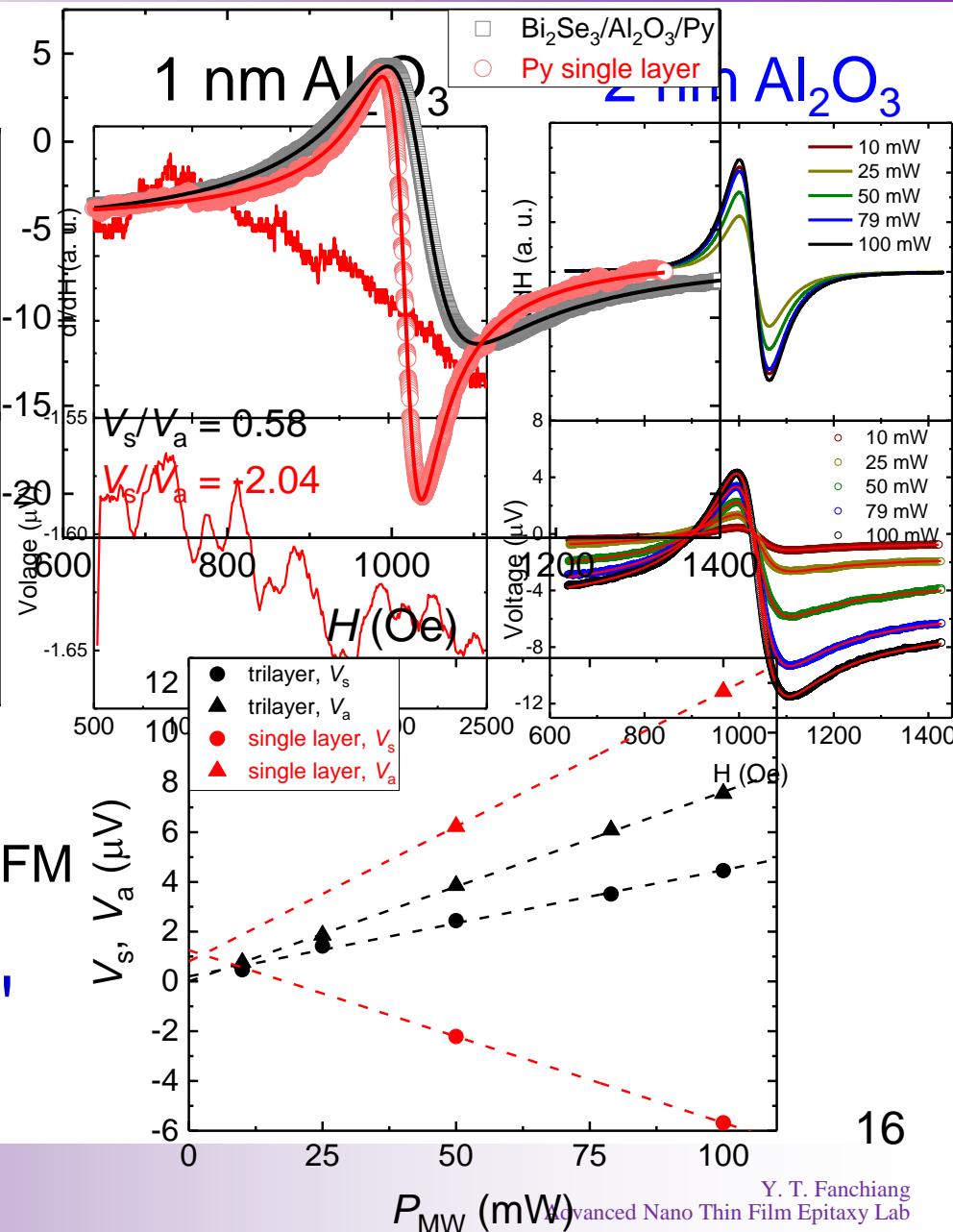
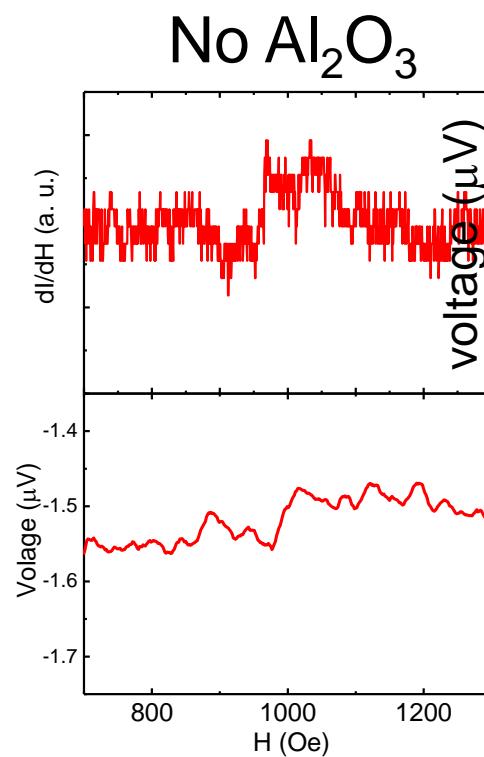
# Comparison of $\theta_{ISHE}$

NM (FM)	Spin mixing conductance ( $m^{-2}$ )	Spin current density ( $Jm^{-2}$ )	Spin Hall Angle $\theta_{ISHE}$	$J_c$ ( $A/cm^2$ )
Bi <sub>2</sub> Se <sub>3</sub> (Fe <sub>3</sub> Si)	$6.66 \times 10^{18}$	$1.98 \times 10^{-9}$	$0.0053 \pm 0.002$	1.32
Bi <sub>2</sub> Te <sub>3</sub> (Fe)	$2.36 \times 10^{18}$	$1.15 \times 10^{-9}$	$0.0068 \pm 0.003$	1.00
p-GaAs(Fe <sub>3</sub> Si)	$5.89 \times 10^{18}$	$8.91 \times 10^{-10}$	0.00019	0.0087
n-GaAs(Fe <sub>3</sub> Si)	$1.46 \times 10^{19}$	$1.53 \times 10^{-9}$	0.000028	0.061
Au (Fe <sub>3</sub> Si)	$4.24 \times 10^{18}$	$6.48 \times 10^{-10}$	0.00505	0.49
Pt (Fe <sub>3</sub> Si)	$1.29 \times 10^{19}$	$1.96 \times 10^{-9}$	0.023	6.34

- ◆ Much larger spin current density and  $\theta_{ISHE}$  than conventional semiconductor GaAs.
- ◆ Comparable to  $\theta_{ISHE} \sim 0.009$  from S. Oh et al
- ◆ Comparable ISHE to Au, but smaller than Pt

# Using $\text{Al}_2\text{O}_3$ as a barrier layer to prevent interdiffusion

$\text{Bi}_2\text{Se}_3$  (10 nm)  
 $\text{Al}_2\text{O}_3$  (0~2 nm)  
Py (20 nm)  
Sapphire

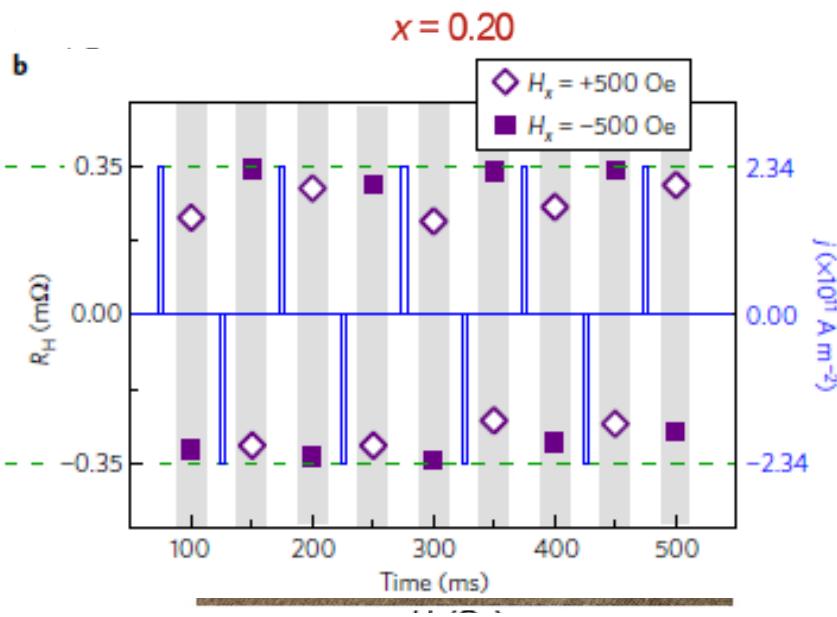
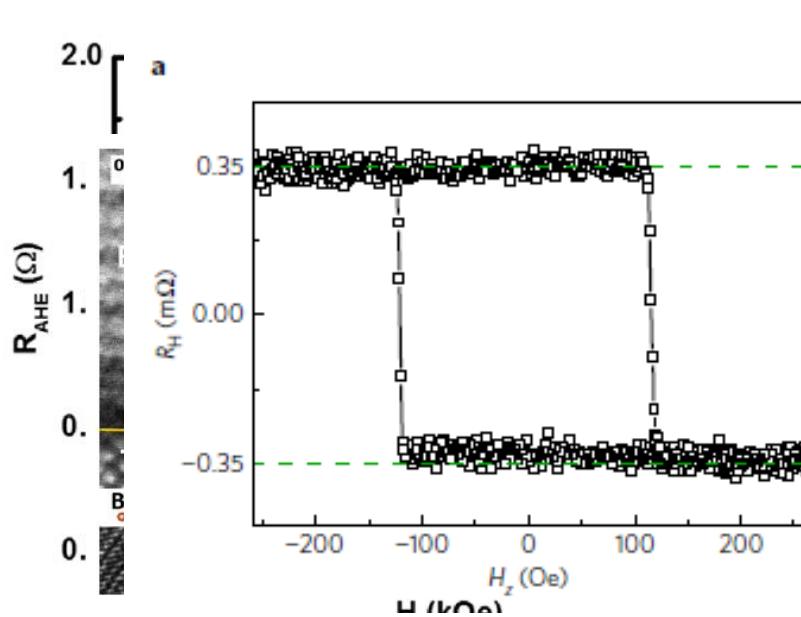


Microwave-induced parasitic effect of FM

"spin-rectification effect"

# Benefits of the ferrimagnetic insulator YIG and TmIG

- **High  $T_C$ :** high-temperature MPE in TI/FI
- **High thermal stability with TIs:** Formation of sharp TI/FI interface
- **Insulating properties:** prevention of current shunting effect

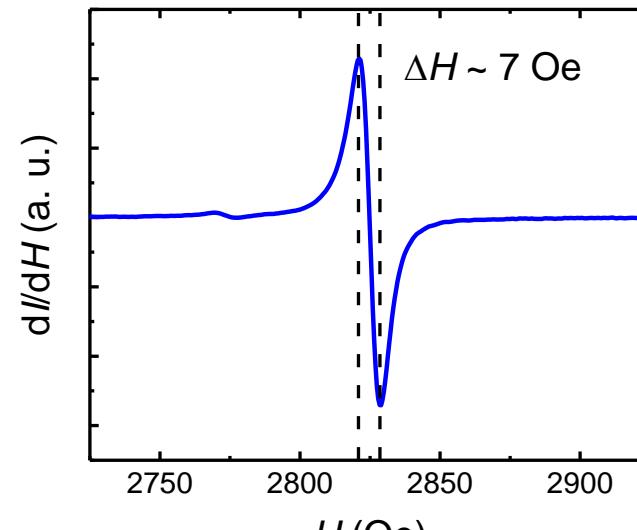
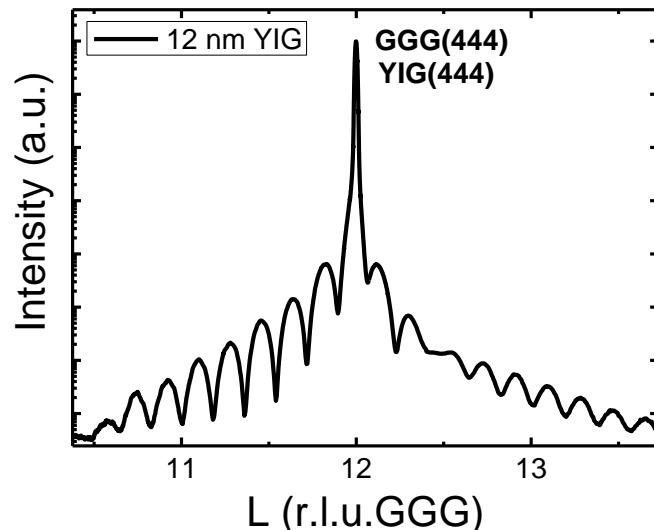


C. C. Chen et al., App  
Mater. Lett. 14, 5409 (2014).

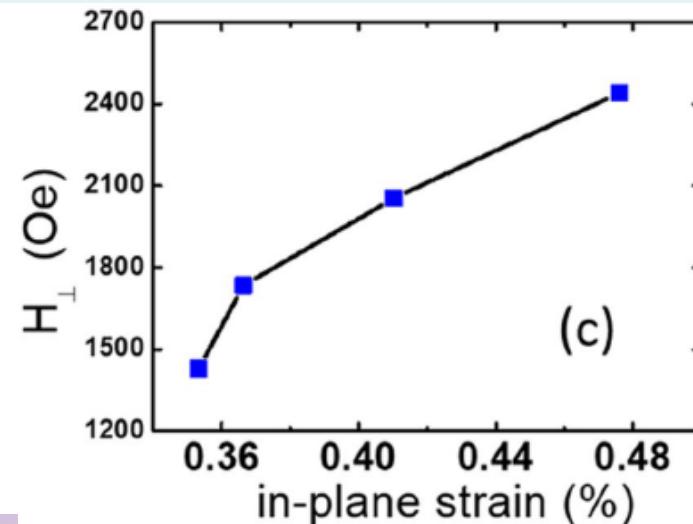
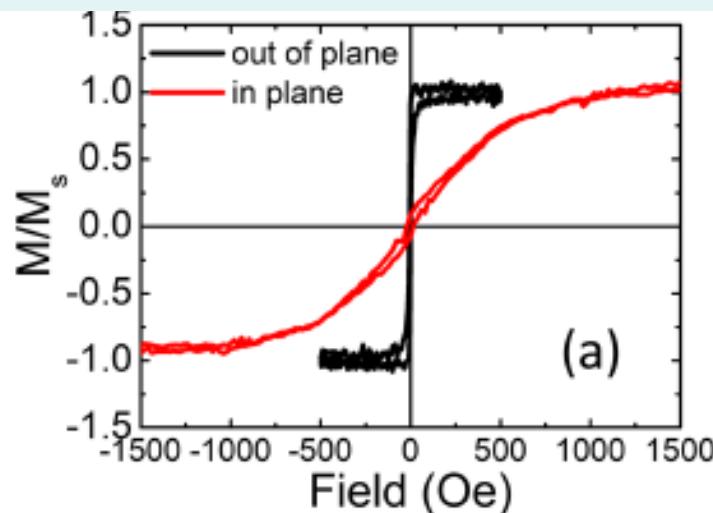
C. O. Avci et al., Nat. Mater. 16, 309 (2016). 3, e1700307 (2017).  
C. Yang et al., Sci. Adv. 3, e1700307 (2017).

