

# Neutrinos!

*Portals to the Dark Sector?*

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# lecture I

# Outline

- introduction to what we know about neutrinos

- ➔ mass

- ★ Majorana vs Dirac

- ➔ mixing

- ➔ oscillation

- ➔ matter effects

- critical open experimental questions

- the neutrino portal

- neutrinos in cosmology and astrophysics

- ➔ effects of sterile neutrinos

- ➔ dark energy coincidence and MaVaNs

} Introductory  
level

} more  
advanced

$\nu$  Mass

# Neutrinos in the Standard Model

- Standard Model was formulated without any neutrino mass, even though it was formulated after neutrino oscillation and neutrino mass had been suggested as a solution to the solar neutrino problem, and neutrino mass suggested as a solution to dark matter problem.

## **Why leave out the neutrinos mass?**

- Now that there is convincing evidence that neutrinos have tiny masses, neutrino mass has been incorporated into “the  $\nu$  standard model(s)” in either of 2 ways.

# Standard Model with Massless Neutrinos: helicity vs chirality

- Chirality = eigenvalue of  $\gamma_5$ .
  - ➔ Lorentz invariant measure of “handedness”.
  - ➔  $P_L = \frac{1}{2}(1 - \gamma_5)$ ,  $P_R = \frac{1}{2}(1 + \gamma_5)$ 
    - ★ Project out “left-handed” and “right-handed” fields
    - ★ chirality is Lorentz invariant
    - ★ for massless particles, (and only for massless states) chiral symmetry  $\Rightarrow$  chirality conservation
- Helicity =  $\mathbf{J} \cdot \mathbf{P}$ 
  - ★ for massless states (and only for massless states), helicity is Lorentz invariant
  - ★ for noninteracting particles, helicity is conserved
  - ➔ for massless states (and only massless) chirality  $\propto$  helicity

## Chirality vs helicity, cont

- Massive states:
  - ➔ Chirality is Lorentz invariant, not conserved
  - ➔ Helicity is not Lorentz invariant, is conserved
- for state initially left chiral:  $\langle \text{helicity} \rangle = -\frac{1}{2}\beta$  (for  $v, \beta \approx 1$ )
- for left handed helicity:  $\langle \text{chirality} \rangle = -\beta$
- left chiral **fields**: left chiral particles or right chiral antiparticles
- only left chiral fields are weak doublets
- in SM: neutrino part of weak doublet
- when  $v$  was massless: “all  $v$ 's are left handed (have negative helicity) and all  $\bar{v}$ 's are right handed (positive helicity)” (both are weak doublets)

$$\begin{pmatrix} \nu_{Le} \\ e_L \end{pmatrix}, \begin{pmatrix} \nu_{L\mu} \\ \mu_L \end{pmatrix}, \begin{pmatrix} \nu_{L\tau} \\ \tau_L \end{pmatrix}$$

# $\nu$ mass in the Standard Model

## Method I: Dirac

- same as any other fermion
  - $\ell_{eL} = \begin{pmatrix} \nu_e \\ e \end{pmatrix}$  weak interaction doublet
  - $\nu_{eR}$  weak interaction singlet. No gauge charges at all!
  - $h$  = Higgs doublet
  - $\lambda_{\nu_e} \langle h \rangle \bar{\nu}_e \ell_{eL} \Rightarrow m_{\nu_e} = \lambda_{\nu_e} \langle h \rangle$
  - no explanation why  $m_\nu$  is so small compared with other masses
- ★  $m_\nu < 1 \text{ eV}$  ( $\hbar=c=1$  units);  $m_e=0.5 \text{ MeV}$



## More about Dirac mass

- For Dirac mass term, need  $\nu_L$  and  $\nu_R$  fields
- The neutrino and the antineutrino are different
- There are 4 particle states:
  - ➔  $\nu_L$  (weak doublet in massless limit),
  - ➔  $\nu_R$  (weak singlet in massless limit),
  - ➔  $\bar{\nu}_L$  (weak singlet in massless limit)
  - ➔  $\bar{\nu}_R$  (weak doublet in massless limit)
- Lepton number is conserved and distinguishes between  $\nu$  and  $\bar{\nu}$
- The  $\nu_R$  field has no interactions other than through the mass term

## Important note about "left" and "right"

- When referring to *fields* "L" and "R" refer to *chirality*
- When referring to *particles*, "L" and "R" refer to *helicity*
- chirality and helicity coincide for massless particles and are opposite for massless antiparticles.
- Neutrinos are so ultra relativistic, so close to massless, that chirality and helicity almost coincide.