# High quality off-axis sputtered YIG and TmIG films

Low damping YIG films of excellent crystallinity

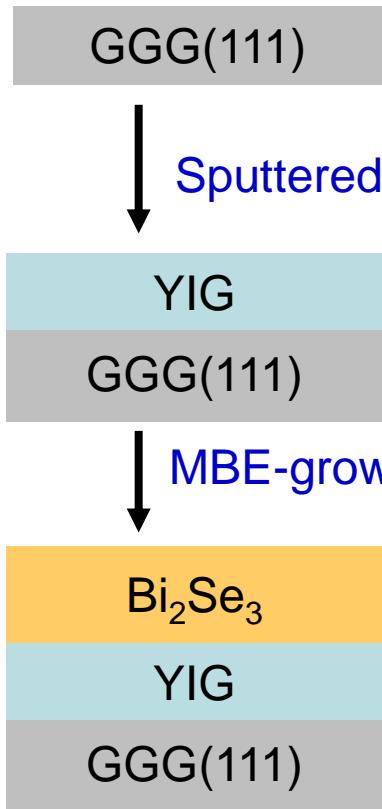


TmIG films with strain-tunable PMA

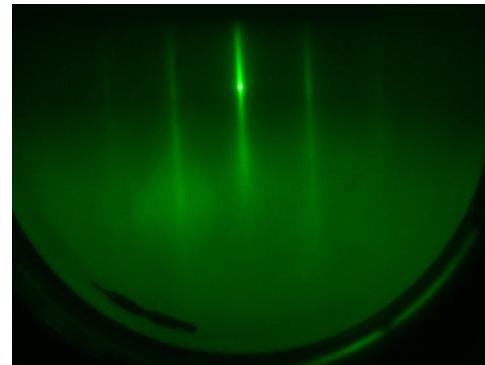


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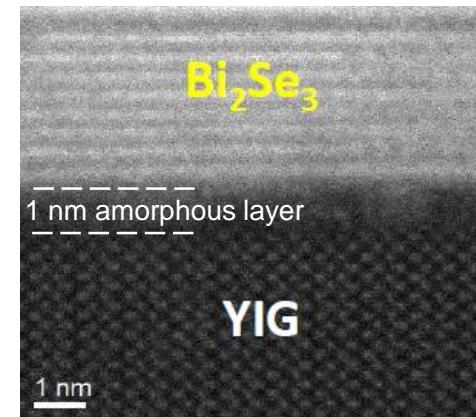
# Growth and structural characterization of $\text{Bi}_2\text{Se}_3/\text{YIG}$



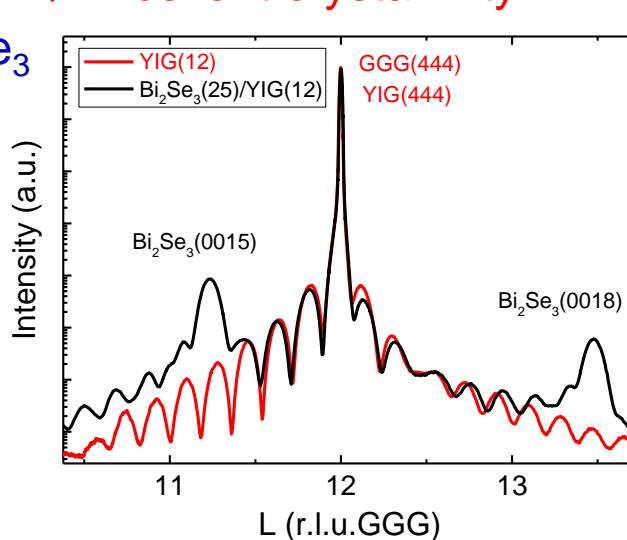
◆ Streaky RHEED pattern



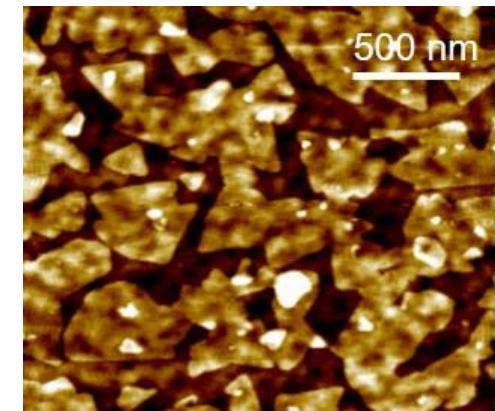
◆ 1 nm interlayer



◆ Excellent crystallinity



◆ High quality layer-by-layer growth

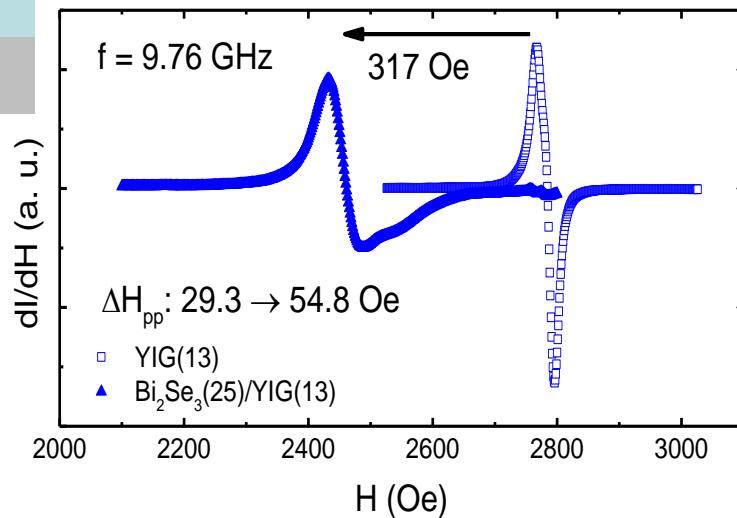


# Magnetic anisotropy in $\text{Bi}_2\text{Se}_3/\text{YIG}$

25 nm  $\text{Bi}_2\text{Se}_3$

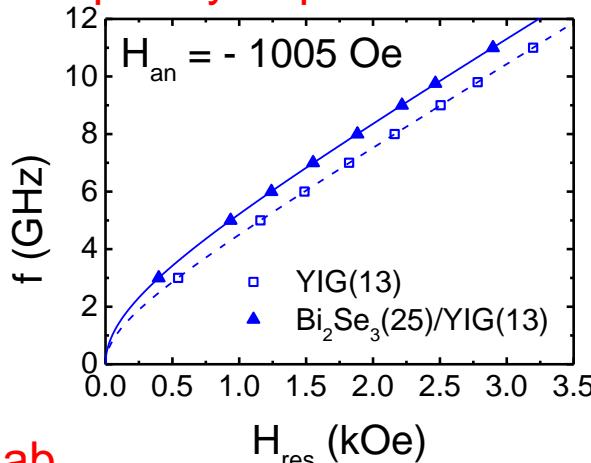
13 nm YIG

GGG(111)

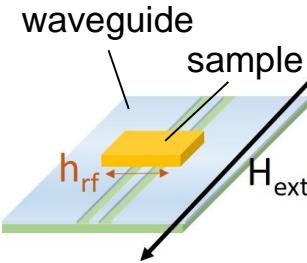
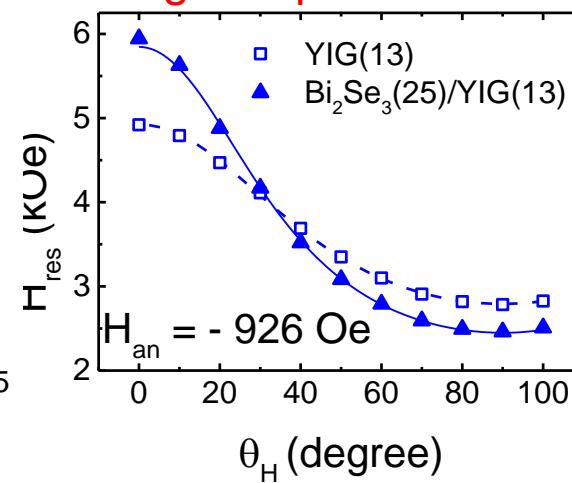


- Large  $H_{\text{res}}$  shift is observed after growing  $\text{Bi}_2\text{Se}_3$  on YIG, due to change of magnetic anisotropy.
- Angle- and frequency-dependent FMR show an enhanced in-plane anisotropy introduced by  $\text{Bi}_2\text{Se}_3$ .

## Frequency-dependent FMR

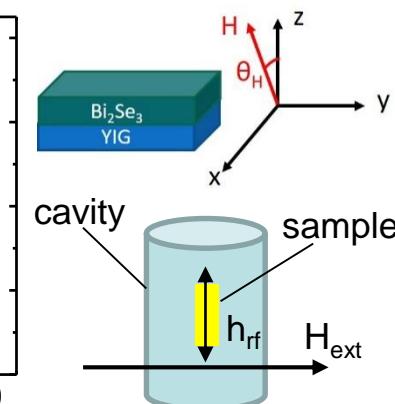


## Angle-dependent FMR



Dr. S. F. Lee's lab  
in Academia Sinica

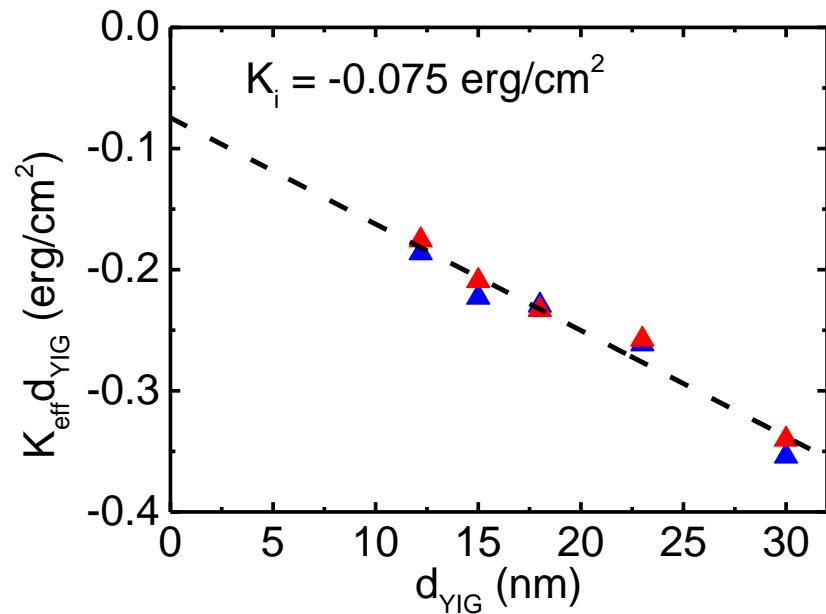
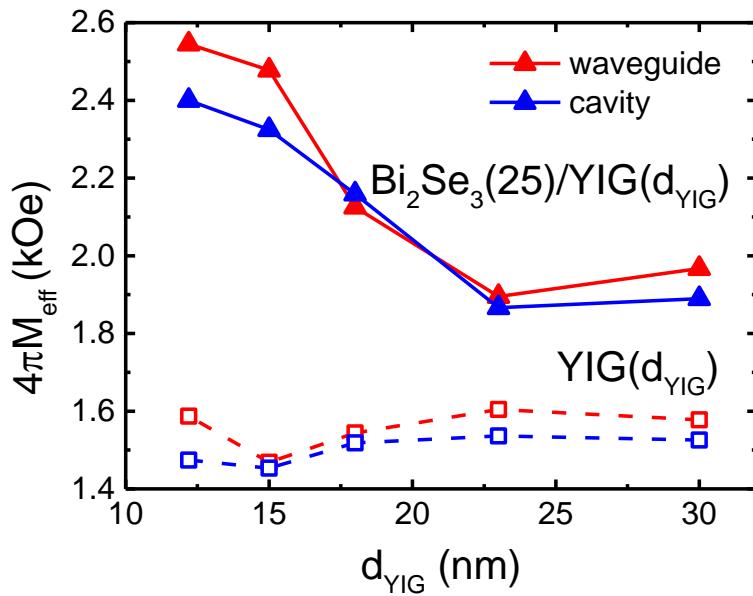
NTU/NTHU



Dr. J. G. Lin's lab  
In NTU/CCMS

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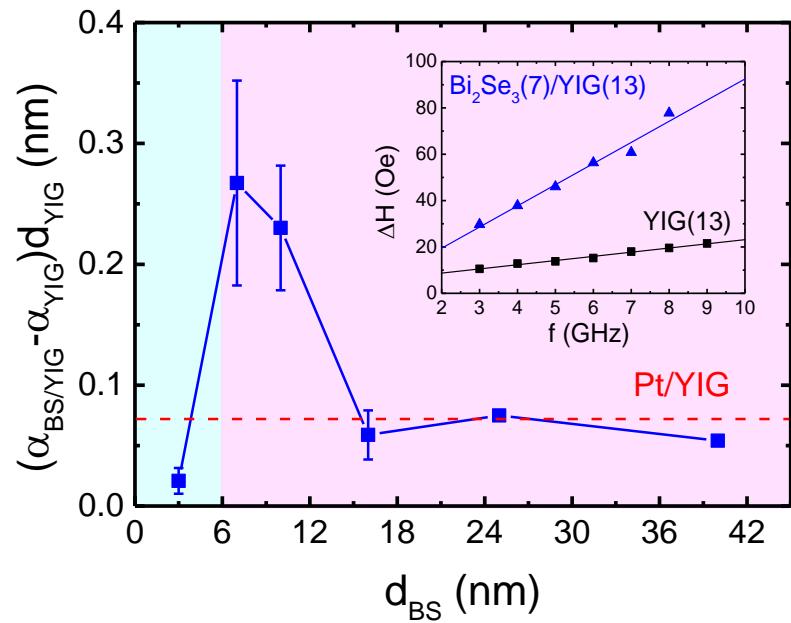
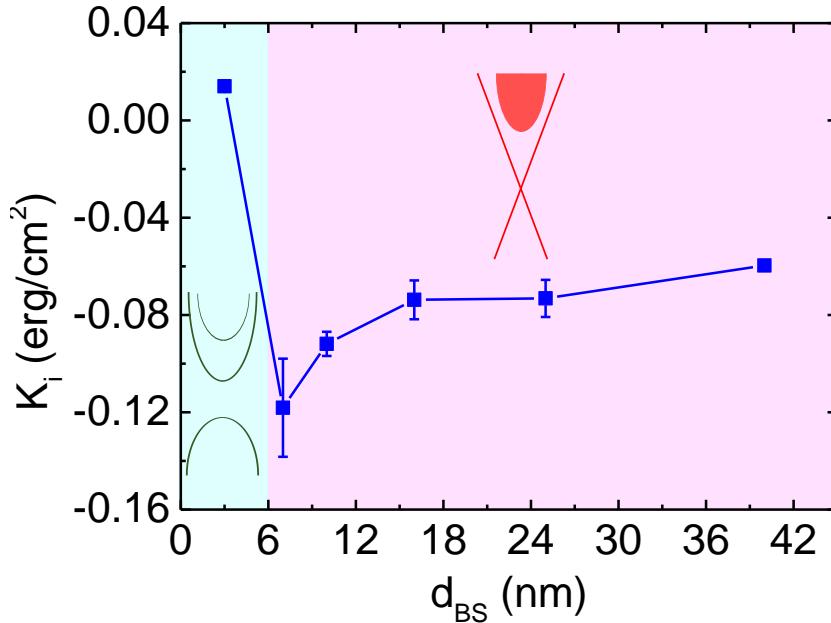
# Interfacial magnetic anisotropy favoring in-plane direction



- The effective magnetization  $M_{eff}$  is larger in thinner YIG samples, which implies the change of anisotropy occurring at TI/YIG interfaces.

$$\begin{aligned} & 4\pi(M_{eff}(\text{Bi}_2\text{Se}_3/\text{YIG}) - M_{eff}(\text{YIG})) \\ &= -\frac{2}{M_s}(K_{eff}(\text{Bi}_2\text{Se}_3/\text{YIG}) - K_{eff}(\text{YIG})) \\ &= -H_{an} \\ &\Rightarrow \frac{2K_i}{M_s} \left( \frac{1}{d_{YIG}} \right) = H_{an} \end{aligned}$$

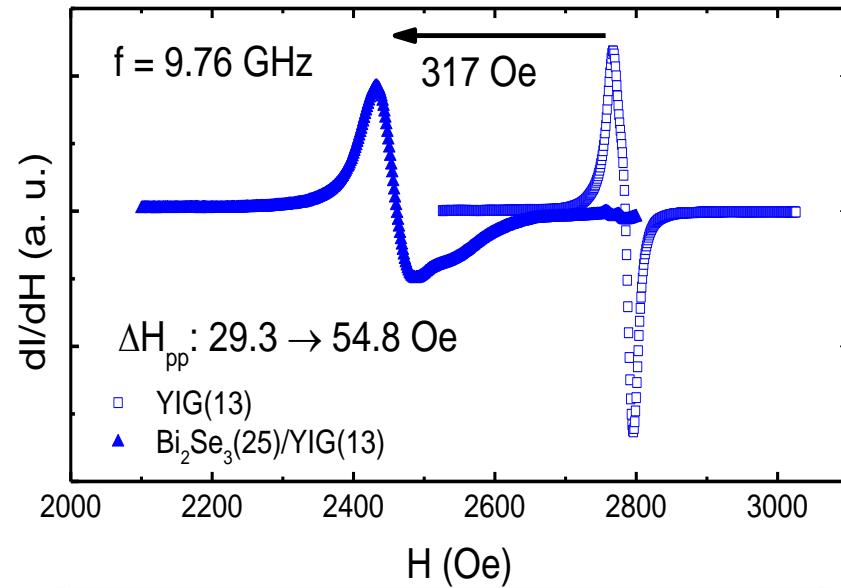
# $\text{Bi}_2\text{Se}_3$ thickness dependence of $K_i$ and damping enhancement



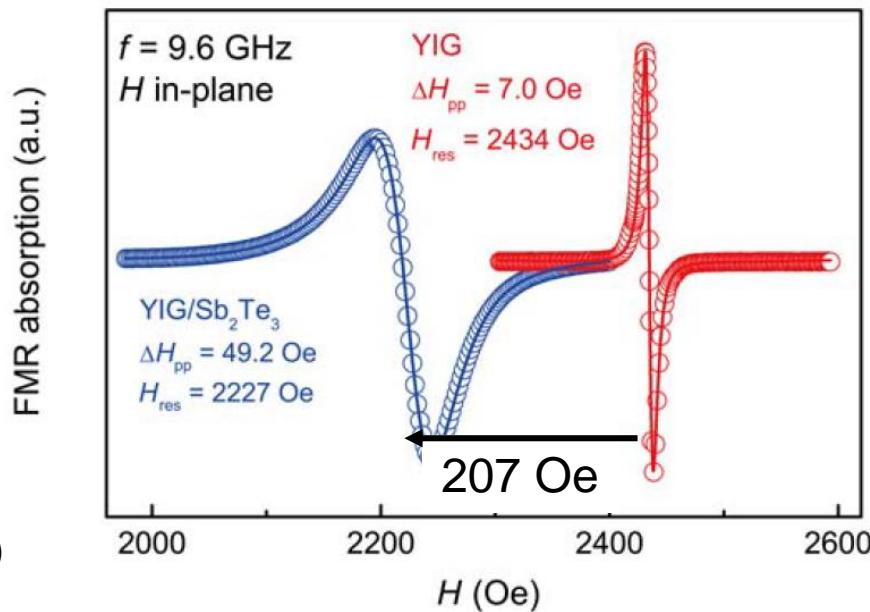
- A. TSS can strongly enhance the magnetic anisotropy of the magnetic layer. (Kim *et al.*, Phys. Rev. Lett. **119**, 027201 (2017))
- B. Such unconventional thickness dependence might be related to the **topological surface states** of  $\text{Bi}_2\text{Se}_3$ .
- C. The normalized damping enhancement peaks near the **2D limit (6 nm)** of  $\text{Bi}_2\text{Se}_3$ , which is **3 times larger than that of Pt/YIG**.