## Majorana mass term

- For a neutral particle, if there is no conserved quantum number, the particle and anti particle may be the same
- $\bar{\nu}_R$  and  $\nu_L$  transform the same way under Lorentz group
- Could have Lorentz invariant mass term  $\nu_L \nu_L$  instead of  $\bar{\nu}_R \nu_L$
- breaks lepton number
- *breaks electroweak gauge invariance*

## $\nu$ mass Method II:

### Seesaw Majorana mass

- $\nu_R$  is gauge singlet field
- $\nu_R \nu_R$  Majorana mass term is gauge and Lorentz invariant
- If both Majorana and Dirac terms are present the  $\nu$  mass terms may be written as a Majorana mass matrix:  
$$\begin{matrix} \nu_L & \overline{\nu_R} \end{matrix}$$
- $m$  is just like the Dirac mass term and could have been written in usual way for Dirac term  
$$\begin{matrix} \nu_L \\ \overline{\nu_R} \end{matrix} \begin{pmatrix} 0 & m \\ m & M \end{pmatrix}$$
- $M$  is a Majorana mass term, breaking lepton number

$$v_L \quad \overline{v_R}$$

$$\frac{v_L}{v_R} \begin{pmatrix} 0 & m \\ m & M \end{pmatrix}$$

*Seesaw continued*

- Consider limit  $M \gg m$  (motivated by GUTs)
- Diagonalize matrix perturbatively
- just like 2 state quantum system
- approximate eigenvalues:  $M + \frac{m^2}{M}, \frac{-m^2}{M}$ 
  - ➔ sign of fermion mass does not matter
  - ➔ as  $M$  gets bigger, small eigenvalue gets smaller!
- ★  $m_\nu \approx 0.1 \text{ eV}, m \approx 100 \text{ GeV} \Rightarrow M \approx 10^{14} \text{ GeV!}$ 
  - (at low energy, we can only determine  $|m^2/M|$ )

# Effective Field theory

- Effective field theory
  - ➔ If a particle is too heavy to make, only see virtual effects
  - ➔ same effects can be approximately included in an effective (nonrenormalizable) local operator in the Lagrangian
    - ★ e.g. 4-fermion operator in Fermi theory of weak interactions
- “Integrate out” heavy particles

$$\int D\Phi_{heavy} D\phi_{light} e^{i \int dx L(\phi, \Phi)} = \int D\phi_{light} e^{i \int dx L_{eff}(\phi)}$$

- ➔  $L_{eff}$  is sum of  $\infty$  local operators
- ➔ approximate  $L_{eff}$  with finite set of terms
  - ★ lowest dimension terms in  $L_{eff}$  dominate
  - ★ dimensional analysis, 3+1 spacetime dimensions: coefficient of dimension  $d$  term of order  $(1/M)^{(d-4)}$ , perturbatively expand in powers of  $(E/M)$

# Effective field theory and seesaw Majorana mass

- Standard model is surely an effective theory
- Minimal Standard Model includes all terms to  $d=4$  (renormalizable)
  - ➔ 19 parameters
- next gauge invariant term in expansion:  $d=5$  (nonrenormalizable)
  - ➔  $L_{eff} \supset c (h^2/M) \ell \ell (+ h.c.)$
  - ➔ for  $c = 1$ ,  $M$  is scale at which approximation of keeping only low dimension terms in expansion of  $L_{eff}$  breaks down
  - ➔  $L_{eff}$  breaks lepton number

# Effective Field Theory of the seesaw

- Integrate out heavy ‘sterile’ singlet with Majorana mass and what do you get?
  - $L_{\text{eff}} \supset -(\lambda^2 h^2/M) \ell \ell$
  - nonrenormalizable dimension 5 term
  - unique dimension 5 term you can add to Standard Model with only Standard model fields
  - $h \rightarrow \langle h \rangle : L_{\text{eff}} \rightarrow$  into tiny Majorana mass term for  $\nu$ 
    - ★  $m_\nu = \lambda^2 \langle h \rangle^2 / M$
- $\nu$  has 2 components: left and right helicity
- Lepton number is broken  $\Rightarrow 0 \nu \beta \beta$  nuclear decay possible
  - ★  $\text{rate} \propto m_\nu^2$
- $\nu$  is its own anti particle.
  - ➔ weak interactions convert  $\nu_L$  to charged lepton and  $\nu_R$  to charged antilepton.
  - ➔ we usually refer to  $\nu_L$  as the “neutrino” and its  $CP$  conjugate  $\nu_R$  as “antineutrino”



# Dirac v Majorana

Dirac

		helicity	$l^-$	$l^+$
$\nu$ $L = 1$		L	1	0
		R	$(\frac{m_\nu}{E})^2$	0
$\bar{\nu}$ $L = -1$		R	0	1
		L	0	$(\frac{m_\nu}{E})^2$

Majorana

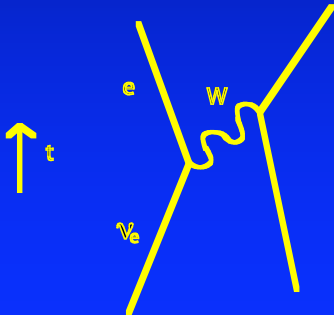
		helicity	$l^-$	$l^+$
$\nu$		L	1	$(\frac{m_\nu}{E})^2$
$\bar{\nu}$		R	$(\frac{m_\nu}{E})^2$	1
$\nu = \bar{\nu}$				

$$\left(\frac{m_\nu}{E}\right)^2 = \left(\frac{1\text{eV}}{1\text{GeV}}\right)^2 = 10^{-18}$$

# Weak Mixing and flavor violation

# What do we know about neutrinos?

- Three types of neutrinos:  $e$ ,  $\mu$ ,  $\tau$ 
  - Type determined by what lepton is produced



See the charged lepton produced!

Need enough energy:

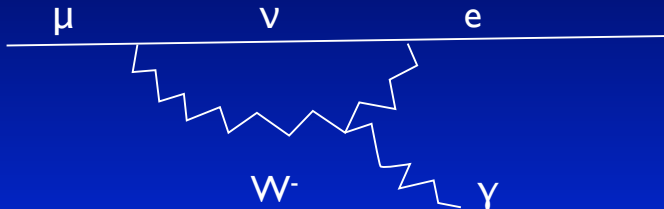
$$\nu_e \rightarrow e \quad .511 \text{ MeV}$$

$$\nu_\mu \rightarrow \mu \quad 105 \text{ MeV}$$

$$\nu_\tau \rightarrow \tau \quad 1777 \text{ MeV}$$

# Lepton flavor

- Discovery of 2 types of neutrinos solved problem of why no  $\mu \rightarrow e\gamma$



- Lepton flavor conservation ( $e, \mu, \tau$  numbers) a key piece of standard model

# Early History of Neutrinos

“I have done a terrible thing. I have postulated a particle which cannot be detected.” -Pauli, 1930

- 1956 Neutrinos discovered by Reines and Cowan
- 1957 Neutrinos showed to have left handed helicity by Goldhaber et al
- 1961 Muon neutrino discovered at Brookhaven
- 1957-62 Pontecorvo, Sakata independently speculate that neutrino variety oscillates between electron and muon

# Weak Interactions violate flavor in the quark sector

- quark doublets:  $\begin{pmatrix} u_L \\ d_L' \end{pmatrix}, \begin{pmatrix} c_L \\ s_L' \end{pmatrix}, \begin{pmatrix} t_L \\ b_L' \end{pmatrix}$  Weak eigenstates

- quark weak eigenstates are not mass eigenstates

- weak quark mixing:  $\begin{pmatrix} d_L' \\ s_L' \\ b_L' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix}$  mass eigenstates

- $V = V_{CKM}$

- $VV^\dagger = I$

- mixing requires both up and down quarks to be massive, with non degenerate masses