# Comparison with BiSbTe/YIG of Prof. Jing Shi (UC riverside)

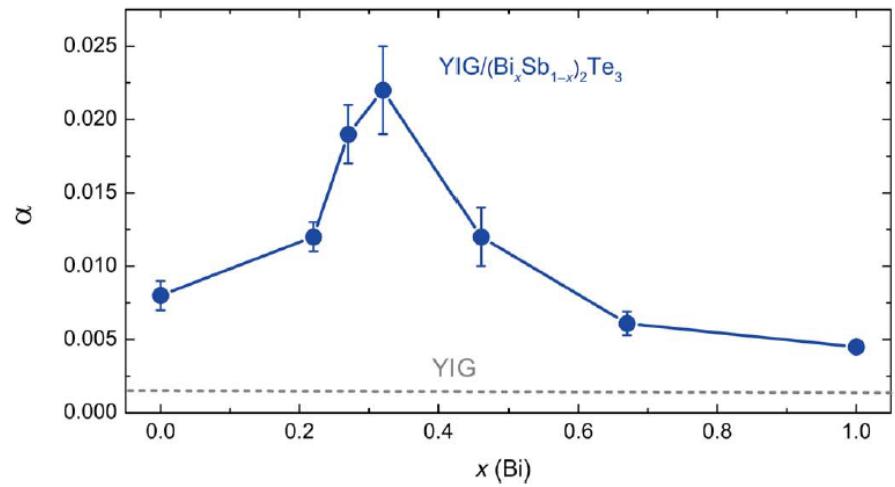
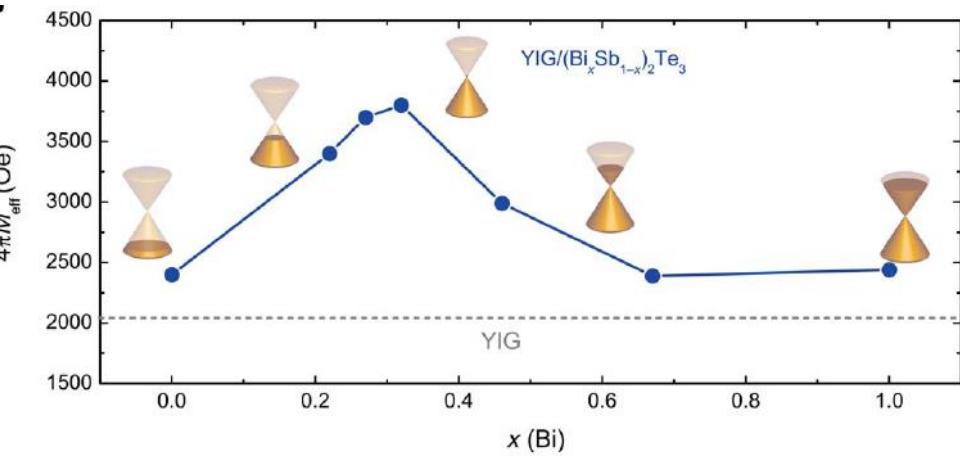
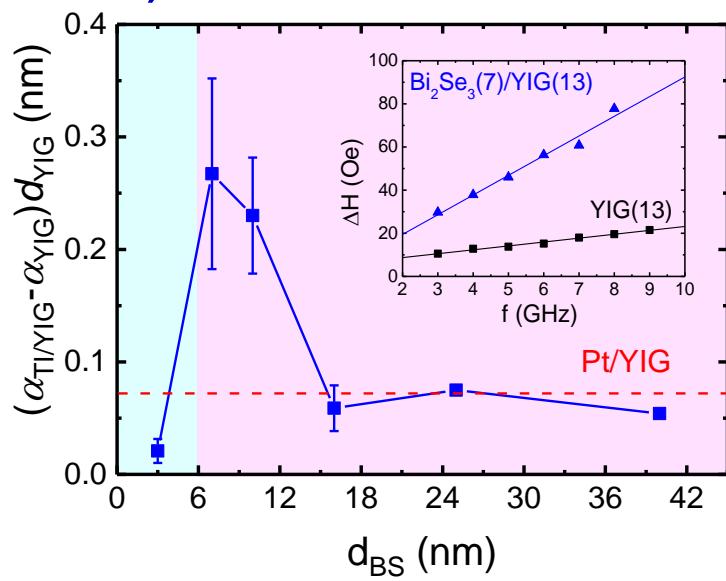
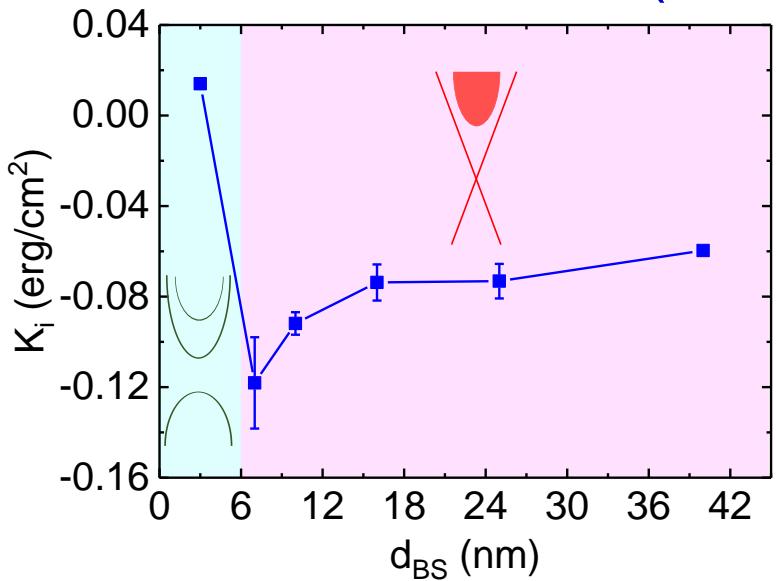
25 QL  $\text{Bi}_2\text{Se}_3$   
13 nm YIG



5 QL  $\text{Sb}_2\text{Te}_3$   
10 nm YIG

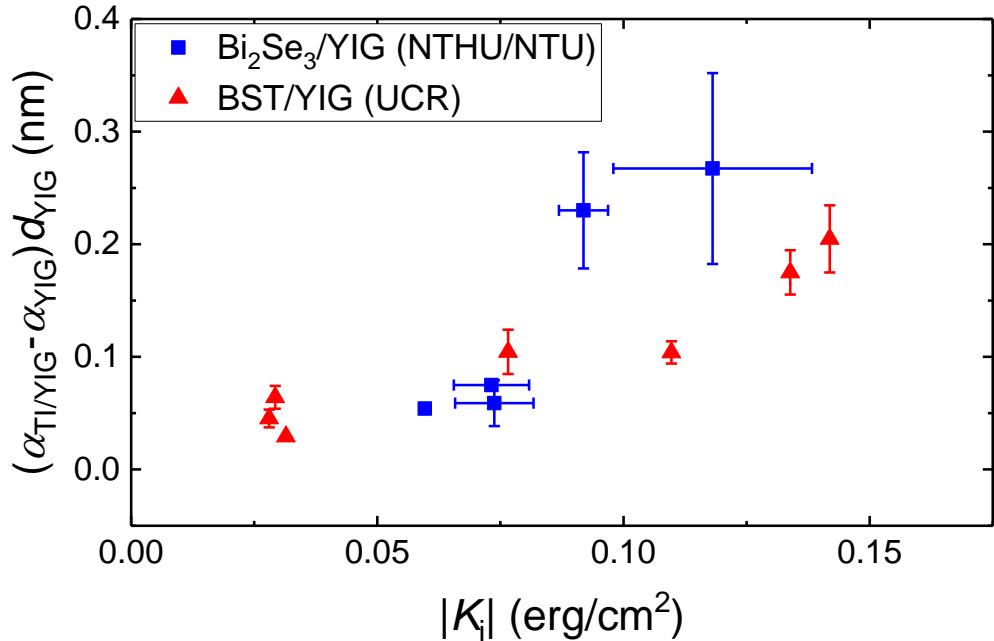
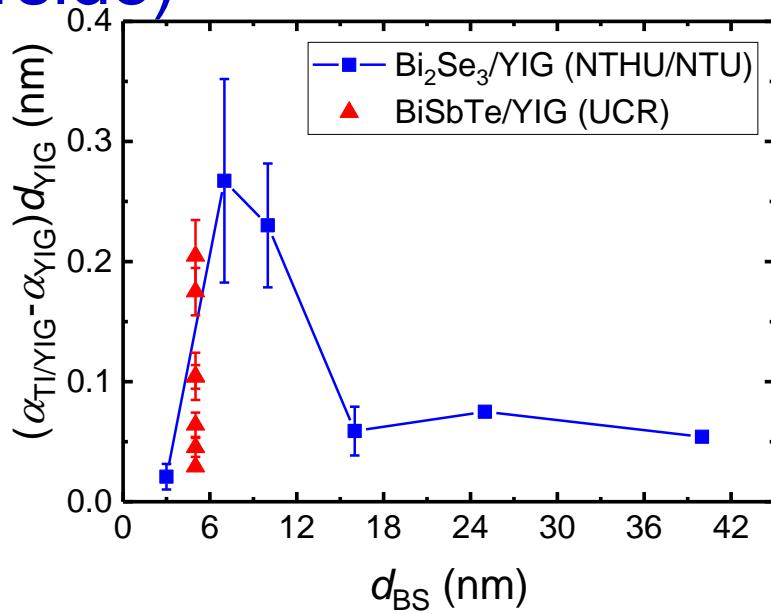
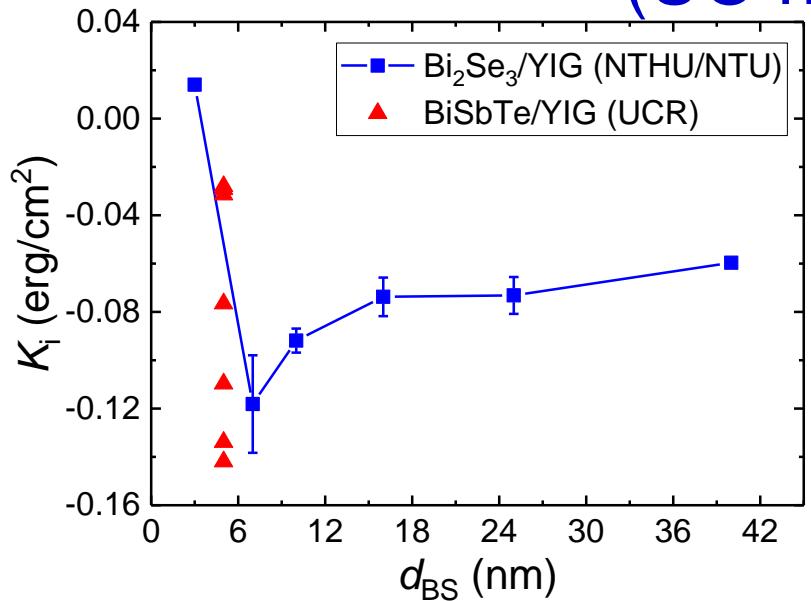


# Comparison with BiSbTe/YIG of Prof. Jing Shi (UC riverside)



Fanchiang et al., Nat. Comm. **9**, 233 (2018)  
Tang et al., Sci. Adv. **4**, eaas8660 (2018)

# Comparison with BiSbTe/YIG of Prof. Jing Shi (UC riverside)



- A. Comparable interfacial magnetic anisotropy and damping enhancement in  $\text{Bi}_2\text{Se}_3/\text{YIG}$  and BST/YIG
- B. Close anisotropy vs damping relations of  $\text{Bi}_2\text{Se}_3/\text{YIG}$  and BST/YIG

Fanchiang et al., Nat. Comm. 9, 233 (2018)  
Tang et al., Sci. Adv. 4, eaas8660 (2018)

# Surface-state-mediated exchange coupling: theoretical aspect

PRL 119, 027201 (2017)

PHYSICAL REVIEW LETTERS

week ending  
14 JULY 2017

## Understanding the Giant Enhancement of Exchange Interaction in $\text{Bi}_2\text{Se}_3$ -EuS Heterostructures

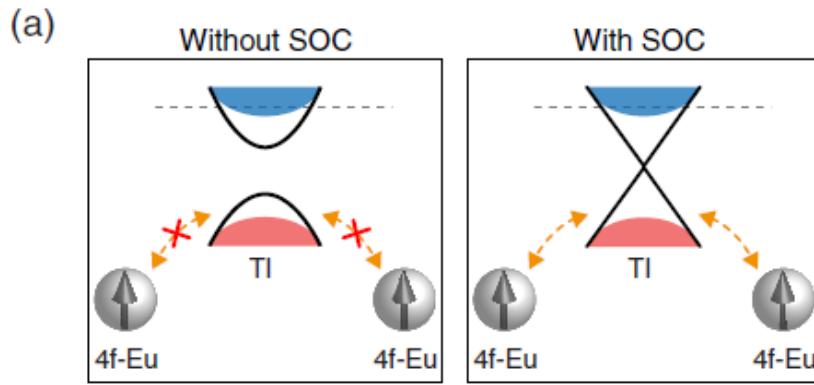
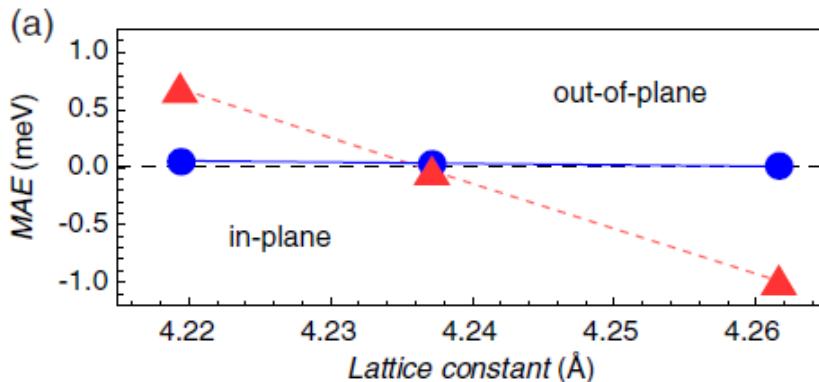
Jeongwoo Kim,<sup>1</sup> Kyoung-Whan Kim,<sup>2</sup> Hui Wang,<sup>1</sup> Jairo Sinova,<sup>2,3</sup> and Ruqian Wu<sup>1,\*</sup>

<sup>1</sup>*Department of Physics and Astronomy, University of California, Irvine, California 92697, USA*

<sup>2</sup>*Institut für Physik, Johannes Gutenberg Universität Mainz, Mainz, 55128, Germany*

<sup>3</sup>*Institute of Physics, Academy of Sciences of the Czech Republic, Cukrovarnická 10, 162 53 Praha 6, Czech Republic*

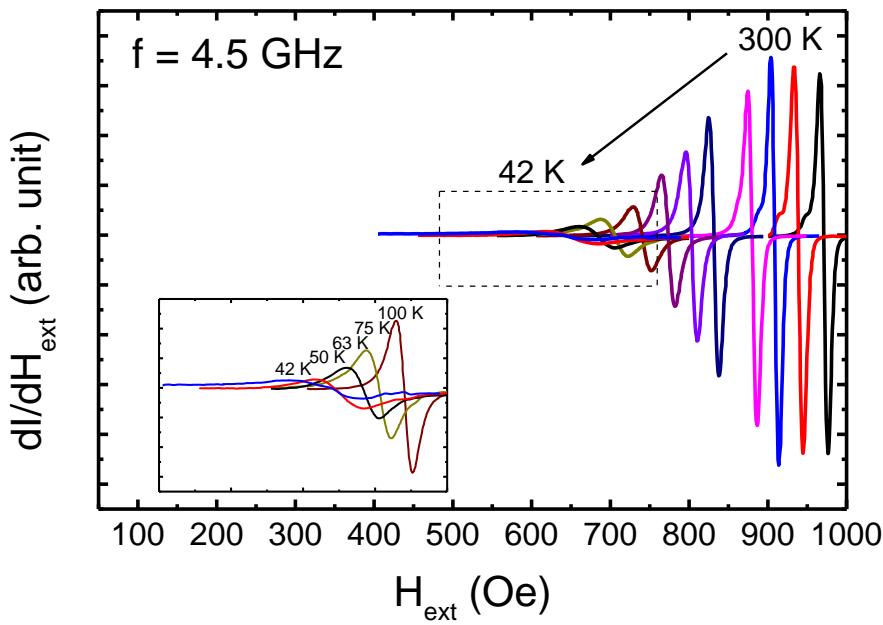
(Received 21 December 2016; revised manuscript received 22 March 2017; published 13 July 2017)



- A. The strong SOC of TI can enhance the magnetic anisotropy of the magnetic insulator.
- B. The sign of anisotropy may depend on atomic structure at the interface.
- C. The TI surface state mediates the exchange coupling of the magnetic ion of the magnetic layer.