- off diagonal CKM elements are small

# Lepton mixing?

- Why not an analog of CKM matrix for leptons?
- In minimal SM, with no  $\nu_R$  field,  $\nu$ 's are massless and lepton flavor conservation is “automatic”
- If neutrinos are massless, then can always make mass eigenstates = flavor eigenstates
- What if  $\nu$ 's have tiny mass? lepton flavor violation should become unobservable as  $m \Rightarrow 0$

# PMNS matrix in Lepton sector

- lepton doublets:  $\begin{pmatrix} \nu_{Le} \\ e_L \end{pmatrix}, \begin{pmatrix} \nu_{L\mu} \\ \mu_L \end{pmatrix}, \begin{pmatrix} \nu_{L\tau} \\ \tau_L \end{pmatrix}$
- lepton weak eigenstates are not mass eigenstates

- lepton mixing: 
$$\begin{pmatrix} \nu_{eL} \\ \nu_{\mu L} \\ \nu_{\tau L} \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_{1L} \\ \nu_{2L} \\ \nu_{3L} \end{pmatrix}$$
- $U = U_{PMNS}$
- $UU^\dagger = I$

- mixing requires neutrinos to be massive, and have nondegenerate masses
- observing mixing requires observing effects of nondegenerate neutrino mass



$\nu$  flavor

oscillations

# Kinematic Effects of mass

- Usually we observe effects of mass through the kinematic relation  $E = \sqrt{p^2 + m^2}$
- Produce  $\nu$  with  $E \gg \text{MeV}$
- $m < \text{eV}$ 
  - ➡  $p \approx E - m^2/(2E)$
  - ➡  $\Delta p < 10^{-15} \text{ MeV}$
  - ➡  $\Delta x > 100 \text{ m}$  ! classical kinematic effects of mass not observable

# Quantum Mechanical Effects of $\nu$ mass

- Neutrino wave packet is so ultra relativistic that it propagates with  $\omega \cong k$
- essentially no dispersion, distance traveled  $x \cong t$
- effect of mass on overall phase of wave packet:  $e^{-i \frac{m^2 t}{2E}}$
- flavor eigenstate produced in coherent superposition of mass eigenstates which acquire different phases as they travel
- If only 2  $\nu$ 's mix (e.g.  $\nu_\mu, \nu_e$ ) simple formula for probability of flavor transition

$$P_{\mu \rightarrow e} = \sin^2(2\theta) \sin^2\left(\frac{(m_1^2 - m_2^2)x}{4E}\right)$$

# mass vs flavor eigenstates

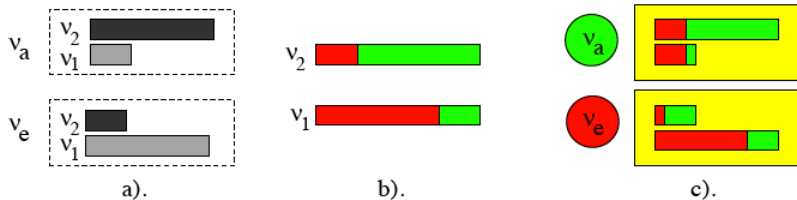


Figure 1: a). Representation of the flavor neutrino states as the combination of the mass eigenstates. The length of the box gives the admixture of (or probability to find) corresponding mass state in a given flavor state. (The sum of the lengths of the boxes is normalized to 1. b). Flavor composition of the mass eigenstates. The electron flavor is shown by red (dark) and the non-electron flavor by green (grey). The sizes of the red and green parts give the probability to find the electron and non-electron neutrino in a given mass state. c). Portraits of the electron and non-electron neutrinos: shown are representations of the electron and non-electron neutrino states as combinations of the eigenstates for which, in turn, we show the flavor composition.

## > 2 flavor mixing

- Probability of producing flavor  $a$  in a beam of flavor  $b$  at a distance  $x$  from the source

$$P_{ab} = \left| \sum_{j=1}^n U_{aj} U_{bj}^* e^{-i \frac{m_j^2 x}{2E}} \right|^2$$

$UU^\dagger = I \Rightarrow$  no flavor change at  $x=0$

- With  $>2$  flavors,  $U$  can have a CPV phase, just like in quark mixing. For antineutrinos:

$$\bar{P}_{ab} = \left| \sum_{j=1}^n U_{aj}^* U_{bj} e^{-i \frac{m_j^2 x}{2E}} \right|^2 = P_{ba} \neq P_{ab}$$

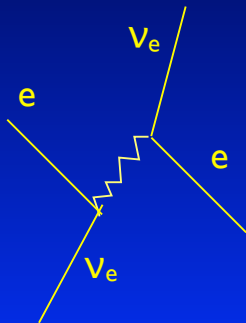
# A brief history of neutrino mass...

- The Standard Model ('67-'68) - massless neutrinos
- 1967 - Homestake Experiment on solar neutrinos: “solar neutrino problem”
  - 50% depletion => need *very* small masses, large angles
  - “Theoretical prejudice that  $\theta_\nu$  should be small makes this an unlikely explanation of [the solar neutrino problem].”  
- anonymous
  - Probably just astrophysics

*effects of matter  
on oscillations*

# The MSW mechanism: effects of propagating through matter

- neutrinos propagate through matter
- matter is full of electrons
- forward scattering of electron neutrino
- additional phase for  $\nu_e$





# Effective $H$ for $\nu$ propagation

- in flavor basis: (simplified case of 2 neutrinos)
- ignore terms  $\propto L$ , only can see  $\Delta m^2 = m_2^2 - m_1^2$

$$H_{\text{eff}} = \begin{pmatrix} -\left(\frac{\Delta m^2}{4E}\right)\cos(2\theta) + V & \left(\frac{\Delta m^2}{4E}\right)\sin(2\theta) \\ \left(\frac{\Delta m^2}{4E}\right)\sin(2\theta) & \left(\frac{\Delta m^2}{4E}\right)\cos(2\theta) \end{pmatrix} \quad (+ \text{ terms } \propto L)$$

- $V$  is matter effect for electron neutrinos from electrons
- $V \propto$  density of electrons
- when diagonal terms are equal, resonant enhancement of mixing

# Level crossing in the sun

- adiabatic conversion “start heavy, stay heavy”

from Smirnov  
hep-ph/0305106

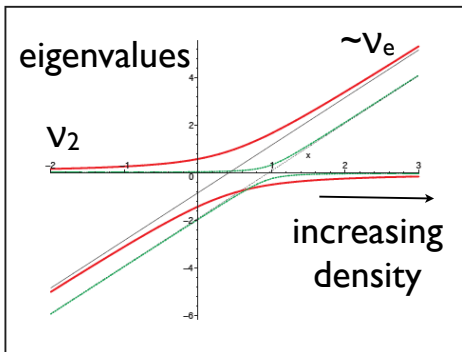


Figure 3: Level crossing scheme. Dependence of the eigenvalues of the Hamiltonian in matter,  $H_{1m}$  and  $H_{2m}$ , on the ratio  $x \equiv l_\nu/l_0$  for two different values of vacuum mixing  $\sin^2 2\theta = 0.825$  (solid, blue lines) and  $\sin^2 \theta = 0.08$  (dashed, red lines).

# More details of MSW

from Smirnov  
hep-ph/0305106

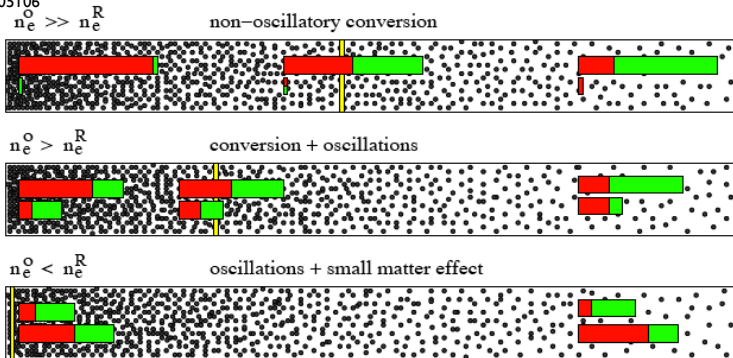
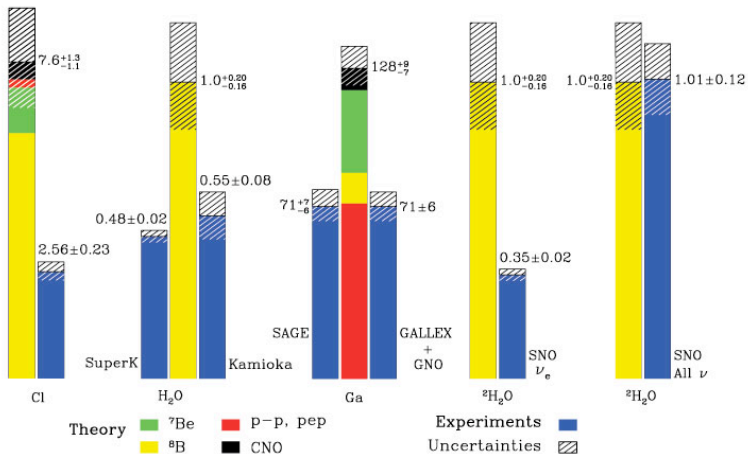