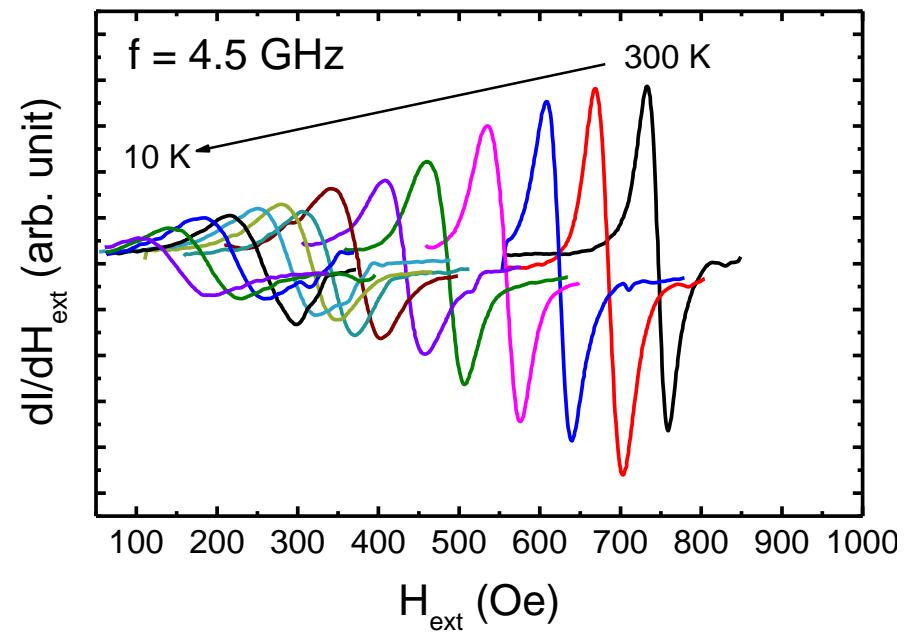
# Temperature-dependent FMR of YIG and $\text{Bi}_2\text{Se}_3/\text{YIG}$

23 nm YIG



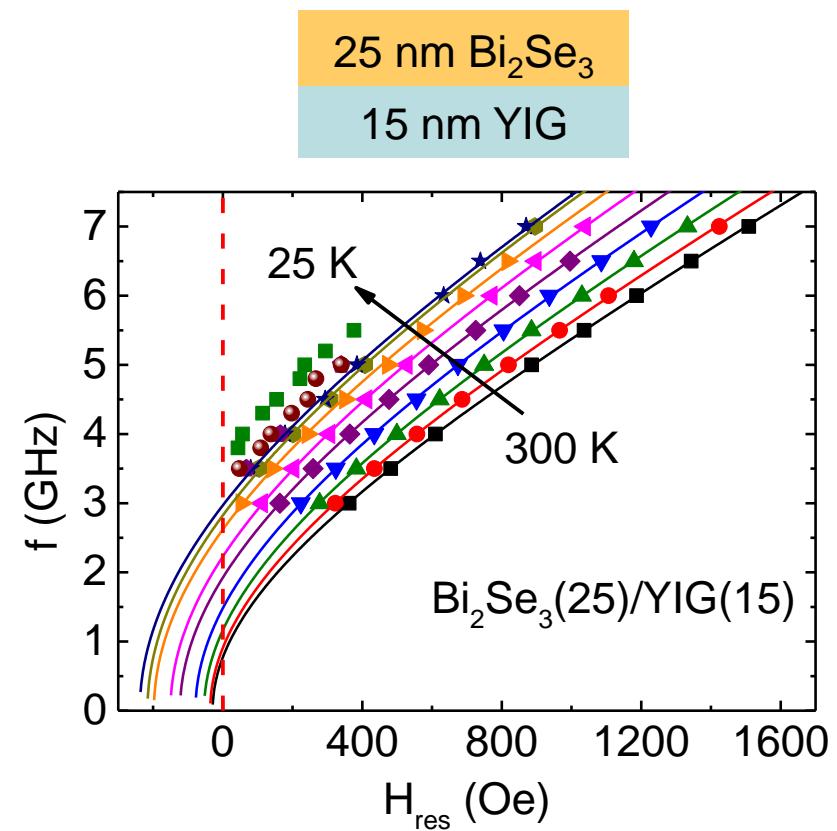
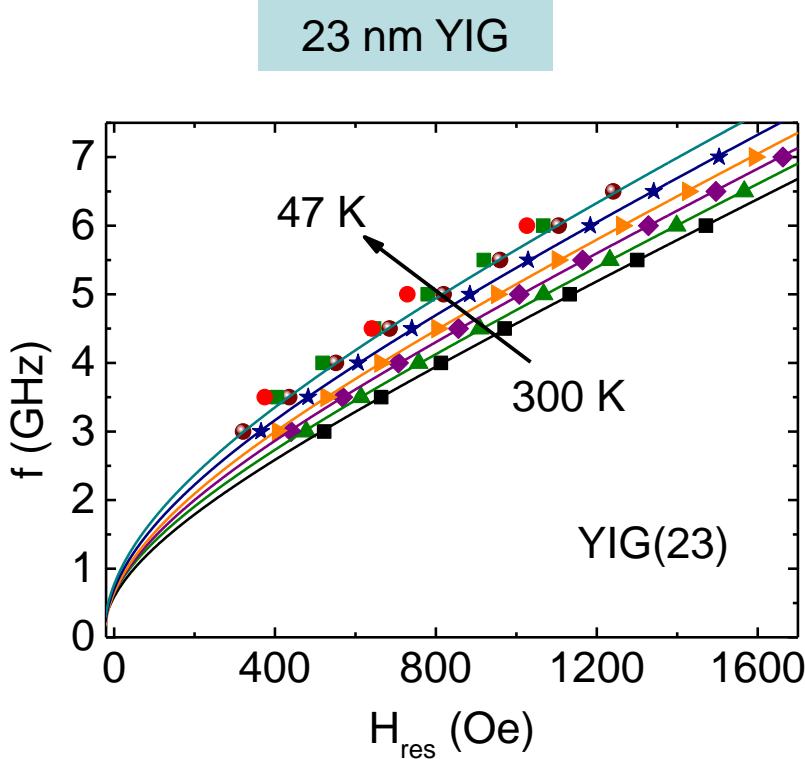
25 nm  $\text{Bi}_2\text{Se}_3$

15 nm YIG



- Larger linewidth and damping  $\rightarrow$  smaller microwave absorption
- **Increasing  $H_{\text{res}}$  shift** at low temperature
- **Less damping** in  $\text{Bi}_2\text{Se}_3/\text{YIG}$  below 50 K

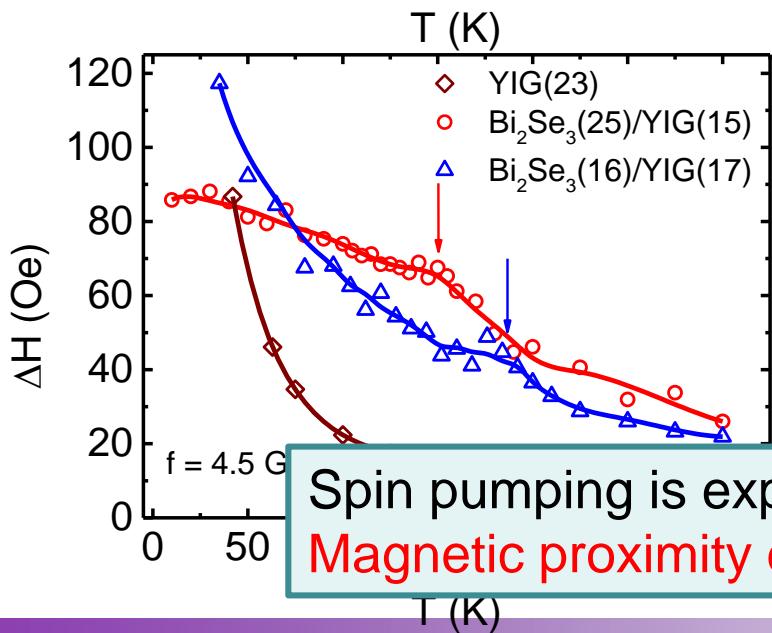
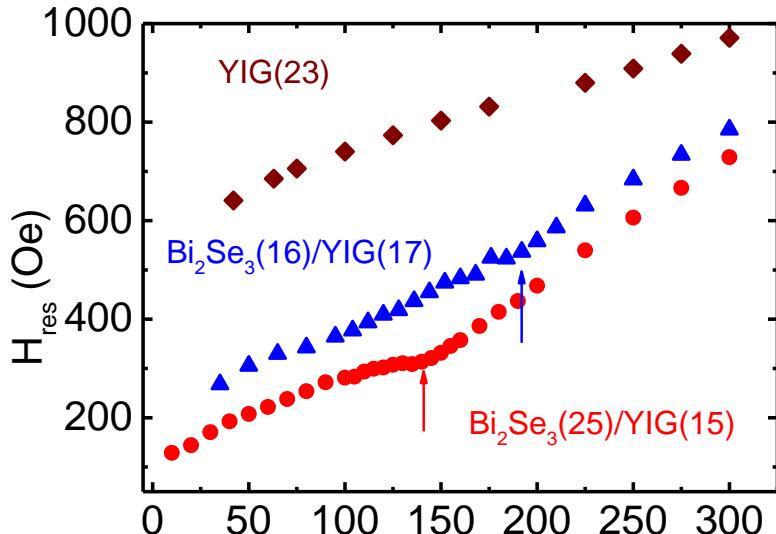
# Temperature-dependent FMR of YIG and $\text{Bi}_2\text{Se}_3$ /YIG



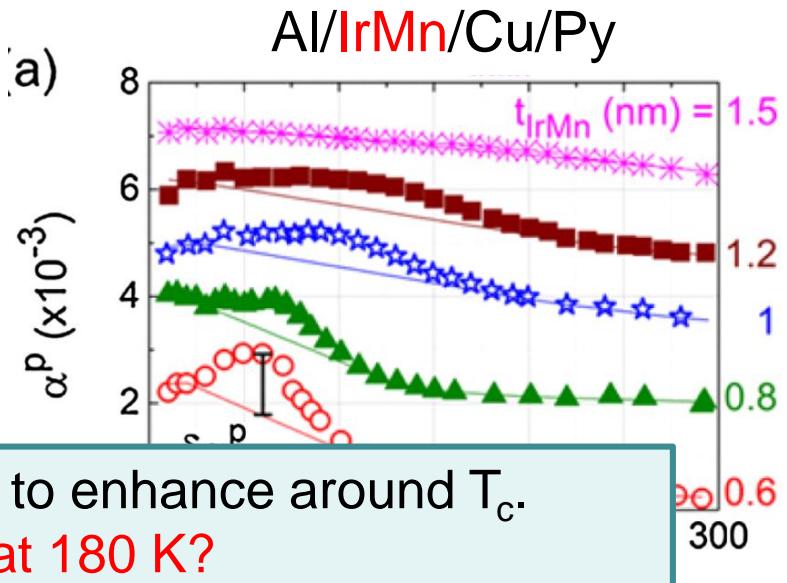
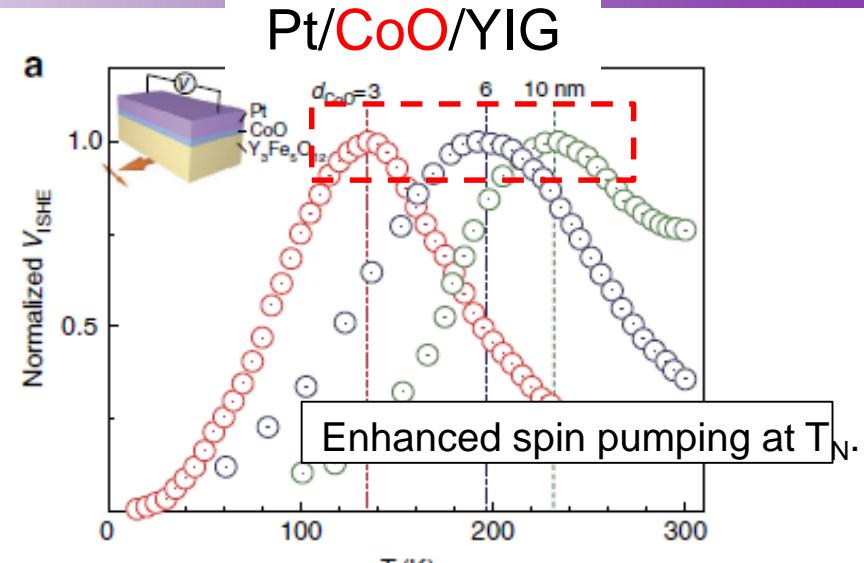
An effective field  $H_{\text{eff}}$  is necessary to fit the data.

$$f = \frac{\gamma}{2\pi} \sqrt{(H + H_{\text{eff}})(H + H_{\text{eff}} + 4\pi M_{\text{eff}})}$$

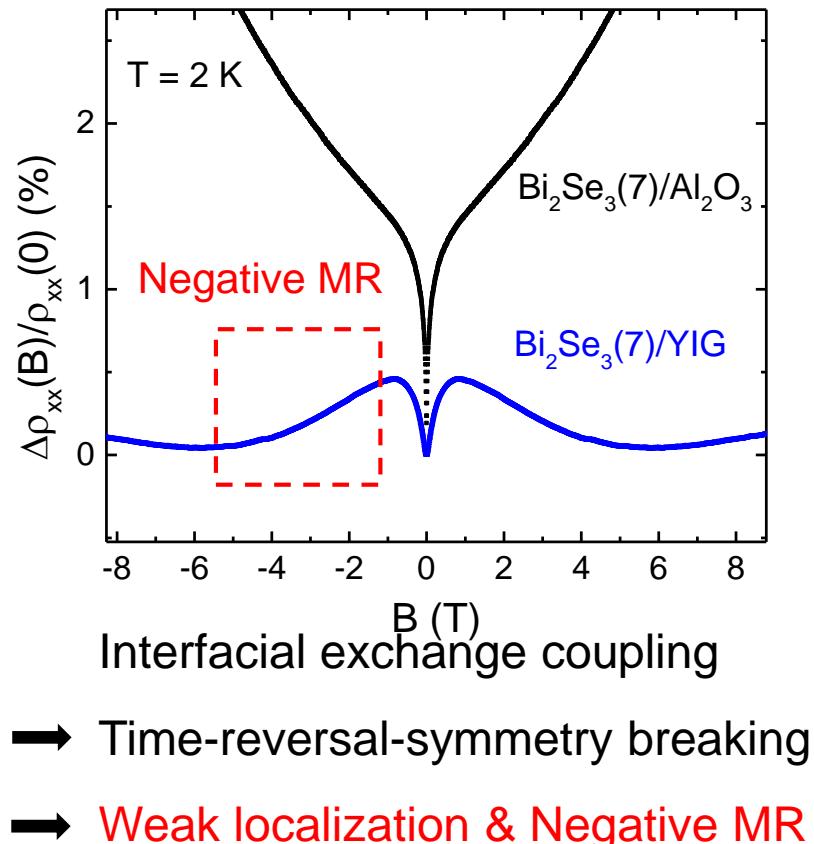
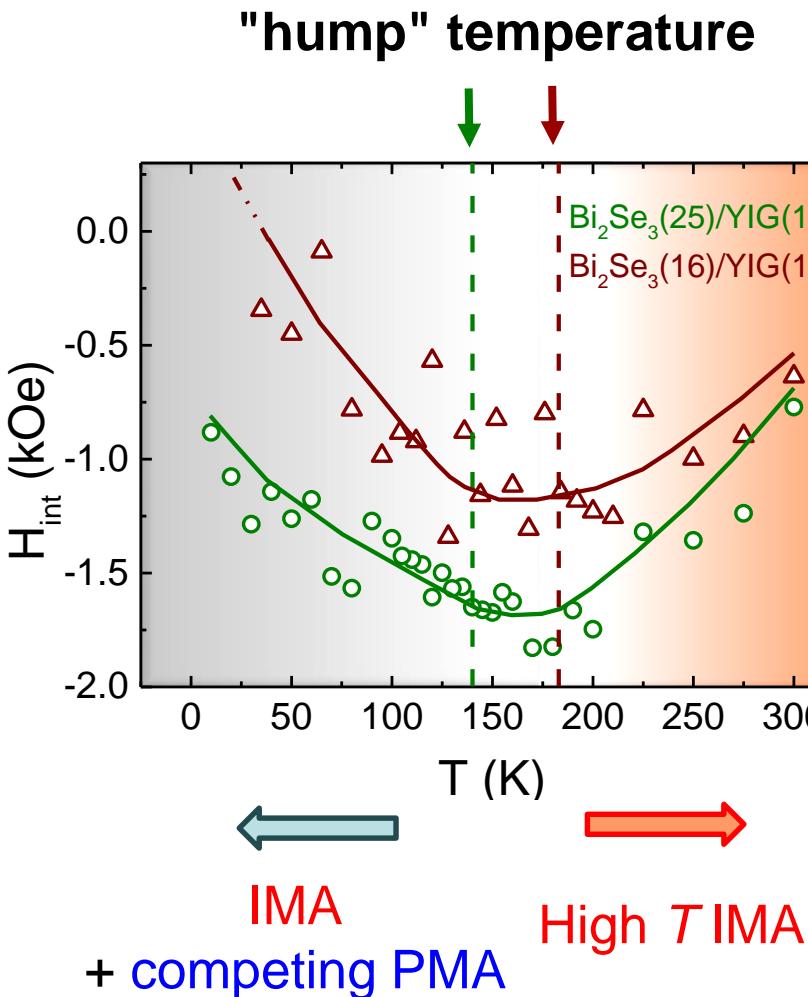
# A possible indicator of MPE provided by spin pumping



Spin pumping is expected to enhance around  $T_c$ .  
Magnetic proximity effect at 180 K?

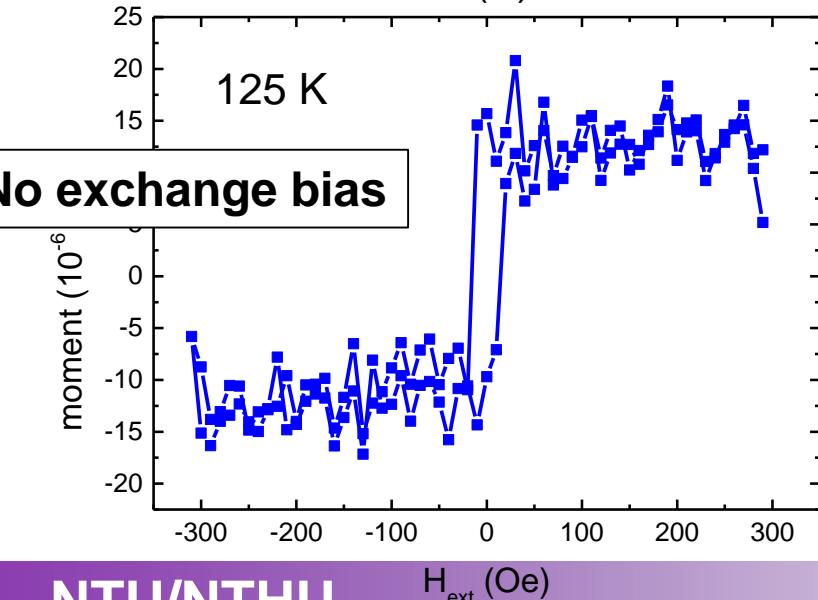
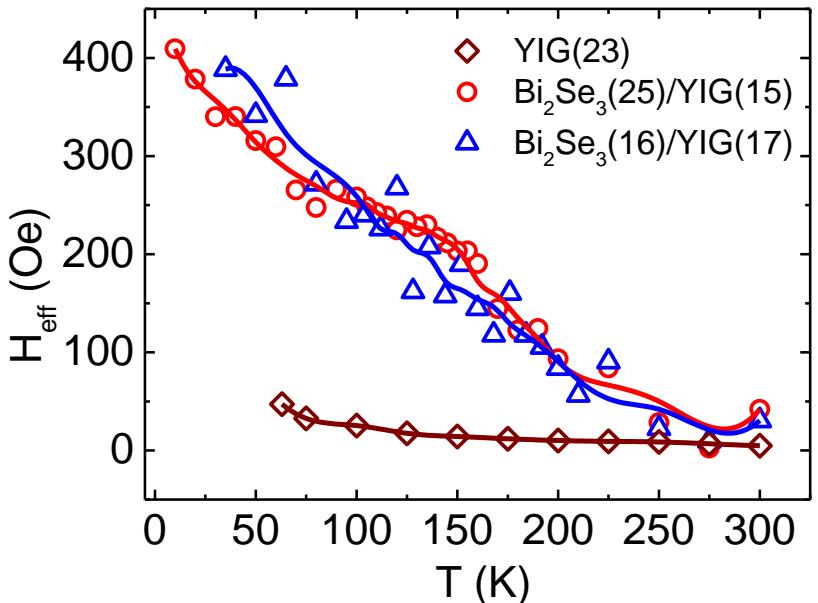


# Emerging low $T$ PMA and negative magnetoresistance

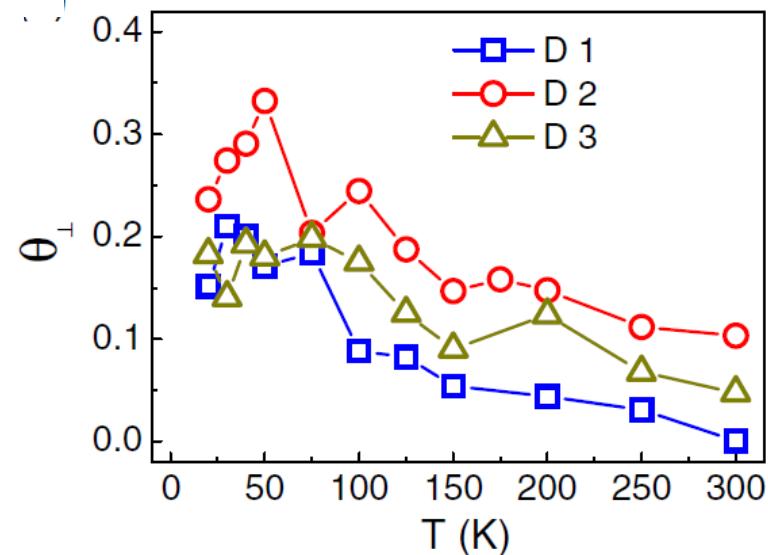


Kim et al., PRL **119**, 027201 (2017).  
Lu et al., PRL **107**, 076801 (2011).

# Spin-pumping-induced exchange effective field $H_{\text{eff}}$



Reported ST-FMR in CoFeB/Bi<sub>2</sub>Se<sub>3</sub>

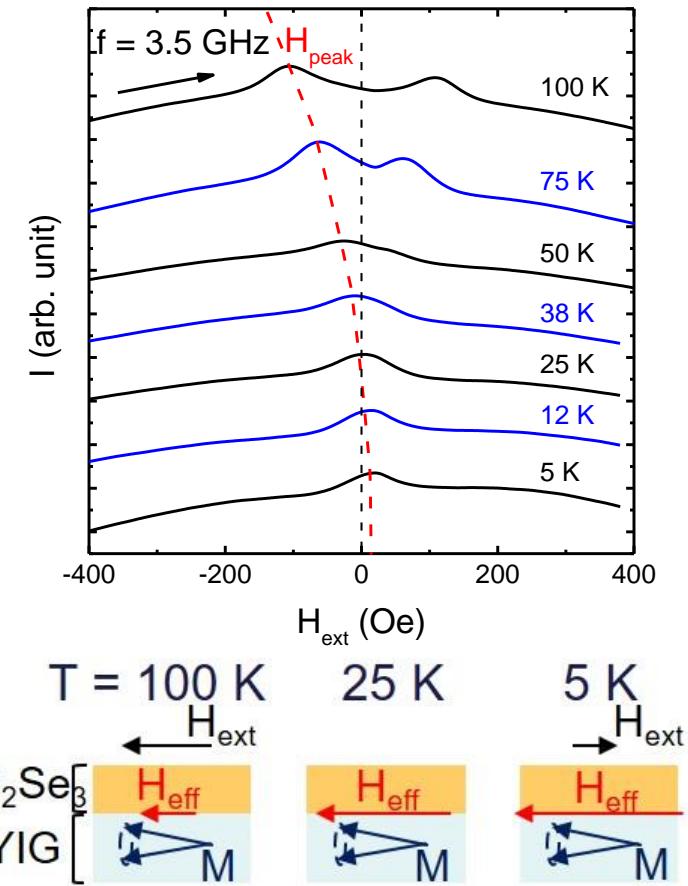
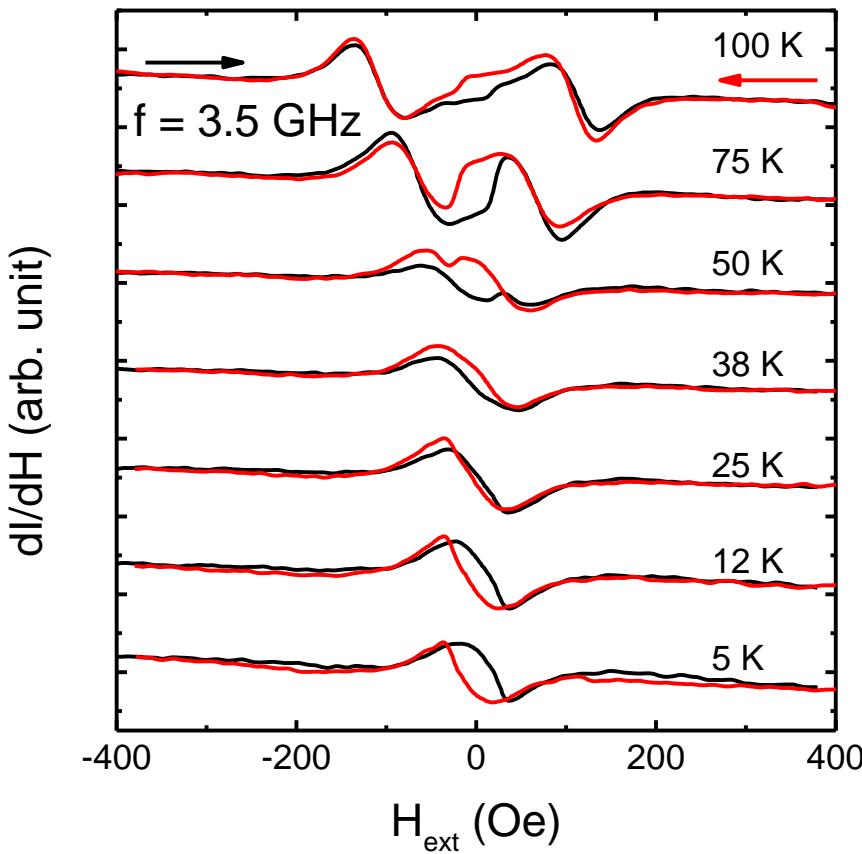


Increasing field-like torque at low T

$$\mathbf{T}_{\text{FL}} = \Delta_{ex} \mathbf{M} \times \langle \mathbf{S} \rangle_{\text{neq}}$$

The  $\mathbf{T}_{\text{FL}}$  in ST-FMR corresponds to a  $H_{\text{eff}}$  in spin pumping.

# Internal effective field induced FMR without an applied field

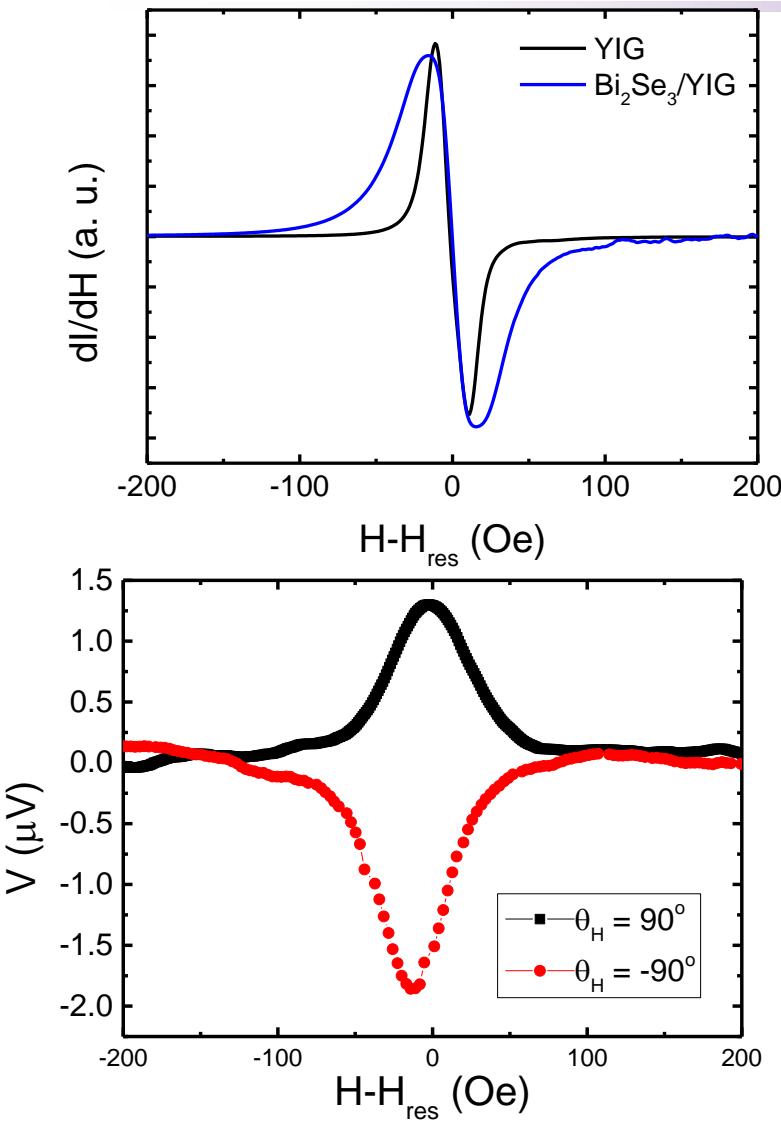


- Internal effective field =  $4\pi M_s + H_{an} + H_{eff}$
- The exchange effective field  $H_{eff}$  becomes larger as  $T$  decreases.
- The strong  $H_{eff}$  has **good potential for spintronic application**.

# Summary-1

- Ferrimagnetic insulator YIG provides thermally stable TI/YIG interface and avoids current shunting.
- Interfacial in-plane magnetic anisotropy in  $\text{Bi}_2\text{Se}_3/\text{YIG}$  is observed, and builds up as T decreases.
- A unprecedentedly large spin mixing conductance ( $2.2 \times 10^{19} \text{ m}^{-2}$ ) for YIG systems was observed in  $\text{Bi}_2\text{Se}_3/\text{YIG}$ , implying an interface with very efficient spin injection.
- Temperature dependence of spin pumping in  $\text{Bi}_2\text{Se}_3/\text{YIG}$  resembles that of antiferromagnetic CoO/YIG, suggesting MPE with a  $T_c$  as high as 180 K.