Figure 5: Adiabatic evolution of neutrino state for three different initial condition ( $n_e^0$ ). Shown are the neutrino states in different moments of propagation in medium with varying (decreasing) density. The yellow vertical line indicates position of resonance. The initial state is  $\nu_e$  in all the cases. The sizes of the boxes do not change, whereas the flavors (colors) follow the density change.

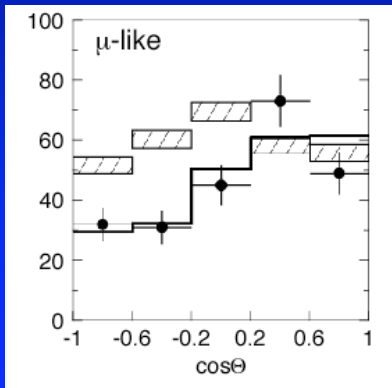
# Fast forward to mid-90's...

Total Rates: Standard Model vs. Experiment  
Bahcall-Pinsonneault 2000



# '98 Super-K Atmospheric $\nu$ 's

- Super-kamiokande sees atmospheric large atmospheric neutrino depletion



## Mass Found in Elusive Particle; Universe May Never Be the Same

### Discovery on Neutrino Rattles Basic Theory About All Matter

By MALCOLM W. BROWNE

**TAKAYAMA, Japan, June 5** — In what colleagues hailed as a historic landmark, 150 physicists from 23 research institutions in Japan and the United States announced today that they had found the existence of mass in a notoriously elusive subatomic particle called the neutrino.

The neutrino, a particle that carries no electric charge, is so light that it was assumed for many years to have no mass at all. After today's announcement, cosmologists will have to confront the possibility that much of the mass of the universe is in the form of neutrinos. The discovery will also compel scientists to revise a highly successful theory of the composition of matter known as the Standard Model.

Word of the discovery had drawn some 300 physicists here to discuss neutrino research. Among other things, they said, the finding of neutrino mass might affect theories about the formation and evolution of galaxies and the ultimate fate of the universe. If neutrinos have sufficient mass, their presence throughout the universe would increase the overall mass of the universe, possibly slowing its present expansion.

Others said the newly detected but as yet unmeasured mass of the neutrino must be too small to cause cosmological effects. But whatever the case, there was general agreement here that the discovery will have far-reaching consequences for the investigation of the nature of matter.

Speaking for the collaboration of scientists who discovered the existence of neutrino mass using a huge underground detector called Super-Kamiokande, Dr. Takaaki Kajita of the Institute for Cosmic Ray Research of Tokyo University said that all explanations for the data collect-

#### Detecting Neutrinos



Neutrinos pass through the Earth's surface to a tank filled with 12.5 million gallons of ultra-pure water.

... and collide with other particles.

... producing a cone-shaped flash of light.

LIGHT



LIGHT AMPLIFIER

The light is recorded by 11,200 20-inch light amplifiers that cover the inside of the tank.

#### And Detecting Their Mass

By analyzing the cones of light, physicists determine that some neutrinos have changed form on their journey. If they can change form, they must have mass.

Source: University of Hawaii

The New York Times

ed by the detector except the existence of neutrino mass had been essentially ruled out.