# Observation of spin-to-charge conversion in $\text{Bi}_2\text{Se}_3/\text{YIG}$

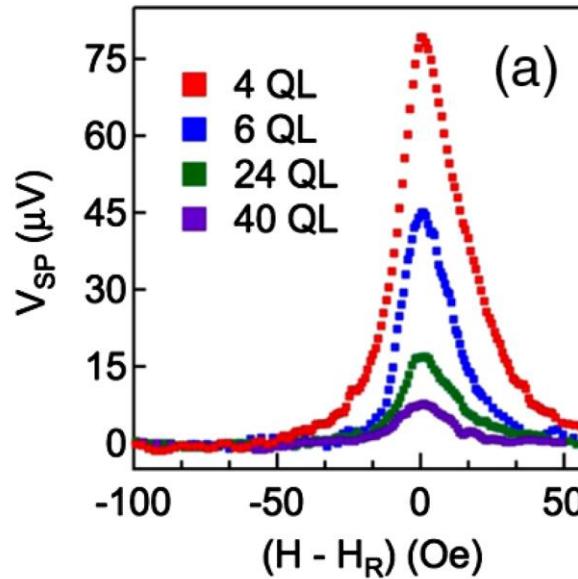


This work:  $\theta_{\text{SH}} \sim 3 \times 10^{-4}$

Explanation of low  $\theta_{\text{SH}}$  of our  $\text{Bi}_2\text{Se}_3/\text{YIG}$ :

1. Strong exchange coupling may modify the spin texture of  $\text{Bi}_2\text{Se}_3$ .
2. Spins are absorbed by the conducting bulk of  $\text{Bi}_2\text{Se}_3$ .

Prof. Samarth's work (PSU)  
 $\theta_{\text{SH}} \sim 0.02$



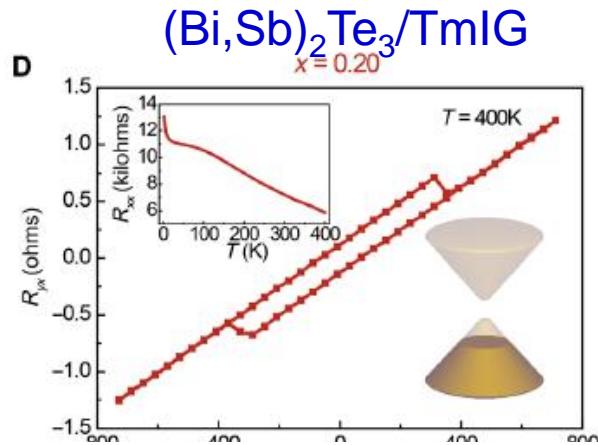
Wang et al., PRL 116, 096602 (2016).

# Negative magnetoresistance (MR) and exchange gap opening in $\text{Bi}_2\text{Se}_3/\text{ReIG}$

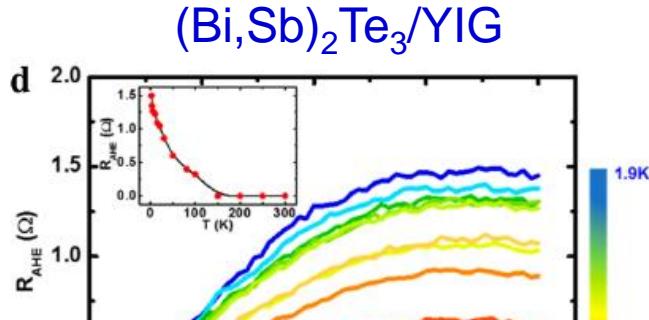
# Challenges of studying the interfacial band structure and transport properties of TI/FI

- Independent check of (a) MPE and (b) Dirac surface gap

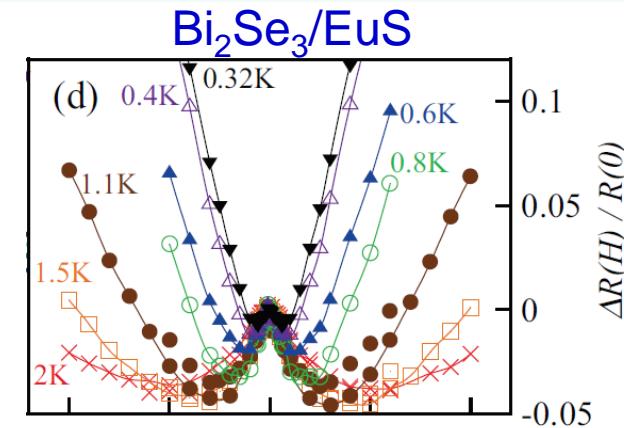
MPE, but no exchange gap



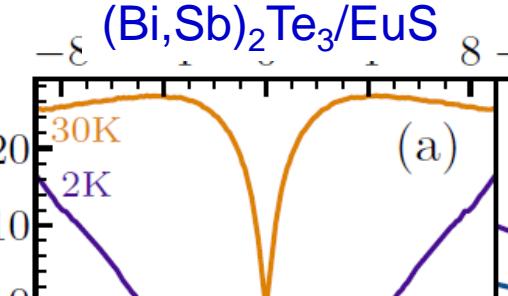
Tang et al., Sci. Adv. 3, e1700307 (2017)



Signatures of surface bandgap, but no ferromagnetism

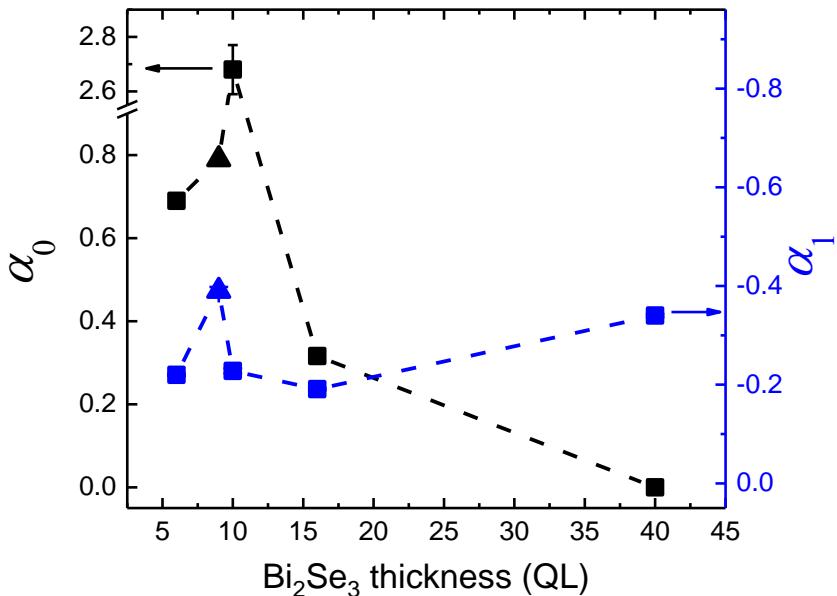
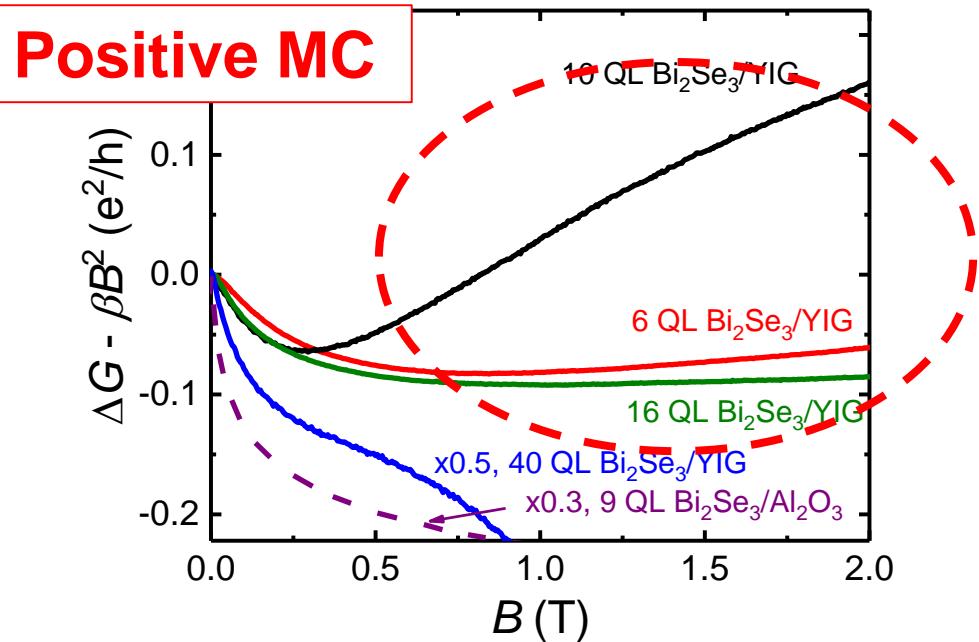
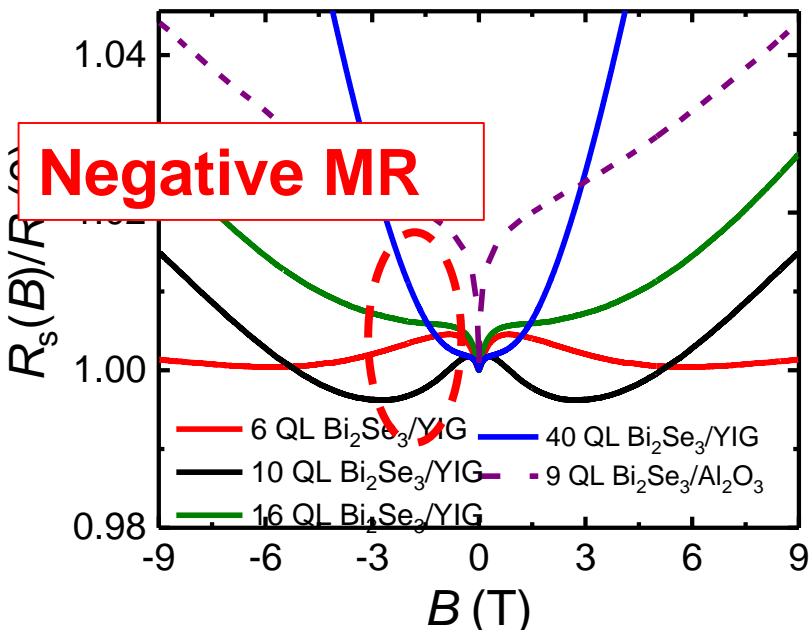


Yang et al., PRB 98, 081407(R) (2013)



A coherent picture that shows transport signatures of the coexisting MPE and exchange Dirac gap is needed.

# WL effect originated from TRS-breaking at the TI/FI interface: thickness dependent study

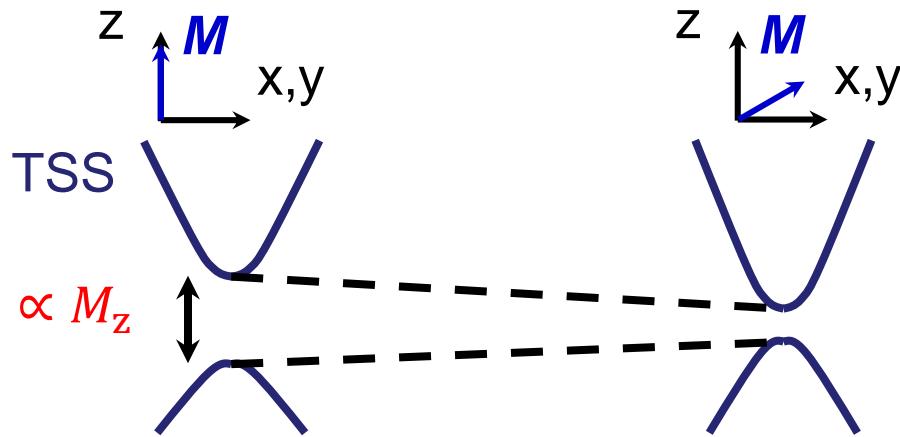
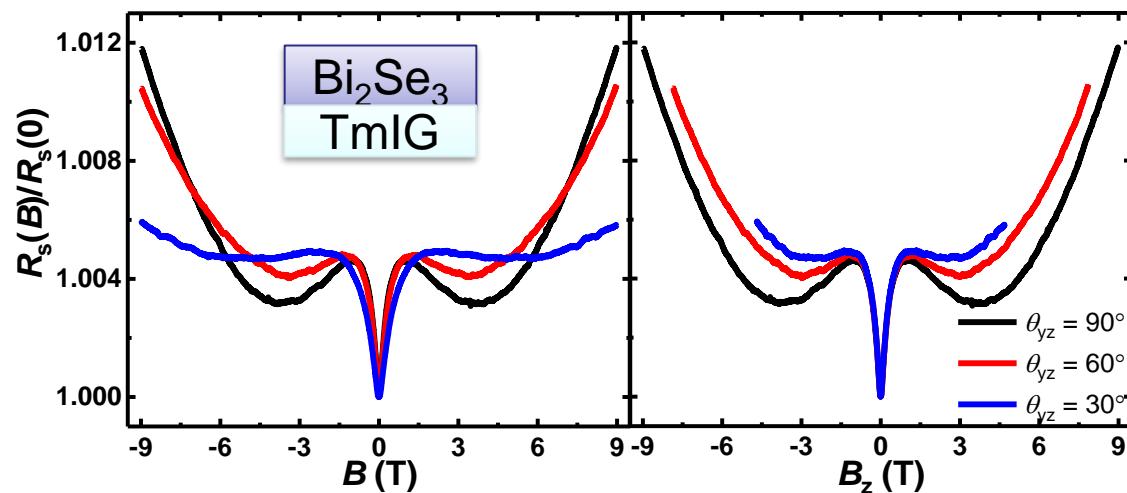


In thinner  $\text{Bi}_2\text{Se}_3$

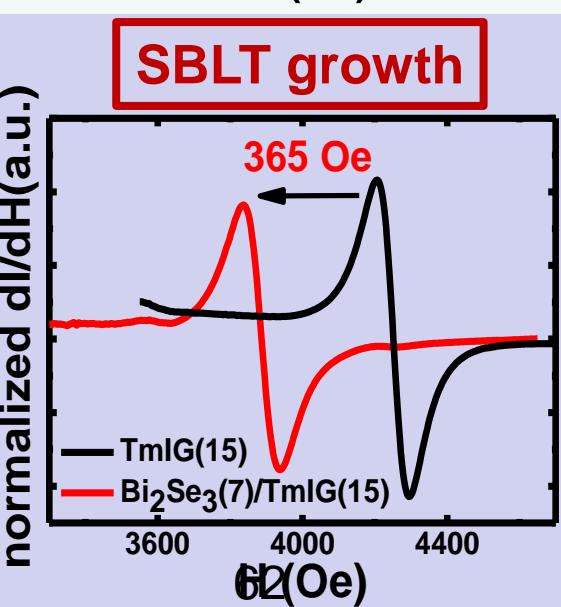
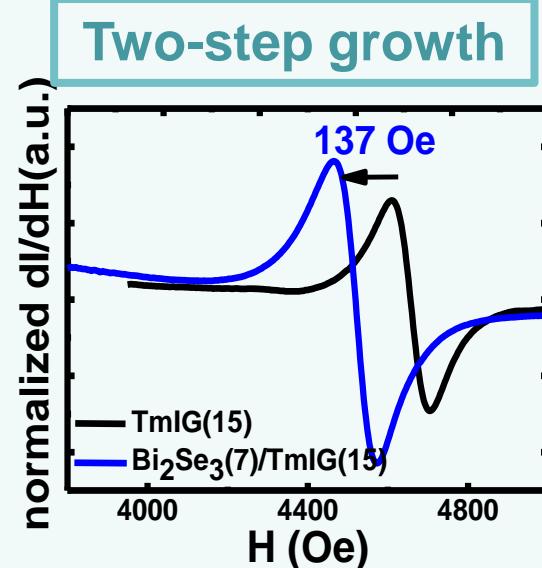
- stronger WL ( $\alpha_0$ ) and weaker WAL ( $\alpha_1$ )
- The WL is most likely due to the TRS broken by interfacial exchange interaction

# Strong interfacial exchange coupling

Transport signatures of exchange Dirac gap opening in  $\text{Bi}_2\text{Se}_3/\text{TmIG}$

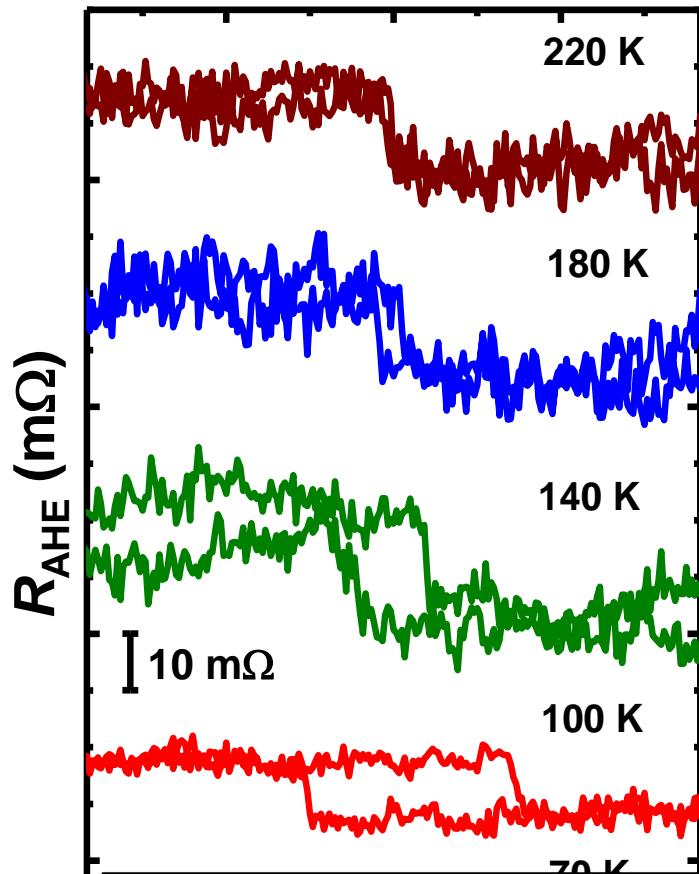


Interfacial magnetic anisotropy

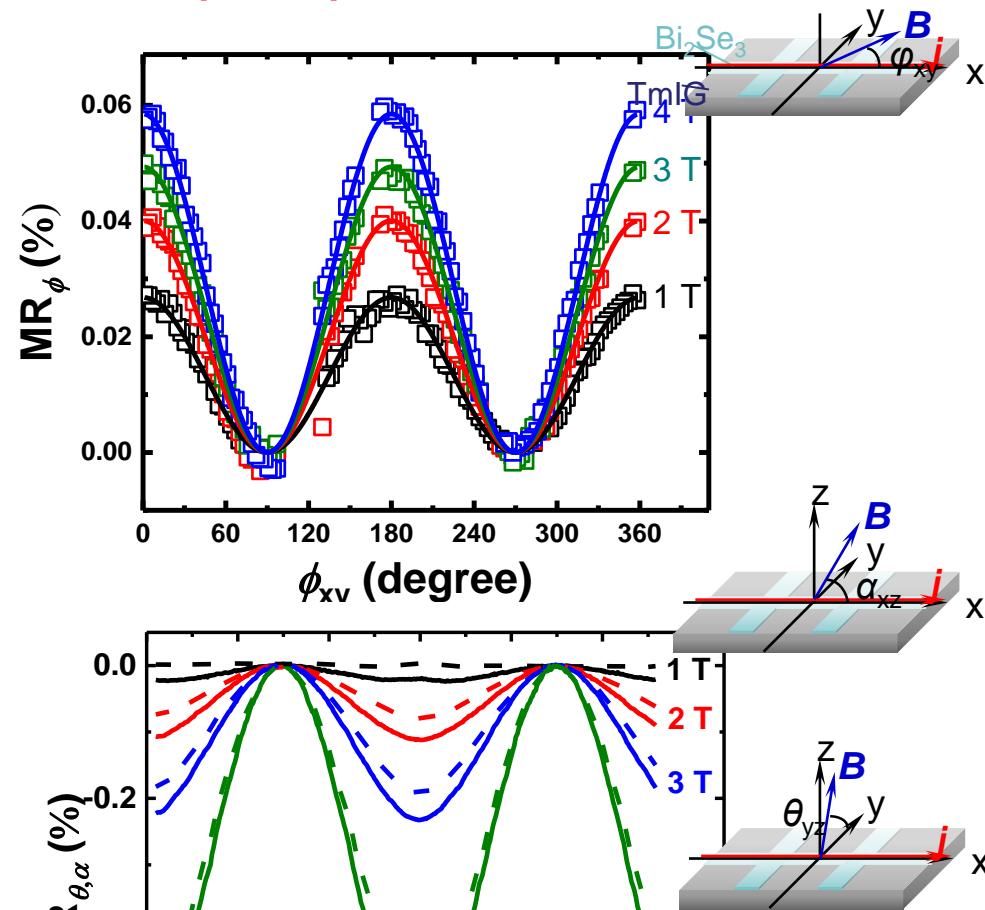


# Observation of AHE and AMR

## Anomalous Hall effect (AHE) loops



## Anisotropic magnetoresistance (AMR) due to MPE



With negative MR, AHE and AMR, we obtained a coherent transport picture of the system that shows both gap opening and MPE.

# **Summary-2**

- Observation of negative magnetoresistance (MR) of the weak localization (WL) effect in  $\text{Bi}_2\text{Se}_3/\text{YIG}$  and  $\text{Bi}_2\text{Se}_3/\text{TmIG}$
- Correlation between the negative MR and exchange gap size
- Proximity-induced long-range ferromagnetic order in TI/FI evidenced by anomalous Hall effect (AHE) and anisotropic magnetoresistance (AMR)

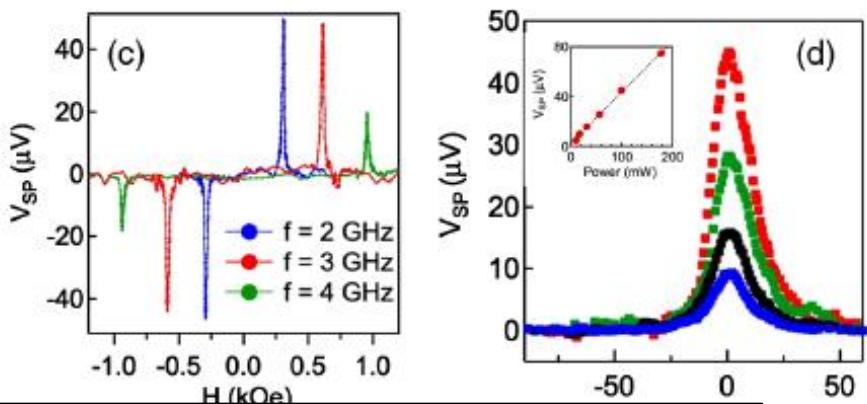
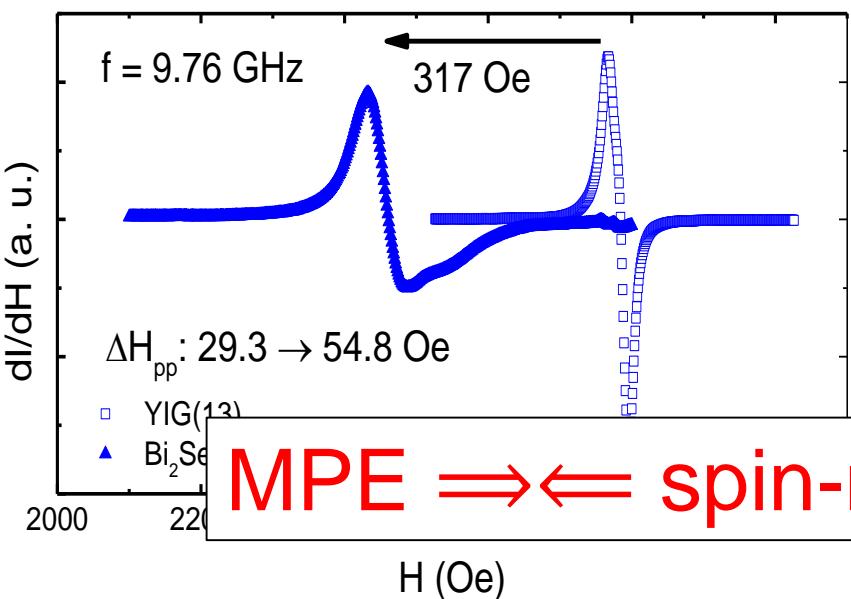
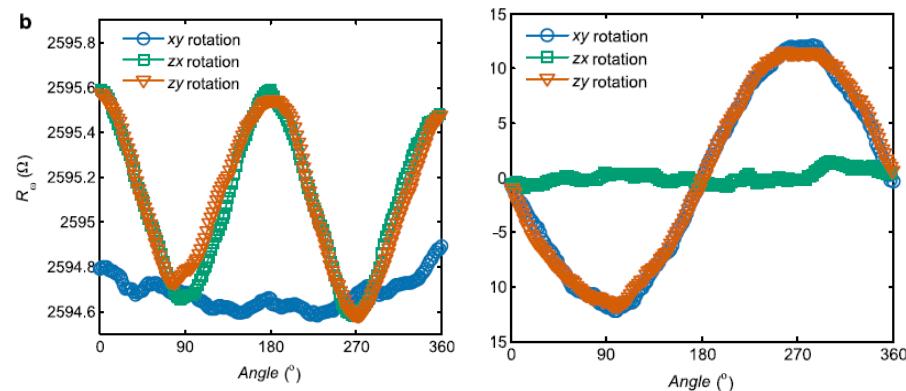
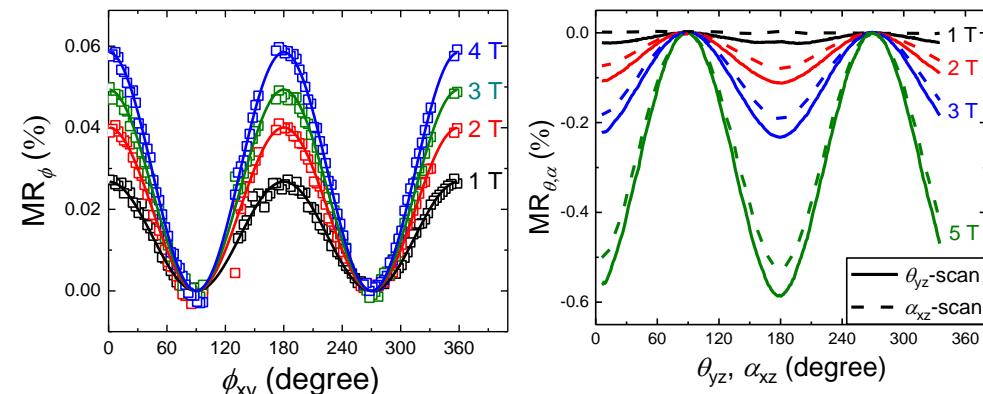
# Comparison

NTHU, NTU

UMN, PSU, CSU

Clear 1<sup>st</sup> harmonic signals  
2<sup>nd</sup> harmonic signals?

No 1<sup>st</sup> harmonic signals  
Strong 2<sup>nd</sup> harmonic signals: UMR

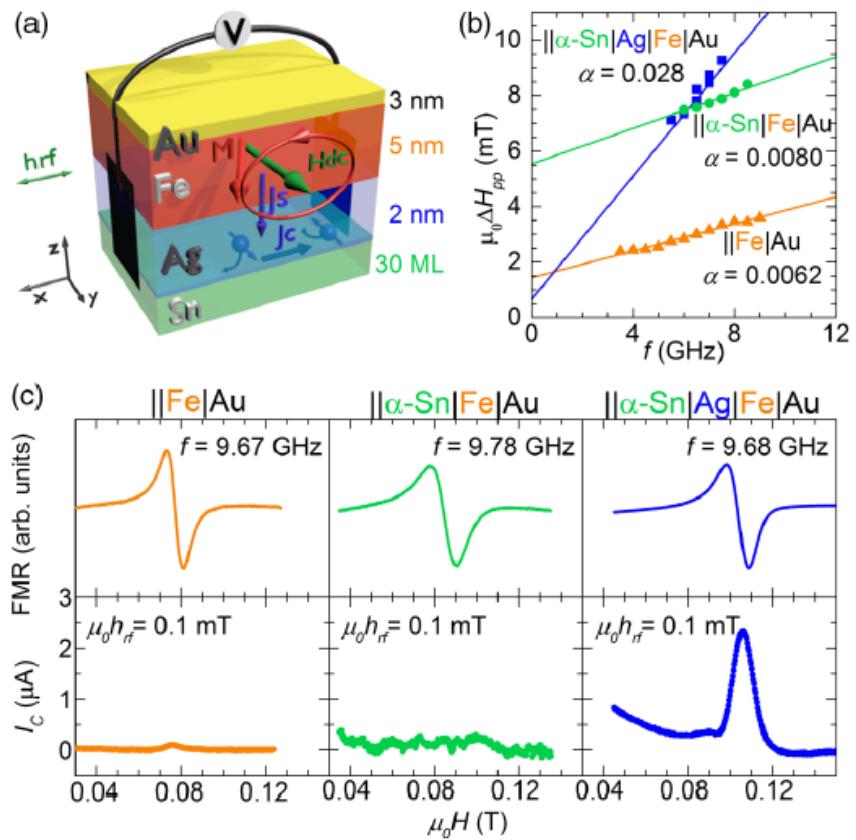
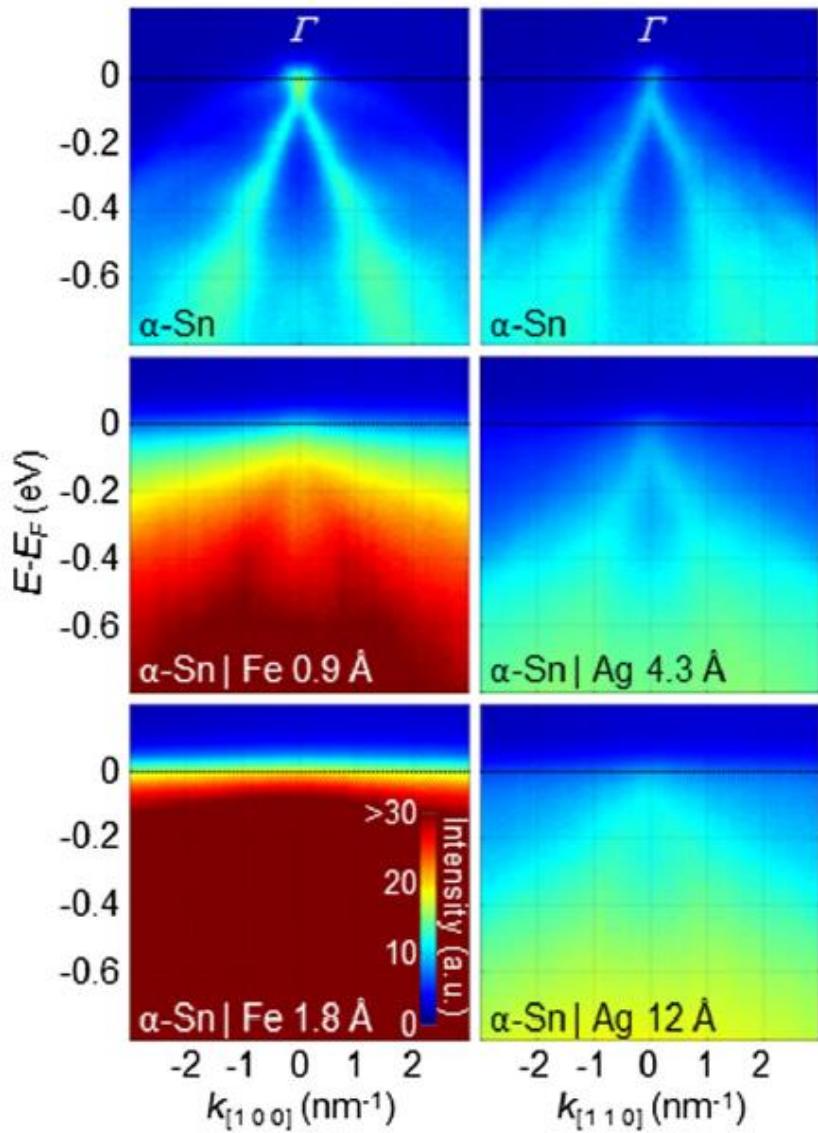


MPE  $\Rightarrow \Leftarrow$  spin-momentum locking?