Dr. Yoji Totsuka, leader of the coalition and director of the Kamioka Neutrino Observatory where the underground detector is situated, 30 miles north of here in the Japan Alps, acknowledged that his group's announcement was "very strong," but said, "We have investigated all

Continued on Page A14

U98, @Takayama  
June 1998

Atmospheric neutrino results  
from Super-Kamiokande & Kamiokande  
— Evidence for  $\nu_\mu$  oscillations —

T. Kajita

Kamioka observatory, Univ. of Tokyo

for the { Kamiokande  
Super-Kamiokande } Collaborations

<http://www-sk.icrr.u-tokyo.ac.jp/nu98/scan/>

# Fast forward to '02-'03

- KamLAND and SNO
  - SNO: Sees neutral currents, missing neutrinos
  - KamLAND: Reactor experiment, controlled source => finds large angle MSW

# 2010 Summary of standard picture

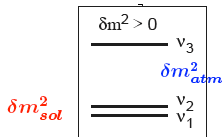
- All confirmed results can be explained with 3 neutrinos

## Masses:

Label the Neutrino mass eigenstates such that:

$\nu_e$  component of  $\nu_1$  >  $\nu_e$  component of  $\nu_2$  >  $\nu_e$  component of  $\nu_3$

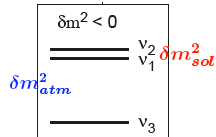
i.e.  $|U_{e1}|^2 > |U_{e2}|^2 > |U_{e3}|^2$



$$\delta m^2_{sol} = +7.6 \times 10^{-5} \text{ eV}^2$$

$$|\delta m^2_{atm}| = 2.4 \times 10^{-3} \text{ eV}^2$$

$$|\delta m^2_{sol}| / |\delta m^2_{atm}| \approx 0.03$$



$$\sqrt{\delta m^2_{atm}} = 0.05 \text{ eV} < \sum m_{\nu_i} < 0.5 \text{ eV} = 10^{-6} * m_e$$

S. Parke Neutrino 2010



# Mixing angles

## Mixing Matrix:

$$|\nu_e, \nu_\mu, \nu_\tau\rangle_{flavor}^T = U_{\alpha i} |\nu_1, \nu_2, \nu_3\rangle_{mass}^T$$

$$U_{\alpha i} = \begin{pmatrix} 1 & & & & & \\ & c_{23} & s_{23} & & & \\ & -s_{23} & c_{23} & & & \\ & & & c_{13} & s_{13}e^{-i\delta} & \\ & & & -s_{13}e^{i\delta} & c_{13} & \\ & & & & & 1 \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & \\ -s_{12} & c_{12} & \\ & & 1 \end{pmatrix} \begin{pmatrix} 1 & & \\ & e^{i\alpha} & \\ & & e^{i\beta} \end{pmatrix}$$

Atmos. L/E  $\mu \rightarrow \tau$     Atmos. L/E  $\mu \leftrightarrow e$     Solar L/E  $e \rightarrow \mu, \tau$      $0\nu\beta\beta$  decay  
 500km/GeV                      15km/MeV

not  
observable  
in  
oscillations

SNO/KamLAND  
 $|U_{e2}|^2$

Reactor/LBL

$$|U_{e3}|^2(1 - |U_{\mu 3}|^2)$$

$$= \begin{pmatrix} c_{13}c_{12} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -c_{23}s_{12} - s_{13}s_{23}c_{12}e^{i\delta} & c_{23}c_{12} - s_{13}s_{23}s_{12}e^{i\delta} & c_{13}s_{23} \\ s_{23}s_{12} - s_{13}c_{23}c_{12}e^{i\delta} & -s_{23}c_{12} - s_{13}c_{23}s_{12}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$

Atm Nus/LBL

$$|U_{\mu 3}|^2(1 - |U_{\mu 3}|^2)$$

$$\frac{CC}{NC}|_{sno} \approx |U_{e2}|^2$$

# Summary of history of neutrino mass theory

- Neutrinos are massless
- Neutrinos have small masses and small mixings, but they're not relevant for anything
- Neutrinos have small mixings, and the MSW mechanism might explain the sun
- Neutrinos have one large mixing for atmospheric neutrinos, and the other two angles are small
- Neutrinos have two large mixings and one small mixing, and this time we really mean it.