Strong MPE, little spin-charge conversion

Fanchiang et al., Nat. Commun. **9**, 223 (2018)  
Wang et al., Phys. Rev. Lett. **117**, 076601 (2016)  
arXiv:1806.09066 (2018)

# Critical role of a normal metal spacer layer: Very efficient SCC in $\alpha$ -Sn at room temperature (A. Fert)

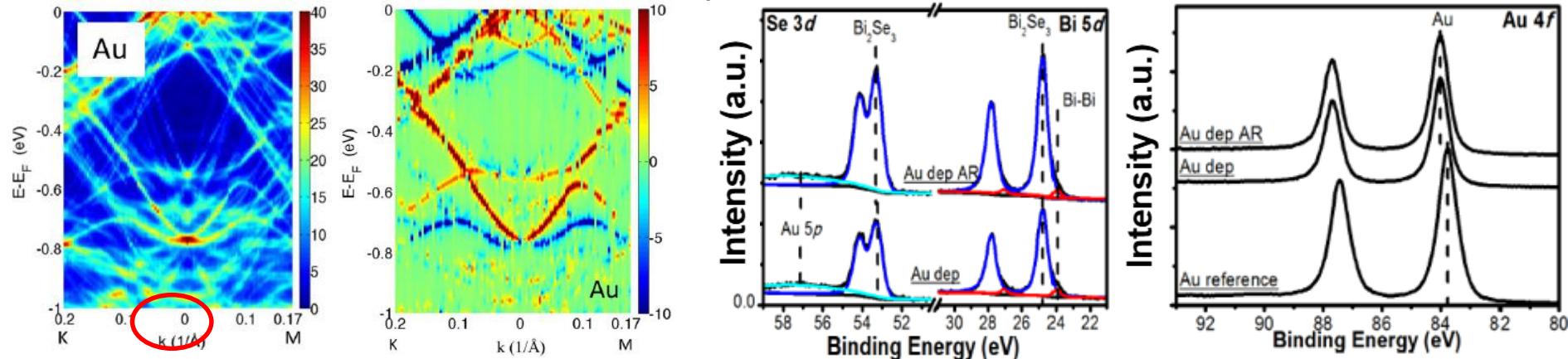


PRL 116, 096602 (2016). 42

# Electronic property and chemistry of metals in contact with $\text{Bi}_2\text{Se}_3$

C. D. Spataru *et al.*, *Phys. Rev. B* **90**, 085115 (2014) L. A. Walsh *et al.*, *J. Phys. Chem.* **121**, 23551–23563 (2017)

Calculated spectral function of Au/ $\text{Bi}_2\text{Se}_3$  XPS result for Se 3d and Bi 5d XPS result for Au 4f

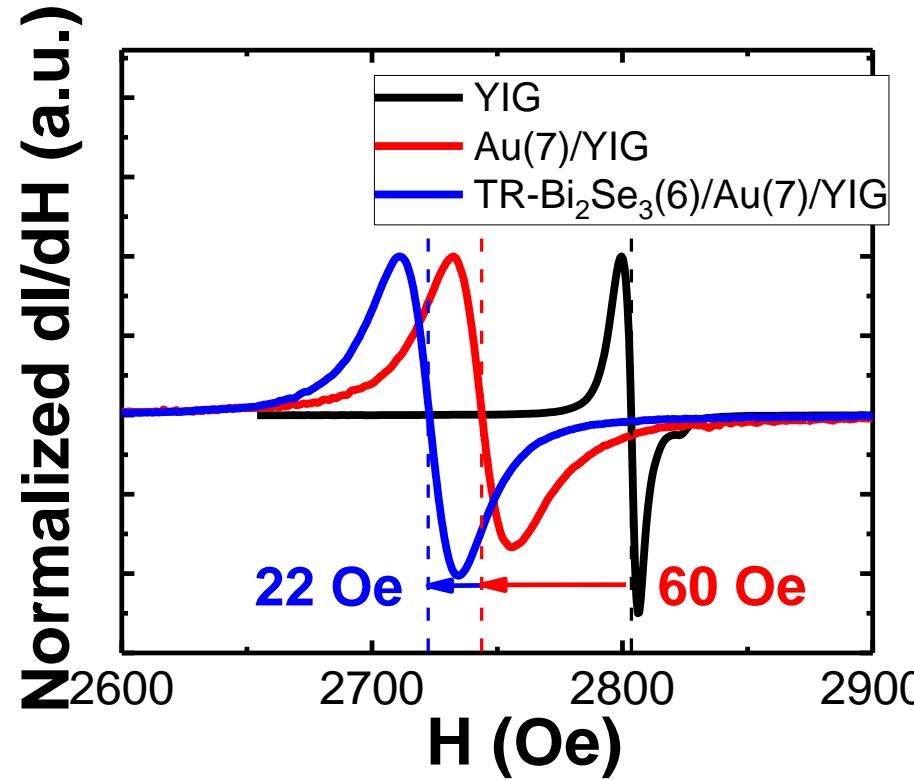
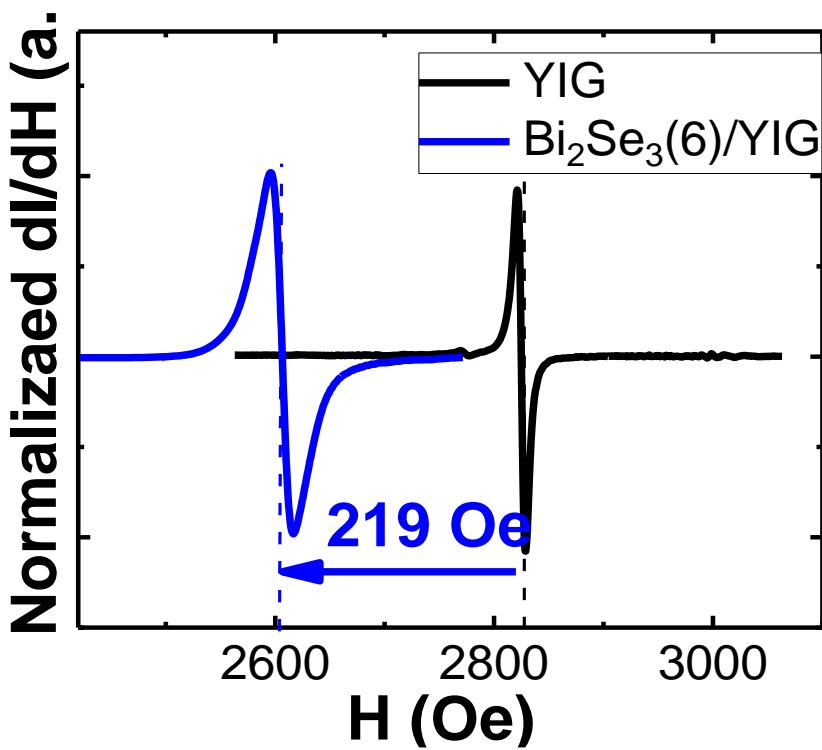


- Preservation of Dirac cone and the spin texture in  $\text{Bi}_2\text{Se}_3$  in contact with Au → No chemical reaction detected
- No discernible change of the peak shape

Au can serve as a promising interlayer, not only reducing the direct exchange coupling between YIG and  $\text{Bi}_2\text{Se}_3$  film, but also preserving TI properties.

It is difficult to directly grow  $\text{Bi}_2\text{Se}_3$  on Au/YIG because of the severe inter-diffusion.

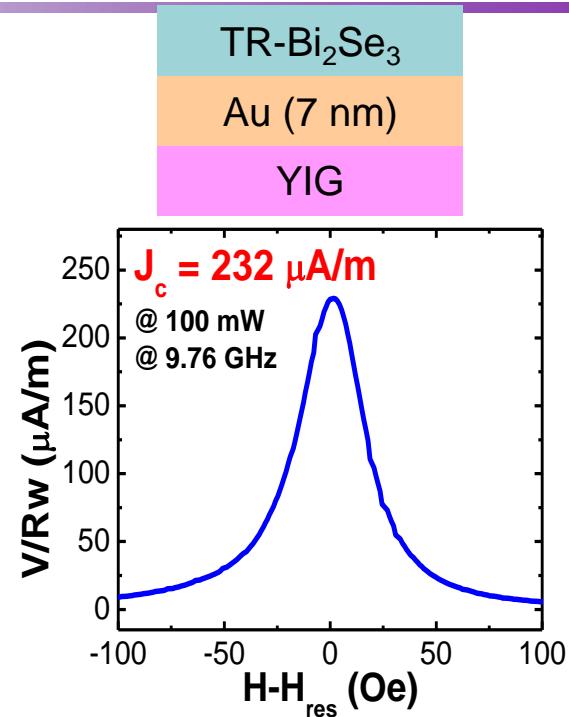
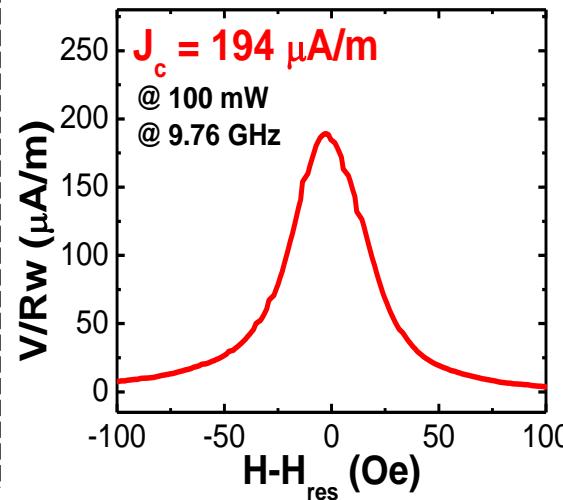
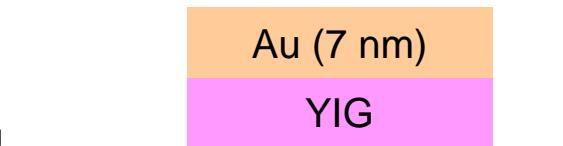
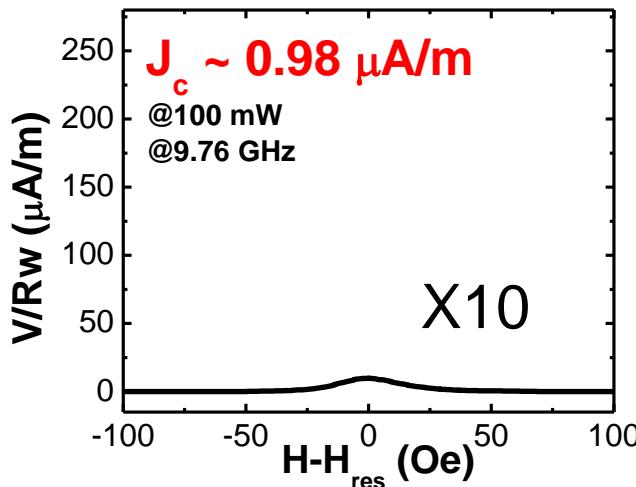
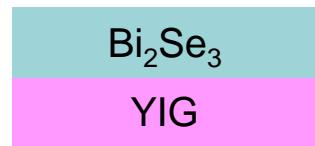
# Decreased interfacial coupling by Au layer



- Smaller  $H_{\text{res}}$  shift in  $\text{Au}/\text{YIG}$  compared to  $H_{\text{res}}$  shift of  $\text{Bi}_2\text{Se}_3/\text{YIG}$
- $H_{\text{res}}$  shift of  $\sim 22$  Oe in  $\text{TR}-\text{Bi}_2\text{Se}_3/\text{Au}/\text{YIG}$  compared to  $H_{\text{res}}$  of  $\text{Au}/\text{YIG}$

Slight enhancement of anisotropy in  $\text{TR}-\text{Bi}_2\text{Se}_3/\text{Au}/\text{YIG}$  implies that there is less direct exchange coupling between  $\text{TR}-\text{Bi}_2\text{Se}_3$  and YIG.

# Spin-to-charge conversion of $\text{Bi}_2\text{Se}_3/\text{Au}$



- Small spin-pumping-induced current density in  $\text{Bi}_2\text{Se}_3/\text{YIG}$
- Sizable enhancement of charge current in  $\text{TR-}\text{Bi}_2\text{Se}_3/\text{Au}/\text{YIG}$

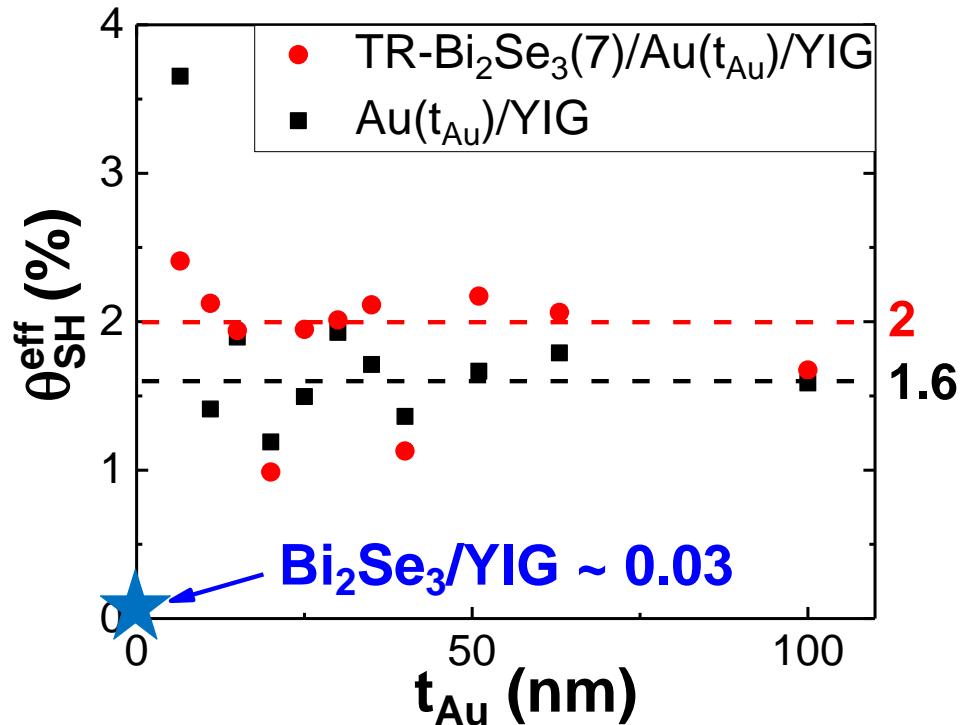
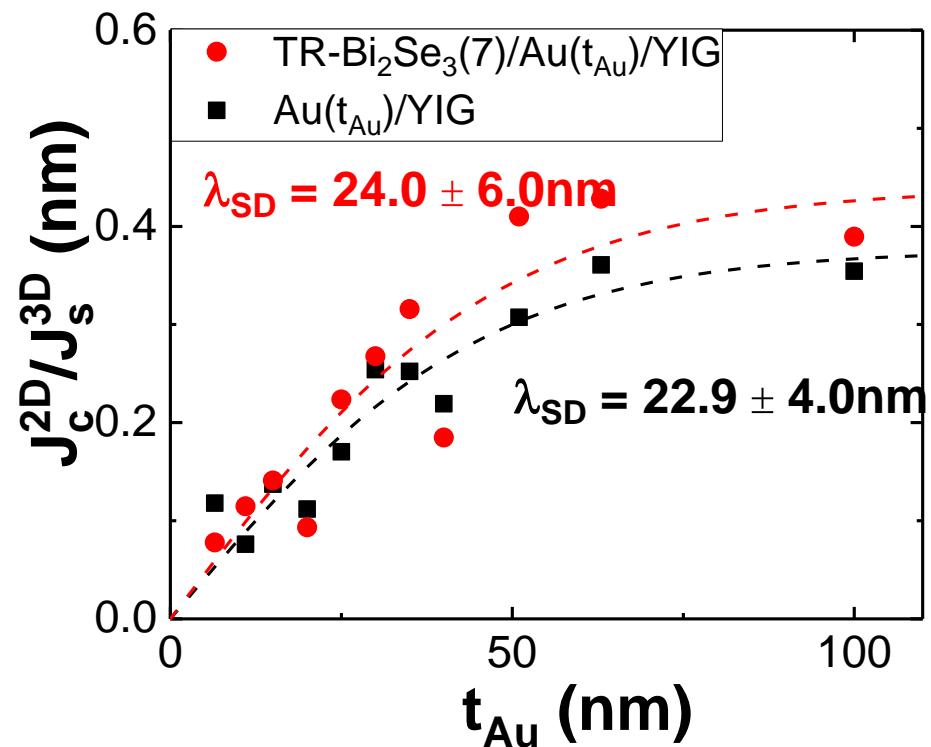
- Enhanced charge current of  $\text{TR-}\text{Bi}_2\text{Se}_3/\text{Au}/\text{YIG}$  is significantly larger than the value of  $\text{Bi}_2\text{Se}_3/\text{YIG}$ , possibly resulted from the decoupling of TSS and YIG.
- First principle calculations show that there can exist large Rashba splitting at the interface.

C. H. Chang *et al.*, *NPG Asia Mater.* **8**, e332 (2016)

32

# Au thickness dependence of SCC in TR-Bi<sub>2</sub>Se<sub>3</sub>/Au

Assuming spin diffusion in normal metal:  $\frac{J_C^{2D}}{J_S^{3D}} = \theta_{SH} \lambda_{SD} \tanh\left(\frac{t_N}{2\lambda_{SD}}\right)$



- SCC shows **overall enhancement** in TR-Bi<sub>2</sub>Se<sub>3</sub>/Au/YIG
- TR-Bi<sub>2</sub>Se<sub>3</sub>/Au interface may play an important role in the SCC.
- Improving TR-Bi<sub>2</sub>Se<sub>3</sub>/Au interface could further enhance SCC.

## ***Summary-3***

- Au served as an interlayer has effectively reduced the direct exchange coupling between TR- $\text{Bi}_2\text{Se}_3$  and YIG, so that little enhancement of IMA is observed.
- The SCC of TR- $\text{Bi}_2\text{Se}_3/\text{Au}$  is larger than the value in  $\text{Bi}_2\text{Se}_3$  on YIG, which may be caused by the decoupling of TSS and YIG, or Rashba splitting of the interface state.

# Conclusions

- Discovery of large interfacial magnetic anisotropy of TI/FI heterostructures
- First demonstration of spin pumping probe of magnetic proximity effect
- Realization of zero-field FMR in  $\text{Bi}_2\text{Se}_3/\text{YIG}$
- Possible incompatibility of interfacial exchange coupling and spin-to-charge conversion (SCC) in TI/FMI

